

Summary of OLS Results - Model Variables

Variable	Coefficient [a]	StdError	t-Statistic	Probability [b]	Robust_SE	Robust_t	Robust_Pr [b]	VIF [c]
Intercept	31.349832	25.713969	1.219175	0.227799	21.733306	1.442479	0.154643	-----
PUBLICSUPP	0.000122	0.000134	0.914184	0.364468	0.000083	1.472462	0.146400	1.326211
DOMESTIC_S	0.000892	0.001682	0.530203	0.598032	0.001538	0.579878	0.564282	1.237817
IRRIGATI_1	0.002580	0.000331	7.801955	0.000000*	0.000586	4.403888	0.000048*	1.064547
AQUACULTUR	14.283092	4.142811	3.447682	0.001072*	5.153368	2.771603	0.007521*	1.040707
MINING_TOT	10.194815	13.142653	0.775705	0.441127	3.445469	2.958905	0.004491*	1.006125
THERMOELEC	12.610216	2.613270	4.825454	0.000011*	2.098422	6.009381	0.000000*	1.060277

## OLS Diagnostics

Input Features:	WaterUsageCO2005	Dependent Variable:	TOTALWITHD
Number of Observations:	64	Akaike's Information Criterion (AICc) [d]:	815.746420
Multiple R-Squared [d]:	0.661725	Adjusted R-Squared [d]:	0.626117
Joint F-Statistic [e]:	18.583638	Prob(>F), (6,57) degrees of freedom:	0.000000*
Joint Wald Statistic [e]:	125.607784	Prob(>chi-squared), (6) degrees of freedom:	0.000000*
Koenker (BP) Statistic [f]:	23.194139	Prob(>chi-squared), (6) degrees of freedom:	0.000734*
Jarque-Bera Statistic [g]:	12.879304	Prob(>chi-squared), (2) degrees of freedom:	0.001597*

### Notes on Interpretation

\* An asterisk next to a number indicates a statistically significant p-value ( $p < 0.01$ ).

[a] Coefficient: Represents the strength and type of relationship between each explanatory variable and the dependent variable.

[b] Probability and Robust Probability (Robust\_Pr): Asterisk (\*) indicates a coefficient is statistically significant ( $p < 0.01$ ); if the Koenker (BP) Statistic [f] is statistically significant, use the Robust Probability column (Robust\_Pr) to determine coefficient significance.

[c] Variance Inflation Factor (VIF): Large Variance Inflation Factor (VIF) values ( $> 7.5$ ) indicate redundancy among explanatory variables.

