

Supplemental Instructions

1

a) $y' = -\frac{3x}{\sqrt{1-3x^2}}$

b) $-2\sin(x)\cos(2\cos(x))$

c) $2(\sin(2x) + \cos(2x))$

2

a) $2x + 2yy' = 0$

$$2yy' = -2x$$

$$y' = \frac{-2x}{2y} = -\frac{x}{y}$$

b) $3x^2 + 3y^2y' = 1 + 2y'$

$$3x^2 - 1 = -3y^2y' + 2y'$$

$$3x^2 - 1 = y'(2 - 3y^2)$$

$$\frac{3x^2-1}{2-3y^2} = y'$$

3

a) $y(x) = x^2 \implies x(y) = \sqrt{y}$

b) $y(x) = 2^x \implies x(y) = \log_2 y$

c) $y(x) = \tan(x) \implies x(y) = \arctan y$

d) $y(x) = 1/x \implies x(y) = 1/y$

4

$$f(x) = x^2 \implies f^{-1}(x) = \sqrt{x}$$

$$f'(x) = 2x$$

$$\frac{d}{dx}f^{-1}(x) = \frac{1}{f'(f^{-1}(x))} \quad \frac{d}{dx}\sqrt{x} = \frac{1}{f'(\sqrt{x})} = \frac{1}{2(\sqrt{x})}$$

5

a) 3

b) $2\sqrt{2}$

c) 1

d) x^5

e) $\ln \frac{64}{81}$

f) $x = \frac{\ln(2)}{\ln(2) - \ln(3)}$

6

a) $e^x(x+1) - 1$

b) e^{x+e^x}

c) $\ln(x)$

7

a) $\frac{1}{\sqrt{-x^2+x+2}}$

b) $2x \arctan(x) + 1$

c) $\arccos(x) - \frac{x}{\sqrt{1-x^2}}$