

Universidad autónoma de baja California

Ingeniería en computación

Inteligencia artificial

Meta 3.1 optimizacion función de rosenbrock

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a- Resultados para 10 vairbales con un rango de búsqueda de [-10,10]

Levenberg-Marquardt:

Variable Learning Rate Gradient Descent (GDX):

```
Iter 0: f(x) = 6.1480e+05 | delta_f| = 2.3534e+05 lr = 1.00e-03
                              |delta_f| = 1.8316e+02 lr = 5.60e-09
Iter 1000: f(x) = 7.5050e+00
                               delta_f| = 1.4249e+00 lr = 1.26e-04
Iter 2000: f(x) = 2.8582e+00
                               delta_f = 2.8406e+01 lr = 1.85e-04
Iter 3000: f(x) = 2.1320e+00
                               delta_f = 6.9247e-01 lr = 2.50e-03
Iter 4000: f(x) = 1.8006e+00
Iter 5000: f(x) = 1.5166e+00
                               delta_f| = 5.9967e-01 lr = 7.51e-03
Iter 6000: f(x) = 1.3282e+00
                               delta_f| = 5.5878e-01 lr = 7.83e-04
Iter 7000: f(x) = 1.1204e+00
                               delta_f| = 2.1758e+00 lr = 4.41e-05
Iter 8000: f(x) = 1.5959e + 00
                               delta_f| = 6.5491e+01 lr = 1.07e-06
Iter 9000: f(x) = 1.3416e+00
                              |delta_f| = 6.0404e+01 lr = 1.35e-07
Iter 10000: f(x) = 9.5935e-01
                               |delta_f| = 4.6692e+01 lr = 3.99e-07
                               delta_f
Iter 11000: f(x) = 4.0433e-01
                                        = 9.5636e+00 lr = 1.37e-05
                               |delta f
Iter 12000: f(x) = 2.7993e-01
                                         = 3.2951e-01 lr = 1.55e-03
Iter 13000: f(x) = 2.6864e-01
                                delta f
                                         = 1.9676e+01 lr = 2.30e-06
Iter 14000: f(x) = 1.2572e-01
                               |delta_f|
                                         = 1.2870e+01 lr = 6.68e-07
Iter 15000: f(x) = 2.2355e-02
                               |delta_f|
                                         = 1.5097e+00 lr = 6.27e-06
Iter 16000: f(x) = 6.3878e-03
                               |delta_f|
                                         = 6.7116e-02 lr = 1.76e-02
Iter 17000: f(x) = 2.1675e-03
                               delta_f
                                         = 1.3851e+00 lr = 5.26e-06
Iter 18000: f(x) = 1.8598e-04
                                delta_f
                                         = 1.7711e-01 lr = 1.30e-06
Iter 19000: f(x) = 3.9954e-05
Iter 20000: f(x) = 7.5267e-06
                                delta_f|
                                         = 1.9360e-01 lr = 3.16e-07
                                delta_f|
                                         = 8.0392e-02 lr = 3.69e-06
Iter 21000: f(x) = 7.4246e-07
                                delta_f|
                                         = 2.1422e-02 lr = 2.27e-05
Iter 22000: f(x) = 7.8582e-08
                                delta_f
                                         = 6.8619e-03 lr = 8.14e-08
Iter 23000: f(x) = 1.2981e-08
                                delta_f|
                                         = 3.1738e-04 lr = 1.30e-04
Iter 24000: f(x) = 2.8633e-09
                                delta_f|
                                         = 1.6258e-03 lr = 2.23e-07
Iter 25000: f(x) = 3.0747e-10
                                delta_f|
                                         = 1.5671e-05 lr = 1.59e-02
Iter 26000: f(x) = 4.1890e-11
                                delta_f|
                                        = 5.3991e-05 lr = 9.09e-05
                               delta_f
Iter 27000: f(x) = 4.5828e-12
                                        = 1.0901e-05 lr = 4.82e-03
Iter 28000: f(x) = 1.8452e-12
                                        = 4.1532e-05 lr = 3.12e-07
                                delta_f|
Iter 29000: f(x) = 2.0841e-13
                                        = 1.3776e-05 lr = 1.12e-07
                                delta_f|
Iter 30000: f(x) = 1.3858e-14
                               |delta_f|
                                        = 1.2111e-06 lr = 3.33e-05
Iter 31000: f(x) = 3.2150e-15
                                        = 2.9569e-07 lr = 1.10e-04
                               |delta_f|
Iter 32000: f(x) = 6.7787e-16 |delta_f| = 7.9241e-07 lr = 4.25e-07
norma gradiente < 1.0e-08
n=10 performance final = 1.2460e-16
solution: [[1.00000001]
[1.000000002]
```

b- Función de Rosenbrock para n par, dado aleatoriamente un punto inicial en el rango de [-10,10] para cada variable y n = 100

