CLASSIFICATIONS

Order from Chaos



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Aarhus University

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- 1 Variables
 - Categorical Variables
 - Continuous Variables
 - Converting Variable Types
- 2 Classifications
 - Logistic Regression
 - K-Means
 - Hierarchies
 - Random Forests
 - Networks

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Types of Variables

Variables can be classed into a multitude of types. The most common classification system knows:

Categorical Variables

- also known as Qualitative Variables
- Scales can be either:
 - Nominal
 - Ordinal

Continuous Variables

- also known as Quantitative Variables
- Scales can be either
 - Discrete
 - Continuous

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Categorical Variables

Categorical variables are those variables which **establish and fall into distinct groups and classes**.

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- assign each unit of the population to one of a finite number of groups
- can sometimes be ordered

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Categorical Variables (Examples)

Examples of categorical variables:

- Biome Classifications (e.g. "Boreal Forest", "Tundra", etc.)
- Sex (e.g. "Male", "Female")
- Hierarchy Position (e.g. " α -Individual", " β -Individual", etc.)
- Soil Type (e.g. "Sandy", "Mud", "Permafrost", etc.)
- Leaf Type (e.g. "Compound", "Single Blade", etc.
- Sexual Reproductive Stage (e.g. "Juvenile", "Mature", etc.)
- Species Membership
- Family Group Membership
- ...

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Examples of categorical variables:

- Temperature
- Precipitation
- Weight
- pH
- Altitude
- Group Size
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Continuous variables can be converted into categorical variables via a method called **binning**:

Given a variable range, one can establish however many "bins" as one wants. For example:

- Given a temperature range of 271K 291K, there may be 4 bins of equa size:
 - Bin A: 271K < X < 276K
 - Bin B: 276K < X < 281K
 - Bin C: $281K < X \le 286K$
 - Bin D: $286K < X \le 291K$

Whilst a **continuous variable** can be both *continuous* and *categorical*, a **categorical variable** can only ever be *categorical*!

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Confusion Of Units



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Theory

Logistic Regression

glm(..., family=binomial(link='logit')) in base R

Purpose: Understand how certain variables drive distinct outcomes.

- - Variable values are **independent** (not paired)
- - Absence of influential outliers
 - Absence of multi-collinearity

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Purpose: Understand how certain variables drive distinct outcomes.

■ Down to *Study-Design*:

Need for Post-Hoc Tests:

- Variable values are **independent** (not paired)
- Binary logistic regression: response variable is binary
- Ordinal logistic regression: response variable is ordinal

Assumptions:

- Absence of influential outliers
 - Absence of influential outliers
 - Absence of multi-collinearity
 - Predictor Variables and log odds are related in a linear fashion

Example - The Data

```
## 68 0 3 male 19
## 69 1 3 female 17
## 70 0 3 male 26
## 71 0 2 male 32
## 72 0 3 female 16
## 73 0 2 male 21
```

 \rightarrow Let's see if there is a good explanation for **Survival** (Survived) to be had based off of *Passenger class* (Pclass), *sex* (Sex), and *age* (Age). Was it really "Women and children first"?

Example - The Model

Number of Fisher Scoring iterations: 5

```
Logistic_Mod <- glm(Survived ~., family=binomial(link='logit'), data = train_df)
summary (Logistic Mod)
## Call:
## glm(formula = Survived ~ ., family = binomial(link = "logit"),
      data = train df)
## Deviance Residuals:
     Min
             10 Median 30 Max
## -2.745 -0.690 -0.405 0.651 2.455
## Coefficients:
             Estimate Std. Error z value Pr(>|z|)
## (Intercept) 5.11787 0.51998 9.84 < 2e-16 ***
         -1.29567 0.14362 -9.02 < 2e-16 ***
## Pclass
## Sexmale -2.45459 0.21484 -11.43 < 2e-16 ***
## Age
         -0.03867 0.00794 -4.87 1.1e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 896.44 on 663 degrees of freedom
## Residual deviance: 604.61 on 660 degrees of freedom
## ATC: 612.6
```

Example - Explanation & Prediction

Obviously, the coefficients of our model can't be **explained** the same way as typical regression coefficients since we are interested in survival probabilities between 0 and 1. However, we can interpret the **direction** and **strength** of effects as well as their statistical significance at a glance: Clearly, women of a young age in first class had the highest survival rate. How do we know this? As class increases (from 1 to 3), survival probability decreases (-1.2957). Furthermore, men had, on average, a much lower survival rate than women (-2.4546). Lastly, increasing age negatively affected survival chances (-0.0387).

