Lab 9 report (mini-project)

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#1. Exploratory data analysis

```
# Save your input data file into your Project directory
fna.data <- "WisconsinCancer.csv"

# Input the data and store as wisc.df
wisc.df <- read.csv(fna.data, row.names=1)</pre>
```

#wisc.df

```
# We can use -1 here to remove the first column
wisc.data <- wisc.df[,-1]
```

```
# Create diagnosis vector for later
diagnosis <- factor(wisc.df[,1])</pre>
```

```
View(wisc.data)
head(wisc.data)
```

##		${\tt radius_mean}$	texture_mea	an perimet	er_mean	area_mean	smooth	ness_mean
##	842302	17.99	10.3	38	122.80	1001.0		0.11840
##	842517	20.57	17.7	77	132.90	1326.0		0.08474
##	84300903	19.69	21.2	25	130.00	1203.0		0.10960
##	84348301	11.42	20.3	38	77.58	386.1		0.14250
##	84358402	20.29	14.3	34	135.10	1297.0		0.10030
##	843786	12.45	15.7	70	82.57	477.1		0.12780
##		compactness	_mean concav	/ity_mean	concave.	.points_mea	n symme	etry_mean
##	842302	0.2	27760	0.3001		0.1471	.0	0.2419
##	842517	0.0	07864	0.0869		0.0701	.7	0.1812
##	84300903	0.3	15990	0.1974		0.1279	0	0.2069
##	84348301	0.2	28390	0.2414		0.1052	20	0.2597
##	84358402	0.3	13280	0.1980		0.1043	30	0.1809
##	843786	0.3	17000	0.1578		0.0808	39	0.2087
##		fractal_dime	ension_mean	radius_se	texture	e_se perime	ter_se	area_se
##	842302		0.07871	1.0950	0.9	9053	8.589	153.40
##	842517		0.05667	0.5435	0.7	7339	3.398	74.08
##	84300903		0.05999	0.7456	0.7	7869	4.585	94.03
##	84348301		0.09744	0.4956	1.1	1560	3.445	27.23
##	84358402		0.05883	0.7572	2 0.7	7813	5.438	94.44
##	843786		0.07613	0.3345	0.8	3902	2.217	27.19

```
smoothness_se compactness_se concavity_se concave.points_se
##
                                                0.05373
## 842302
                  0.006399
                                  0.04904
                                                                   0.01587
## 842517
                  0.005225
                                   0.01308
                                                0.01860
                                                                   0.01340
## 84300903
                  0.006150
                                   0.04006
                                                0.03832
                                                                   0.02058
## 84348301
                  0.009110
                                  0.07458
                                                0.05661
                                                                   0.01867
## 84358402
                  0.011490
                                  0.02461
                                                0.05688
                                                                   0.01885
## 843786
                                  0.03345
                  0.007510
                                                0.03672
                                                                   0.01137
##
            symmetry_se fractal_dimension_se radius_worst texture_worst
## 842302
                0.03003
                                     0.006193
                                                       25.38
                                                                     17.33
## 842517
                0.01389
                                     0.003532
                                                      24.99
                                                                     23.41
## 84300903
                 0.02250
                                     0.004571
                                                      23.57
                                                                     25.53
## 84348301
                                                      14.91
                                                                     26.50
                0.05963
                                     0.009208
## 84358402
                0.01756
                                     0.005115
                                                      22.54
                                                                     16.67
                                                      15.47
## 843786
                 0.02165
                                     0.005082
                                                                     23.75
##
            perimeter_worst area_worst smoothness_worst compactness_worst
## 842302
                      184.60
                                 2019.0
                                                   0.1622
                                                                      0.6656
## 842517
                      158.80
                                 1956.0
                                                   0.1238
                                                                      0.1866
## 84300903
                      152.50
                                 1709.0
                                                   0.1444
                                                                      0.4245
## 84348301
                                                   0.2098
                       98.87
                                  567.7
                                                                      0.8663
## 84358402
                      152.20
                                 1575.0
                                                   0.1374
                                                                      0.2050
## 843786
                      103.40
                                  741.6
                                                   0.1791
                                                                      0.5249
##
            concavity_worst concave.points_worst symmetry_worst
## 842302
                      0.7119
                                            0.2654
                                                            0.4601
## 842517
                      0.2416
                                                            0.2750
                                            0.1860
## 84300903
                      0.4504
                                            0.2430
                                                            0.3613
## 84348301
                      0.6869
                                            0.2575
                                                            0.6638
## 84358402
                      0.4000
                                            0.1625
                                                            0.2364
                      0.5355
                                                            0.3985
## 843786
                                            0.1741
##
            fractal_dimension_worst
## 842302
                             0.11890
## 842517
                             0.08902
                             0.08758
## 84300903
## 84348301
                             0.17300
## 84358402
                             0.07678
## 843786
                             0.12440
```

dim(wisc.data)

[1] 569 30

nrow(wisc.data)

[1] 569

length(wisc.data)

[1] 30

Q1. How many observations are in this dataset?

There are 569 observations in this dataset.

table(diagnosis)

```
## diagnosis
## B M
## 357 212
```

Q2. How many of the observations have a malignant diagnosis?

