

Authors:

Erick Rosete Beas — er165@uni-freiburg.de

Jessica Lizeth Borja Diaz — jb986@uni-freiburg.de

Principles of AI Planning

Exercise Sheet 10

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Exercise 10.1 - Affecting labels vs. orthogonality

Recall: For a transition system \mathcal{A} and a label l of \mathcal{A} , we say that l affects \mathcal{A} if \mathcal{A} has a transition $\langle s, l, t \rangle$ with $s \neq t$.

Prove the following: Let \mathcal{A}_i be an abstraction of some transition system \mathcal{T} with abstraction mapping α_i for $i \in \{1, 2\}$. If no label of \mathcal{T} affects both \mathcal{A}_1 and \mathcal{A}_2 , then α_1 and α_2 are orthogonal.

Take an arbitrary label $l \in \mathcal{T}$, by the premise we know that this label can affect at most one abstraction \mathcal{A}_i for $i \in \{1, 2\}$. If it doesn't affect any abstraction \mathcal{A}_i then there is no transition $\langle s, l, t \rangle \in \mathcal{T}$ such that $\alpha_1(s) \neq \alpha_1(t)$ or $\alpha_2(s) \neq \alpha_2(t)$.

If the label affects only one abstraction, we take the affected abstraction \mathcal{A}_i , we know there is at least one $\langle s, l, t \rangle \in \mathcal{T}$ such that $\alpha_i(s) \neq \alpha_i(t)$, but in the other abstraction \mathcal{A}_j where $j \in \{1, 2\}$ and $j \neq i$ for each transition $\langle s, l, t \rangle$ of \mathcal{T} we have $\alpha_j(s) = \alpha_j(t)$ as the label does not affect \mathcal{A}_j . Therefore no matter which label l is selected there is no transition $\langle s, l, t \rangle \in \mathcal{T}$ where $\alpha_i(s) \neq \alpha_i(t)$ for both $i \in \{1, 2\}$ then by definition α_1 and α_2 are orthogonal.

Exercise 10.2 - Potential heuristics: consistency constraints

Let $\Pi = \langle V, I, O, \gamma \rangle$ be an SAS^+ planning task in transition normal form, and let $\mathcal{F} = \{f_{v=d} \mid v \in V, d \in \mathcal{D}_v\}$ be the set of all atomic features over Π . Finally, let:

$$h(s) = \sum_{fact\ v=d} w_{v=d} \cdot f_{v=d}(s)$$

be the potential heuristic with potentials $w_{v=d}$ for all $v \in V, d \in \mathcal{D}_v$, such that for all $o \in O$, the following constraint is satisfied:

$$\sum_{fact\ v=d \text{ consumed by } o} w_{v=d} - \sum_{fact\ v=d \text{ produced by } o} w_{v=d} \leq cost(o)$$

Prove: Then h is consistent, i. e., $h(s) - h(t) \leq cost(o)$ for all transitions (s, o, t) in $\mathcal{T}(\Pi)$.

Taking an arbitrary transition (s, o, t) in $\mathcal{T}(\Pi)$ as it is consistent

$$\begin{aligned} h(s) - h(t) &\leq cost(o) \\ \iff \sum_{fact\ v=d} w_{v=d} \cdot f_{v=d}(s) + \sum_{fact\ v=d} w_{v=d} \cdot f_{v=d}(t) &\leq cost(o) \end{aligned}$$

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$$\iff \sum_{fact\ v=d} w_{v=d} \cdot f_{v=d}(s) + \sum_{fact\ v=d} w_{v=d} \cdot f_{v=d}(t) \leq cost(o)$$