Introduction

An automobile company plans to enter new markets, and they have deduced that the behavior of the new market is similar to their existing market, in which the sales team had classified all customers into 4 segments (A, B, C, D) and found this strategy to work exceptionally well. In this study our aim is to analyze data of the previous customers and try to classify potential customers from the new automobile industry market into the four segments.

Data Description and Questions of Interest

The training dataset includes 8068 observations from the existing market customers and 11 variables that are: ID, gender of the customer, marital status, age, graduation status, profession, work experience in years, spending score, number of family members, and an anonymised category provided by the company (Var_1). Most of the variables in the dataset are categorical except ID, age, work experience and number of family members. The test data contains 2627 observations and the same variables.

By utilizing the variables along with different methodologies such as logistic regression, K-nearest neighbors algorithm, and linear discriminant analysis, our goal is to find the most suitable model to classify the customers. Key questions that we also wish to address are what are the variables that play the biggest role in prediction, and what are the limitations of our methods.

Data Exploration

As mentioned, the training dataset contains 3 numerical variables and 6 categorical variables as the potential predictors. We first check the distributions of numerical variables. From Figure 1 we see that age is approximately normally distributed with mean around 40. Work experience is heavily right skewed as the majority are 0 or 1. Family size distribution is also right skewed with the most common being 2. To analyze the relationships between them, we plot a scatter plot matrix with the correlation coefficients displayed in Figure 2. The plot shows low correlation for all pairs.

For the categorical variables, including the response (Segmentation), we created pie charts to inspect the classes each variable has, as well as the percentage distributions. We see that the customers are: approximately half-and-half in terms of gender distribution; forty-sixty in terms of marital history and graduation status; working in nine total professions, with health care being the most; mostly having average spending score; mostly classified into the second anonymised category by the company; evenly distributed in terms of final segmentation.

It is also important to discover interactions between the predictors for modeling, so we created side-by-side boxplots of the categorical predictors versus the numerical predictors, shown in Figure 4 to 6. From the plots, the key interactions for age are spending score, marital history, graduation, and profession. Specifically, we see that customers who have high spending scores are having a median of 60 in age, which is older compared to the average ages of both average and low spending score customers. Also, customers who were married at least once are generally older than those who were never married, customers who have graduated are generally older than those who have not graduated, and customers that are lawyers are generally the oldest in the group while those who work in health care are generally the youngest. Besides these, the other interactions shown are not as significant.

Finally, we check how the classes in segmentation are distributed over the three quantitative variables. In Figure 7, it shows that distribution of classes changes over different ages. For example, the proportion of class D customers is the highest around the age of 20, and

the proportion of all classes is about the same as age gets larger. For different values of work experience and family size, the distribution of segmentations remains relatively the same.

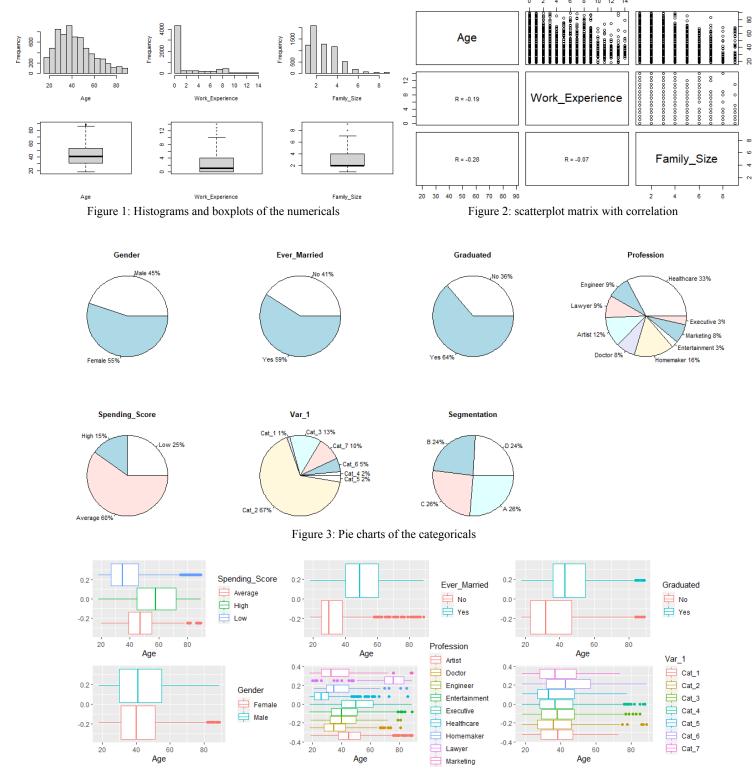


Figure 4: Side-by-side boxplots of the categoricals against Age

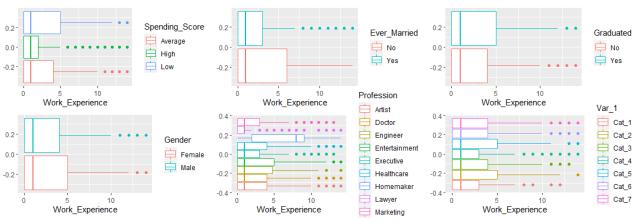


Figure 5: Side-by-side boxplots of the categoricals against Work Experience

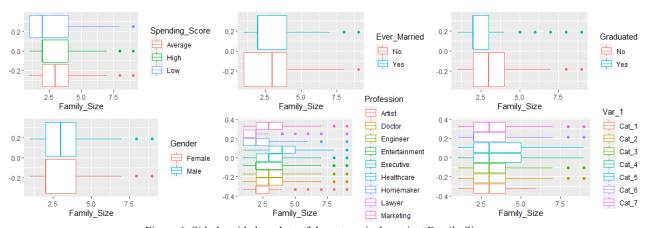


Figure 6: Side-by-side boxplots of the categoricals against Family Size

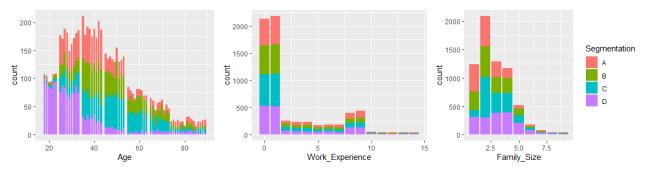


Figure 7: Composition of cases with respect to segmentation

Methods

1. Logistic Regression

Logistic regression is a statistical model that uses a logistic function to model a binary dependent variable. The output of the regression model is the likelihood of an event happening. When using logistic regression to classify binary categorical response variables, the usual method is to replace the response variable with 0 and 1 before modeling.

The dataset in our project contains four different segmentations. If we still want to try logistic regression for classification, the only way is to apply logistic regression three times and classify one segmentation each time. However, the error rate would become very high. So, in this project, we separated the dataset into six binary groups, performed logistic regression on each group, and used them to find the variables that play the biggest role in prediction.

For each model, we first fitted a full model on every variable, and used the stepwise regression procedures to choose the best model. Specifically, we use the backward elimination, which starts from a full model, and delete variables that give the biggest improvement of the criterion regarding AIC, until the criterion cannot be improved anymore. Finally, we investigated the ANOVA table of each model, and made conclusions of the variables that play the biggest role in prediction.

Model 1: segmentations A & B

The accuracy of this model is 0.6480552. As shown in the table (Figure 8), when sequentially adding the Age, Graduated, Profession, Spending_Score variables in the model, the residual deviance decreases more than adding other variables in the model. This indicates that these four variables play a relatively more important role in the model.

	Df	Deviance	Resid. Df	Resid. Dev
NULL			3187	796.85
Gender	1	0.048	3186	796.80
Age	1	11.336	3185	785.46
Graduated	1	8.220	3184	777.24
Profession	8	28.070	3176	749.17
Work_Experience	1	2.613	3175	746.56
Spending_Score	2	36.582	3173	709.98
Family_Size	1	2.123	3172	707.86
Var_1	6	3.132	3166	704.72

Figure 8: ANOVA table of the first logistic model

Model 2: segmentations A & C

The accuracy of this model is 0.7419065. From the ANOVA table we can observe that when sequentially adding variables into the model, the residual deviance decreases more when adding the variables Graduated, Profession, Spending_Score. This indicates that these three variables play a relatively more important role in the model.

Model 3: segmentations A & D

The accuracy of this model is 0.7571894. From the ANOVA table we can observe that when sequentially adding variables into the model, the residual deviance decreases more when adding the variables Ever_Married, Age, Graduated, Profession. This indicates that these four variables play a relatively more important role in this model.