There are 212 observations having a malignant diagnosis.

```
length(grep("_mean", colnames(wisc.data)))
```

[1] 10

```
length(grep("_mean", rownames(wisc.data)))
```

[1] 0

Q3. How many variables/features in the data are suffixed with _mean?

There are 10 variables/features in the data are suffixed with _mean.

#2. Principal Component Analysis Performing PCA

Check column means and standard deviations colMeans(wisc.data)

radius_mean	texture_mean	perimeter_mean
1.412729e+01	1.928965e+01	9.196903e+01
area_mean	${\tt smoothness_mean}$	compactness_mean
6.548891e+02	9.636028e-02	1.043410e-01
${\tt concavity_mean}$	concave.points_mean	symmetry_mean
8.879932e-02	4.891915e-02	1.811619e-01
<pre>fractal_dimension_mean</pre>	radius_se	texture_se
6.279761e-02	4.051721e-01	1.216853e+00
perimeter_se	area_se	smoothness_se
2.866059e+00	4.033708e+01	7.040979e-03
compactness_se	concavity_se	concave.points_se
2.547814e-02	3.189372e-02	1.179614e-02
symmetry_se	fractal_dimension_se	radius_worst
2.054230e-02	3.794904e-03	1.626919e+01
texture_worst	perimeter_worst	area_worst
2.567722e+01	1.072612e+02	8.805831e+02
smoothness_worst	compactness_worst	concavity_worst
1.323686e-01	2.542650e-01	2.721885e-01
concave.points_worst	symmetry_worst	${\tt fractal_dimension_worst}$
1.146062e-01	2.900756e-01	8.394582e-02
	1.412729e+01	1.412729e+01

apply(wisc.data,2,sd)

```
##
               radius mean
                                        texture mean
                                                               perimeter mean
              3.524049e+00
                                        4.301036e+00
##
                                                                  2.429898e+01
##
                  area mean
                                     smoothness mean
                                                             compactness mean
              3.519141e+02
                                        1.406413e-02
                                                                 5.281276e-02
##
##
            concavity_mean
                                 concave.points_mean
                                                                 symmetry mean
              7.971981e-02
                                        3.880284e-02
                                                                  2.741428e-02
##
                                           radius_se
##
    fractal dimension mean
                                                                    texture se
##
              7.060363e-03
                                        2.773127e-01
                                                                  5.516484e-01
##
              perimeter_se
                                                                 smoothness se
                                             area_se
##
              2.021855e+00
                                        4.549101e+01
                                                                  3.002518e-03
##
            compactness_se
                                        concavity_se
                                                            concave.points_se
##
              1.790818e-02
                                        3.018606e-02
                                                                  6.170285e-03
##
                symmetry_se
                               fractal_dimension_se
                                                                  radius_worst
                                                                  4.833242e+00
##
              8.266372e-03
                                        2.646071e-03
##
             texture_worst
                                     perimeter_worst
                                                                    area_worst
##
              6.146258e+00
                                        3.360254e+01
                                                                  5.693570e+02
##
          smoothness_worst
                                   compactness_worst
                                                              concavity_worst
##
              2.283243e-02
                                        1.573365e-01
                                                                  2.086243e-01
##
      concave.points_worst
                                      symmetry_worst fractal_dimension_worst
##
              6.573234e-02
                                        6.186747e-02
                                                                  1.806127e-02
```

```
# Perform PCA on wisc.data
wisc.pr <- prcomp(wisc.data, scale = TRUE)
# Look at summary of results
summary(wisc.pr)</pre>
```

```
Importance of components:
                             PC1
                                    PC2
                                            PC3
                                                     PC4
                                                             PC5
                                                                     PC6
                                                                             PC7
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Standard deviation
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
  Cumulative Proportion
                          0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
                              PC8
                                     PC9
                                             PC10
                                                   PC11
                                                            PC12
                                                                    PC13
## Standard deviation
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
  Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
                             PC15
                                     PC16
                                             PC17
                                                      PC18
                                                              PC19
                                                                      PC20
                                                                             PC21
##
## Standard deviation
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion
                          0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
##
                             PC22
                                     PC23
                                                     PC25
                                                             PC26
                                                                     PC27
                                                                             PC28
                                             PC24
## Standard deviation
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
  Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                             PC29
                                     PC30
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?

From my results, 0.4427 (44.27%) of the original variance is caputured by the first principal components (PC1).

 ${\it Q5.}$ How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

Based on the Cumulative Proportion, 3 principal components (PCs) are required to describe at least 70% of the original variance in the data (Cumulative Proportion of PC3: 0.72636).

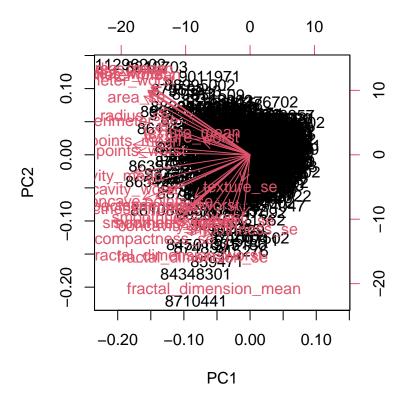
 ${\it Q6.}$ How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

Based on the Cumulative Proportion, 7 principal components (PCs) are required to describe at least 90% of the original variance in the data (Cumulative Proportion of PC7: 0.91010).

Interpreting PCA results

Q7. What stands out to you about this plot? Is it easy or difficult to understand? Why?

biplot(wisc.pr)

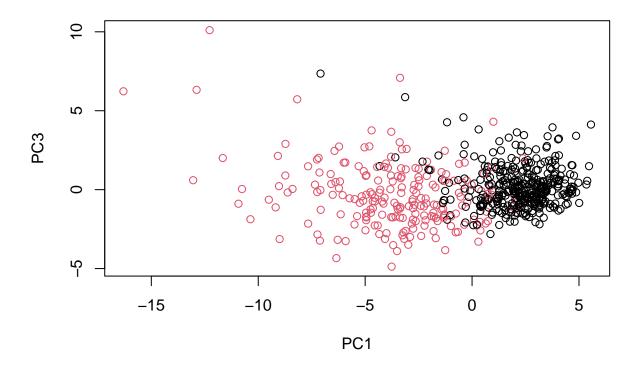


As this data contains a non-trivial number of observations and variables, this is a hot mess of a plot, which makes it is difficult to understand. We cannot clearly see the distribution pattern of observations and variables in this kind of plot. Thus, we will need to generate our own plots to make sense of this PCA result.

To make this plot ourselves we need access the PCA scores data.



Q8. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?

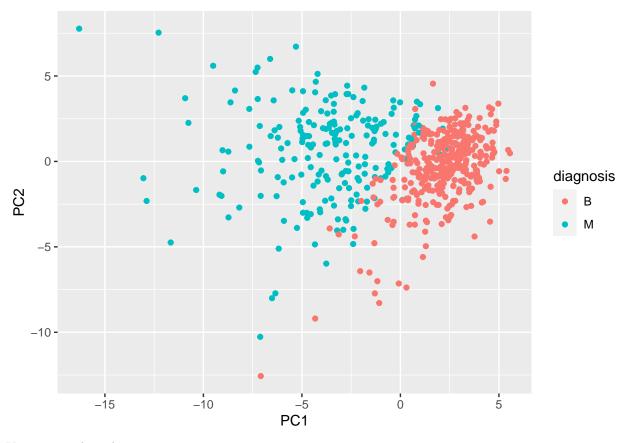


Because principal component 2 explains more variance in the original data than principal component 3, the first plot has a cleaner cut separating the two subgroups. For these plots, they indicate that principal component 1 is capturing a separation of malignant (red) from benign (black) samples. the principal component 2 explains less variance in the original data than principal component 1 but more variance than principal component 3. Thus, the first plot has a cleaner cut separating the two subgroups compared to the second plot (PC1 vs PC3).