Levenberg-Marquardt:

Variable Learning Rate Gradient Descent (GDX):

```
ter 0: f(x) = 1.1093e+07 |delta_f| = 1.1317e+06 lr = 1.00e-03
ter 1000: f(x) = 3.6500e+02 |delta_f| = 1.6058e+03 lr = 1.32e-07
ter 2000: f(x) = 3.0195e+02 |delta_f| = 1.3484e+03 lr = 1.14e-06
ter 3000: f(x) = 3.0475e+02 |delta_f| = 1.4207e+03 lr = 2.80e-07
                                |delta_f|
ter 4000: f(x) = 2.9376e+02
                                          = 1.5597e+03 lr = 1.39e-07
ter 5000: f(x) = 2.1658e+02
                                |delta_f|
                                           = 9.8062e+02 lr = 1.63e-07
                                |delta_f|
|delta_f|
ter 6000: f(x) = 1.4334e+02
                                          = 5.6027e+00 lr = 1.44e-03
Tter 7000: f(x) = 1.6291e + 02
                                          = 6.8849e+02 lr = 5.15e-06
ter 8000: f(x) = 2.1545e+02 |delta_f| = 1.0842e+03 lr = 1.39e-07
ter 9000: f(x) = 1.1237e+02 |delta_f| = 5.6249e+00 lr = 9.73e-04
                                 |delta_f| = 7.3684e+00 lr = 8.76e-05
|delta_f| = 3.0933e+01 lr = 3.35e-05
ter 10000: f(x) = 1.0197e+02
Iter 11000: f(x) = 9.3363e+01
ter 12000: f(x) = 8.4294e+01
                                 |delta_f|
                                            = 1.4050e+01 lr = 5.87e-05
                                            = 5.3166e+00 lr = 2.64e-04
ter 13000: f(x) = 7.4661e+01
                                  |delta_f|
ter 14000: f(x) = 6.3965e+01
                                  |delta_f|
                                            = 4.1342e+01 lr = 2.09e-05
Iter 15000: f(x) = 5.9105e+01
                                  delta_f
                                            = 3.0834e+02 lr = 8.39e-06
ter 16000: f(x) = 6.8596e+01
                                 |delta_f|
                                            = 5.5697e+02 lr = 9.64e-07
                                            = 4.5169e + 02 lr = 1.33e - 08
ter 17000: f(x) = 4.8509e+01
                                  |delta_f|
Iter 18000: f(x) = 1.9365e+01
                                            = 3.9631e+00 lr = 7.89e-03
                                  |delta_f
ter 19000: f(x) = 1.4691e+01
                                  |delta_f|
                                            = 2.7264e+00 lr = 1.82e-03
ter 20000: f(x) = 1.2484e+01
                                  |delta_f|
                                            = 8.4265e+01 lr = 1.51e-05
ter 21000: f(x) = 9.1116e+00
                                  delta_f|
                                            = 3.8742e+00 lr = 5.88e-05
Iter 22000: f(x) = 9.0645e+00
                                  |delta_f|
                                            = 1.6783e+02 lr = 3.10e-06
ter 23000: f(x) = 4.2050e+00
                                  |delta_f|
                                            = 1.3321e+00 lr = 1.23e-02
                                  |delta_f|
                                            = 1.0381e+00 lr = 7.39e-03
ter 24000: f(x) = 3.5007e+00
ter 25000: f(x) = 2.9195e+00
                                  delta_f|
                                            = 9.3811e-01 lr = 2.56e-04
Iter 26000: f(x) = 2.3500e+00
                                  delta_f
                                            = 4.2310e+00 lr = 6.51e-05
ter 27000: f(x) = 3.2100e+00
