

1.) 1.1

a.) ob 1000 1110

$$\text{decimal} = (2^0 \cdot 0) + (2^1 \cdot 1) + (2^2 \cdot 1) + (2^3 \cdot 1) + (2^4 \cdot 0) + (2^5 \cdot 0) \\ + (2^6 \cdot 0) + (2^7 \cdot 1) = 0 + 2 + 4 + 8 + 0 + 0 + 0 + 128$$

$$\boxed{= 142}$$

hexadecimal 1000 1110 = $\boxed{8E}$

b.) 0x C3BA C=1100 3=0011 B=1011 A=1010

$$\boxed{\text{binary} = 1100 \ 0011 \ 1011 \ 1010}$$

$$\text{decimal} = (2^0 \cdot 0) + (2^1 \cdot 1) + (2^2 \cdot 0) + (2^3 \cdot 1) + (2^4 \cdot 1) \\ + (2^5 \cdot 1) + (2^6 \cdot 0) + (2^7 \cdot 1) + (2^8 \cdot 1) + (2^9 \cdot 1) \\ + (2^{10} \cdot 0) + (2^{11} \cdot 0) + (2^{12} \cdot 0) + (2^{13} \cdot 0) + (2^{14} \cdot 1) \\ + (2^{15} \cdot 1) = \boxed{50106}$$

c.) 81

binary

$$\begin{array}{l} 81/2 = 40 \ R_1 \\ 40/2 = 20 \ R_0 \\ 20/2 = 10 \ R_0 \\ 10/2 = 5 \ R_0 \\ 5/2 = 2 \ R_1 \\ 2/2 = 1 \ R_0 \\ 1/2 = 0 \ R_1 \end{array}$$

$$\boxed{\text{ans} = 1010001}$$

hex.

$$\begin{array}{c} 101 \\ 5 \end{array}$$

$$\begin{array}{c} 0001 \\ 1 \end{array}$$

$$\boxed{\text{hex} = 51}$$

d.) 0b 1001 001001
 0010 0100 1001
 hex = 2 4 9 $\Rightarrow 249 = \text{hex.}$

$$\begin{aligned} \text{decimal} &= (2^0 \cdot 1) + (2^1 \cdot 0) + (2^2 \cdot 0) + (2^3 \cdot 1) + (2^4 \cdot 0) \\ &+ (2^5 \cdot 0) + (2^6 \cdot 1) + (2^7 \cdot 0) + (2^8 \cdot 0) + \\ &(2^9 \cdot 1) = 1 + 8 + 2^6 + 2^9 = \boxed{585} \end{aligned}$$

e.) B C A I B=11 C=12 A=10 I=1

binary 1011 1100 1010 0001

$$\begin{aligned} &= 1 + 2^5 + 2^7 + 2^{10} + 2^{11} + 2^{12} + 2^{13} + 2^{15} \\ &= 48289 \end{aligned}$$

f.) 0

binary = 0000 0000
 hex = 0

g.) 42

binary

$$\begin{aligned} 42/2 &= 21 \text{ } R_0 \\ 21/2 &= 10 \text{ } R_1 \\ 10/2 &= 5 \text{ } R_0 \\ 5/2 &= 2 \text{ } R_1 \\ 2/2 &= 1 \text{ } R_0 \\ 1/2 &= 0.5 \text{ } R_1 \end{aligned}$$

Ans = 101010

hex = 0010 1010 $\Rightarrow \boxed{2A}$

h.) B A C 4 B=11 A=10 C=12 4=4

binary = 1011 1010 1100 0100

decimal = 47812

~~1.2~~ 1.2

a.) $2^{14} = 16 \text{ Ki}$

b.) $2^{43} = 8 \text{ Ti}$

c.) $2^{23} = 8 \text{ Mi}$

d.) $2^{58} = 256 \text{ Pi}$

e.) $2^{64} = 16 \text{ Ei}$

f.) $2^{42} = 4 \text{ Ti}$

1.3.)

a.) $2 \text{ Ki} = 2^{11}$

b.) $512 \text{ Pi} = 2^{59}$

c.) $256 \text{ Ki} = 2^{18}$

d.) $32 \text{ Gi} = 2^{35}$

e.) $64 \text{ Mi} = 2^{26}$

f.) $8 \text{ Ei} = 2^{63}$

Section 2

- 1.) The largest 8bit unsigned number is $1111\ 1111 = 255$ when all bits are 1's. When we add 1 to the largest 8bit integer we get an overflow.

$$\begin{array}{r} 1111\ 1111 \\ +1 \\ \hline 1\ 0000\ 0000 \end{array}$$

The largest 8bit ~~sig~~ signed number is $0111\ 1111 = 127$ where the 0 means it's positive. When we add 1 to this number we get

$$\begin{array}{r} 0111\ 1111 \\ +1 \\ \hline 1\ 000\ 0000 = 128 \end{array}$$

- 2.) $0 = 0000\ 0000$ - unsigned
 $0000\ 0000$ - two's complement
 $3 = 0000\ 0011$ - unsigned
 $0000\ 0011$ - two's complement
~~does not apply for signed~~
 $-3 =$ Not applicable for unsigned.

$$\begin{array}{r} 0000\ 0011 \\ +1 \\ \hline 0000\ 0100 \end{array}$$

flip $\rightarrow 1111\ 1011$ - 3 two's complement

$$\begin{array}{r} 1111\ 1100 \\ +1 \\ \hline 1111\ 1101 \end{array}$$

3.) $42 = 00101010$ unsigned
 00101010 two's complement

$-42 =$ not applicable for unsigned.

$$\begin{array}{r} 00101010 \rightarrow \text{flip} = 11010101 \\ \hline + 1 \\ \hline 11010110 \end{array}$$

Ans = $10101010 = -4$ signed. Two's complement

4.) the largest integer that can represent by 8bits could be as large as infinity depending on how large your encoding scheme can go up to. The larger range of the encoding scheme the larger the 8bit number, therefore if we have a really large encoding scheme then our largest 8bit number can be infinity.

5.) if $x = 0101$

$$\begin{array}{r} x' = 1010 + 1 \Rightarrow 0 \quad 1010 \quad 0101 \\ \hline + 1 \quad + 1 \\ \hline 1011 \quad 0110 \end{array}$$

$$x = 1111$$

$$x + x' = 1111$$

$$x + x' + 1 = 10000 \text{ with overflow.}$$

6.) Binary numbers shine because they are very useful for computer and machine learning.

Where 1 = ON or 0 = OFF or 1 = true and 0 = false. It has many meanings and uses for computers.

Decimal numbers shine in the human world where it is easier for us to record ~~as~~ most things using decimal numbers.

Hexadecimal numbers ~~are use~~ shine when binary numbers become too large. We are able to use hexadecimal in order to shorten the binary length seeing that ~~the~~ it is a higher use of encoding scheme.

A = 10 = 1010 B = 11 = 1011 C = 12 = 1100

D = 13 = 1101 E = 14 = 1110 F = 15 = 1111

Section 3.

- 1.) We need at most 2 bits which can go as high as 3 in decimal which is as high as need because $0=0$ $\pi=3.14$ and $e=2.7$.
- 2.) $2 \text{ TiB} = 2^{41}$ so 41 bytes long.
- 3.) I would say we need 2 bits be 1 bit which is $(2^{0.1}) = 1$ which is not enough because $e=2.7$ here for we would need the 2 bits which go to 3 in decimal value which is ~~enough~~ enough to represent e .