But how sure can we be of our model accuracy? We can test it by **predicting** some new data and **validating** our predictions:

```
fitted.results <- predict(Logistic_Mod, newdata-test_df, type='response') # predict on test data fitted.results <- ifelse(fitted.results > 0.5 , 1, 0) # if predicted survival probability above .5 assume survival misclasificError <- mean(fitted.results != test_df$survived) # compare actual data with predictions print(paste('Accuracy',1-misClasificError)) # output
```

[1] "Accuracy 0.8"

Theory

K-Means Clustering

Mclust() in mclust package

Purpose: Identify a number of *k* clusters in our data.

- Variance of the distribution of each variable is spherica
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 - \blacksquare Prior probability for all k clusters are the same

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Example - The Data

data("iris")

```
head(iris)
##
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1
              5.1
                           3.5
                                        1.4
                                                     0.2
                                                          setosa
## 2.
              4.9
                           3.0
                                        1.4
                                                     0.2
                                                          setosa
## 3
              4.7
                           3.2
                                        1.3
                                                     0.2
                                                          setosa
              4.6
                           3.1
                                        1.5
                                                     0.2
## 4
                                                          setosa
## 5
              5.0
                          3.6
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                                                     0.4
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```

→ Let's see if we can accurately identify the Species contained within the data set by clustering according to Sepal.Length, Sepal.Width, Petal.Length, and Petal.Width.

mclust is capable of identifying the statistically most appropriate number of clusters for the data set. Here, we decide to limit the number of clusters to the number of species present so we can test how well the prediction went.

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Example - The Data

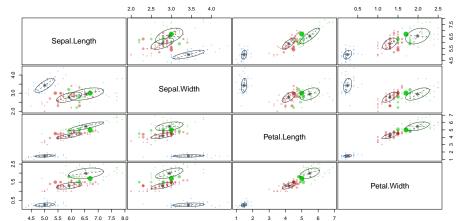
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Example - The Model



Example - Explanation & Prediction

K-means clusters can be interpreted to a certain degree. For example, by calling <code>Mclust_mod[["parameters"]][["mean"]]</code> we can assess the mean value of each cluster for each variable. These allow for some biological interpretation. Personally, I prefer a visualization as seen on the previous slide. Clearly, <code>Petal.Length</code>, and <code>Petal.Width</code> are extremely good separators for our different clusters with the green and red clusters overlapping a lot in <code>Sepal.Length</code> and <code>Sepal.Width</code> space.

But how sure can we be of our model accuracy? We can test it by **predicting** the cluster membership and **validating** our predictions against the real data:

```
Mclust_pred <- predict.Mclust(Mclust_mod, iris[,-5]) # prediction
# extract predicted species number
fitted.results <- Mclust_pred$classification
# compare actual data with predictions
misClasificError <- mean(fitted.results != as.numeric(iris$Species))
print(paste('Accuracy', 1-misClasificError)) # output</pre>
```

[1] "Accuracy 0.966666666666667"

Attention! We wouldn't want to do this in a real analysis. There, we would like to split the data in

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Attention! We wouldn't want to do this in a real analysis. There, we would like to split the data in training and test data like we did with the logistic regression example.

[1] "Accuracy 0.966666666666667"

Theory

Hierarchical Clustering

hclust() in base R or rpart() in rpart package and many others

Purpose: Build a decision tree for classification of our data.

very easy to explain and if

Easy to visualize.

- Easily handle qualitative predictors without the need to create dummy variables.
- Very sensitive to the choice of linkage.
- Generally do not have the same level of predictive accuracy as some of the other regression and classification approaches.
- Irees can be very non-robust

Disadvantages

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→ Again, let's see if we can accurately identify the Species contained within the data set by clustering according to Sepal. Length, Sepal. Width, Petal. Length, and Petal. Width.

hclust () can only handle distance matrices. We generate one between the numeric components of our data set as seen below.

```
dist_mat <- dist(iris[, -5])</pre>
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A distance matrix stores information about the dissimilarity of different observations

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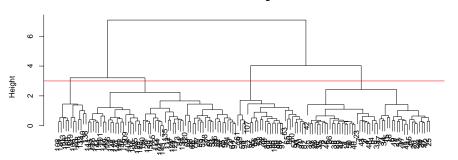
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Example - The Model

```
clusters <- hclust(dist_mat)
plot(clusters)
abline(h = 3, col = "red")</pre>
```

Cluster Dendrogram



dist_mat hclust (*, "complete")

Example - Explanation & Prediction

Obviously, our initial dendrogramm recognizes way more clusters than we are interested in. In fact, it recognizes as many clusters as their are observations. We may wish to cut the tree down to a proper size. We know that we have three species in our data, so we may want to cut the tree at a height of 3 - not because that's the number of species, but because the tree just so happens to recognize three clusters at that level of decision-making.

```
clusterCut <- cutree(clusters, 3) # cut tree
table(clusterCut, iris$Species) # assess fit
##
## clusterCut setosa versicolor virginica
###</pre>
```

1 50 0 0 ## 2 0 23 49 ## 3 0 27 1

As we can see here, our decision tree has had no issue identifying *setosa* and *virginica* into clusters 1 and 2 respectively. However, it is struggling with placing the species *versicolor*.