Model 4: segmentations B & C

The accuracy of this model is 0.6479344. From the ANOVA table we can observe that when sequentially adding variables into the model, the residual deviance decreases more when adding the variables Profession and Spending_Score. This indicates that these two variables play a relatively more important role in this model.

Model 5: segmentations B & D

The accuracy of this model is 0.8224692. From the ANOVA table we can observe that when sequentially adding variables into the model, the residual deviance decreases more when adding the variables Ever_Married, Age, Graduated, Profession, Spending_Score. This indicates that these five variables play a relatively more important role in this model.

Model 6: segmentations C & D

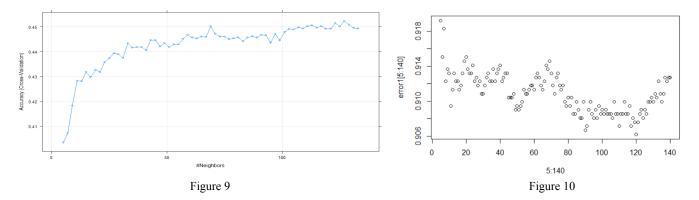
The accuracy of this model is 0.851021. From the ANOVA table we can observe that when sequentially adding variables into the model, the residual deviance decreases more when adding the variables Age, Graduated, Profession, Spending_Score. This indicates that these four variables play a relatively more important role in this model.

From the six logistic regression model, we can observe that generally, the Graduated, Profession, Spending_Score variables play important roles in segmentation for A,B,C and D. Besides, since the accuracies for performing logistic regression on A&D, B&D, C&D are pretty high than the others, we can make the conclusion that the segmentation D is more easily to be segmented from the others.

2. k-NN

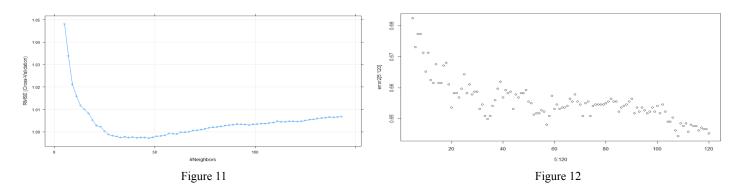
k-NN is the abbreviation for K-Nearest Neighbors. It is a non-parametric method not only used for classification but also used for regression. The reason for non-parametric is for that it does not set up any assumptions on the underlying data distribution. In general, we use k-NN classification when predicting categorical outcome and apply k-NN regression when predicting a continuous outcome. The principle of the k-NN algorithm is when we make predictions or classification, there are nonlinear boundaries separating labels or classes of interest. K-NN would examine the classes or labels of points or neighbors which are surrounding the point we are interested in and classify the interest points or data based on the similar measure. Specifically, the similar measure is defined as the distance between two data and the popular method to calculate the distance is Euclidean distance. Besides that, based on different data properties, the distance measure could be different, such as Manhattan, Minkowski, Jaccard distance and so on. Thus, efficiency of the k-NN algorithm mainly depends on the optimal number of k and generally we could apply a cross-validation approach to get the relatively optimal K. In short, the method allows us to resampling train data so that it evaluates performance of different possible k based on those data applying the best k into the model, which could minimize the validation error. In our study, in order to train a model to better predict the segmentation (A,B,C,D) of the customer, we designed three k-NN models based on different scenarios. Two of them separately apply different distance measures, Euclidean distance and Jaccard distance.

As we all know, we need to apply numeric variables for calculating the distance between data points. Thus, we firstlt include all three quantitative variables as predictor variables in the first k-NN model. They are "Age", "Work_Experience" and "Family_Size" and our outcome variable is "Segmentation". As three predictor variables are different from each in scale, we used the scale function to standardize these predictors. After that, before we use the train function of the class package we learned this semester to run k-NN classification, we initially apply 10-fold cross validation in the training data with 75% training percentage sampling to find the optimal number of neighbors. According to the train function in Caret package(Caret, pp.163-169), we could achieve that goal and generate a plot.



Based on it, we are aware the optimal k for the final model to use is 127 (Figure 9). In order to test that, we use the train function of the class package to run classification and plot the final model prediction error rate in an interval including the optimal k. We can see the lowest error rate of the model appears when k is roundly equal to 120, though the error rate is pretty high, almost 90% (Figure 10). It is reasonable to predict, as this model only has three quantitative variables and does not contain enough information.

In the second k-NN model, we decide to transform all of the categorical variables into numeric. Same as the first model procedure, we apply 10-fold cross validation in the training data with 75% training percentage sampling to get the optimal k equals to 47 (Figure 11).



Then, we run a classification function and plot the error rate interval using the same procedure as mentioned in the first model. At this time, we notice that the overall error rate improves a lot and when k equals to 47, the error rate approximately equals to 65%. However, we do find the error rate of k that equals to 47 obtained from cross validation approach is relatively higher than the error rate of 64% obtained from the k around 100 (Figure 12). In fact, the error can be expected, as the k value of cross validation approach is trained on the 75% training percentage data and tested on the remaining 25% data. Thus, when we apply the k-NN classification with the optimal k value and test on the new test data, the final result may cause a certain error. Although the error rate improves a lot, the model we generated does not obtain practical meaning. As in the train function of the class package, the default distance measure method is Euclidean distance, which calculates the straight distance between two data points. However, the categorical variable does not fit for that distance approach. For example, the "Profession" variable has 9 different levels so that we convert each of them with a number from 1 to 9. However, this data of "Profession" does not contain these order relationships.

Therefore, in the third k-NN model, we found a method to calculate the distance of categorical variables. We first convert each of these categorical variables into dummy variables and then we could apply the Jaccard distance measure (Teknomo). It could measure the asymmetric information of binary and the distance defined as the size of interaction of two data divided by the union of them. We learned a knn function of the package named "Neighbr" that could apply k–NN classification with Jaccard distance(Neighbr, pp.3). However, when we apply that function to our dataset, the computational time of cost is too long and even costs a whole day to test one k. Thus, we have to sample a portion of data from our converted train data and test data. Lastly, we use 1000 samples as our training data and 300 samples as our test data. After applying the k-NN classification with Jaccard distance, we plot the final model prediction error rate in a wide interval of k, from 10 to 200. We can see the best error rate is relatively the lowest 66 % when k equals to around 50 (Figure 13).

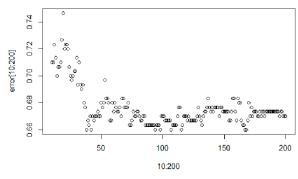


Figure 13

3. LDA

Linear Discriminant Analysis (LDA) is a sound machine learning technique and classification method for predicting categorical. The Linear Discriminant Analysis has two functions: dimensionality reduction and classification. So, this method can project multi-dimensional data to a low-dimensional plane, making our data categories easily distinguishable. And the dimension of the data after dimensionality reduction is called the discriminant function. After using LDA, only a few discriminant functions are left in the original data with many features. The primary problem with too high data dimensions (too many predictor variables) is that many dimensions cannot provide helpful information to the model and even interfere with model performance. When the number of dimensions increases, the data becomes sparse. Linear Discriminant Analysis is to help us reduce computational costs for classification tasks, but it can also be helpful by avoiding overfitting via minimizing the error in parameter estimation. In our case, by fitting the LDA model with our training data, we got the prior probability of groups, group means, Coefficients of linear discriminants, and Proportion of trace. According to the result, the Group means can give us some information like "GenderMale," "Work Experience," "Family Size" and "Var 1Cat 7" have almost the same value among the four segmentations (A, B, C, D), which means these variables are not that useful for predicting. However, "ProfessionHealthcare" has an especially high mean in D and low in others, meaning that this variable is very useful for predicting the D group. Importantly, we can see that the LDA model helps us to reduce our dimensions by classifying our 23 variables into only three features: "LD1", "LD2," and "LD3". In other words, LDA uses fewer variables to predict ABCD four segmentation. The Coefficients of linear discriminants show us the

correlation of 23 variables and the three LD, respectively. Furthermore, we calculate the confusion matrix to help us evaluate the performance of the classification model, and we further get the misclassification error rate: 0.6722377. The high error rate implies that linear function cannot perform well in helping us separate our clusters with our data.

Results and Conclusion

In summary, we created models adopting three different methodologies: logistic regression, k-nearest neighbor, and Bayes' classifier. Here we compare their performance and answer our questions of interest.

