

# APACE - Accelerated Permutation Inference for ACE models

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# Introduction

- Matlab-based tool, specially designed for heritability analysis of neuroimaging data of twins
- Non-iterative linear regression-based estimation method, a variant of Haseman-Elston regression
- Use permutation test to correct for family-wise error rate
- Allow the use of spatial and summary statistics

# Background

- ACE decomposition:  $\sigma^2 = A + C + E$
- Heritability:  $h^2 = A/(A+C+E)$
- LR-SqD: linear regression with squared twin-pair difference

$$\mathbb{E} [(MZ_1 - MZ_2)^2] = 2E$$

$$\mathbb{E} [(DZ_1 - DZ_2)^2] = A + 2E$$

$$\mathbb{E} [(I_1 - I_2)^2] = 2A + 2C + 2E$$

- Use NNLS to estimate A,C,E and heritability

# Optional Inference Approaches

Bootstrapping CI's

Voxel-wise inference

Cluster-based inference

Summary measure inference

Aggregate heritability inference

Permutation-based  
p-values

# Inputs

- Create a structure array **ACEfit\_Par** with Required fields:
  - **.Model** – model ACE or AE
  - **.P\_nm** – specify input data, allowing different file formats
  - **.InfMx** – kinship information file
  - **.ResDir** – path to result folder
- Can use default values when optional fields are empty
- Save **ACEfit\_Par** to a mat file

# Inputs

- Create a structure array **ACEfit\_Par** with Required fields:

- **.Model** – model ACE or AE

- **.P\_nm** – specify input data, allowing different file formats

1. String, the name of a text file of filepaths to nifti OR cifti images, one filepath per row. Each image file consists of all of the data for that subject.
2. Cell array, one element per subject, where each element is a string, a file path to a nifti OR cifti image. Each image file consists of all the data for that subject.
3. Cell array of `_length_ _1_`, where the single element is a string, the filepath to a multi-subject nifti OR cifti image (e.g. `{'AllMySubjects.nii'}` or `{'AllMySubjects.dtseries.nii'}`). For either, the final dimension is equal to the number of subjects. For example, for 120 subjects, it could be a 2D image, 3000 x 120, or a 3D image, 3000 x 2 x 120, or a 4D image, 91 x 109 x 91 x 120.
4. A real matrix variable, where the final dimension is equal to the number of subjects.

- Ca

- Sa

# Inputs

- Create a structure array **ACEfit\_Par** with Required fields:
  - **.Model** – model ACE or AE
  - **.P\_nm** – specify input data, allowing different file formats
  - `.../Subj1/con_0001.img`
  - `.../Subj2/con_0001.img`
  - `.../Subj3/con_0001.img`
  - `.../Subj4/con_0001.img`
  - `.../Subj5/con_0001.img`
  - `.../Subj6/con_0001.img`
- Ca
- Sa

# Inputs

- Create a structure array **ACEfit\_Par** with Required fields:
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n	MotherID	FatherID	Zygotity
1	1	1	MZ
2	1	1	MZ
3	2	2	NotMZ
4	2	2	NotMZ
5	3	3	NotTwin
6	4	4	NotTwin

- Ca

- Sa



Inputs → [README\\_APACE\\_intro.pdf](#)

- Create a structure array **ACEfit\_Par** with Required fields:
  - **.Model** – model ACE or AE
  - **.P\_nm** – specify input data, allowing different file formats
  - **.InfMx** – kinship information file
  - **.ResDir** – path to result folder
- Can use default values when optional fields are empty
- Save **ACEfit\_Par** to a mat file

