



For this Tutorial, while still aiming to grasp the concept of "program correctness", we would delve into Logical Equivalence and verify if select propositions are **tautology** or **contradiction**

We would be given a program already designed but with some lines of code redacted. The program would give an output based on the proposition we feed into it.

We would also engage our conditional **for, if and else-if** statements.

Consider the truth table for tautology below with a proposition **$p \vee \neg p$**

p	$\neg p$	$p \vee \neg p$
True	False	True
False	True	True

Practice 1

The code below is designed to receive the right syntax for $(p \vee q) \vee (q \implies p)$ and check if the logical expression is a tautology or contradiction while drawing the truth table for verification

```
In [3]: %pip install pandas
```

^C

Note: you may need to restart the kernel to use updated packages.

Collecting pandas

Downloading pandas-2.2.3-cp312-cp312-win_amd64.whl.metadata (19 kB)

Collecting numpy>=1.26.0 (from pandas)

Downloading numpy-2.1.1-cp312-cp312-win_amd64.whl.metadata (59 kB)

Requirement already satisfied: python-dateutil>=2.8.2 in c:\users\bistr\appdata\roaming\python\python312\site-packages (from pandas) (2.9.0.post0)

Collecting pytz>=2020.1 (from pandas)

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Collecting tzdata>=2022.7 (from pandas)

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Downloading tzdata-2024.2-py2.py3-none-any.whl (346 kB)

Installing collected packages: pytz, tzdata, numpy, pandas

Successfully installed numpy-2.1.1 pandas-2.2.3 pytz-2024.2 tzdata-2024.2

WARNING: The scripts f2py.exe and numpy-config.exe are installed in 'c:\Users\bistr\AppData\Local\Programs\Python\Python312\Scripts' which is not on PATH.

Consider adding this directory to PATH or, if you prefer to suppress this warning, use --no-warn-script-location.

In []:

In [2]: `import pandas as pd`
`import itertools`

In [5]: `print(pd.__version__)`

2.2.3

In [7]: `# Define a function to evaluate the logical expression $(p \vee q) \vee (q \rightarrow p)$`
`def evaluate_expression(p, q):`
 `return (p or q) or (p ** q)`

`# Create a list of all possible truth values for p and q`
`possible_truth_values = [(p, q) for p in [True, False] for q in [True, False]]`

`# Create a table to store the truth values and the results of the expression`
`table_data = []`

`# Evaluate the expression for each combination of truth values`
`for p, q in possible_truth_values:`
 `result = evaluate_expression(p, q)`
 `table_data.append((p, q, result))`

`# Create a DataFrame to display the truth table`
`df = pd.DataFrame(table_data, columns=['p', 'q', ' $(p \vee q) \vee (q \rightarrow p)$ '])`

`# Display the truth table`
`print(df)`

`print()`
`# Determine whether the logical expression is a tautology, contradiction, or neither`
`if all(df[' $(p \vee q) \vee (q \rightarrow p)$ ']):`
 `print(" $(p \vee q) \vee (q \rightarrow p)$ is a tautology.")`
`elif not any(df[' $(p \vee q) \vee (q \rightarrow p)$ ']):`
 `print(" $(p \vee q) \vee (q \rightarrow p)$ is a contradiction.")`
`else:`
 `print(" $(p \vee q) \vee (q \rightarrow p)$ is neither a tautology nor a contradiction.")`

	p	q	$(p \vee q) \vee (q \rightarrow p)$
0	True	True	True
1	True	False	True
2	False	True	True
3	False	False	1

$(p \vee q) \vee (q \rightarrow p)$ is a tautology.