1) What is the most suitable model to classify the customers?

According to the result we get from the three different models, we found that logistic is the most efficient method to do the classification for this dataset, since it has the highest accuracy rate. However, the logistic model can only analyze two segmentations simultaneously. Comparison between LDA and k-NN, though the third k-NN model seems to have a relatively higher accuracy rate 0.34 than that of LDA 0.33. However, as the k-NN model here does not include the whole dataset, instead it samples a proportion of training data and test data. Overall, the LDA model is more comprehensive.

2) What are the variables that play the biggest role in prediction?

According to the logistic regression models, different groups of segmentation have different significant variables. So we cannot give an absolute idea of what are the variables that play the biggest role in classifying the customers into four segments A, B, C and D. However, by summing up the all six models, we can observe that the Graduated, Profession, Spending_Score variables have high influence in deviance reduction for all six models. Hence, we can conclude that these are the variables that play the biggest role in prediction. According to the Group means in the LDA model, we can see that Profession, Ever_Married and Age have more influence on predicting the four segmentations A, B, C and D. However, we cannot tell who plays the biggest role in prediction only based on the Group means.

3) What are the limitations of our methods?

The limitations using the logistic model mainly is that it can only classify two different categories simultaneously. As a result, we can only analyze between two of the four segmentations which may lead to ignoring the relationship between them and cause errors on the classification.

The third k-NN model requires too much time and computational power, so our suggestion is that if the dataset is mostly full of categorical variables and also would like to consider the notion of distance. It may be better to consider "partitioning around medoids (PAM)".

As shown above, the highest accuracies we achieved using our selected methods were around thirty percent. This could be due to either due to the low ceiling of the predictive ability of the data, or the inadequacy of the methods, which we did find limitations of. If the latter is true, methodologies such as neural networks or decision trees may be more suitable for the task.

References

- (1) Data source https://www.kaggle.com/kaushiksuresh147/customer-segmentation
- (2) Teknomo, Kardi. *Jaccard's Coefficient* https://people.revoledu.com/kardi/tutorial/Similarity/Jaccard.html.
- (3) Package 'Caret' https://cran.r-project.org/web/packages/caret/caret.pdf.
- (4) Package 'neighbr' https://cran.r-project.org/web/packages/neighbr/neighbr.pdf

STA 141A Project Code

Customer Segmentation Classification

Authors: Jake Gwo, Qinyi Qiu, Mingrui Gao, Guanghao He, Qiangwei Li

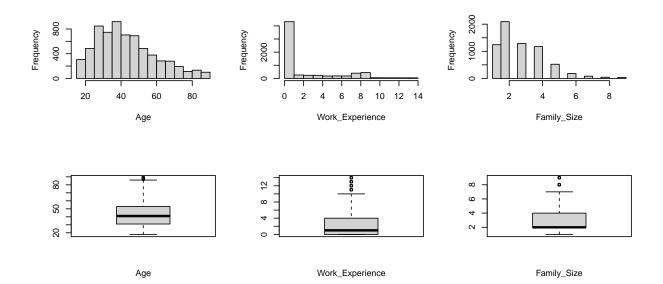
```
library(readr)
library(ggplot2)
library(gridExtra)
#loading data
train.c <- read_csv("Train.csv")</pre>
test.c <- read_csv("Test.csv")</pre>
train <- na.omit(train.c)</pre>
test <- na.omit(test.c)</pre>
str(train)
## tibble [6,665 x 11] (S3: tbl_df/tbl/data.frame)
## $ ID
## $ Gender
                    : num [1:6665] 462809 466315 461735 461319 460156 ...
                    : chr [1:6665] "Male" "Female" "Male" "Male" ...
## $ Ever_Married : chr [1:6665] "No" "Yes" "Yes" "Yes" ...
## $ Age : num [1:6665] 22 67 67 56 32 33 61 55 26 19 ...
## $ Graduated
                    : chr [1:6665] "No" "Yes" "Yes" "No" ...
## $ Graduated : Chr [1:0005] NO 165 165 165 ...
## $ Profession : chr [1:6665] "Healthcare" "Engineer" "Lawyer" "Artist" ...
## $ Work_Experience: num [1:6665] 1 1 0 0 1 1 0 1 1 4 ...
## $ Spending_Score : chr [1:6665] "Low" "Low" "High" "Average" ...
## $ Family_Size : num [1:6665] 4 1 2 2 3 3 3 4 3 4 ...
## $ Var 1
                     : chr [1:6665] "Cat_4" "Cat_6" "Cat_6" "Cat_6" ...
## $ Segmentation : chr [1:6665] "D" "B" "B" "C" ...
## - attr(*, "na.action")= 'omit' Named int [1:1403] 2 5 13 14 25 34 40 44 46 48 ...
     ..- attr(*, "names")= chr [1:1403] "2" "5" "13" "14" ...
```

EDA

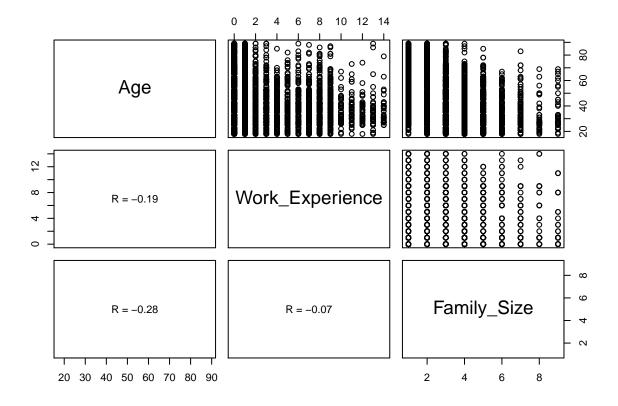
```
summary(train[, c(4,7,9)])
```

```
Work_Experience
                                 Family_Size
##
        Age
        :18.00
                 Min. : 0.000
## Min.
                                 Min. :1.000
## 1st Qu.:31.00
                                 1st Qu.:2.000
                1st Qu.: 0.000
## Median :41.00
                 Median : 1.000
                                 Median :2.000
## Mean :43.54 Mean : 2.629
                                 Mean :2.841
## 3rd Qu.:53.00
                 3rd Qu.: 4.000
                                 3rd Qu.:4.000
## Max. :89.00 Max. :14.000
                                Max. :9.000
```

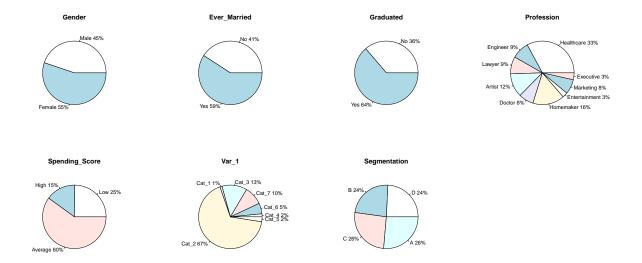
```
layout(mat = matrix(c(1,2,3,4,5,6), ncol = 3))
for(j in 1:ncol(train)){
   if(j %in% c(4,7,9)) { #if a numerical variable
     hist(train[[j]], xlab = colnames(train)[j], main = "")
     boxplot(train[[j]], xlab = colnames(train)[j], main = "")
}
```



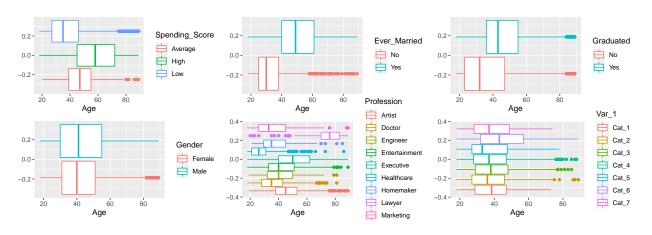
```
panel.cor <- function(x, y) {
    par(usr = c(0, 1, 0, 1))
    r <- round(cor(x, y, use = "complete.obs"), 2)
    txt <- paste0("R = ", r)
    cex.cor <- 0.8/strwidth(txt)
    text(0.5, 0.5, txt, cex = cex.cor * r)
}
pairs(train[c("Age", "Work_Experience", "Family_Size")], lower.panel=panel.cor)</pre>
```