# Outputs → [README\\_APACE\\_outputs.pdf](#)

Outputs from the **ACEfit** function of APACE software for the **ACE** model

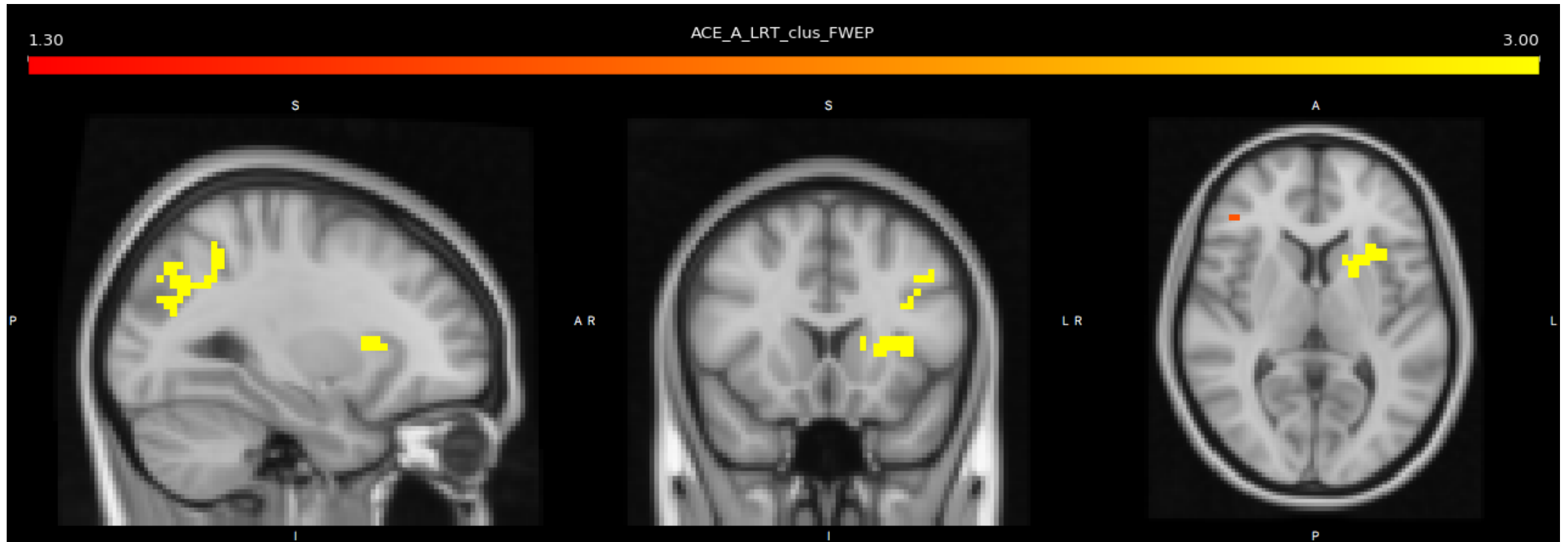
Filename	Description	Comments/Caveats
<i>Basic summaries</i>		
Stdev.nii	Phenotypic standard deviation	Computed and saved if image-wise inference is made.
<i>Heritability</i>		
h2_dist.pdf	Cumulative distribution of all in-mask $h^2$	
h2_hist.pdf	Histogram of positive in-mask $h^2$	Percentage of positive $h^2$ is provided.
ACE_A_h2.nii	Narrow sense heritability, $h^2$	Computed and saved if image-wise inference is made.
ACE_A_LRT.nii	Likelihood ratio test (LRT) statistic for testing $H_0: h^2=0$	Basis for all thresholding procedures. Computed and saved if image-wise inference is made.
ACE_A_LRT_vox_Pasym.nii	$-\log_{10}(\text{P-value})$ for testing $H_0: h^2=0$ using large sample parametric null distribution	Not trustworthy except for very large samples. Computed and saved if image-wise inference is made.

# Outputs

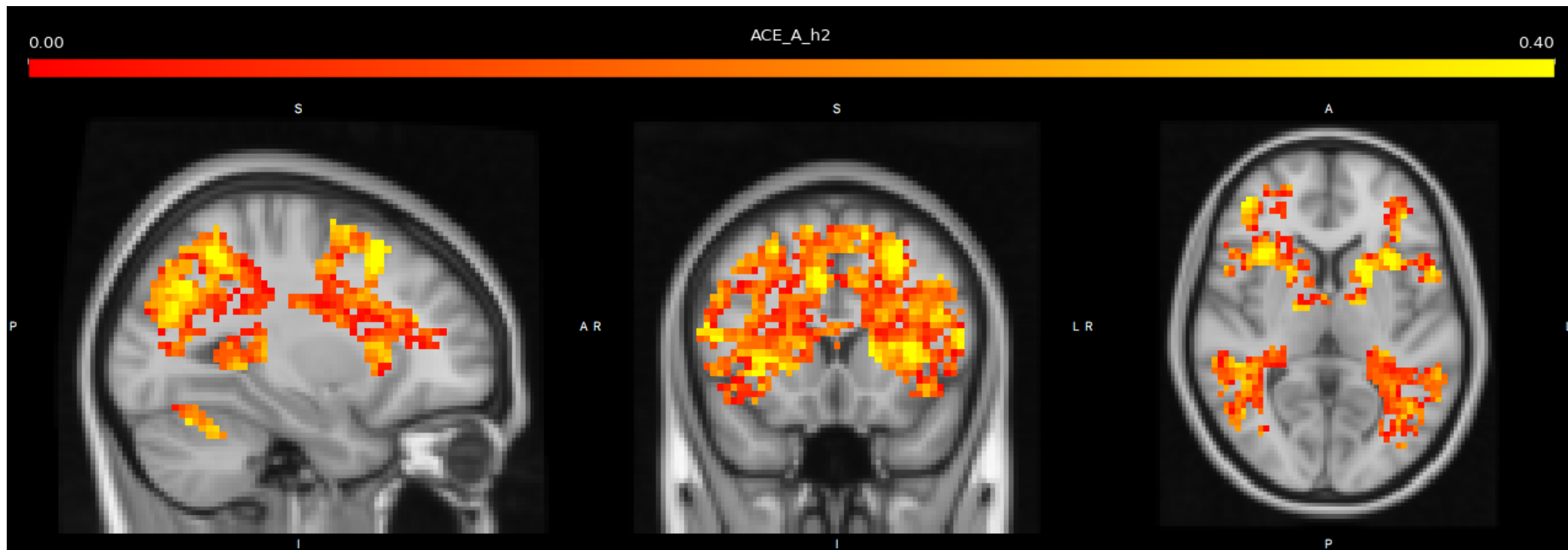
Additional outputs from permutation inference of APACE software for the **ACE** model

