

## Part One

$\langle \text{Sentence} \rangle ::= \langle \text{NounPhrase} \rangle \langle \text{VerbPhrase} \rangle$   
 $\langle \text{NounPhrase} \rangle ::= \langle \text{Determiner} \rangle \langle \text{Noun} \rangle \langle \text{RelClause} \rangle \mid \langle \text{Name} \rangle$   
 $\langle \text{VerbPhrase} \rangle ::= \langle \text{TransVerb} \rangle \langle \text{NounPhrase} \rangle \mid \langle \text{NounPhrase} \rangle \langle \text{TransVerb} \rangle \mid \langle \text{IntransVerb} \rangle$   
 $\langle \text{RelClause} \rangle ::= \text{who } \langle \text{VerbPhrase} \rangle \mid \epsilon$

$\langle \text{Determiner} \rangle ::= \text{every} \mid \text{a}$   
 $\langle \text{Noun} \rangle ::= \text{man} \mid \text{woman} \mid \text{child}$   
 $\langle \text{Name} \rangle ::= \text{john} \mid \text{mary} \mid \text{eric} \mid \text{aiden}$   
 $\langle \text{TransVerb} \rangle ::= \text{loves} \mid \text{knows}$   
 $\langle \text{IntransVerb} \rangle ::= \text{lives} \mid \text{runs}$

$\text{det}(S, P1, P2, [\text{every}|X], X, \text{all}(S, \text{imply}(P1, P2)))$ .  
 $\text{det}(S, P1, P2, [\text{a}|X], X, \text{exists}(S, \text{and}(P1, P2)))$ .

$\text{noun}(N, [\text{man}|X], X, \text{man}(N))$ .  
 $\text{noun}(N, [\text{woman}|X], X, \text{woman}(N))$ .  
 $\text{noun}(N, [\text{child}|X], X, \text{child}(N))$ .

$\text{name}([\text{john}|X], X, \text{john})$ .  
 $\text{name}([\text{mary}|X], X, \text{mary})$ .  
 $\text{name}([\text{eric}|X], X, \text{eric})$ .  
 $\text{name}([\text{aiden}|X], X, \text{aiden})$ .

$\text{trVerb}(S, O, [\text{loves}|X], X, \text{loves}(S, O))$ .  
 $\text{trVerb}(S, O, [\text{knows}|X], X, \text{knows}(S, O))$ .

$\text{intrVerb}(S, [\text{lives}|X], X, \text{lives}(S))$ .  
 $\text{intrVerb}(S, [\text{runs}|X], X, \text{runs}(S))$ .

$\text{sen}(X0, X, P) :- \text{nounPh}(N, P1, X0, X1, P),$   
 $\quad \text{verbPh}(N, X1, X, P1)$ .

$\text{nounPh}(N, P1, X0, X, P) :- \text{det}(N, P2, P1, X0, X1, P),$   
 $\quad \text{noun}(N, X1, X2, P3),$   
 $\quad \text{relCl}(N, P3, X2, X, P2)$ .  
 $\text{nounPh}(N, P1, X0, X, P1) :- (\text{name}(X0, X, N))$ .

$\text{verbPh}(S, X0, X, NP) :- \text{trVerb}(S, O, X0, X1, P1),$   
 $\quad \text{nounPh}(O, P1, X1, X, NP)$ .  
 $\text{verbPh}(S, X0, X, TV) :- \text{nounPh}(O, P, X0, X1, TV),$   
 $\quad \text{trVerb}(O, S, X1, X, P)$ .  
 $\text{verbPh}(S, X0, X, IV) :- \text{intrVerb}(S, X0, X, IV)$ .

```
relCl(S,P1,[who|X1],X,and(P1,P2)) :- verbPh(S,X1,X,P2).  
relCl(_,P1,X,X,P1).
```

**Below is an example of the TransVerb swap.**

```
| ?- sen([every,child,who,knowns,aiden,runs],[],X).  
X = all(A,imply(and(child(A),knowns(A,aiden)),runs(A)))
```

```
| ?- sen([every,child,who,aiden,knowns,runs],[],X).  
X = all(A,imply(and(child(A),knowns(aiden,A)),runs(A)))
```