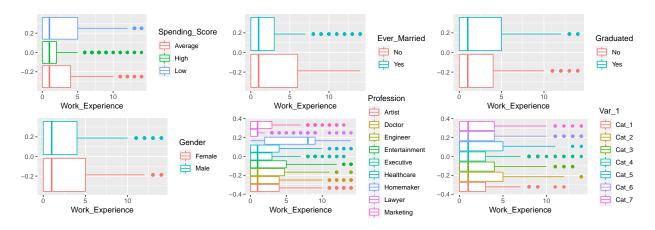
```
par(mfrow=c(2,4))
n <- nrow(train)
for(i in 1:ncol(train)){
   if(!i %in% c(1,4,7,9)) { #if not a numerical variable
     lbls <- unique(train[,i])[[1]]
     pct <- round(100*table(train[,i])/n)
     lab <- paste(lbls, pct)
     lab <- paste(lab,'%',sep='')
     pie(table(train[,i]), main = colnames(train)[i], labels=lab)
}
</pre>
```



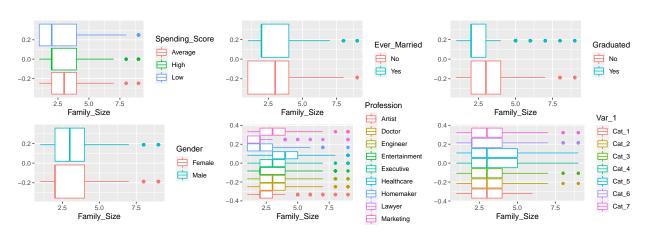
```
interaction_box <- function(quant_var) {
   name <- deparse(substitute(quant_var))
   name <- substring(name, 7)
   plots <- list(
        ggplot(train, aes(x=quant_var, color=Spending_Score))+geom_boxplot()+labs(x=name),
        ggplot(train, aes(x=quant_var, color=Ever_Married))+geom_boxplot()+labs(x=name),
        ggplot(train, aes(x=quant_var, color=Graduated))+geom_boxplot()+labs(x=name),
        ggplot(train, aes(x=quant_var, color=Gender))+geom_boxplot()+labs(x=name),
        ggplot(train, aes(x=quant_var, color=Profession))+geom_boxplot()+labs(x=name),
        ggplot(train, aes(x=quant_var, color=Var_1))+geom_boxplot()+labs(x=name))
   grid.arrange(grobs = plots, nrow = 2)
}
interaction_box(train$Age)</pre>
```



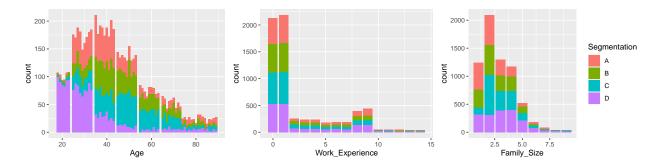
interaction_box(train\$Work_Experience)



interaction_box(train\$Family_Size)



bp1 <- ggplot(train, aes(x=Age))+geom_bar(aes(fill=Segmentation)) + theme(legend.position="none")
bp2 <- ggplot(train, aes(x=Work_Experience))+geom_bar(aes(fill=Segmentation)) + theme(legend.position="none")
bp3 <- ggplot(train, aes(x=Family_Size))+geom_bar(aes(fill=Segmentation))
grid.arrange(bp1,bp2,bp3, nrow = 1)</pre>



```
trainA <- train[which(train$Segmentation=='A'),]
trainB <- train[which(train$Segmentation=='B'),]
trainC <- train[which(train$Segmentation=='C'),]
trainD <- train[which(train$Segmentation=='D'),]

testA <- test[which(test$Segmentation=='A'),]
testB <- test[which(test$Segmentation=='B'),]
testC <- test[which(test$Segmentation=='C'),]
testD <- test[which(test$Segmentation=='D'),]</pre>
```