Exercise 1

Complete the code below and state if the logical expression $(p \implies q) \vee p$ is a tautology or contradiction.

```
In [14]: # Define a function to evaluate the logical expression  $(p \rightarrow q) \vee p$ 
def evaluate_expression(p, q):
    # Return the expression
    # complete the code below
    #return  $(q ** p)$  or p #This ocde returns 1 for every time it evaluates
    return (not p or q) or p

# Create a List of all possible truth values for p and q
possible_truth_values = [(p, q) for p in [True, False] for q in [True, False]]

# Create a table to store the truth values and the results of the expression
table_data = []

# Evaluate the expression for each combination of truth values
for p, q in possible_truth_values:
    result = evaluate_expression(p, q)
    table_data.append((p, q, result))

# Create a DataFrame to display the truth table
df = pd.DataFrame(table_data, columns=['p', 'q', ' $(p \rightarrow q) \vee p$ '])

# Display the truth table
print(df)

print()
# Determine whether the expression is a tautology, contradiction, or 9neither
if all(df[' $(p \rightarrow q) \vee p$ ']):
    print(" $(p \rightarrow q) \vee p$  is a tautology.")
elif not any(df[' $(p \rightarrow q) \vee p$ ']):
    print(" $(p \rightarrow q) \vee p$  is a contradiction.")
else:
    print(" $(p \rightarrow q) \vee p$  is neither a tautology nor a contradiction.")
```

	p	q	$(p \rightarrow q) \vee p$
0	True	True	True
1	True	False	True
2	False	True	True
3	False	False	True

$(p \rightarrow q) \vee p$ is a tautology.

Practice 2

Recall that for two propositions to be logically equivalent, their truth values must be same regardless of the truth values of individual propositions.

Consider the proposition $(p \implies q) \wedge (r \implies q)$ **AND** $(p \wedge r) \implies q$. A program has been designed to check if the two propositions are logically equivalent or not.

```
In [7]: # Define the symbolic variables p, q, and r
p_values = [True, False]
q_values = [True, False]
r_values = [True, False]

# Create a table to store the truth values and results
table_data = []

# Generate all possible combinations of truth values for p, q, and r
for p, q, r in itertools.product(p_values, q_values, r_values):
    # Evaluate the expressions
    expr1_result = (not p or q) and (not r or q) # (q ** p) and (q ** r)
    expr2_result = (not (p and r) or q) # q ** (p and r)

    # Determine if they are equivalent
    equivalent = expr1_result == expr2_result

    # Append the values to the table
    table_data.append((p, q, r, expr1_result, expr2_result, equivalent))

# Create a DataFrame to display the truth table
import pandas as pd
df = pd.DataFrame(table_data, columns=['p', 'q', 'r', '(p → q) ∧ (r → q)', '(p ∧ r) → q', 'Equivalent'])

# Check if the expressions are equivalent for all rows
equivalent = all(df['Equivalent'])
# Display the truth table
print(df)
# Determine the result
if equivalent:
    print("The expressions are logically equivalent.")
else:
    print("The expressions are not logically equivalent.")
```

	p	q	r	$(p \rightarrow q) \wedge (r \rightarrow q)$	$(p \wedge r) \rightarrow q$	Equivalent
0	True	True	True	True	True	True
1	True	True	False	True	True	True
2	True	False	True	False	False	True
3	True	False	False	False	True	False
4	False	True	True	True	True	True
5	False	True	False	True	True	True
6	False	False	True	False	True	False
7	False	False	False	True	True	True

The expressions are not logically equivalent.

Exercise 2

Using the same concept as above complete the code below to check if the two propositions $p \wedge (p \implies q)$ **AND** $p \wedge q$ are logically equivalent. Also complete the code to draw the truth table

```
In [9]: # Define the symbolic variables p and q
p_values = [True, False]
q_values = [True, False]

# Create a table to store the truth values and results
table_data = []

# Generate all possible combinations of truth values for p and q
for p, q in itertools.product(p_values, q_values):
    # Evaluate the expressions
    # complete the code code below
    expr1_result = (p and (not p or q))
    expr2_result = (p and q)

    # Determine if they are equivalent
    equivalent = expr1_result == expr2_result

    # Append the values to the table
    table_data.append((p, q, expr1_result, expr2_result, equivalent))

# Create a DataFrame to display the truth table
import pandas as pd
df = pd.DataFrame(table_data, columns=['p', 'q', 'p ^ (p→ q)', 'q ^ p', 'Equivalent'])

# Check if the expressions are equivalent for all rows
equivalent = all(df['Equivalent'])

# Determine the result
if equivalent:
    print("The expressions are logically equivalent.")
else:
    print("The expressions are not logically equivalent.")

# Display the truth table
# insert code below
print(df)
```

