

# CusToM Workshop

## **Kinematic tutorial**



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20/12/2019

# Pre-Work

Go in `Examples\1_Walking_Kinematic\POC0980A_normal_Anthropo`

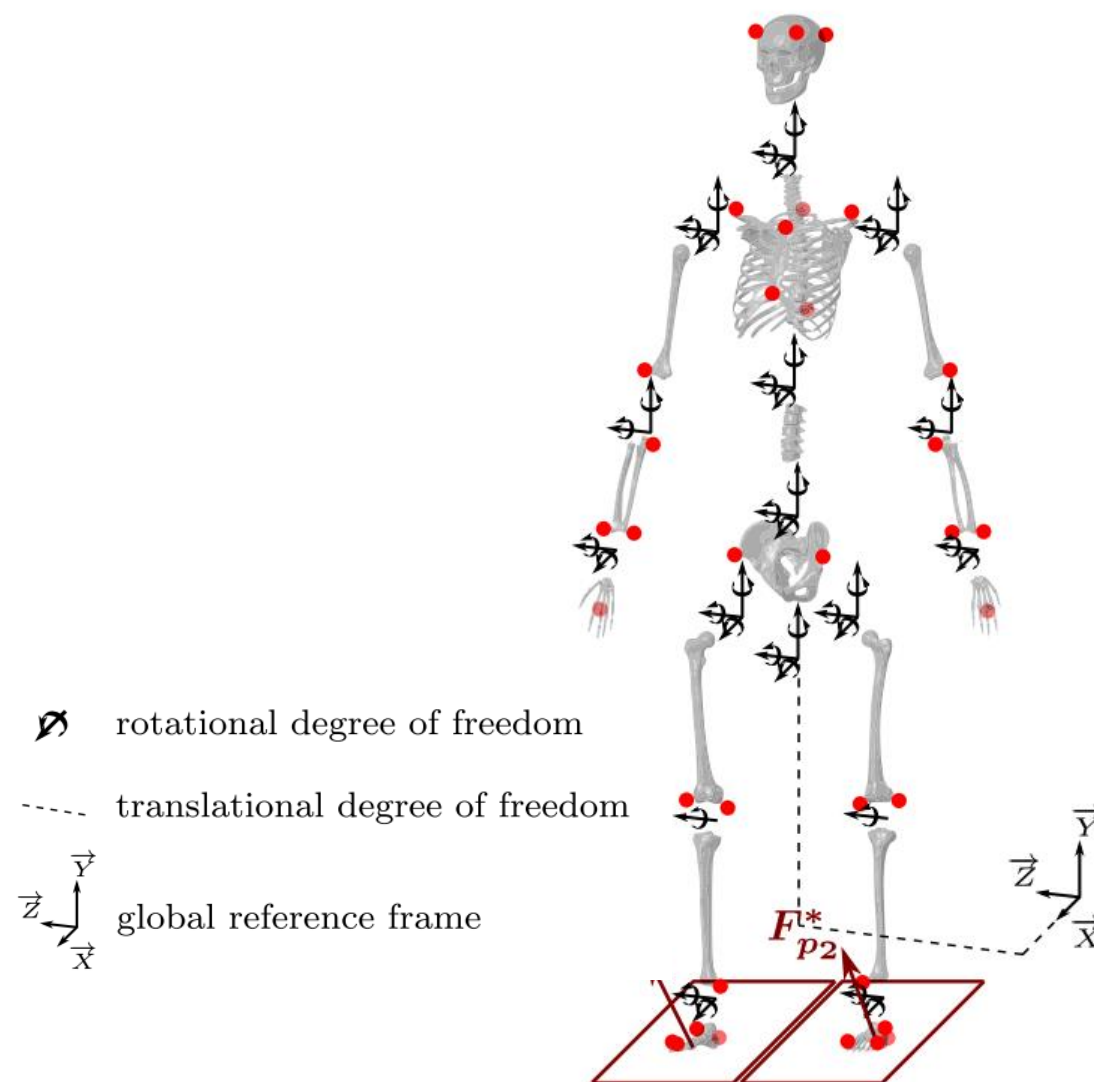
It contains :

|  |                  |             |
|--|------------------|-------------|
|  Marche.c3d                         | 16/12/2019 11:28 | Fichier C3D |
|  PostProcessingKinematic_Anthropo.m | 16/12/2019 11:52 | MATLAB Code |