```
# Create a data.frame for ggplot
df <- as.data.frame(wisc.pr$x)
df$diagnosis <- diagnosis

# Load the ggplot2 package
library(ggplot2)

# Make a scatter plot colored by diagnosis
ggplot(df) +
   aes(PC1, PC2, col=diagnosis) +
   geom_point()</pre>
```

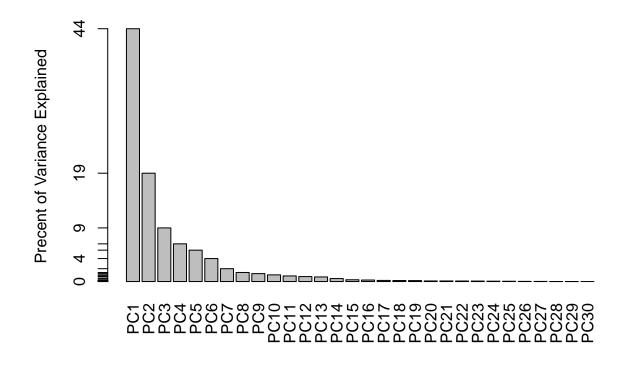


Variance explained

```
# Calculate variance of each component
pr.var <- wisc.pr$sdev^2
head(pr.var)</pre>
```

[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357

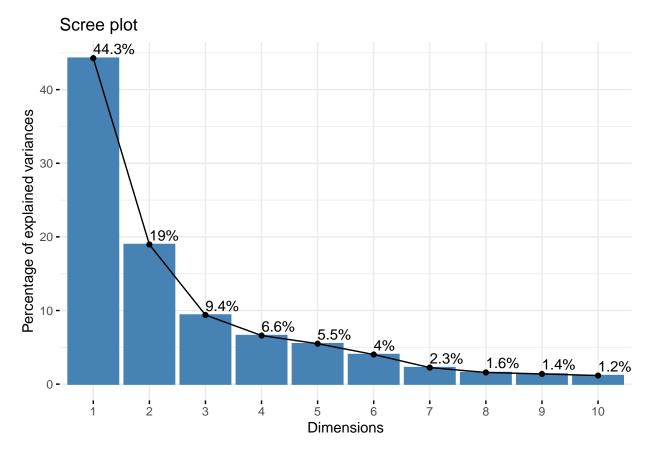




```
## ggplot based graph
#install.packages("factoextra")
library(factoextra)

## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

fviz_eig(wisc.pr, addlabels = TRUE)
```



Communicating PCA results $\mathbf{Q9}$. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean?