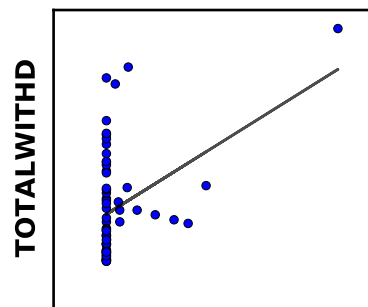
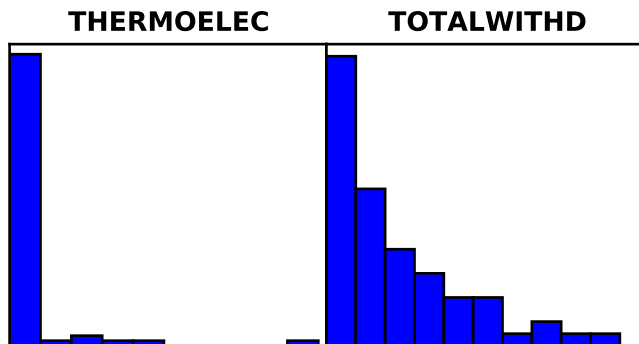
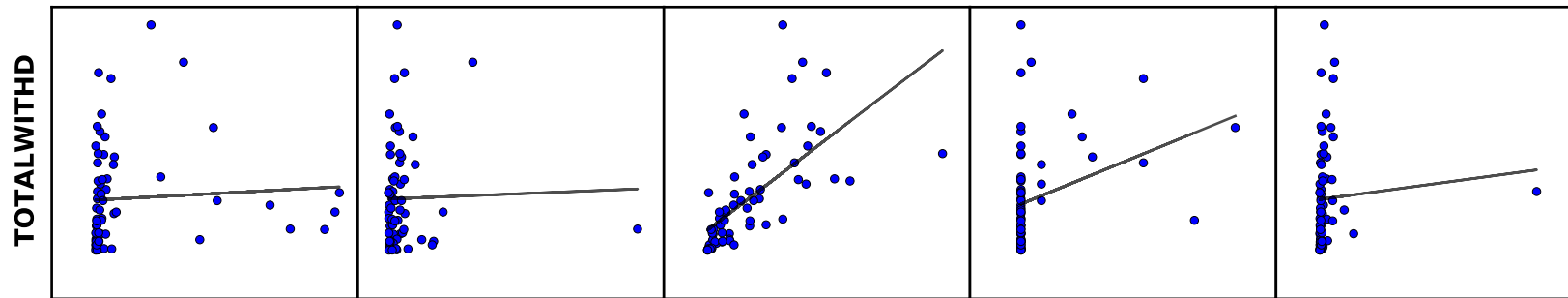
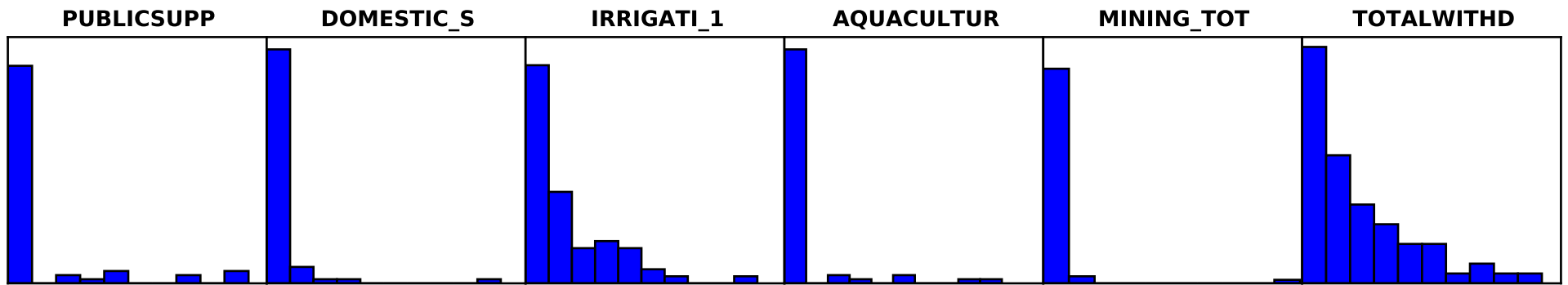
[d] R-Squared and Akaike's Information Criterion (AICc): Measures of model fit/performance.

[e] Joint F and Wald Statistics: Asterisk (\*) indicates overall model significance ( $p < 0.01$ ); if the Koenker (BP) Statistic [f] is statistically significant, use the Wald Statistic to determine overall model significance.

[f] Koenker (BP) Statistic: When this test is statistically significant ( $p < 0.01$ ), the relationships modeled are not consistent (either due to non-stationarity or heteroskedasticity). You should rely on the Robust Probabilities (Robust\_Pr) to determine coefficient significance and on the Wald Statistic to determine overall model significance.

[g] Jarque-Bera Statistic: When this test is statistically significant ( $p < 0.01$ ) model predictions are biased (the residuals are not normally distributed).