# Generate Parameters of the Model

```
>> GenerateParameters|
```

- Size : 1.74 m
- Mass : 64 Kg
- Osteo-articular model – full body
  - Pelvis
  - Pelvis LowerTrunk
  - Leg
  - Arms
- Marker Set
  - MarkerSet\_2 (M2S makerset)
  - 1 markers on hand



# Generate Parameters of the Model

```
>> GenerateParameters
```

General Osteoarticular Markers Muscles

**Trunk**

Pelvis / Lower trunk PelvisLowerTrunk ▼

Upper trunk UpperTrunkClavicle ▼

Head Skull ▼

**Right leg**

Leg ▼

**Left leg**

Leg ▼

**Right arm**

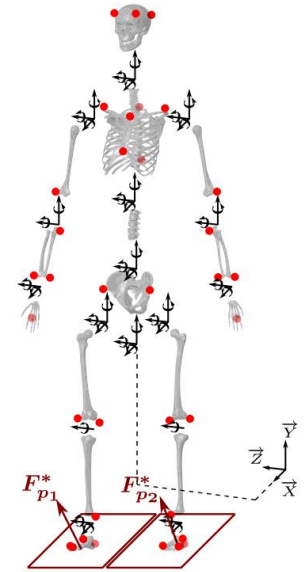
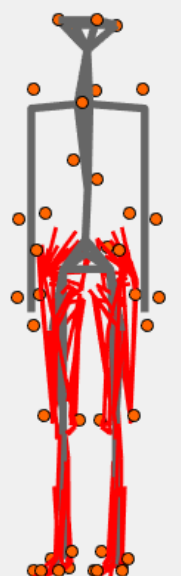
Arm ▼


**Left arm**


Arm ▼

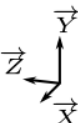
**Root** PelvisSacrum ▼

Generate parameters



 rotational degree of freedom

 translational degree of freedom

 global reference frame

- **Generate Parameters**

# Generate Parameters of the Model

```
>> GenerateParameters
```

General

Osteoarticular

Markers

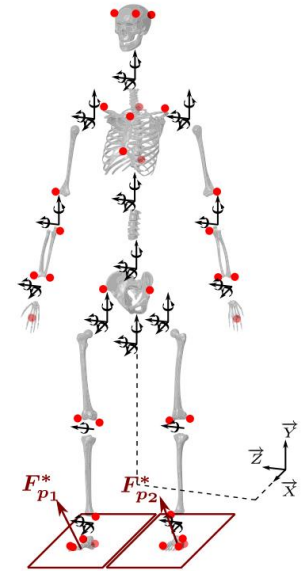
Muscles


Marker\_set2


Markers on hands1

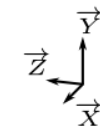
|      |       |      |      |
|------|-------|------|------|
| STRN | CLAV  | T10  | C7   |
| RSHO | LSHO  | RFWT | LFWT |
| RBWT | LBWT  | RFHD | LFHD |
| RBHD | LBHD  | RKNE | RANE |
| RANI | RKNI  | RHEE | RTAR |
| RTOE | RTARI | LKNE | LANE |
| LANI | LKNI  | LHEE | LTAR |
| LTOE | LTARI | RHUM | RRAD |
| RWRA | RWRB  | RCAR | LHUM |
| LRAD | LWRA  | LWRB | LCAR |