Model A&B

```
trainAB <- rbind(trainA, trainB)</pre>
trainAB$Segmentation <- ifelse(trainAB$Segmentation=="A",1,0)</pre>
glmAB <- glm(Segmentation~., data=trainAB, family='binomial')</pre>
stepAIC(glmAB, scope=list(upper=glmAB, lower=~1), direction = "backward",
    k = 2, trace = FALSE)
##
##
   Call: glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +
       Work_Experience + Spending_Score + Family_Size + Var_1, family = "binomial",
##
##
       data = trainAB)
##
## Coefficients:
##
               (Intercept)
                                           GenderMale
                                                                            Age
                                                                       -0.02304
                   0.30147
                                              0.27053
##
##
              GraduatedYes
                                    ProfessionDoctor
                                                            ProfessionEngineer
##
                   -0.36533
                                              0.52883
                                                                        0.79281
## ProfessionEntertainment
                                 ProfessionExecutive
                                                           ProfessionHealthcare
                    0.91209
##
                                              0.26173
                                                                        0.05395
##
       ProfessionHomemaker
                                    ProfessionLawyer
                                                            ProfessionMarketing
##
                   0.40270
                                              1.37157
                                                                        0.74073
##
           Work_Experience
                                  {\tt Spending\_ScoreHigh}
                                                              Spending_ScoreLow
##
                    0.03822
                                              0.38152
                                                                        1.03880
##
               Family_Size
                                           Var_1Cat_2
                                                                     Var_1Cat_3
##
                  -0.10022
                                             -0.43675
                                                                       -0.05828
                Var_1Cat_4
##
                                           Var_1Cat_5
                                                                     Var_1Cat_6
##
                    0.19515
                                             -0.50795
                                                                       -0.13380
##
                Var_1Cat_7
##
                    0.02278
##
## Degrees of Freedom: 3187 Total (i.e. Null); 3166 Residual
## Null Deviance:
                         4419
## Residual Deviance: 4030 AIC: 4074
glmAB_ <- glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +
    Work_Experience + Spending_Score + Family_Size + Var_1, family = "binomial",
    data = trainAB)
predictAB_ <- ifelse(glmAB_$fitted.values>0.5, 'A', 'B')
confusionAB <- table(predictAB, ifelse(trainAB$Segmentation==1,'A','B'), dnn=c("Predicted","True"))
confusionAB
```

```
##
            True
                      В
## Predicted
                Α
##
           A 1063
                   575
           B 553 997
##
sum(diag(confusionAB_)) / sum(confusionAB_)
## [1] 0.6461731
anova(glmAB_)
## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: Segmentation
## Terms added sequentially (first to last)
##
##
                    Df Deviance Resid. Df Resid. Dev
##
## NULL
                                     3187
                                               4418.9
## Gender
                          0.191
                                     3186
                                               4418.7
                         45.651
                                     3185
                                               4373.1
## Age
                    1
## Graduated
                    1
                         33.516
                                     3184
                                               4339.5
## Profession
                    8
                      116.839
                                     3176
                                               4222.7
## Work Experience 1
                        10.890
                                     3175
                                               4211.8
## Spending_Score
                    2 157.936
                                     3173
                                               4053.9
## Family_Size
                    1
                          9.861
                                     3172
                                               4044.0
## Var_1
                    6
                         14.051
                                     3166
                                               4030.0
Model A&C
trainAC <- rbind(trainA, trainC)</pre>
trainAC$Segmentation <- ifelse(trainAC$Segmentation=="A",1,0)</pre>
glmAC <- glm(Segmentation~., data=trainAC, family='binomial')</pre>
stepAIC(glmAC, scope=list(upper=glmAC, lower=~1), direction = "backward",
    k = 2, trace = FALSE)
##
## Call: glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +
       Work_Experience + Spending_Score + Family_Size + Var_1, family = "binomial",
##
##
       data = trainAC)
##
## Coefficients:
                                           GenderMale
##
               (Intercept)
                                                                            Age
##
                   0.92325
                                              0.25494
                                                                       -0.02350
##
              GraduatedYes
                                    ProfessionDoctor
                                                            ProfessionEngineer
##
                  -0.73378
                                              0.60248
                                                                        1.60905
## ProfessionEntertainment
                                 ProfessionExecutive
                                                          ProfessionHealthcare
##
                    1.43516
                                              0.42152
                                                                       -0.53428
##
       ProfessionHomemaker
                                    ProfessionLawyer
                                                           ProfessionMarketing
##
                    1.11633
                                              1.41283
                                                                        0.40739
##
           Work_Experience
                                  Spending_ScoreHigh
                                                             Spending_ScoreLow
```

```
##
                   0.04111
                                             0.69753
                                                                       1.61618
##
               Family_Size
                                          Var_1Cat_2
                                                                    Var_1Cat_3
                  -0.32641
                                                                       0.15753
##
                                            -0.23116
##
                Var_1Cat_4
                                          Var_1Cat_5
                                                                    Var_1Cat_6
##
                   0.84200
                                            -0.05978
                                                                      -0.37823
##
                Var 1Cat 7
                  -0.03324
##
##
## Degrees of Freedom: 3335 Total (i.e. Null); 3314 Residual
## Null Deviance:
                        4621
## Residual Deviance: 3503 AIC: 3547
glmAC_ <- glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +</pre>
    Work_Experience + Spending_Score + Family_Size + Var_1, family = "binomial",
    data = trainAC)
predictAC_ <- ifelse(glmAC_$fitted.values>0.5,'A','C')
confusionAC_ <- table(predictAC_, ifelse(trainAC$Segmentation==1,'A','C'), dnn=c("Predicted","True"))</pre>
confusionAC_{-}
##
            True
                     C
## Predicted
                Α
##
           A 1176 421
##
           C 440 1299
sum(diag(confusionAC_)) / sum(confusionAC_)
## [1] 0.7419065
anova(glmAC_)
## Analysis of Deviance Table
## Model: binomial, link: logit
##
## Response: Segmentation
##
## Terms added sequentially (first to last)
##
##
                   Df Deviance Resid. Df Resid. Dev
##
## NULL
                                     3335
                                              4621.4
## Gender
                    1
                          0.06
                                     3334
                                              4621.4
## Age
                    1
                         84.99
                                     3333
                                              4536.4
## Graduated
                    1
                        150.53
                                     3332
                                              4385.9
                        343.33
                                     3324
## Profession
                    8
                                              4042.5
## Work Experience 1
                         18.29
                                     3323
                                              4024.2
## Spending_Score
                    2 366.09
                                     3321
                                              3658.1
## Family_Size
                    1
                         83.54
                                     3320
                                              3574.6
## Var_1
                    6
                         71.40
                                     3314
                                              3503.2
Model A&D
```

```
trainAD <- rbind(trainA,trainD)
trainAD$Segmentation <- ifelse(trainAD$Segmentation=="A",1,0)
glmAD <- glm(Segmentation~., data=trainAD, family='binomial')</pre>
```

```
stepAIC(glmAD, scope=list(upper=glmAD, lower=~1), direction = "backward",
    k = 2, trace = FALSE)
##
## Call: glm(formula = Segmentation ~ Gender + Ever Married + Age + Graduated +
##
       Profession + Work_Experience + Spending_Score + Family_Size,
##
       family = "binomial", data = trainAD)
##
##
  Coefficients:
##
               (Intercept)
                                          GenderMale
                                                              Ever_MarriedYes
##
                   1.13813
                                            -0.37499
                                                                       0.43830
##
                                        GraduatedYes
                       Age
                                                              ProfessionDoctor
##
                   0.02198
                                                                      -1.12548
                                             0.61117
##
        ProfessionEngineer ProfessionEntertainment
                                                          ProfessionExecutive
                  -0.84361
##
                                            -0.65089
                                                                      -1.46281
##
      ProfessionHealthcare
                                ProfessionHomemaker
                                                              ProfessionLawyer
##
                  -2.85500
                                            -1.56710
                                                                      -1.92905
##
       ProfessionMarketing
                                     Work_Experience
                                                            Spending_ScoreHigh
##
                  -2.24809
                                            -0.02241
                                                                      -0.09116
##
                                         Family_Size
         Spending_ScoreLow
##
                  -0.77079
                                            -0.12549
##
## Degrees of Freedom: 3372 Total (i.e. Null); 3356 Residual
## Null Deviance:
                        4670
## Residual Deviance: 3391 AIC: 3425
glmAD_ <- glm(formula = Segmentation ~ Gender + Ever_Married + Age + Graduated +
    Profession + Work_Experience + Spending_Score + Family_Size,
    family = "binomial", data = trainAD)
predictAD_ <- ifelse(glmAD_$fitted.values>0.5,'A','D')
confusionAD_ <- table(predictAD_, ifelse(trainAD$Segmentation==1,'A','D'), dnn=c("Predicted","True"))</pre>
confusionAD_{-}
            True
## Predicted
               Α
                     D
           A 1279 482
##
           D 337 1275
sum(diag(confusionAD_)) / sum(confusionAD_)
## [1] 0.7571894
anova(glmAD_)
## Analysis of Deviance Table
## Model: binomial, link: logit
##
## Response: Segmentation
## Terms added sequentially (first to last)
##
##
##
                   Df Deviance Resid. Df Resid. Dev
## NULL
                                     3372
                                              4670.1
```

```
7.76
## Gender
                                    3371
                                             4662.3
                    1
## Ever_Married
                        373.25
                                    3370
                                             4289.1
                    1
## Age
                        155.17
                                    3369
                                             4133.9
## Graduated
                                             3974.0
                    1
                        159.91
                                    3368
## Profession
                    8
                       537.50
                                    3360
                                             3436.5
## Work Experience 1
                        1.92
                                    3359
                                             3434.6
## Spending Score
                    2
                         25.30
                                    3357
                                             3409.3
## Family_Size
                        18.74
                                    3356
                                             3390.5
                    1
```

