

# Calculus Assignment 7

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- 1 Solve the following integrals using integration by parts:

$$\int_0^1 te^{2t} dt = \left[ \frac{t^2 e^{2t}}{2} - \frac{1}{2} \int e^{2t} dt \right]_0^1 = \frac{1e^2}{2} - \frac{e^2}{4} + C - \frac{0e^0}{2} + \frac{e^0}{4} + C = \frac{e^2 + 1}{4}$$

$$\begin{aligned} \int_{-1}^1 t^2 e^t dt &= [t^2 e^t - \int 2te^t dt]_0^1 = [t^2 e^t - 2te^t + 2e^t]_0^1 = \\ &= e - 2e + 2e + C - \left( \frac{1}{e} + \frac{2}{e} + \frac{2}{e} + C \right) = \frac{e^2 - 5}{e} \end{aligned}$$

$$\begin{aligned} \int_0^\pi t \cos(t) dt &= [t \sin(t) - \int \sin(t) dt]_0^1 = \\ &= \pi \sin(\pi) + \cos(\pi) + C - 0 \sin(0) - \cos(0) - C = -1 - 1 = -2 \end{aligned} \tag{1}$$

- 2 Compute the following integral using integration by parts:

$$\begin{aligned} \int_1^2 \ln(t) dt &= \int_1^2 1 * \ln(t) dt = [t \ln(t) - \int \frac{t}{t} dt]_1^2 = \\ &= 2 \ln(2) - 2 + C - \ln(1) + 1 - C = 2 \ln(2) - 1 \end{aligned} \tag{2}$$

3 Solve the following integrals using integration by parts:

$$\int_0^1 t e^{\frac{t^2}{2}} dt = \int_0^{\frac{1}{2}} e^{\frac{t^2}{2}} d\left(\frac{t^2}{2}\right) = [e^{\frac{t^2}{2}} + C]_0^1 = e^{\frac{1}{2}} - 1$$

$$\begin{aligned} \int_0^{\frac{\pi}{2}} e^{\cos(t)} \sin(t) dt &= \int_0^{\frac{\pi}{2}} -e^{\cos(t)} (-\sin(t)) dt = \int_0^{\frac{\pi}{2}} -e^{\cos(t)} d(\cos(t)) = \\ &= [-e^{\cos(t)}]_0^{\frac{\pi}{2}} = -1 + C + e - C = e - 1 \end{aligned} \quad (3)$$