The expressions are logically equivalent.

	p	q	$p \wedge (p \implies q)$	$q \wedge p$	Equivalent
0	True	True	True	True	True
1	True	False	False	False	True
2	False	True	False	False	True
3	False	False	False	False	True

Practice 3

Consider the following statement in English " **The square of every number is at least 0.**". A logical expression with the same meaning could be written as $\forall x (x^2 \geq 0)$

Write a program to check if the value holds true for a range of numbers between -10 to 10

```
In [ ]: # Define a function to check the condition for a given number
def check_condition(x):
    return x ** 2 >= 0

# Define the range of numbers to check (for example, from -10 to 10)
# Reason for the range is to save calculation time
for x in range(-10, 10):
    if not check_condition(x):
        print(f"The statement does not hold for {x}.")
        break
else:
    print("The statement holds for all numbers in the range.")
```

The statement holds for all numbers in the range.

Check if the program holds true when x is 2

```
In [ ]: check_condition(-2)
```

Out[]: True

```
In [1]: %pip install nbconvert
```



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Downloading bleach-6.1.0-py3-none-any.whl (162 kB)
Downloading jinja2-3.1.4-py3-none-any.whl (133 kB)
Downloading MarkupSafe-2.1.5-cp312-cp312-win_amd64.whl (17 kB)
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Downloading nbformat-5.10.4-py3-none-any.whl (78 kB)
Downloading pandocfilters-1.5.1-py2.py3-none-any.whl (8.7 kB)
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Downloading jupyterlab_pygments-0.3.0-py3-none-any.whl (15 kB)
Downloading tinycss2-1.3.0-py3-none-any.whl (22 kB)
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Downloading referencing-0.35.1-py3-none-any.whl (26 kB)
Downloading rpds_py-0.20.0-cp312-none-win_amd64.whl (214 kB)
Installing collected packages: webencodings, fastjsonschema, tinycss2, soupsieve, rpds-py, pandocfilters, mistune, markupsafe, jupyterlab-pygments, defusedxml, bleach, attrs, referencing, jinja2, beautifulsoup4, jsonschema-specifications, jsonschema, nbformat, nbclient, nbconvert
Successfully installed attrs-24.2.0 beautifulsoup4-4.12.3 bleach-6.1.0 defusedxml-0.7.1 fastjsonschema-2.20.0 jinja2-3.1.4 jsonschema-4.23.0 jsonschema-specifications-2023.12.1 jupyterlab-pygments-0.3.0 markupsafe-2.1.5 mistune-3.0.2 nbclient-0.10.0 nbconvert-7.16.4 nbformat-5.10.4 pandocfilters-1.5.1 referencing-0.35.1 rpds-py-0.20.0 soupsieve-2.6 tinycss2-1.3.0 webencodings-0.5.1
Note: you may need to restart the kernel to use updated packages.
```

WARNING: The script jsonschema.exe is installed in 'c:\Users\bistr\AppData\Local\Programs\Python\Python312\Scripts' which is not on PATH.

Consider adding this directory to PATH or, if you prefer to suppress this warning, use --no-warn-script-location.

WARNING: The script jupyter-trust.exe is installed in 'c:\Users\bistr\AppData\Local\Programs\Python\Python312\Scripts' which is not on PATH.

Consider adding this directory to PATH or, if you prefer to suppress this warning, use --no-warn-script-location.

WARNING: The script jupyter-execute.exe is installed in 'c:\Users\bistr\AppData\Local\Programs\Python\Python312\Scripts' which is not on PATH.

Consider adding this directory to PATH or, if you prefer to suppress this warning, use --no-warn-script-location.

WARNING: The scripts jupyter-dejavu.exe and jupyter-nbconvert.exe are installed in 'c:\Users\bistr\AppData\Local\Programs\Python\Python312\Scripts' which is not on PATH.

Consider adding this directory to PATH or, if you prefer to suppress this warning, use --no-warn-script-location.