                                  delta_f
                                            = 9.5576e+01 lr = 4.44e-07
ter 28000: f(x) = 1.3729e+00
                                  |delta_f|
                                            = 7.4313e+00 lr = 4.74e-03
    29000: f(x) = 9.7376e-01
                                  delta_f|
                                            = 6.6821e+00
                                                           lr = 2.55e-03
ter
ter 30000: f(x) = 7.2536e-01
                                            = 5.6156e-01 lr = 4.91e-04
                                  delta_f
ter 31000: f(x) = 8.0236e-01
                                  |delta_f|
                                            = 3.9277e+01 lr = 4.01e-07
                                            = 3.6800e-01 lr = 2.85e-03
ter 32000: f(x) = 2.7685e-01
                                  |delta_f|
ter 33000: f(x) = 1.4527e-01
                                  |delta_f|
                                            = 9.5253e+00
                                                          lr = 2.57e-05
Iter 34000: f(x) = 6.6119e-02
                                  delta_f
                                            = 8.7754e+00 lr = 4.01e-08
ter 35000: f(x) = 1.3741e-02
                                  delta_f|
                                            = 1.2249e-01 lr = 3.52e-04
Iter 36000: f(x) = 2.3242e-03
                                            = 7.1616e-02 lr = 5.18e-02
                                  delta_f
ter 37000: f(x) = 6.9038e-04
                                  |delta_f|
                                            = 4.4122e-01 lr = 5.39e-05
ter 38000: f(x) = 7.7478e-05
                                 |delta_f|
                                            = 7.8768e-03 lr = 5.12e-02
                                 |delta_f|
ter 39000: f(x) = 1.3096e-05
                                            = 9.4703e-02 lr = 4.48e-07
```

```
Iter 39000: f(x) = 1.3096e-05
                                     |delta_f| = 9.4703e-02 lr = 4.48e-07
Iter 40000: f(x) = 1.9946e-06
                                    |delta_f| = 1.2632e-03 lr = 2.22e-03
Iter 41000: f(x) = 2.4726e-07
                                     |delta_f| = 1.1165e-03 lr = 1.65e-04
                                    Iter 42000: f(x) = 5.2139e-08
Iter 43000: f(x) = 5.7324e-09
Iter 44000: f(x) = 7.2443e-10
                                     |delta_f| = 2.7846e-05 lr = 1.27e-04
Iter 45000: f(x) = 8.8069e-11
                                    |delta_f| = 1.1535e-04 lr = 6.42e-07
|delta_f| = 1.3356e-06 lr = 5.19e-03
|delta_f| = 4.1783e-07 lr = 6.39e-03
Iter 46000: f(x) = 1.6709e-11
Iter 47000: f(x) = 2.2324e-12
Iter 48000: f(x) = 2.1849e-13
Iter 49000: f(x) = 2.4928e-14
                                    |delta_f| = 1.4120e-07 lr = 4.32e-03
Iter 50000: f(x) = 2.9642e-15 |delta_f| = 1.3549e-07 |delta_f| = 1.3549e-07 |delta_f| = 5.1159e-07 |delta_f| = 5.1159e-07 |delta_f| = 5.1159e-07 |delta_f| = 5.1159e-07
norma gradiente < 1.0e-08
n=100 performance final = 1.2315e-16
solution: [[1.
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```

c- Función de Rosenbrock para n par, dado aleatoriamente un punto inicial en el rango de [-10,10] para cada variable y n = 1000

Levenberg-Marquardt:

Variable Learning Rate Gradient Descent (GDX):