# Variable Distributions and Relationships

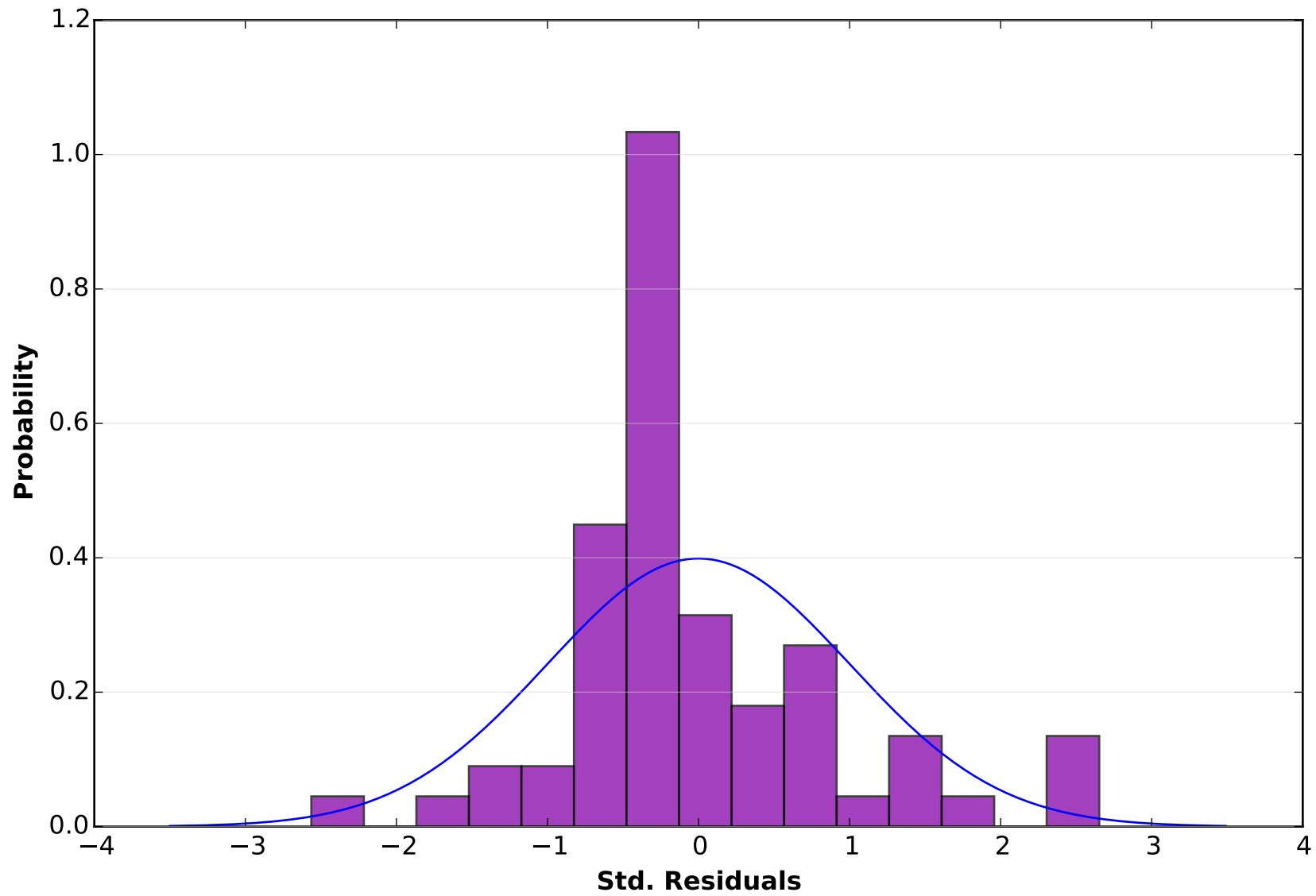


## Variable Distributions and Relationships (Cont.)

The above graphs are Histograms and Scatterplots for each explanatory variable and the dependent variable. The histograms show how each variable is distributed. OLS does not require variables to be normally distributed. However, if you are having trouble finding a properly-specified model, you can try transforming strongly skewed variables to see if you get a better result.