Generate parameters



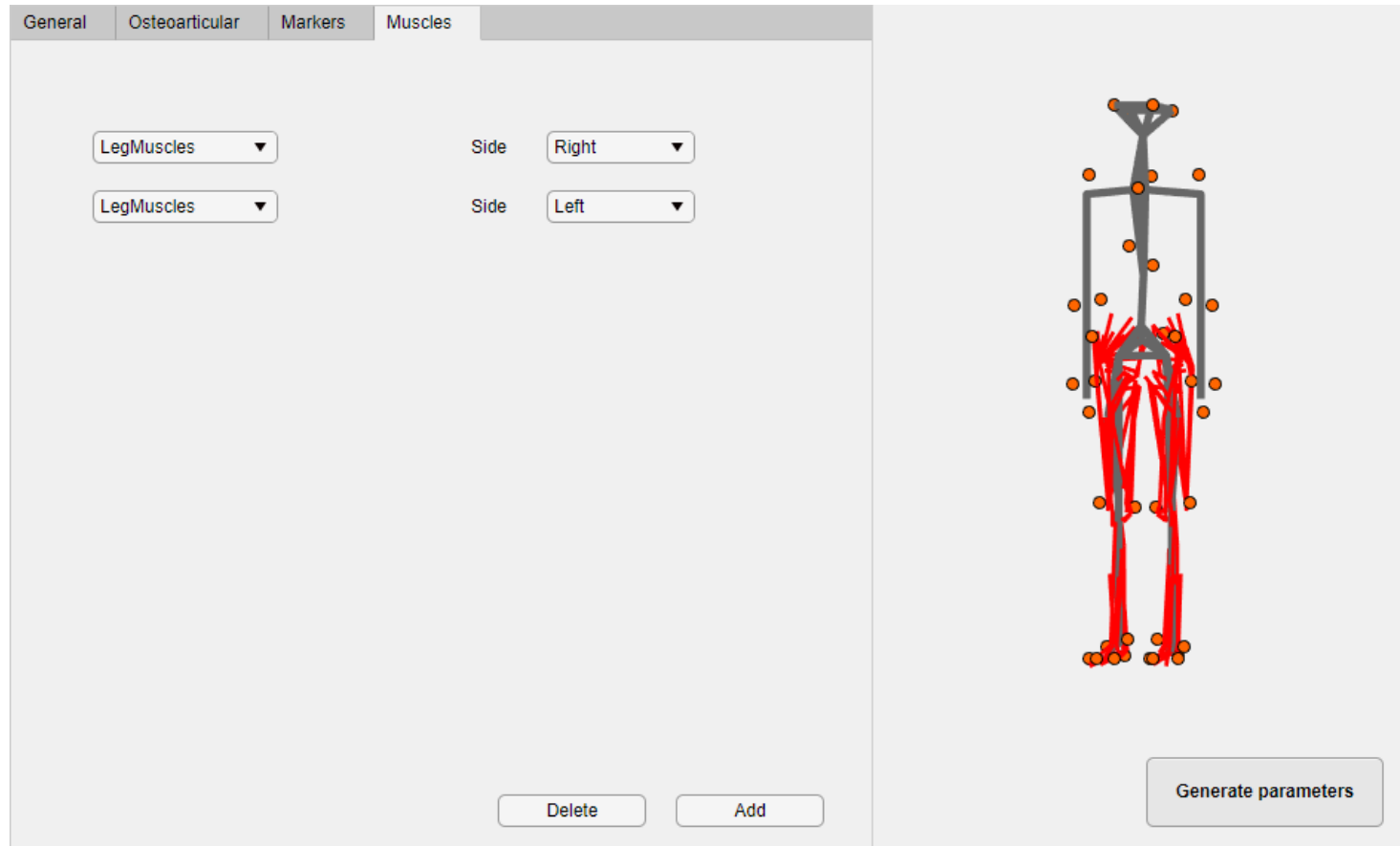
 rotational degree of freedom

 translational degree of freedom

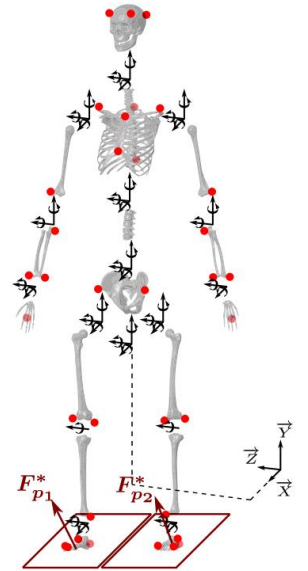
 global reference frame


# Generate Parameters of the Model


```
>> GenerateParameters
```

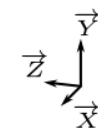


- **Generate Parameters**



 rotational degree of freedom

 translational degree of freedom

 global reference frame

## Only Inverse Kinematic Active Step

- Levenberg-marquardt
- 5Hz filter butterworth 2<sup>nd</sup> order zero lag

# What CusToM is Doing ?

```
Anthropometric Model Generation ...  
... Anthropometric Model Generation done
```

The osteoarticular model comes from cadaveric data.