```
wisc.pr$rotation["concave.points_mean", 1]
```

[1] -0.2608538

The component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean is -0.2608538.

Q10. What is the minimum number of principal components required to explain 80% of the variance of the data?

```
var <- summary(wisc.pr)</pre>
var$importance[3,] < 0.8</pre>
##
    PC1
           PC2
                 PC3
                       PC4
                             PC5
                                   PC6
                                         PC7
                                               PC8
                                                     PC9
                                                          PC10
                                                                 PC11
                                                                       PC12
##
   TRUE
          TRUE
                TRUE
                      TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
          PC15
               PC16
                      PC17
                            PC18
                                 PC19
                                        PC20
                                              PC21
                                                    PC22
                                                         PC23
                                                                PC24
                                                                       PC25 PC26
## FALSE FALSE
   PC27 PC28 PC29
                      PC30
## FALSE FALSE FALSE
sum(var$importance[3,] < 0.8)</pre>
```

[1] 4

var

```
## Importance of components:
##
                             PC1
                                    PC2
                                            PC3
                                                    PC4
                                                             PC5
                                                                     PC6
                                                                             PC7
## Standard deviation
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
## Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
                                     PC9
                                                   PC11
                                                            PC12
##
                              PC8
                                            PC10
                                                                    PC13
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Standard deviation
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
##
                             PC15
                                     PC16
                                             PC17
                                                     PC18
                                                              PC19
                                                                      PC20
## Standard deviation
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
##
                             PC22
                                     PC23
                                            PC24
                                                    PC25
                                                             PC26
## Standard deviation
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
## Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                             PC29
                                     PC30
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

Based on the Cumulative Proportion, 5 principal components (PCs) are required to describe at least 80% of the original variance in the data (Cumulative Proportion of PC5: 0.84734).

#3. Hierarchical clustering

data.dist <- dist(data.scaled)</pre>

```
# Scale the wisc.data data using the "scale()" function
data.scaled <- scale(wisc.data)

#Calculate the (Euclidean) distances between all pairs of observations in the new scaled dataset</pre>
```

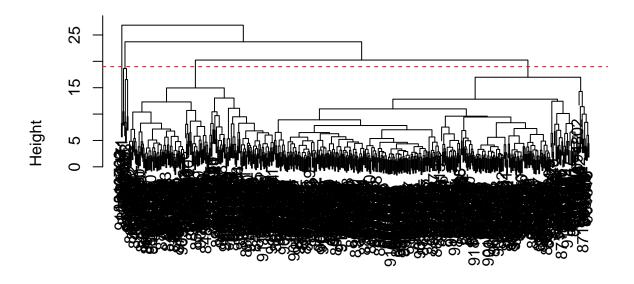
```
wisc.hclust <- hclust(data.dist, method = "complete")
wisc.hclust</pre>
```

```
##
## Call:
## hclust(d = data.dist, method = "complete")
##
## Cluster method : complete
## Distance : euclidean
## Number of objects: 569
```

Q11. Using the plot() and abline() functions, what is the height at which the clustering model has 4 clusters?

```
plot(wisc.hclust)
abline(h = 19, col="red", lty=2)
```

Cluster Dendrogram



data.dist hclust (*, "complete")

The height at which the clustering model has 4 clusters can be 19. Selecting number of clusters

```
wisc.hclust.clusters <- cutree(wisc.hclust, k = 4)</pre>
```

table(wisc.hclust.clusters, diagnosis)

```
## diagnosis
## wisc.hclust.clusters B M
## 1 12 165
## 2 2 5
## 3 343 40
## 4 0 2
```

Q12. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

```
wisc.hclust.clusters2 <- cutree(wisc.hclust, k = 2)
wisc.hclust.clusters3 <- cutree(wisc.hclust, k = 3)
wisc.hclust.clusters4 <- cutree(wisc.hclust, k = 4)
wisc.hclust.clusters5 <- cutree(wisc.hclust, k = 5)
wisc.hclust.clusters6 <- cutree(wisc.hclust, k = 6)
wisc.hclust.clusters7 <- cutree(wisc.hclust, k = 7)
wisc.hclust.clusters8 <- cutree(wisc.hclust, k = 8)
wisc.hclust.clusters9 <- cutree(wisc.hclust, k = 9)</pre>
```

```
wisc.hclust.clusters10 <- cutree(wisc.hclust, k = 10)</pre>
table(wisc.hclust.clusters2, diagnosis)
##
                       diagnosis
## wisc.hclust.clusters2
                         B M
##
                      1 357 210
##
                         0 2
table(wisc.hclust.clusters3, diagnosis)
##
                       diagnosis
## wisc.hclust.clusters3
                         В
##
                      1 355 205
##
                         2
                              5
##
                      3
                         0
                              2
table(wisc.hclust.clusters4, diagnosis)
##
                       diagnosis
## wisc.hclust.clusters4
                         B M
##
                      1 12 165
##
                             5
                      2
                         2
##
                      3 343 40
##
                          0
                              2
table(wisc.hclust.clusters5, diagnosis)
                       diagnosis
##
## wisc.hclust.clusters5
                         B M
##
                         12 165
##
                      2
                         0
                             5
##
                      3 343 40
##
                      4
                          2
                              0
                              2
##
table(wisc.hclust.clusters6, diagnosis)
##
                       diagnosis
## wisc.hclust.clusters6
                         В
                      1 12 165
##
##
                      2
                         0
                              5
##
                      3 331 39
##
                         2
                              0
                      4
                        12
##
                      5
                              1
##
                         0
```

table(wisc.hclust.clusters7, diagnosis)

```
##
                        diagnosis
## wisc.hclust.clusters7
                          В
                               М
                         12 165
##
##
                       2
                           0
                               3
                       3 331 39
##
##
                          2
                               0
                       5
##
                         12
##
                       6
                           0
                               2
                       7
                               2
##
                           0
```

table(wisc.hclust.clusters8, diagnosis)