**Below are four more examples of at least length 10.**

```
| ?- sen([every,man,who,john,loves,loves,a,woman,who,runs],[],X).  
X = all(A,imply(and(man(A),loves(john,A)),exists(B,and(and(woman(B),runs(B)),loves(A,B)))))
```

```
| ?- sen([every,woman,who,eric,knowns,loves,a,woman,who,lives],[],X).  
X =  
all(A,imply(and(woman(A),knowns(eric,A)),exists(B,and(and(woman(B),lives(B)),loves(A,B)))))
```

```
| ?- sen([a,man,who,runs,every,child,who,loves,aiden,knowns],[],X).  
X = exists(A,and(and(man(A),runs(A)),all(B,imply(and(child(B),loves(B,aiden)),knowns(B,A)))))
```

```
| ?- sen([a,woman,who,lives,every,man,who,loves,a,child,knowns],[],X).  
X =  
exists(A,and(and(woman(A),lives(A)),all(B,imply(and(man(B),exists(C,and(child(C),loves(B,C)))),knowns(B,A))))) ?
```

Below I reverse tested the previous query because Dr. Wilson stated that I should show the program finding a previous input. While there are more than one possible solution to the following query, it does find the original. I have placed the match in bold.

```
| ?-  
sen(X,[],exists(A,and(and(woman(A),lives(A)),all(B,imply(and(man(B),exists(C,and(child(C)),loves(B,C)))),knowns(B,A)))))).
```

```
B = A  
X = [a,woman,who,lives,knowns,every,man,who,loves,a,child] ? ;
```

```
B = A  
C = A  
X = [a,woman,who,lives,knowns,every,man,who,a,child,loves] ? ;
```

```
X = [a,woman,who,lives,every,man,who,loves,a,child,knowns] ? ;
```

```
C = B  
X = [a,woman,who,lives,every,man,who,a,child,loves,knowns] ? ;
```

**Which ship carries tea?  
The French one.**

**Part2.2 with extra credit.**  
**Changes to program are in bold.**

**The extra credit has been commented out so I could include the original as well.**

```
% N is size of rows/columns, T is tour taken (as list of positions m(P1,P2))
knightTour(N,M,T) :- N2 is N*M, % N2 is the number of positions on the board (N*M)
kT(N,M,N2,[m(0,0)],T). % [m(0,0)] is starting position of the knight

% kT(N,M,N2,[m(P1,P2)|Pt],T)
% N is the row size
% M is the column size
% N2 is the number of positions on the board
% [m(P1,P2)|Pt] is the accumulator for the tour
% m(P1,P2) is the current position of the knight
% Pt (partial tour) is the list of previous positions of the knight
% T is the full tour

% Finished: Length of tour is equal to size of board and at a spot that is one valid
% move away from m(0,0).
% return accumulator as tour adding the final move back to m(0,0).
kT(_,_,N2,T,T) :- length(T,N2).
REPLACE THE LINE ABOVE ^^^ WITH THE LINE BELOW vvvvv FOR EXTRA CREDIT!
% kT(_,_,N2,[H|T],[m(0,0),H|T]) :- (H==m(1,2);H==m(2,1)),length([H|T],N2).

kT(N,M,N2,[m(P1,P2)|Pt],T) :-
    moves(m(P1,P2),m(D1,D2)), % get next position from current position
    D1>=0,D2>=0,D1<N,D2<M, % verify next position is within board dimensions
    \+ member(m(D1,D2),Pt), % next position has not already been covered in tour
    kT(N,M,N2,[m(D1,D2),m(P1,P2)|Pt],T). % append next position to front of accumulator

% 8 possible moves for a knight
% P1,P2 is knight's position, D1,D2 is knight's destination after one move
% Iterated list solution
moves(m(X,Y), m(U,V)) :-
    member(m(A,B), [m(1,2),m(1,-2),m(-1,2),m(-1,-2),m(2,1),m(2,-1),m(-2,1),m(-2,-1)]),
    U is X + A,
    V is Y + B.

% "Number Hacking" solution
offsets(N1,N2) :-
    member(N,[1,2]),member(B1,[1,-1]),member(B2,[1,-1]),
    N1 is N*B1, N2 is (3-N)*B2.
% moves(m(P1,P2),m(D1,D2)) :-
% offsets(A,B), D1 is P1+A, D2 is P2+B.
```