Anthropometric scaling:

- Segments lengths
- Anatomical landmarks

$$k_0 = \frac{\textit{size of the subject}}{\textit{size of the cadaver}}$$



# What CusToM is Doing ?

Preliminary Computations ...

... Preliminary Computations done

A priori known location of anatomical landmarks are computed in the global reference frame  $R_0$  function of joint coordinates  $\mathbf{q}$

Jacobian matrix  $\mathbf{J}$  are computed analytically

- For Inverse kinematics using Levenberg-Marquardt algorithms

$$\mathbf{J} = \mathbf{J}_{f,q} + \mathbf{J}_{f,cut} * (\mathbf{J}_{cut,cut} * \mathbf{J}_{cut,q})$$

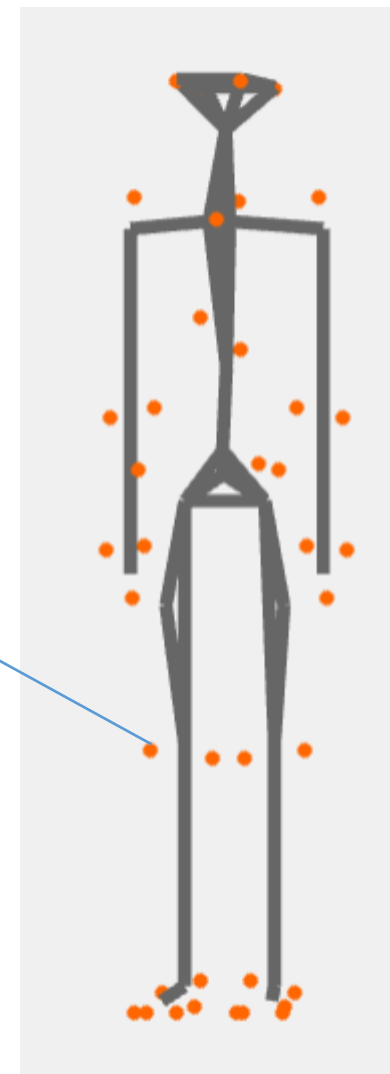
$${}^{R_0}\mathbf{X}_{marker} = f(\mathbf{q})$$

$$\mathbf{J}_{f,q}$$

$$\mathbf{J}_{f,cut}$$

$$\mathbf{J}_{cut,q}$$

$$\mathbf{J}_{cut,cut}$$



# What CusToM is Doing ?

```
Inverse kinematics (ChgtDirection04) ...  
... Inverse kinematics (ChgtDirection04) done
```

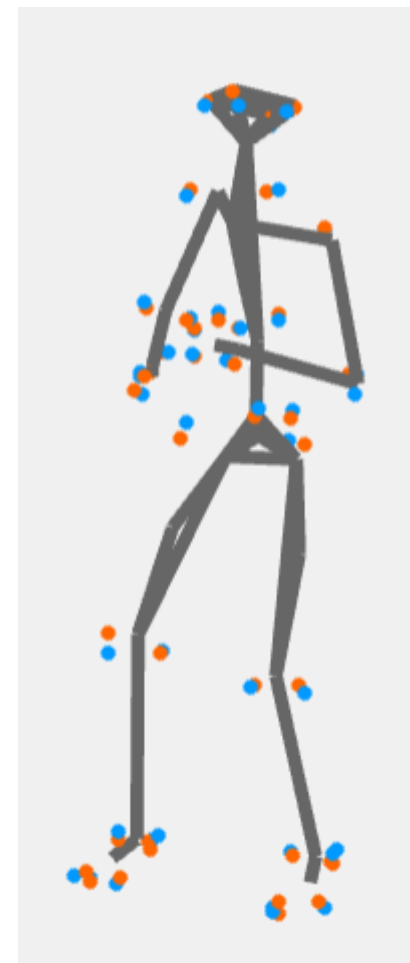
Euclidian distance minization between experimental markers  ${}^{R_0}\mathbf{X}_{exp,i}$  and *a priori* know location of anatomical landmarks  ${}^{R_0}\mathbf{X}_{mod,m}(\mathbf{q})$  in the global frame  $R_0$

$$\min_{\mathbf{q}} \sum_i^{N_{markers}} \left\| {}^{R_0}\mathbf{X}_{exp,i} - {}^{R_0}\mathbf{X}_{mod,m}(\mathbf{q}) \right\|^2$$

We get the joint coordinates  $\mathbf{q}$ .

