

Circuito 1

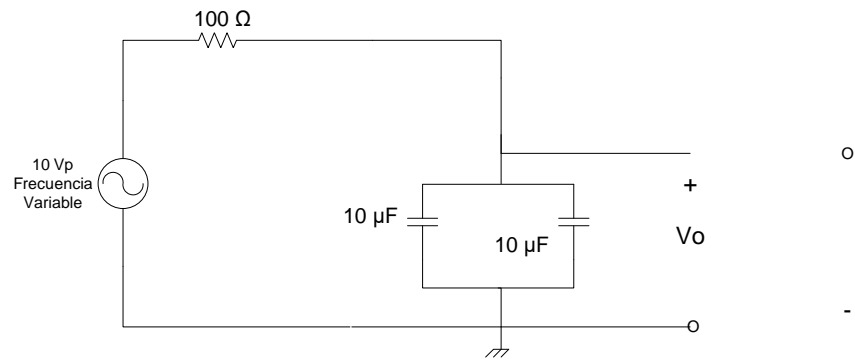


Figura 3: Esquema del circuito eléctrico con capacitores

Frecuencia 0 Hz

$$I=0$$

$$-V_p + 0 \times 100 + V_o = 0 \text{ (LTK)}$$

$$V_o = V_p = 10 \angle 0^\circ \text{ [V]}$$

Frecuencia 10 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(10)$$

$$\omega = 20 \pi$$

$$v(t) = 10 \cos(20 \pi t)$$

$$\frac{1}{j\omega C} = \frac{1}{j(20\pi)(10 \times 10^{-6})} = -j1591.54$$

$$Z_{eq} = c_1 \vee c_2 = \frac{(-j 1591.54)(-j 1591.54)}{-j 1591.54 - j 1591.54} = -j 795.77$$

$$V_o = \frac{-795.77}{100 - j 795.77} * (10)$$

$$V_o = 9.84 + 1.24 j \text{ [V] } V_o = 9.92 \angle 7.16^\circ$$

$$I = \frac{\frac{10}{100 - j 795.77} * 100 + j 795.77}{100 + j 795.77}$$

$$I = 1.55 \exp -3 + 0.0123 j \text{ [A] }$$

$$I = 12.47 \angle 82.86^\circ \text{ [mA] }$$

Frecuencia 50 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(50)$$

$$\omega = 100 \pi$$

$$v(t) = 10 \cos(100\pi t)$$

$$c_1 = c_2 = \frac{1}{-j 318.330} j \omega c$$

$$Z_{eq} = c_1 \vee c_2 = \frac{(-j 318.30)(-j 318.30)}{-j 318.30 - j 318.30} = -j 159.15$$

$$V_o = \frac{-159.15}{100 - j 159.15} * (10)$$

$$V_o = 7.16944 - j4.5048 \text{ [V]}$$

$$V_o = 8.4672 \angle -32.14^\circ$$

$$I = \frac{\frac{10}{100 - j159.15} * 100 + j159.15}{100 + j159.15}$$

$$I = 0.0283 + j0.045048 \text{ [A]}$$

$$I = 53.2 \angle 57.86^\circ \text{ [mA]}$$

Frecuencia 100 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(100)$$

$$\omega = 200 \pi$$

$$v(t) = 10 \cos(200\pi t)$$

$$Z_{C1} = Z_{C2} = \frac{1}{-j159.1549} = j\omega C$$

$$Z_{eq} = Z_{C1} \parallel Z_{C2} = \frac{(-j159.1549)(-j159.1549)}{-j159.1549 - j159.1549} = -j79.57$$

$$V_o = \frac{-j79.57}{100 - j79.57} * (10)$$

$$V_o = 3.88 - j4.87$$

$$V_o = 6.2266 \angle -51.455^\circ \text{ [V]}$$

$$I = \frac{\frac{10}{100 - j79.58} * 100 + j79.58}{100 + j79.58}$$

$$I=0.06122+j0.04872 \text{ [A]}$$

$$I=78.24\angle 38.513 \text{ [mA]}$$

Frecuencia 500 Hz

$$\omega=2\pi f \quad \omega=2\pi(500)$$

$$\omega=1000 \pi$$

$$v(t)=10\cos(1000\pi t)$$

$$Z_{c1}=Z_{c2}=\frac{1}{j\omega C}=-j31.8330$$

$$Z_{eq}=Z_{c1} \parallel Z_{c2}=\frac{(-j31.8330)(-j31.8330)}{-j31.8330-j31.8330}=-j15.915$$

$$V_o=\frac{-j15.915}{100-j15.915}*(10)$$

$$V_o=0.2477-j1.55$$

$$V_o=1.57\angle -80.96^\circ \text{ [V]}$$

$$I=\frac{\frac{10}{100-j15.913}*(100+j15.913)}{100+j15.913}$$

$$I=0.0975+j0.01552 \text{ [A]}$$

$$I=98.76\angle 9.04^\circ \text{ [mA]}$$

Frecuencia 1000 Hz

$$V_p = 10 \angle 0^\circ = 10 + 0j = 10 \text{ [V]}$$

$$Z = \frac{1}{\frac{1}{100} + j\omega C} = \frac{1}{\frac{1}{100} + j \times 1000 \times 10^{-7}} = -100j \text{ [} \Omega \text{]}$$

$$Z_{eq1} = \frac{Z}{2} = -50j \text{ [} \Omega \text{]}$$

$$V_o = V_{eq1} = \frac{Z_{eq1}}{Z_{eq1} + 100} V_p = \frac{-50j}{-50j + 100} 10 = 2 - 4j = 4.47 \angle -26.57^\circ \text{ [V]}$$

$$Z_{eq2} = Z_{eq1} + 100 = 100 - 50j \text{ [} \Omega \text{]}$$

$$I = \frac{V_p}{Z_{eq2}} = \frac{10}{100 - 50j} = 0.08 + 0.04j \text{ [A]} = 0.09 \angle 26.57^\circ \text{ [A]}$$