##	diagnosis				
##	wisc.hclust.clusters8	В	М		
##	1	12	86		
##	2	0	79		
##	3	0	3		
##	4	331	39		
##	5	2	0		
##	6	12	1		
##	7	0	2		
##	8	0	2		

table(wisc.hclust.clusters9, diagnosis)

##	(diagn	osis
##	wisc.hclust.clusters9	В	M
##	1	12	86
##	2	0	79
##	3	0	3
##	4	331	39
##	5	2	0
##	6	12	0
##	7	0	2
##	8	0	2
##	9	0	1

table(wisc.hclust.clusters10, diagnosis)

```
diagnosis
##
                           В
                               М
## wisc.hclust.clusters10
##
                      1
                          12 86
                      2
                              59
##
                           0
##
                      3
                           0
                               3
##
                      4
                         331
                              39
##
                      5
                           0
                              20
                      6
                           2
                              0
##
##
                      7
                          12 0
##
                      8
                               2
##
                      9
                           0
                               2
##
                      10
```

As I explore how different numbers of clusters affect the ability of the hierarchical clustering to separate the different diagnoses above, by cutting into a different number of clusters between 2 and 10, I found that as the number of clusters increases, the capacity to separate the different diagnoses is higher. So, I can find a better cluster vs diagnoses match by cutting into a higher number of clusters than 4 (5 clusters can be better for a higher specificity).

Using different methods Q13. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

The method "ward.D2" gives my favorite results for the same data.dist dataset. As the method = "ward.D2" creates groups whose variance can be minimized within clusters. So, this has the effect of looking for spherical clusters with the process beginning with all points in individual clusters (bottom up) and then repeatedly merging a pair of clusters such that when merged there is a minimum increase in total within-cluster variance. This process continues until a single group including all points (the top of the tree) is defined, which really makes sense for me so it would be my favorite method.

#4. OPTIONAL: K-means clustering K-means clustering and comparing results

```
wisc.km <- kmeans(scale(wisc.data), centers= 2, nstart= 20)

table(wisc.km$cluster, diagnosis)

## diagnosis
## B M
## 1 343 37
## 2 14 175

table(wisc.hclust.clusters, diagnosis)</pre>
```

```
##
                          diagnosis
## wisc.hclust.clusters
                              В
                                  М
##
                         1
                            12 165
##
                              2
                                  5
##
                         3 343
                                 40
                                  2
##
                              0
```

Q14. How well does k-means separate the two diagnoses? How does it compare to your helust results?

```
table(wisc.hclust.clusters, wisc.km$cluster)
```

Clusters 1, 2, and 4 from the hierarchical clustering model can be interpreted as the cluster 1 equivalent from the k-means algorithm, and cluster 3 can be interpreted as the cluster 2 equivalent.

Based on the table here, k-means separates the two diagnoses well (the first can be interpreted as the group largely corresponding to malignant cells and the second can be seen as the group largely corresponding to benign cells). Compared to my helust results, k-means seems to separate the two diagnoses better as it has a higher sensitivity (same specificity) than helust does.

#5. Combining methods

We take the results of our PCA analysis and cluster in this space 'wisc.pr\$x'

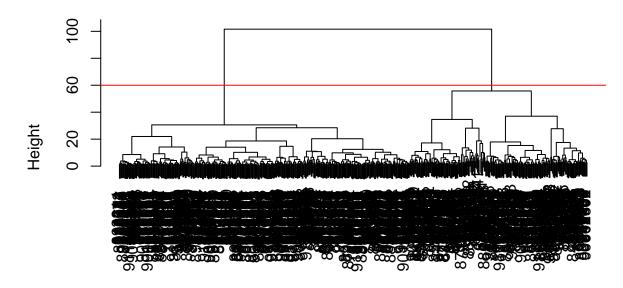
```
summary(wisc.pr)
```

```
## Importance of components:
##
                             PC1
                                    PC2
                                             PC3
                                                     PC4
                                                             PC5
                                                                     PC6
                                                                             PC7
## Standard deviation
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
## Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
##
                              PC8
                                     PC9
                                             PC10
                                                    PC11
                                                            PC12
                                                                    PC13
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Standard deviation
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
##
                             PC15
                                     PC16
                                              PC17
                                                      PC18
                                                              PC19
                                                                      PC20
## Standard deviation
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                             PC22
                                     PC23
                                             PC24
                                                     PC25
                                                             PC26
                                                                     PC27
## Standard deviation
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
## Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                             PC29
                                     PC30
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
wisc.pr.hclust <- hclust( dist(wisc.pr$x[,1:7]), method = "ward.D2" )</pre>
wisc.pr.hclust.clusters <- cutree(wisc.pr.hclust, k=2)</pre>
```