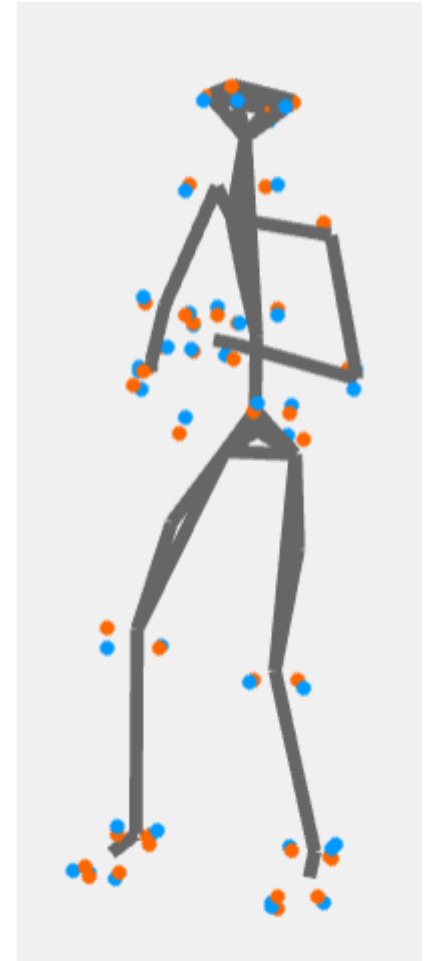
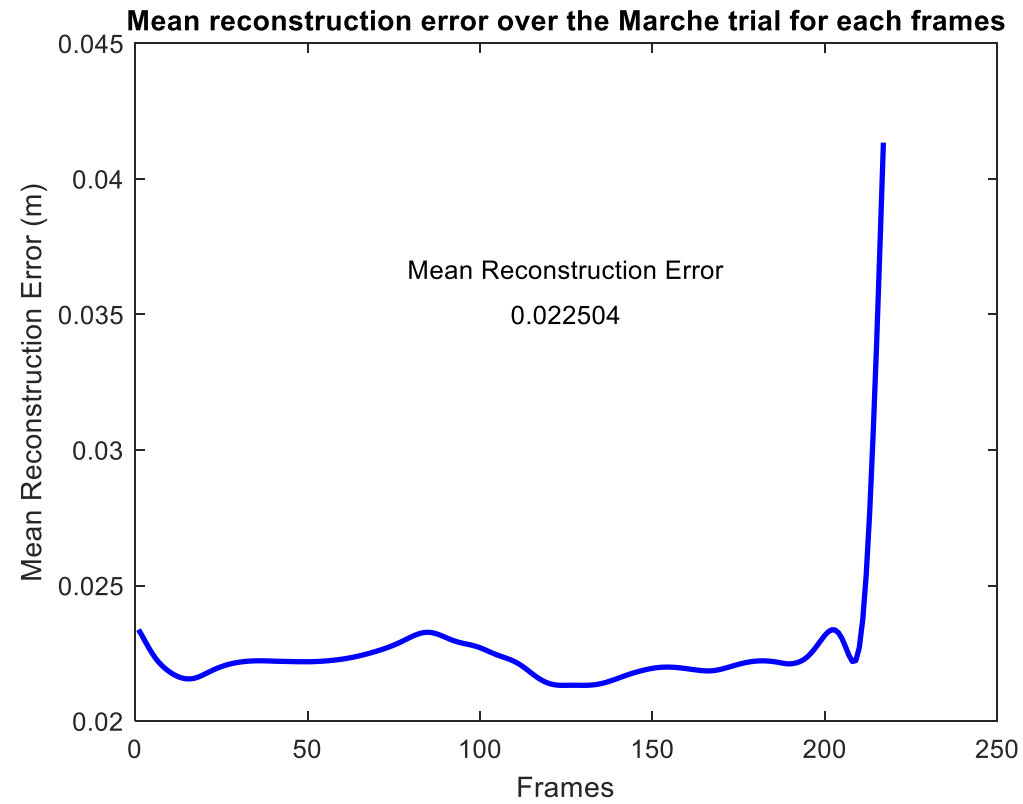
Levenberg-marquardt :  $(\mathbf{J}^T \mathbf{J} + \lambda \cdot \text{diag}(\mathbf{J}^T \mathbf{J})) \Delta \mathbf{q} = \mathbf{J}^T (\mathbf{X}_{exp} - \mathbf{X}_{mod}(\mathbf{q}))$

More details in Muller, A., 2017. Contributions méthodologiques à l'analyse musculo-squelettique de l'humain dans l'objectif d'un compromis précision performance. École normale supérieure de Rennes.



