

Tarefa Básica - Determinantes - Cálculo Geral

$$0 - 1 + 0$$

01 -

A) $\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -1 & 1 \end{vmatrix} \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix} \rightarrow \det = 1 - (-1)$
 $\det = 2$
 $1 + 0 + 0$

B) $\begin{vmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & -1 & 4 \\ 0 & 0 & 0 & 3 \\ 0 & 1 & 1 & 4 \end{vmatrix}$ 1. Cal (B22) 2. Cal (B42)

1. Cal (B22) $0 + 3 + 0$

$\begin{vmatrix} 1 & 0 & 3 \\ 0 & 0 & 3 \\ 0 & 1 & 4 \end{vmatrix} \begin{vmatrix} 1 & 0 \\ 0 & 0 \end{vmatrix} \det = 0 - 3$
 $\det = -3$
 $0 + 0 + 0$

1. Cal (B42) $0 + 0 + 0$

$\begin{vmatrix} 1 & 0 & 3 \\ 0 & -1 & 4 \\ 0 & 0 & 3 \end{vmatrix} \begin{vmatrix} 1 & 0 \\ 0 & -1 \end{vmatrix} \det = -3 - 0$
 $\det = -3$
 $-3 + 0 + 0$

$\det B = -3 - 3$
 $\det B = -6$

$$02- \begin{vmatrix} x^2 & 0 & x & -\frac{1}{10} \\ 7,5 & 0 & 5 & 2 \\ 10 & 0 & 4 & 2 \\ 1 & 1 & 1 & 1 \end{vmatrix} = 0$$

1. col (42)

↓

$$-5 + 8x^2 + 15x$$

~~$$\begin{vmatrix} x^2 & x & -0,1 \\ 7,5 & 5 & 2 \\ 10 & 4 & 2 \end{vmatrix} \begin{vmatrix} x^2 & x \\ 7,5 & 5 \\ 10 & 4 \end{vmatrix} = 0$$~~

$$10x^2 + 10x + 3$$

$$\det = (10x^2 + 10x + 3) - (8x^2 + 15x - 5) = 0$$

$$\det = 2x^2 - 5x - 2 = 0$$

$$\Delta = -(-5)^2 - 4 \cdot 2 \cdot (-2)$$

$$\Delta = 25 - 16$$

$$\Delta = 9$$

$$x = \frac{-5 \pm \sqrt{9}}{4} = \begin{cases} x_1 = -\frac{1}{2} \\ x_2 = -2 \end{cases}$$

03-

$$\begin{vmatrix} x & 0 & 0 & 3 \\ -1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{vmatrix}$$

3 *impr*
 \downarrow $0+0+0$

$$\begin{vmatrix} -1 & x & 0 & -1 & x \\ 0 & -1 & x & 0 & -1 \\ 0 & 0 & -1 & 0 & 0 \end{vmatrix} \det = -1, 3$$

$-1+0+0$

1 *impr*
 \downarrow $0+0+0$

$$\begin{vmatrix} x & 0 & 0 & x & 0 \\ -1 & x & 0 & -1 & x \\ 0 & 0 & -1 & 0 & 0 \end{vmatrix} \det = -1x^2 \rightarrow \boxed{-2x^3 + 1x^2 + 3}$$

$-1x^2+0+0$

-2 *Por*
 \downarrow $0+0+0$

$$\begin{vmatrix} x & 0 & 0 & x & 0 \\ -1 & x & 0 & -1 & x \\ 0 & -1 & x & 0 & -1 \end{vmatrix} \det = x^3, -2$$

x^3+0+0

04.

A =

$$\begin{vmatrix} x & 1 & 0 & 0 & 0 \\ 0 & x & 1 & 0 & 0 \\ 0 & 0 & x & 1 & 0 \\ 0 & 0 & 0 & x & k \\ 0 & 0 & 0 & 1 & x \end{vmatrix} \rightarrow \begin{vmatrix} x & 1 & 0 & 0 \\ 0 & x & 1 & 0 \\ 0 & 0 & x & k \\ 0 & 0 & 1 & x \end{vmatrix}$$

$0 + 1 \cdot k + 0$

↓

$$\det = x \cdot (x^3 - 1 \cdot k)$$
$$\det = x^4 - x^2 k$$

$$\begin{vmatrix} x & 1 & 0 & x & 1 \\ 0 & x & x & 0 & x \\ 0 & 1 & x & 0 & 1 \end{vmatrix}$$

$x^3 + 0 + 0$

$$\det \text{ final} = x \cdot (x^4 - x^2 k)$$

$$\det \text{ final} = x^5 - x^3 k$$

$$\begin{cases} f(x) = \det A \\ f(-2) = 8 \end{cases}$$

$$(-2)^5 - (-2)^3 k = 8$$

$$-32 + 8k = 8$$

$$8k = 8 + 32$$

$$8k = 40$$

$$k = \frac{40}{8}$$

$$\boxed{k = 5}$$