Plot my dendrogram

```
plot( wisc.pr.hclust )
abline (h = 60, col = "red")
```

Cluster Dendrogram



dist(wisc.pr\$x[, 1:7]) hclust (*, "ward.D2")

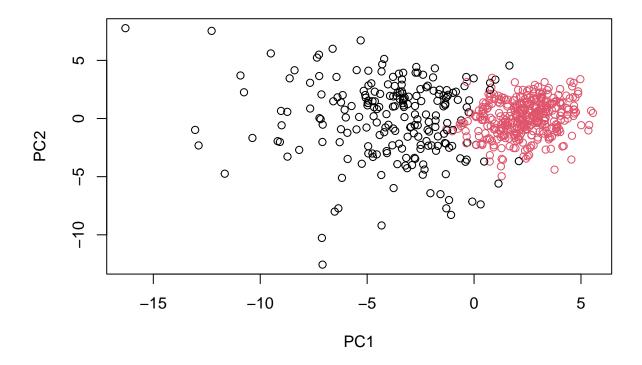
```
grps <- cutree(wisc.pr.hclust, k=2)
table(grps)

## grps
## 1 2
## 216 353

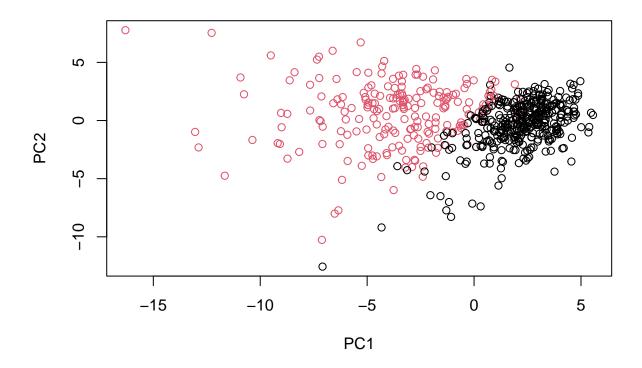
table(grps, diagnosis)

## diagnosis
## grps B M
## 1 28 188
## 2 329 24

plot(wisc.pr$x[,1:2], col=grps)</pre>
```



plot(wisc.pr\$x[,1:2], col=diagnosis)



(practice) Cut the tree into k=2 groups

```
grps <- cutree( wisc.pr.hclust, k = 2)
table(grps)</pre>
```

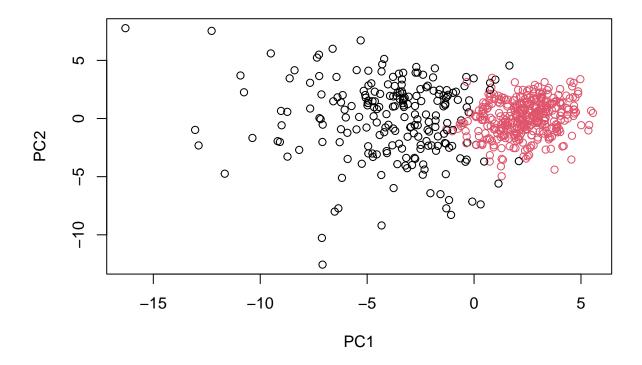
grps ## 1 2 ## 216 353

Cross table compare of diagnosis and my cluster groups

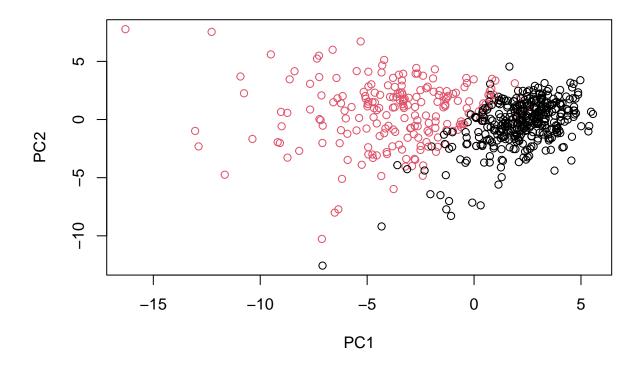
```
table(grps, diagnosis)
```

```
## diagnosis
## grps B M
## 1 28 188
## 2 329 24
```

plot(wisc.pr\$x[,1:2], col=grps)



plot(wisc.pr\$x[,1:2], col=diagnosis)