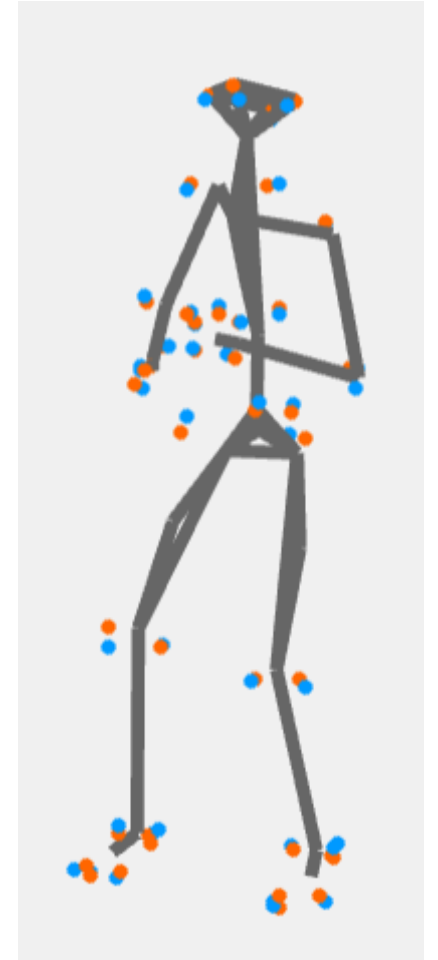
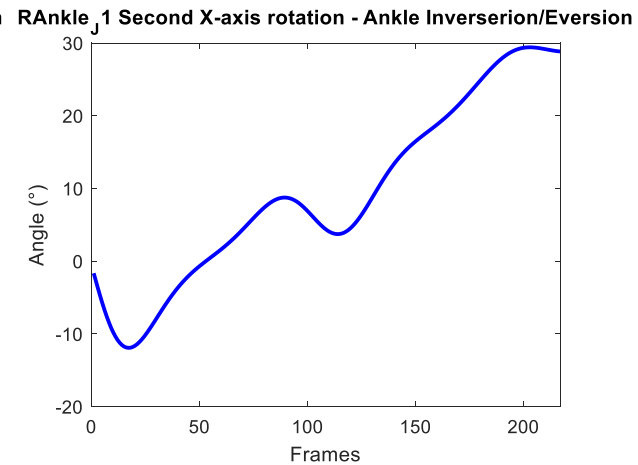
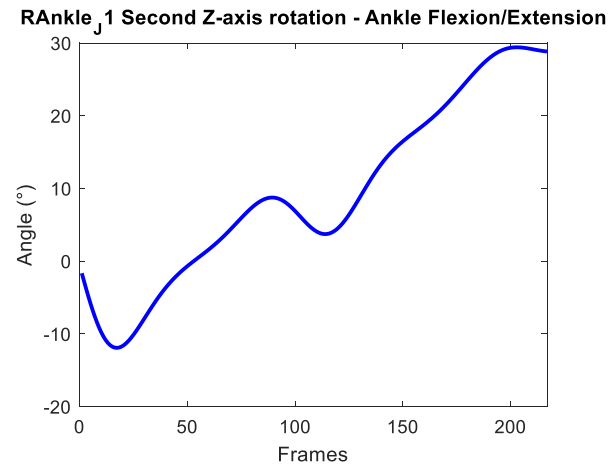
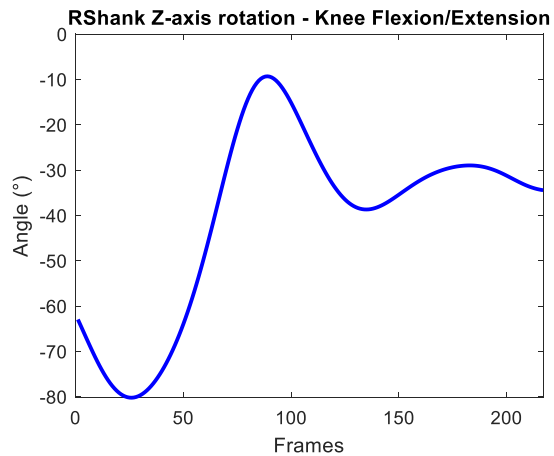
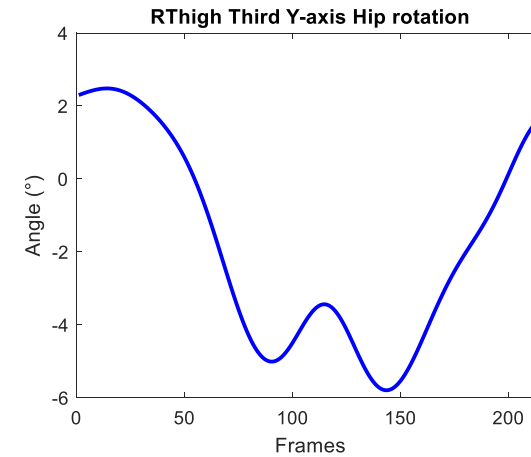