Model B&C

```
trainBC <- rbind(trainB, trainC)</pre>
trainBC$Segmentation <- ifelse(trainBC$Segmentation=="B",1,0)</pre>
glmBC <- glm(Segmentation~., data=trainBC, family='binomial')</pre>
stepAIC(glmBC, scope=list(upper=glmBC, lower=~1), direction = "backward",
    k = 2, trace = FALSE)
##
## Call: glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +
##
       Spending_Score + Family_Size + Var_1, family = "binomial",
##
       data = trainBC)
##
## Coefficients:
##
               (Intercept)
                                          GenderMale
                                                                            Age
##
                  0.557458
                                            0.119099
                                                                      -0.007687
##
              GraduatedYes
                                    ProfessionDoctor
                                                            ProfessionEngineer
##
                  -0.491081
                                            0.188615
                                                                       1.142981
## ProfessionEntertainment
                                 ProfessionExecutive
                                                          ProfessionHealthcare
                  0.811586
                                            0.309467
##
                                                                      -0.568501
##
       ProfessionHomemaker
                                    ProfessionLawyer
                                                           ProfessionMarketing
##
                  1.163062
                                            0.419431
                                                                      -0.320363
                                                                   Family_Size
##
        Spending_ScoreHigh
                                   Spending_ScoreLow
##
                  0.398582
                                            0.780922
                                                                      -0.195134
##
                Var_1Cat_2
                                          Var_1Cat_3
                                                                     Var_1Cat_4
##
                  0.130605
                                            0.171596
                                                                       0.806180
##
                Var_1Cat_5
                                          Var_1Cat_6
                                                                     Var_1Cat_7
##
                  0.387076
                                           -0.139419
                                                                       0.085298
## Degrees of Freedom: 3291 Total (i.e. Null); 3271 Residual
## Null Deviance:
                         4557
## Residual Deviance: 4203 AIC: 4245
glmBC <- glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +</pre>
    Spending_Score + Family_Size + Var_1, family = "binomial",
    data = trainBC)
predictBC <- ifelse(glmBC $fitted.values>0.5,'B','C')
confusionBC_ <- table(predictBC_, ifelse(trainBC$Segmentation==1,'B','C'), dnn=c("Predicted","True"))</pre>
confusionBC_
##
            True
## Predicted
                В
                     C
           B 930 517
           C 642 1203
```

```
sum(diag(confusionBC_)) / sum(confusionBC_)
## [1] 0.6479344
anova(glmBC_)
## Analysis of Deviance Table
## Model: binomial, link: logit
##
## Response: Segmentation
##
## Terms added sequentially (first to last)
##
##
##
                  Df Deviance Resid. Df Resid. Dev
## NULL
                                    3291
                                             4557.0
                                    3290
## Gender
                        0.039
                                             4557.0
## Age
                   1
                        5.684
                                    3289
                                             4551.3
## Graduated
                       47.564
                                    3288
                   1
                                             4503.7
## Profession
                   8 107.890
                                    3280
                                             4395.8
## Spending_Score 2 114.577
                                    3278
                                             4281.3
## Family_Size
                                    3277
                                             4251.5
                   1
                       29.763
## Var 1
                       48.745
                                    3271
                                             4202.8
Model B&D
trainBD <- rbind(trainB, trainD)</pre>
trainBD$Segmentation <- ifelse(trainBD$Segmentation=="B",1,0)</pre>
glmBD <- glm(Segmentation~., data=trainBD, family='binomial')</pre>
stepAIC(glmBD, scope=list(upper=glmBD, lower=~1), direction = "backward",
    k = 2, trace = FALSE)
##
  Call: glm(formula = Segmentation ~ Gender + Ever_Married + Age + Graduated +
       Profession + Work_Experience + Spending_Score + Var_1, family = "binomial",
       data = trainBD)
##
##
  Coefficients:
                                                               Ever_MarriedYes
##
               (Intercept)
                                          GenderMale
                   0.79601
                                            -0.58881
##
                                                                       0.33755
##
                                        GraduatedYes
                                                              ProfessionDoctor
                        Age
##
                   0.03693
                                             0.91022
                                                                      -1.56430
##
        ProfessionEngineer ProfessionEntertainment
                                                           ProfessionExecutive
##
                  -1.68466
                                            -1.57940
                                                                       -1.71245
                                                              ProfessionLawyer
##
      ProfessionHealthcare
                                 ProfessionHomemaker
##
                  -2.81064
                                            -1.94790
                                                                      -2.80849
##
       ProfessionMarketing
                                     Work_Experience
                                                            Spending_ScoreHigh
##
                  -2.95069
                                            -0.07615
                                                                       -0.42440
##
         Spending_ScoreLow
                                          Var_1Cat_2
                                                                    Var_1Cat_3
##
                  -1.77249
                                             0.92486
                                                                       0.56443
                                          Var_1Cat_5
                                                                    Var_1Cat_6
##
                Var_1Cat_4
##
                   0.01167
                                             0.79443
                                                                       0.41402
```

```
##
                Var 1Cat 7
##
                   0.55725
##
## Degrees of Freedom: 3328 Total (i.e. Null); 3307 Residual
## Null Deviance:
                        4605
## Residual Deviance: 2752 AIC: 2796
glmBD_ <- glm(formula = Segmentation ~ Gender + Ever_Married + Age + Graduated +</pre>
   Profession + Work_Experience + Spending_Score + Var_1, family = "binomial",
   data = trainBD)
predictBD_ <- ifelse(glmBD_$fitted.values>0.5, 'B', 'D')
confusionBD_ <- table(predictBD_, ifelse(trainBD$Segmentation==1,'B','D'), dnn=c("Predicted","True"))</pre>
confusionBD
##
            True
## Predicted
              В
                     D
##
           B 1290 309
##
           D 282 1448
sum(diag(confusionBD_)) / sum(confusionBD_)
## [1] 0.8224692
anova(glmBD_)
## Analysis of Deviance Table
## Model: binomial, link: logit
## Response: Segmentation
## Terms added sequentially (first to last)
##
##
##
                   Df Deviance Resid. Df Resid. Dev
## NULL
                                    3328
                                             4604.7
                         10.31
## Gender
                    1
                                    3327
                                             4594.4
                        784.05
                                    3326
                                             3810.3
## Ever_Married
                    1
                    1
                        181.46
                                    3325
                                             3628.9
## Age
## Graduated
                    1
                        227.83
                                    3324
                                             3401.0
## Profession
                    8 461.05
                                             2940.0
                                    3316
## Work Experience 1
                        24.41
                                    3315
                                             2915.6
## Spending_Score
                    2 144.09
                                    3313
                                             2771.5
## Var_1
                        19.37
                                    3307
                                             2752.1
Model C&D
trainCD <- rbind(trainC,trainD)</pre>
```

```
trainCD <- rbind(trainC,trainD)
trainCD$Segmentation <- ifelse(trainCD$Segmentation=="C",1,0)
glmCD <- glm(Segmentation~., data=trainCD, family='binomial')
stepAIC(glmCD, scope=list(upper=glmCD, lower=~1), direction = "backward",
    k = 2, trace = FALSE)</pre>
```

##

```
## Call: glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +
##
       Work_Experience + Spending_Score + Family_Size + Var_1, family = "binomial",
##
       data = trainCD)
##
##
  Coefficients:
                                          GenderMale
##
               (Intercept)
                                                                            Age
                  -0.04193
                                             -0.39914
                                                                        0.03749
##
                                    ProfessionDoctor
              GraduatedYes
##
                                                            ProfessionEngineer
##
                   1.20850
                                             -1.54516
                                                                       -2.28253
##
  ProfessionEntertainment
                                 ProfessionExecutive
                                                          ProfessionHealthcare
                  -1.95901
                                            -1.71081
                                                                       -2.33919
##
       ProfessionHomemaker
                                    ProfessionLawyer
                                                           ProfessionMarketing
                  -2.50197
##
                                            -2.44365
                                                                       -2.47576
##
           Work_Experience
                                  Spending_ScoreHigh
                                                             Spending_ScoreLow
##
                  -0.06224
                                            -0.64709
                                                                       -2.18601
##
               Family_Size
                                          Var_1Cat_2
                                                                    Var_1Cat_3
##
                   0.27567
                                             0.42948
                                                                        0.37791
##
                Var 1Cat 4
                                          Var 1Cat 5
                                                                    Var 1Cat 6
##
                  -0.77128
                                            -0.17661
                                                                        0.55369
##
                Var 1Cat 7
##
                   0.32445
##
## Degrees of Freedom: 3476 Total (i.e. Null); 3455 Residual
## Null Deviance:
                         4820
## Residual Deviance: 2533 AIC: 2577
glmCD_ <- glm(formula = Segmentation ~ Gender + Age + Graduated + Profession +
    Work_Experience + Spending_Score + Family_Size + Var_1, family = "binomial",
    data = trainCD)
predictCD_ <- ifelse(glmCD_$fitted.values>0.5,'C','D')
confusionCD_ <- table(predictCD_, ifelse(trainCD$Segmentation==1,'C','D'), dnn=c("Predicted","True"))</pre>
confusionCD_{-}
##
            True
## Predicted
                C
                     D
##
           C 1426 224
##
           D 294 1533
sum(diag(confusionCD_)) / sum(confusionCD_)
## [1] 0.851021
anova(glmCD_)
## Analysis of Deviance Table
## Model: binomial, link: logit
## Response: Segmentation
## Terms added sequentially (first to last)
##
                   Df Deviance Resid. Df Resid. Dev
## NULL
                                     3476
                                              4819.8
```

##	Gender	1	9.51	3475	4810.2	
##	Age	1	913.15	3474	3897.1	
##	Graduated	1	381.73	3473	3515.4	
##	Profession	8	556.12	3465	2959.2	
##	Work_Experience	1	17.81	3464	2941.4	
##	Spending_Score	2	302.33	3462	2639.1	
##	Family_Size	1	44.38	3461	2594.7	
##	Var_1	6	61.24	3455	2533.5	

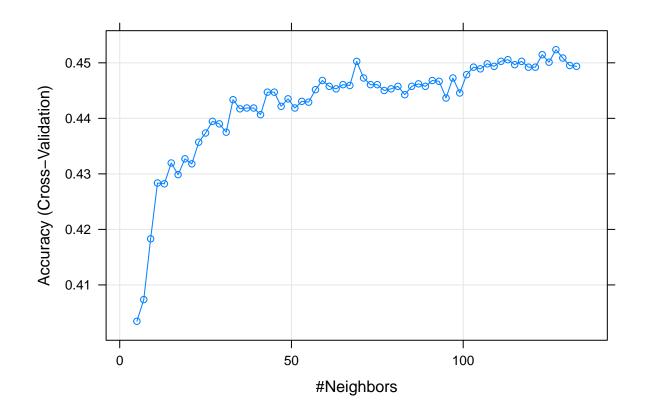
```
train <- na.omit(read_csv("Train.csv"))
test <- na.omit(read_csv("Test.csv"))
str(train)</pre>
```