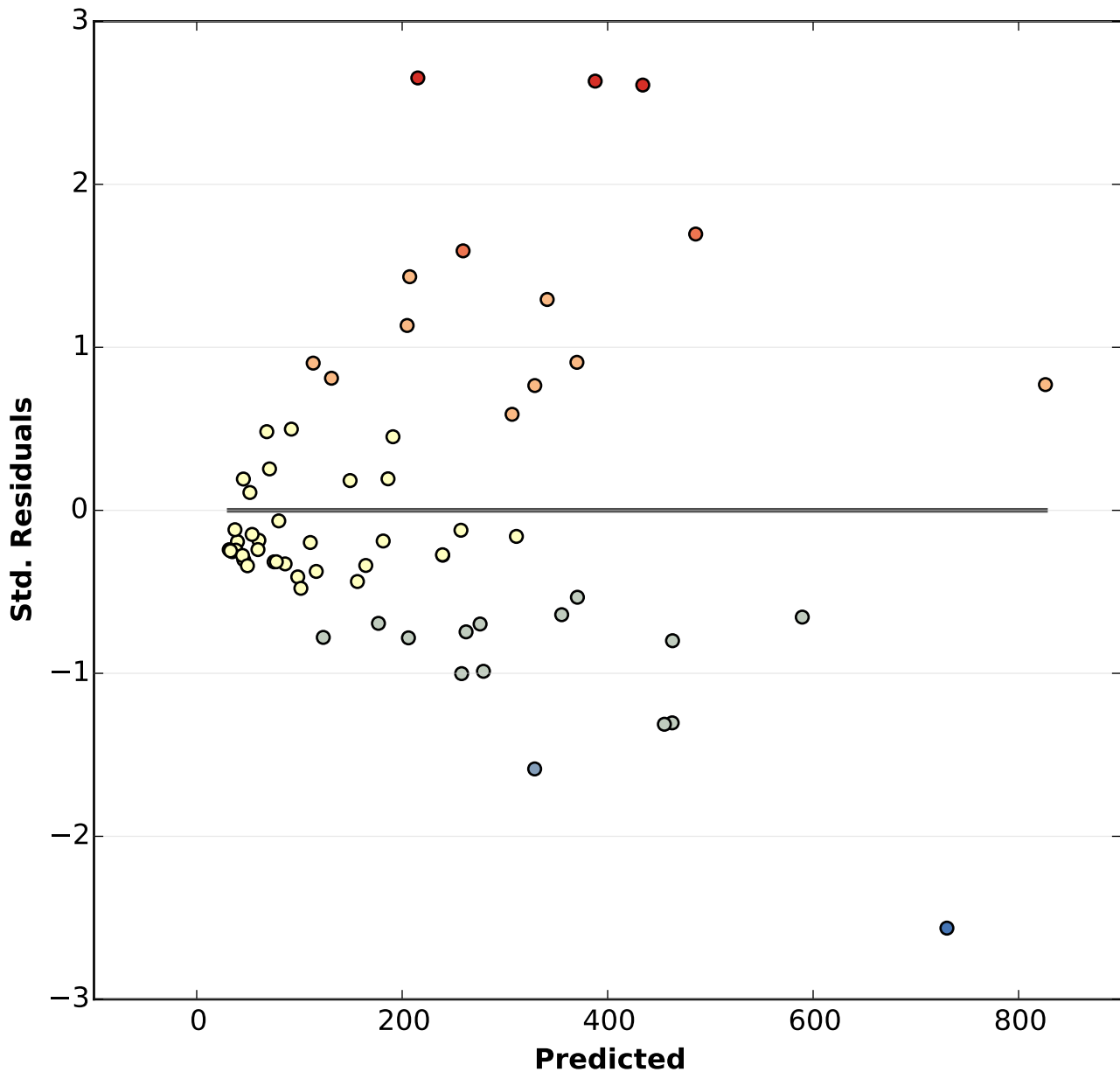
Each scatterplot depicts the relationship between an explanatory variable and the dependent variable. Strong relationships appear as diagonals and the direction of the slant indicates if the relationship is positive or negative. Try transforming your variables if you detect any non-linear relationships. For more information see the Regression Analysis Basics documentation.

## Histogram of Standardized Residuals

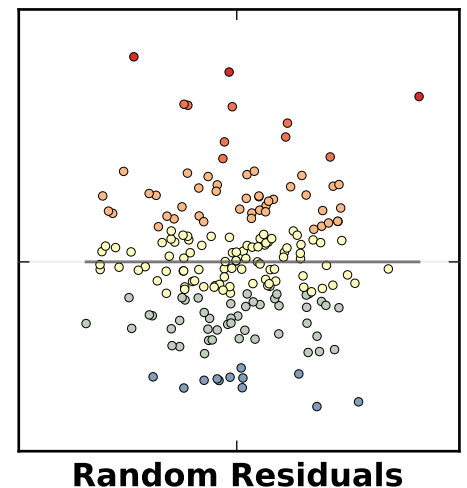


Ideally the histogram of your residuals would match the normal curve, indicated above in blue. If the histogram looks very different from the normal curve, you may have a biased model. If this bias is significant it will also be represented by a statistically significant Jarque-Bera p-value (\*).

## Residual vs. Predicted Plot



This is a graph of residuals (model over and under predictions) in relation to predicted dependent variable values. For a properly specified model, this scatterplot will have little structure, and look random (see graph on the right). If there is a structure to this plot, the type of structure may be a valuable clue to help you figure out what's going on.



# Ordinary Least Squares Parameters

Parameter Name	Input Value
Input Features	WaterUsageCO2005
Unique ID Field	OBJECTID
Output Feature Class	None
Dependent Variable	TOTALWITHD
Explanatory Variables	PUBLICSUPP
	DOMESTIC_S
	IRRIGATI_1
	AQUACULTUR
	MINING_TOT
	THERMOELEC
Selection Set	False