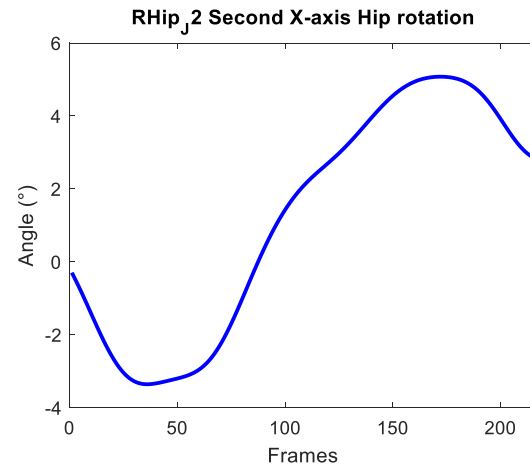
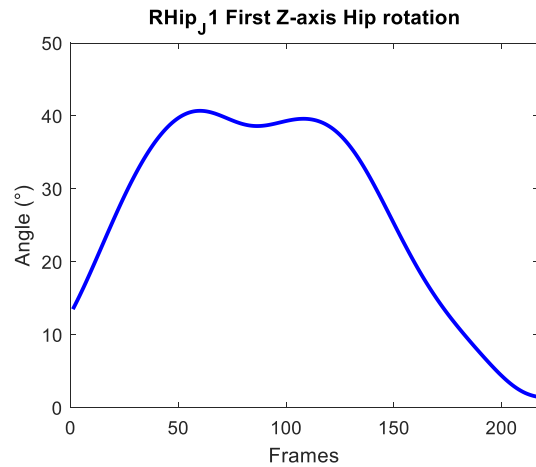
# First results – Kinematic residuals

```
>> PostProcessingKinematic_Anthropo
```