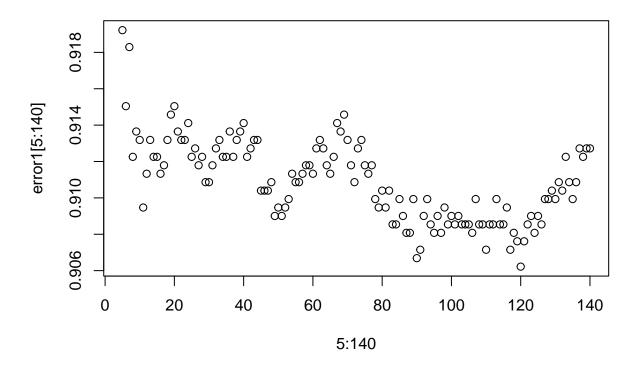
First KNN Model:

```
train.set <- train[,-1]</pre>
set.seed(123)
control <- trainControl(method = 'cv', number = 10)</pre>
model <- train(Segmentation~.,train.set[,c(3,6,8,10)],</pre>
              method = 'knn',preProcess="scale",
               trControl = control,tuneLength=65)
model
## k-Nearest Neighbors
##
## 6665 samples
##
      3 predictor
##
      4 classes: 'A', 'B', 'C', 'D'
##
## Pre-processing: scaled (3)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 5998, 5998, 5999, 5998, 5999, ...
## Resampling results across tuning parameters:
##
##
         Accuracy
    k
                     Kappa
##
      5 0.4034577 0.2028580
##
      7 0.4073558 0.2080819
##
      9 0.4183075 0.2225901
##
      11 0.4283561 0.2359381
##
      13 0.4282068 0.2356714
     15 0.4319577 0.2405476
##
##
     17 0.4298576 0.2375914
##
     19 0.4327107 0.2413202
##
      21 0.4318057 0.2400950
##
      23 0.4357087 0.2452556
##
      25 0.4373597 0.2474201
##
      27 0.4394580 0.2502838
##
      29 0.4390050 0.2495916
      31 0.4375096 0.2474977
##
##
      33 0.4433612 0.2553345
##
      35 0.4417123 0.2530781
##
      37 0.4418633 0.2532456
##
      39 0.4418615 0.2530975
##
      41 0.4406614 0.2513887
##
      43 0.4447123 0.2567816
     45 0.4447137 0.2568130
##
##
     47 0.4421627 0.2533445
##
     49 0.4435123 0.2550757
##
     51 0.4418622 0.2526841
     53 0.4430643 0.2543205
##
```

```
55 0.4429139 0.2540701
##
##
     57 0.4451623 0.2570583
     59 0.4468138 0.2593029
##
##
     61 0.4457634
                    0.2578076
##
     63 0.4453134
                    0.2572632
##
     65 0.4460644 0.2581716
##
     67 0.4459131 0.2579924
##
     69 0.4502636 0.2637778
##
     71 0.4472642 0.2597490
##
     73 0.4460646 0.2581522
##
     75 0.4460630
                    0.2581127
##
     77 0.4450144
                    0.2565884
##
     79 0.4453127
                    0.2569816
##
     81 0.4457641 0.2575397
##
     83 0.4442644
                    0.2555583
##
     85 0.4457634
                    0.2576333
##
     87 0.4462129
                    0.2582048
##
     89 0.4457636 0.2576397
##
     91 0.4468147
                    0.2590224
     93 0.4466641 0.2588592
##
##
     95 0.4436635 0.2548757
##
     97 0.4472647 0.2597095
##
     99 0.4445660 0.2561623
##
    101 0.4478664
                    0.2605754
##
    103 0.4492173 0.2623792
##
    105 0.4489159
                    0.2619709
##
    107 0.4498145
                   0.2631752
##
    109 0.4493643
                    0.2625749
##
    111 0.4502647
                    0.2637210
##
    113 0.4505646
                    0.2641212
##
    115 0.4496639
                    0.2629309
##
    117 0.4502629
                    0.2636678
##
    119 0.4492139
                    0.2622584
##
    121 0.4492144
                    0.2622508
##
    123 0.4514653
                    0.2652959
##
    125 0.4501148 0.2634681
##
    127 0.4523653
                    0.2664563
##
    129 0.4508656
                    0.2643161
##
    131 0.4495156
                    0.2625419
##
    133 0.4493643 0.2623087
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was k = 127.
```

plot(model)





Third KNN model with Dummy Varible(As it computation cost of time is too long, we do not choose to knit it)

```
nrow(train)
train.set <- train[,-1]</pre>
test.set <- test[,-1]</pre>
#Convert Categorical varibale into dummy variable
train.setnew <- dummy_cols(train.set, select_columns = c("Gender", "Ever_Married", "Graduated", "Profession
train.setnew[,c("Age","Family_Size")]<-scale(train.setnew[,c("Age","Family_Size")])</pre>
test.setnew <-dummy_cols(test.set, select_columns = c("Gender", "Ever_Married", "Graduated", "Profession",</pre>
test.setnew[,c("Age","Family_Size")]<-scale(test.setnew[,c("Age","Family_Size")])</pre>
error <- numeric()</pre>
for(i in 10:200){
pred1 <- neighbr:::knn(train_set=train.setnew[1:1000,-c(1:3)],test_set=test.setnew[1:300,-c(1:4)],k=i,c
pred1result <- pred1[["test_set_scores"]][["categorical_target"]]</pre>
tab<- table(pred1result, as.matrix(test.setnew[1:300,4]))</pre>
error[i] <- (1- sum(diag(tab))/sum(tab))</pre>
}
plot(10:200,error[10:200])
```

Convert categorical columns to numeric:

```
temp <- train
must_convert<-sapply(temp,is.character)
temp2<-sapply(temp[,must_convert],function(x){unclass(as.factor(x))})
train.num<-cbind(temp[,!must_convert],temp2)

temp <- test
must_convert<-sapply(temp,is.character)
temp2<-sapply(temp[,must_convert],function(x){unclass(as.factor(x))})
test.num<-cbind(temp[,!must_convert],temp2)</pre>
```

KNN second model

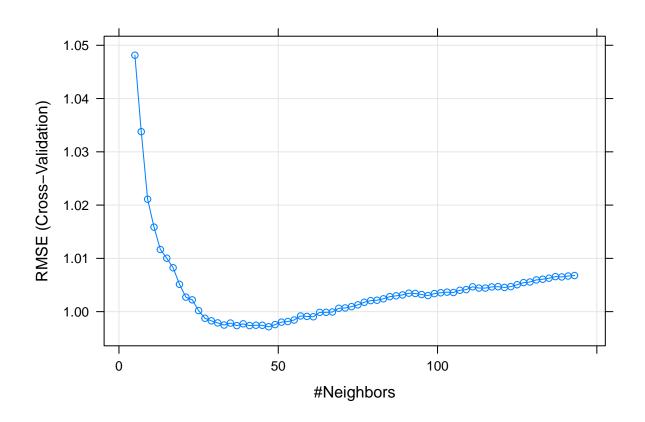
```
set.seed(123)
control <- trainControl(method = 'cv', number = 10,)</pre>
model2 <- train(Segmentation~.,train.num[,c(2:11)],</pre>
              method = 'knn',
              trControl = control,tuneLength=70)
model2
## k-Nearest Neighbors
##
## 6665 samples
##
     9 predictor
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 5998, 5999, 5998, 5999, 5999, 5998, ...
## Resampling results across tuning parameters:
##
##
    k
         RMSE
                    Rsquared MAE
##
      5 1.0481336 0.1665634 0.8166304
      7 1.0337842 0.1762270 0.8131512
##
##
      9 1.0211055 0.1880340 0.8091198
     11 1.0158628 0.1924518 0.8099176
##
     13 1.0116639 0.1965879 0.8101013
##
##
     15 1.0100283 0.1977287 0.8108885
     17 1.0082344 0.1993456 0.8114001
##
##
     19 1.0051292 0.2031531 0.8103063
##
     21 1.0027243 0.2062889 0.8089257
##
     23 1.0022127 0.2066451 0.8098545
     25 1.0001966 0.2092712 0.8095640
##
     27 0.9987559 0.2112101 0.8097898
##
##
     29 0.9982782 0.2116849 0.8097119
     31 0.9978841 0.2119801 0.8105058
##
##
     33 0.9974799 0.2124700 0.8113297
##
     35 0.9978557 0.2118079 0.8121565
##
     37 0.9973762 0.2123821 0.8123400
     39 0.9977117 0.2117434 0.8135274
##
```