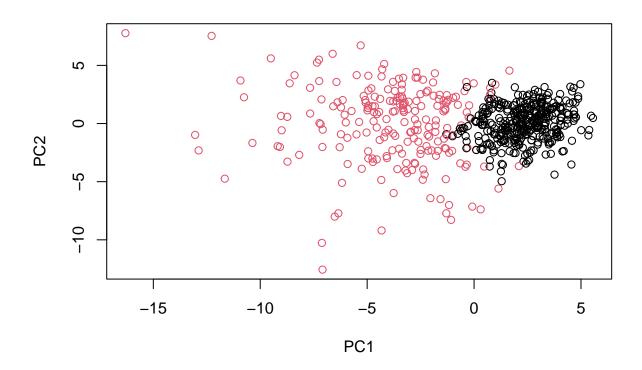
```
g <- as.factor(grps)
levels(g)

## [1] "1" "2"

g <- relevel(g,2)
levels(g)

## [1] "2" "1"

# Plot using our re-ordered factor
plot(wisc.pr$x[,1:2], col=g)</pre>
```



```
library(rgl)
plot3d(wisc.pr$x[,1:3], xlab="PC 1", ylab="PC 2", zlab="PC 3", cex=1.5, size=1, type="s", col=grps)

## Use the distance along the first 7 PCs for clustering i.e. wisc.pr$x[, 1:7]
wisc.pr.hclust <- hclust(dist(wisc.pr$x[,1:7]), method="ward.D2")

wisc.pr.hclust.clusters <- cutree(wisc.pr.hclust, k=2)</pre>
```

Q15. How well does the newly created model with four clusters separate out the two diagnoses?

```
# Compare to actual diagnoses
table(wisc.hclust.clusters, diagnosis)
```

```
## diagnosis
## wisc.hclust.clusters B M
## 1 12 165
## 2 2 5
## 3 343 40
## 4 0 2
```

table(wisc.pr.hclust.clusters,diagnosis)

diagnosis

```
## wisc.pr.hclust.clusters B M
## 1 28 188
## 2 329 24
```

The newly created model with four clusters separates out the two diagnoses really well.

Q16. How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table() function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

```
table(grps, diagnosis)
##
       diagnosis
##
          В
               М
   grps
##
         28
            188
##
      2 329
              24
table(wisc.km$cluster, diagnosis)
##
      diagnosis
##
          В
              М
##
       343
             37
##
        14 175
```

```
##
                          diagnosis
##
   wisc.hclust.clusters
                              В
                                  М
##
                             12 165
                         1
##
                         2
                              2
                                  5
##
                         3
                           343
                                 40
##
                              0
                                  2
```

table(wisc.hclust.clusters, diagnosis)

Before PCA, the k-means and hierarchical clustering models separate the diagnoses well. In the k-means model, group 1 can be interpreted as the group largely corresponding to benign cells, and group 2 can be seen as the group largely corresponding to malignant cells. In the hierarchical clustering model, group 1 can be seen as the group largely corresponding to malignant cells, and group 3 can be interpreted as the group largely corresponding to benign cells. Compared to my holust results, k-means seems to separate the two diagnoses better as it has a higher sensitivity (same specificity) than holust does.

#6. Sensitivity/Specificity **Accuracy** What proportion did we get correct if we call cluster 1 M and cluster 2 B

```
(329 + 188)/nrow(wisc.data)
```

```
## [1] 0.9086116
```

Sensitivity refers to a test's ability to correctly detect ill patients who do have the condition. In our example here the sensitivity is the total number of samples in the cluster identified as predominantly malignant (cancerous) divided by the total number of known malignant samples. In other words: TP/(TP+FN).

```
#
188/(188+24)
```

```
## [1] 0.8867925
```

Specificity relates to a test's ability to correctly reject healthy patients without a condition. In our example specificity is the proportion of benign (not cancerous) samples in the cluster identified as predominantly benign that are known to be benign. In other words: TN/(TN+FN).

```
329/(329 + 28)
```

[1] 0.9215686

Q17. Which of your analysis procedures resulted in a clustering model with the best specificity? How about sensitivity?

```
table(grps, diagnosis)
```

```
## diagnosis
## grps B M
## 1 28 188
## 2 329 24
```

table(wisc.km\$cluster, diagnosis)

```
## diagnosis
## B M
## 1 343 37
## 2 14 175
```

table(wisc.hclust.clusters, diagnosis)

```
##
                        diagnosis
## wisc.hclust.clusters
                           В
                               Μ
##
                          12 165
##
                       2
                           2
                              5
                       3 343
##
                              40
##
                           0
                               2
```

```
#specificity
PCA_hierarchical_clustering_spe <- 329/(329+28)
kmeans_clustering_spe <- 343/(343+14)
hierarchical_clustering_spe <- 343/(343+12+2)
PCA_hierarchical_clustering_spe</pre>
```

```
## [1] 0.9215686
```

kmeans_clustering_spe

[1] 0.9607843

hierarchical_clustering_spe

[1] 0.9607843

```
#sensitivity
PCA_hierarchical_clustering_sen <- 188/(188+24)
kmeans_clustering_sen <- 175/(175+37)
hierarchical_clustering_sen <- 172/(165+5+2+40)
PCA_hierarchical_clustering_sen</pre>
```

[1] 0.8867925

kmeans_clustering_sen

[1] 0.8254717

hierarchical_clustering_sen

[1] 0.8113208

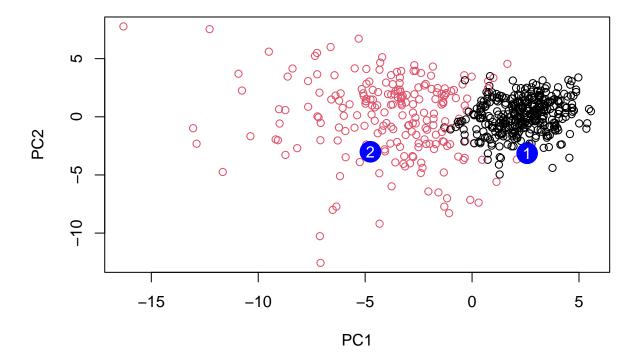
The k-means and hierarchical clustering resulted in a clustering model with the best specificity, and the PCA hierarchical clustering resulted in a clustering model with the best sensitivity.