Circuito 2

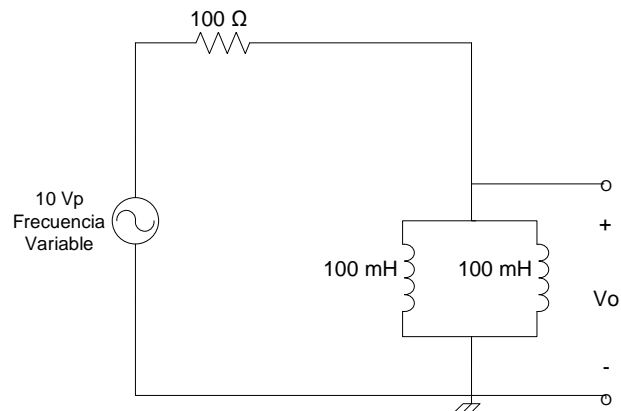


Figura 4: Esquema del circuito eléctrico con inductores

Frecuencia 0 Hz

$$V_o=0$$

$$\frac{V_p}{I} = 0.1 \text{ [A] } R$$

Frecuencia 10 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(10)$$

$$\omega = 20 \pi$$

$$v(t) = 10\cos(\pi t)$$

$$L_1 = L_2 = j\omega L = j0.02\pi$$

$$Z_{eq} = L_1 \vee L_2 = \frac{(j0.02\pi)(j0.02\pi)}{j0.02\pi + j0.02\pi} = j2\pi$$

$$V_o = \frac{j2\pi}{100 + j2\pi} * (10)$$

$$V_o = 0.0393 + j0.626$$

$$V_o = 0.627 \angle 86.4^\circ \text{ [V]}$$

$$I = \frac{\frac{10}{100 + j2\pi} * 100 - j2\pi}{100 - j2\pi}$$

$$I = 0.0996 - j0.00625 \text{ [A]}$$

$$I = 0.0998 \angle -3.59^\circ \text{ [mA]}$$

Frecuencia 50 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(50)$$

$$\omega = 100 \pi$$

$$v(t) = 10\cos(100\pi t)$$

$$L_1 = L_2 = j\omega L = j10\pi$$

$$Z_{eq} = L_1 \parallel L_2 = \frac{(j10\pi)(j10\pi)}{j10\pi + j10\pi} = j5\pi$$

$$V_o = \frac{j5\pi}{100 + j5\pi} * (10)$$

$$V_o = 0.2407 + j1.5329$$

$$V_o = 1.55168 \angle 81.07^\circ \text{ [V]}$$

$$= \frac{10}{100 + j5\pi} * 100 - j5\pi I$$

$$I = \frac{100 + j5\pi}{100 - j5\pi}$$

$$I = 0.09759 - j0.01533 \text{ [A]}$$

$$I = 98.78668 \angle -8.927^\circ \text{ [mA]}$$

Frecuencia 100 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(100)$$

$$\omega = 200 \pi$$

$$v(t) = 10\cos(200\pi t)$$

$$L1=L2=j\omega L=j20\pi$$

$$Z_{eq}=L1 \vee L2 = \frac{(j20\pi)(j20\pi)}{j20\pi + j20\pi} = j10\pi$$

$$V_o = \frac{j10\pi}{100 + j10\pi} * (10)$$

$$V_o = 0.898 + j2.86$$

$$V_o = 2.99 \angle 72.56^\circ [V]$$

$$I = \frac{\frac{10}{100 + j10\pi} * 100 - j10\pi j}{100 - j10\pi} \quad I = 0.0910 - 0.02859j [A]$$

$$I = 95.38 \angle -17.4299^\circ [mA]$$

Frecuencia 500 Hz

$$\omega = 2\pi f \quad \omega = 2\pi(500)$$

$$\omega = 1000\pi$$

$$v(t) = 10\cos(1000\pi t)$$

$$L1=L2=j\omega L=j100\pi$$

$$Z_{eq}=L1 \vee L2 = \frac{(j100\pi)(j100\pi)}{j100\pi + j100\pi} = j50\pi$$

$$V_o = \frac{j50\pi}{100 + j50\pi} * (10)$$

$$V_o = 7.11 + j4.53$$

$$V_o = 8.4357 \angle 32.48^\circ \text{ [V]}$$

$$I = \frac{\frac{10}{100 - j50\pi} * 100 - j50\pi}{100 + j50\pi}$$

$$I = 0.0288 - j0.0453 \text{ [A]}$$

$$I = 53.7 \angle -57.52^\circ \text{ [mA]}$$

Frecuencia 1000 Hz

$$V_p = 10 \angle 0^\circ = 10 + 0j = 10 \text{ [V]}$$

$$Z = j\omega L = j \times 1000 \times 0.1 = 100j \text{ [\Omega]}$$

$$Z_{eq1} = \frac{Z}{2} = 50j \text{ [\Omega]}$$

$$V_o = V_{eq1} = \frac{Z_{eq1}}{Z_{eq1} + 100} V_p = \frac{50j}{100 + 50j} 10 = 2 + 4j = 4.47 \angle 26.57^\circ \text{ [V]}$$

$$Z_{eq2} = \frac{Z}{2} + 100 = 100 + 50j \text{ [\Omega]}$$

$$I = \frac{V_p}{Z_{eq2}} = \frac{10}{100 + 50j} = 0.08 - 0.04j \text{ [A]} = 0.09 \angle -26.57^\circ \text{ [A]}$$