Note that we did not take into account any special linkages here

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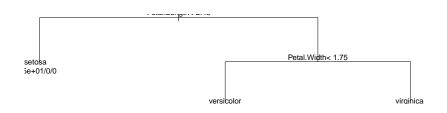
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Example - Decisions

So far we weren't able to tell the actual decision rules of how to cluster our data. Let's do this:

```
library(rpart)
fit <- rpart(Species ~. , data = iris)
plot(fit)
text(fit, use.n = TRUE)</pre>
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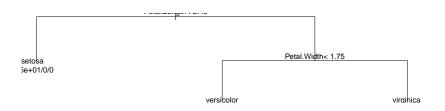


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Purpose:

Random Forests

tuneRF() in randomForest package

Identify which variables to use for clustering our data and

build a tree.

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Very robust.

Easy to interpret

■ A **black box** algorithm.

Computationally expensive

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Disadvantages:

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→ Once more, let's see if we can accurately identify the Species contained within the data set by clustering according to Sepal. Length, Sepal. Width, Petal. Length, and Petal. Width.

Example - The Model

```
set.seed(42) # set seed because the process is random
RF_Mod <- tuneRF(x = iris[,-5], # variables which to use for clustering
               y = iris[,5], # correct cluster assignment
               strata = iris[,5], # consider this for stratified sampling
               doBest = TRUE, # run the best overall tree
               ntreeTry = 20000, # consider this number of trees
               improve = 0.0001, # use an improvement for tuning if this margin is exceeded
               trace = FALSE, plot = FALSE)
## -0 1429 0 0001
## 0 0.0001
RF Mod
## Call:
  randomForest(x = x, y = y, mtry = res[which.min(res[, 2]), 1], strata = ..1)
               Type of random forest: classification
##
##
                     Number of trees: 500
## No. of variables tried at each split: 2
##
        OOB estimate of error rate: 4%
## Confusion matrix:
       setosa versicolor virginica class.error
## setosa 50 0 0
                                           0.00
## versicolor 0 47 3
                                           0.06
## virginica 0 3 47
                                           0.06
```

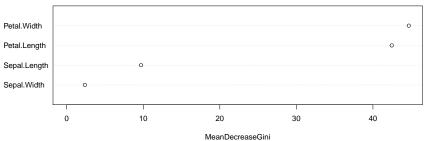
That is one **stunningly accurate** tree!

Example - Explanation

Let's see which variables where actually the most useful when making our clustering decisions:

varImpPlot (RF_Mod)



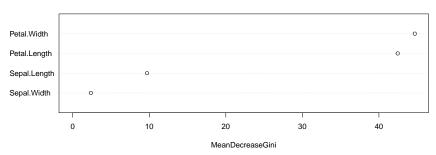


Example - Explanation

Let's see which variables where actually the most useful when making our clustering decisions:

varImpPlot (RF_Mod)





Again, Petal. Width and Petal. Length alone seem to be almost enough to accurately classify all of our iris data in their respective species memberships!

Network Clustering

cluster_optimal(), etc. in igraph package and many others

Purpose:

Identify compartments which are strongly connected within, but not between each other.

Advantages:

- Highly flexible approaches.
- Network analyses offer much more than clustering.
- Allow for clustering of very different data and identification relationships than other approaches.
- Steep learning curve

Disadvantages.

- Tricky in formatting data correctly.
- Choices can become overwhelming

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Disadvantages:

- Tricky in formatting data correctly.
- Choices can become overwhelming

Here, we take a foodweb contained within the foodwebs data collection of the igraphdata package. We are using the Middle Chesapeake Bay in Summer foodweb (Hagy, J.D. (2002) Eutrophication, hypoxia and trophic transfer efficiency in Chesa-peake Bay PhD Dissertation, University of Maryland at College Park (USA), 446 pp.).

```
library(igraph)
library(igraphdata)
data("foodwebs")
Foodweb_ig <- foodwebs[[2]]</pre>
```

→ Let's see what kind of network-internal clusters we can make out.

Example - A Directed Network

A directed network is one in which we know which node/vertex is acting one which other node/vertex.

We identify the clusters as follows:

```
Clusters <- cluster_optimal(Foodweb_ig)
Colours <- Clusters$membership
Colours <- rainbow(max(Colours))[Colours]
plot(Foodweb_ig,
    vertex.color = Colours,
    vertex.size = degree(Foodweb_ig) *0.5,
    layout=layout.grid, edge.arrow.size=0.001)</pre>
```

This identifies sub-networks/clusters by optimizing the modularity score of the overall network (i.e. optimizing connections within vs. between clusters).