#7. Prediction

```
#url <- "new_samples.csv"
url <- "https://tinyurl.com/new-samples-CSV"
new <- read.csv(url)
npc <- predict(wisc.pr, newdata=new)
npc</pre>
```

```
##
              PC1
                        PC2
                                   PC3
                                              PC4
                                                        PC5
                                                                   PC6
                                                                              PC7
## [1,] 2.576616 -3.135913 1.3990492 -0.7631950 2.781648 -0.8150185 -0.3959098
## [2,] -4.754928 -3.009033 -0.1660946 -0.6052952 -1.140698 -1.2189945 0.8193031
##
              PC8
                         PC9
                                   PC10
                                             PC11
                                                       PC12
                                                                 PC13
                                                                          PC14
## [1,] -0.2307350 0.1029569 -0.9272861 0.3411457 0.375921 0.1610764 1.187882
## [2,] -0.3307423 0.5281896 -0.4855301 0.7173233 -1.185917 0.5893856 0.303029
                        PC16
                                    PC17
                                                            PC19
                                                PC18
## [1,] 0.3216974 -0.1743616 -0.07875393 -0.11207028 -0.08802955 -0.2495216
  [2,] 0.1299153 0.1448061 -0.40509706 0.06565549
                                                      0.25591230 -0.4289500
              PC21
                         PC22
                                    PC23
                                               PC24
                                                           PC25
##
                                                                        PC26
## [1,] 0.1228233 0.09358453 0.08347651 0.1223396 0.02124121
                                                                 0.078884581
## [2,] -0.1224776 0.01732146 0.06316631 -0.2338618 -0.20755948 -0.009833238
                                         PC29
##
                PC27
                            PC28
## [1,] 0.220199544 -0.02946023 -0.015620933 0.005269029
## [2,] -0.001134152  0.09638361  0.002795349 -0.019015820
```

```
plot(wisc.pr$x[,1:2], col= g)
points(npc[,1], npc[,2], col="blue", pch=16, cex=3)
text(npc[,1], npc[,2], c(1,2), col="white")
```



Q18. Which of these new patients should we prioritize for follow up based on your results?

New patients in 2 (Patients 2). Based on my results, since patients in 2 are in the cluster identified as predominantly malignant (cancerous), we should prioritize these new patients for follow up.

#About this document

sessionInfo()

```
## R version 4.1.1 (2021-08-10)
## Platform: aarch64-apple-darwin20 (64-bit)
## Running under: macOS Big Sur 11.6
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/4.1-arm64/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/4.1-arm64/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
##
## attached base packages:
## [1] stats graphics grDevices utils datasets methods base
```

```
##
## other attached packages:
                        factoextra_1.0.7 ggplot2_3.3.5
## [1] rgl_0.107.14
##
## loaded via a namespace (and not attached):
                                                               haven_2.4.3
  [1] tidyselect 1.1.1 xfun 0.26
                                            purrr_0.3.4
  [5] carData 3.0-4
                          colorspace 2.0-2 vctrs 0.3.8
                                                               generics_0.1.1
                          yaml_2.2.1
                                            utf8_1.2.2
## [9] htmltools_0.5.2
                                                               rlang_0.4.11
## [13] pillar_1.6.3
                          ggpubr_0.4.0
                                            foreign_0.8-81
                                                               glue_1.4.2
## [17] withr_2.4.2
                          DBI_1.1.1
                                            readxl_1.3.1
                                                               lifecycle_1.0.1
## [21] stringr_1.4.0
                          cellranger_1.1.0
                                            munsell_0.5.0
                                                               ggsignif_0.6.3
## [25] gtable_0.3.0
                          zip_2.2.0
                                            htmlwidgets_1.5.4 evaluate_0.14
## [29] forcats_0.5.1
                                            knitr_1.36
                                                               rio_0.5.27
                          labeling_0.4.2
## [33] fastmap_1.1.0
                          curl_4.3.2
                                            fansi_0.5.0
                                                               highr_0.9
## [37] broom_0.7.9
                          Rcpp_1.0.7
                                            scales_1.1.1
                                                               backports_1.2.1
## [41] jsonlite_1.7.2
                          abind_1.4-5
                                            farver_2.1.0
                                                               hms_1.1.1
## [45] digest_0.6.28
                          openxlsx_4.2.4
                                            stringi_1.7.5
                                                               rstatix_0.7.0
## [49] dplyr 1.0.7
                          ggrepel_0.9.1
                                            grid_4.1.1
                                                               tools 4.1.1
## [53] magrittr_2.0.1
                          tibble_3.1.5
                                            crayon_1.4.1
                                                               tidyr_1.1.4
## [57] car_3.0-11
                          pkgconfig_2.0.3
                                            ellipsis_0.3.2
                                                               data.table_1.14.2
## [61] assertthat_0.2.1 rmarkdown_2.11
                                            R6_2.5.1
                                                               compiler_4.1.1
```