```
Iter 0: f(x) = 9.7902e+07 |delta_f| = 3.3458e+06 lr = 1.00e-03
Iter 10000: f(x) = 1.5261e+03 |delta_f| = 3.5779e+03 lr = 8.19e-08
Iter 20000: f(x) = 1.8872e+02 |delta_f| = 1.0005e+03 lr = 5.33e-09
Iter 30000: f(x) = 1.2028e+01 |delta_f| = 1.0936e+02 lr = 1.08e-08
Iter 40000: f(x) = 3.1596e-05 |delta_f| = 5.0186e-03 lr = 1.67e-02
Iter 50000: f(x) = 5.9825e-14 |delta_f| = 2.5611e-07 lr = 2.96e-04
norma gradiente < 1.0e-08
n=1000 performance final = 1.2349e-16
```

d- Función de Rosenbrock para n par, dado aleatoriamente un punto inicial en el rango de [-100,100] para cada variable y n = 1000

```
0: f(x) = 9.7593e+11 | ||grad|| = 3.3391e+09 | gama = 1.0000e-03 | ||x_norm|| = 1.8004e+03
Converged at iteration 5
n=1000 performance final =1.22e-11
solucion : [1.
                      0.99999999 1
                                  0.99999999 1.
                                             0.99999999 0.99999996
            0.99999999 1.
                                  0.99999999
                                  0.9999999
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```

Variable Learning Rate Gradient Descent (GDX):

En esta opcion el algoritmos tardo mucho y al parecer no encontró satifactoriamente el resultado:

```
1 - 10 variables - rango [-10,10]
2 - 100 variables - rango [-10,10]
3 - 1000 variables - rango [-10,10]
4 - 1000 variables - rango [-100,100]
5 - salir
: 4
Iter 0: f(x) = 9.1828e+11 | delta_f| = 3.2034e+09 lr = 1.00e-05
Iter 10000: f(x) = 1.2253e+04 | delta_f = 4.2025e+03 | lr = 8.11e-05
Iter 20000: f(x) = 1.2012e+04 | delta_f| = 1.1705e+02 | lr = 9.25e-06
Iter 30000: f(x) = 1.1910e+04 | delta_f| = 1.1828e+02 lr = 8.81e-06
                                                                                          |delta_f| = 8.0766e+01 lr = 1.34e-05
Iter 40000: f(x) = 1.1817e+04
                                                                                          |delta f| = 2.2028e+04 lr = 4.68e-07
Iter 50000: f(x) = 1.4974e+04
Iter 60000: f(x) = 1.1640e+04 | delta_f| = 4.7756e+02 | lr = 1.89e-06
Iter 70000: f(x) = 1.9347e+04 | delta_f| = 3.6533e+04 | lr = 5.32e-09
Iter 80000: f(x) = 2.0554e+04 | delta_f| = 3.9494e+04 | delta_f| = 3.9494e+04 | delta_f|
Iter 90000: f(x) = 1.6122e+04 | delta_f| = 2.8100e+04 | delta_f| = 2.8100e+0
Iter 100000: f(x) = 1.1311e+04 | delta_f| = 2.6875e+01 | lr = 2.78e-05
Iter 110000: f(x) = 1.1226e+04 | delta_f| = 1.0594e+02 | lr = 8.64e-06
Iter 120000: f(x) = 2.0165e+04 | delta_f| = 3.9093e+04 lr = 8.47e-09
```

```
Iter 920000: f(x) = 8.8091e+03 |delta_f| = 2.1642e+04 lr = 2.82e-09
Iter 930000: f(x) = 4.8373e+03 | delta_f| = 1.2001e+03 | lr = 3.09e-06
Iter 940000: f(x) = 4.9741e+03 |delta_f| = 4.8386e+03 lr = 1.33e-07 Iter 950000: f(x) = 4.6834e+03 |delta_f| = 1.3583e+01 lr = 1.91e-05
Iter 960000: f(x) = 4.6113e+03 | delta_f | = 1.2595e+01 | lr = 3.38e-04
Iter 970000: f(x) = 4.5418e+03 | delta_f| = 2.8710e+02 | lr = 5.41e-06 | Iter 980000: f(x) = 7.0417e+03 | lelta_f| = 1.7097e+04 | lr = 2.65e-07
Iter 990000: f(x) = 4.5187e+03 | delta_f | = 3.5705e+03 | lr = 1.76e-04
Iter 1000000: f(x) = 4.3310e+03 |delta_f| = 1.2128e+01 | lr = 2.96e-04
n=1000 performance final = 4.3310e+03
solution: [[ 0.99999993]
 [ 0.9999985]
 [ 0.9999993]
 [ 0.99999985]
 [-4.12410601]
 [17.01437278]
 [ 0.9999993]
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            [ כוכבבבבים ]
            [-2.440087 ]
            [ 5.96078952]
           [ 0.9999993]
            [ 0.99999985]
            [ 0.99999992]
            [ 0.99999984]
            [ 5.47928021]
            [30.02656532]
            [ 0.99999993]
            [ 0.99999985]
            [ 1.00002046]
            [ 1.00004099]
            [ 0.9999993]
            [ 0.99999985]
```