Filename	Description	Comments/Caveats
<b><i>Heritability</i></b>		
H0dist_mean.pdf	Null distribution of mean of all in-mask $h^2$	Permutation-based p-value is displayed in plot title.
H0dist_wh2.pdf	Null distribution of variance-weighted average of all in-mask $h^2$	Permutation-based p-value is displayed in plot title.
H0dist_median.pdf	Null distribution of median (Q2) of all in-mask $h^2$	Permutation-based p-value is displayed in plot title.
H0dist_q3.pdf	Null distribution of the third quartile (Q3) of all in-mask $h^2$	Permutation-based p-value is displayed in plot title.
H0dist_mGTmedian.pdf	Null distribution of mean of in-mask $h^2 \geq Q2(h^2)$	Permutation-based p-value is displayed in plot title.
H0dist_mGTq3.pdf	Null distribution of mean of in-mask $h^2 \geq Q3(h^2)$	Permutation-based p-value is displayed in plot title.
Pvals_h2.mat	Permutation-based p-values for summary statistics	Heritability summary measures include mean, variance-weighted average, Q2, Q3, mean of $h^2 \geq Q2(h^2)$ , and mean of $h^2 \geq Q3(h^2)$ .
H0dist_test_statistic.pdf	Null distribution of maximum LRT statistic	Permutation-based p-value is displayed in plot title. Only produced if

# FWE-corrected P-value Image



# Heritability Estimates



# Result Summary

	Heritability $h^2$ (aka $a^2$ )			Common Env. $c^2$		
	Estimate	95%CI	P-val	Estimate	95%CI	P-val
Mean	0.433	( 0.207 , 0.607 )	0.003	0.004	( 0.000 , 0.160 )	.
VarWtMean	0.417	( 0.199 , 0.618 )	0.003	0.002	( 0.000 , 0.145 )	.
AgHe	0.250	( -0.202 , 0.666 )	0.114	.	( . , . )	.
Median Q2	0.428	( 0.192 , 0.605 )	0.002	0.000	( 0.000 , 0.311 )	.
Q3	0.526	( 0.315 , 0.698 )	0.006	0.000	( 0.000 , 0.503 )	.
Mean( $\geq$ Q2)	0.534	( 0.317 , 0.699 )	0.009	0.137	( 0.000 , 0.385 )	.
Mean( $\geq$ Q3)	0.594	( 0.366 , 0.756 )	0.023	0.137	( 0.000 , 0.538 )	.
MaxLRT	6.336	( . , . )	0.128	.	( . , . )	.
MaxSize	97.000	( . , . )	0.018	.	( . , . )	.
MaxMass	360.264	( . , . )	0.029	.	( . , . )	.

- The APACE tool can be downloaded at <http://www.nisox.org/Software/APACE/>  
<https://github.com/NISOx-BDI/APACE>
- For more information, please refer to Chen, et al. (2019). Accelerated estimation and permutation inference for ACE modeling. *Human Brain Mapping* (Epub ahead of print). <https://doi.org/10.1002/hbm.24611>

**Thank you!**