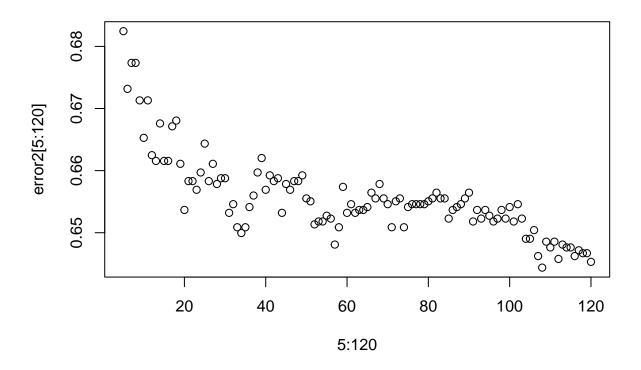
```
##
          0.9973742
                      0.2121801
                                  0.8143498
                      0.2119375
##
      43
          0.9974504
                                  0.8152208
##
          0.9974348
                      0.2118649
                                  0.8158460
          0.9971574
                      0.2123035
                                  0.8159947
##
      47
##
      49
          0.9975652
                      0.2116346
                                  0.8168275
                      0.2108923
##
          0.9980311
                                  0.8176461
      51
                      0.2106724
##
      53
          0.9981430
                                  0.8182342
##
      55
          0.9984278
                      0.2101852
                                  0.8189695
##
      57
          0.9991897
                      0.2089695
                                  0.8199925
##
      59
          0.9991051
                      0.2090539
                                  0.8202486
##
          0.9990382
                      0.2091200
                                  0.8207094
      61
          0.9998631
                      0.2078401
                                  0.8217672
##
##
          0.9998729
                      0.2077828
                                  0.8224014
      65
                      0.2076819
##
          0.9999272
                                  0.8227343
##
          1.0006301
                      0.2065560
                                  0.8239326
      69
##
      71
          1.0006900
                      0.2064228
                                  0.8243838
##
          1.0009367
                      0.2059997
      73
                                  0.8252408
##
          1.0012779
                      0.2054068
                                  0.8258449
          1.0017541
                      0.2046258
##
                                  0.8266452
##
          1.0020655
                      0.2041280
                                  0.8273514
##
          1.0021406
                      0.2039960
                                  0.8277855
##
          1.0024051
                      0.2035584
                                  0.8283847
          1.0028112
                      0.2028996
##
                                  0.8288981
      85
          1.0029680
                      0.2026216
                                  0.8295441
##
      87
##
      89
          1.0031344
                      0.2023529
                                  0.8300656
##
      91
          1.0034632
                      0.2018170
                                  0.8306467
##
          1.0034089
                      0.2018998
                                  0.8309411
      93
                      0.2022168
##
      95
          1.0032074
                                  0.8311022
##
          1.0030159
                      0.2025313
      97
                                  0.8311811
##
          1.0033846
                      0.2019361
                                  0.8317079
      99
##
     101
          1.0035383
                      0.2016634
                                  0.8322125
##
     103
          1.0036589
                      0.2015101
                                  0.8324826
##
     105
          1.0035957
                      0.2015819
                                  0.8328399
                      0.2009265
##
     107
          1.0040085
                                  0.8335584
##
     109
          1.0041318
                      0.2007399
                                  0.8340048
##
                      0.1998900
     111
          1.0046653
                                  0.8344960
##
     113
          1.0044259
                      0.2002342
                                  0.8345074
##
          1.0044251
                      0.2002392
                                  0.8348515
     115
##
          1.0046379
                      0.1998911
                                  0.8351727
     117
##
          1.0046882
                      0.1997979
     119
                                  0.8354208
##
                      0.2000175
     121
          1.0045428
                                  0.8356005
##
          1.0047006
                      0.1997697
                                  0.8359042
     123
                      0.1991931
##
     125
          1.0050548
                                  0.8365605
##
          1.0054456
                      0.1985585
                                  0.8369985
     127
                      0.1983655
##
     129
          1.0055606
                                  0.8373271
##
          1.0059533
                      0.1977376
     131
                                  0.8378330
##
     133
          1.0060846
                      0.1975109
                                  0.8380189
##
     135
          1.0062779
                      0.1971884
                                  0.8383435
##
     137
          1.0065766
                      0.1967027
                                  0.8387354
##
     139
          1.0065129
                      0.1967867
                                  0.8389980
##
     141
          1.0066852
                      0.1964948
                                  0.8392961
##
          1.0067792
                      0.1963423
                                  0.8396225
##
```

RMSE was used to select the optimal model using the smallest value.

The final value used for the model was k = 47.

```
plot(model2,)
```





LDA:

```
library (MASS)
lda_fit <- lda(Segmentation ~ ., data=train.set)</pre>
lda_fit
## Call:
## lda(Segmentation ~ ., data = train.set)
## Prior probabilities of groups:
          Α
                    В
                             C
## 0.2424606 0.2358590 0.2580645 0.2636159
##
## Group means:
    GenderMale Ever MarriedYes
                                  Age GraduatedYes ProfessionDoctor
## A 0.5420792
                   0.5816832 44.42141
                                          0.6342822
                                                          0.10396040
## B 0.5343511
                     0.7334606 48.11323
                                          0.7321883
                                                          0.08078880
## C 0.5377907
                     0.8034884 49.32791
                                          0.8337209
                                                          0.07151163
## D 0.5896414
                     0.2669323 32.95674
                                          0.3636881
                                                          0.09903244
    ProfessionEngineer ProfessionEntertainment ProfessionExecutive
## A
            0.13675743
                                   0.19801980
                                                       0.06064356
## B
            0.10114504
                                   0.12150127
                                                       0.09478372
## C
            0.03720930
                                   0.07267442
                                                       0.09534884
## D
            0.07854297
                                   0.09846329
                                                       0.05350028
    ProfessionHealthcare ProfessionHomemaker ProfessionLawyer ProfessionMarketing
              0.05445545
                            0.02970297
                                                  0.09715347
## B
              0.05407125
                                 0.02798982
                                                  0.08460560
                                                                     0.01526718
## C
              0.07209302
                                 0.01104651
                                                  0.07209302
                                                                     0.01686047
## D
              0.44393853
                                 0.03642573
                                                  0.04894707
                                                                     0.07626636
    Work_Experience Spending_ScoreHigh Spending_ScoreLow Family_Size Var_1Cat_2
                                                           2.431931 0.04393564
                                             0.7004950
## A
           2.888614
                           0.13242574
           2.393766
                            0.20038168
                                              0.4821883
                                                           2.682570 0.05661578
## B
## C
           2.224419
                            0.21511628
                                              0.3226744
                                                           2.961628 0.05000000
           2.997154
                            0.05976096
                                              0.8844622
                                                           3.241320 0.06602163
    Var_1Cat_3 Var_1Cat_4 Var_1Cat_5 Var_1Cat_6 Var_1Cat_7
## A 0.10829208 0.15965347 0.009900990 0.6373762 0.02599010
## B 0.09541985 0.11959288 0.012722646 0.6787532 0.02353690
## C 0.06860465 0.05348837 0.009883721 0.7813953 0.02325581
## D 0.10870803 0.17700626 0.011952191 0.5890723 0.02675014
## Coefficients of linear discriminants:
##
                                             LD2
                                                          LD3
## GenderMale
                          -0.27567501 -0.06744037 -0.055580025
## Ever MarriedYes
                          0.21238480 -0.36086140 0.606531538
                          ## GraduatedYes
                          ## ProfessionDoctor
                          -0.70548986 -0.25836226 -0.005320386
## ProfessionEngineer
                          -0.86792383 -1.17444903 0.968693436
## ProfessionEntertainment -0.76830638 -1.17992758 -0.545072715
## ProfessionExecutive
                          -0.67735270 -0.05011896 0.877298992
                         -1.73700523 1.50622088 1.020471421
## ProfessionHealthcare
```

```
## ProfessionHomemaker -1.13915853 -0.23702131 2.355337729
## ProfessionLawyer -1.38220299 -0.59633827 -1.082904651
## Family Size
                       0.05755677 0.25138063 -0.064077802
                        0.31634364 -0.10532162 1.461754618
## Var_1Cat_2
## Var_1Cat_3
                        0.18130552 -0.28510612 0.669520252
                       -0.10071548 -0.65989092 0.793716770
## Var_1Cat_4
## Var_1Cat_5
                        0.38267613 -0.30263089 1.756152842
                        ## Var_1Cat_6
## Var_1Cat_7
                        0.20777755 -0.26907176 0.064541355
##
## Proportion of trace:
##
     LD1
          LD2
                  LD3
## 0.8260 0.1687 0.0053
lda_conf_mat <- table(predict(lda_fit, newdata = test)$class, test$Segmentation)</pre>
lda_conf_mat
##
##
        A B C D
##
    A 250 165 119 179
    B 98 68 73 67
##
    C 183 135 150 147
##
    D 161 82 39 238
#misclassification error rate
1-sum(diag(lda_conf_mat)) / sum(lda_conf_mat)
```

[1] 0.6722377