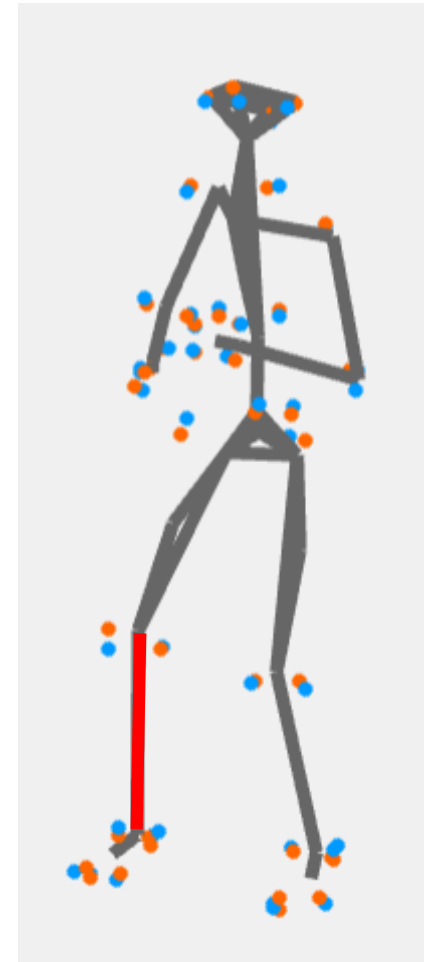
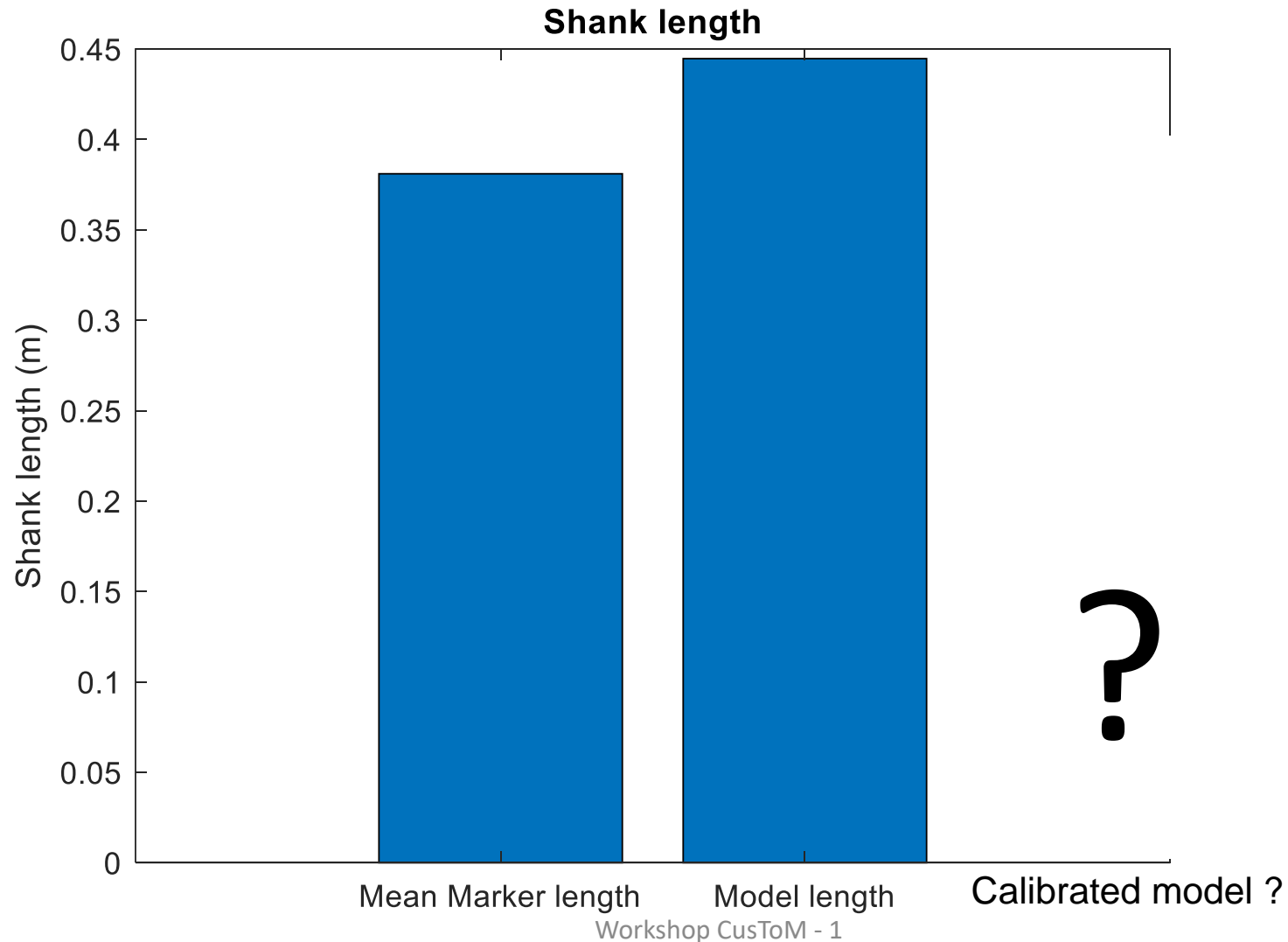
# First results – Joint coordinates

```
>> PostProcessingKinematic_Anthropo
```



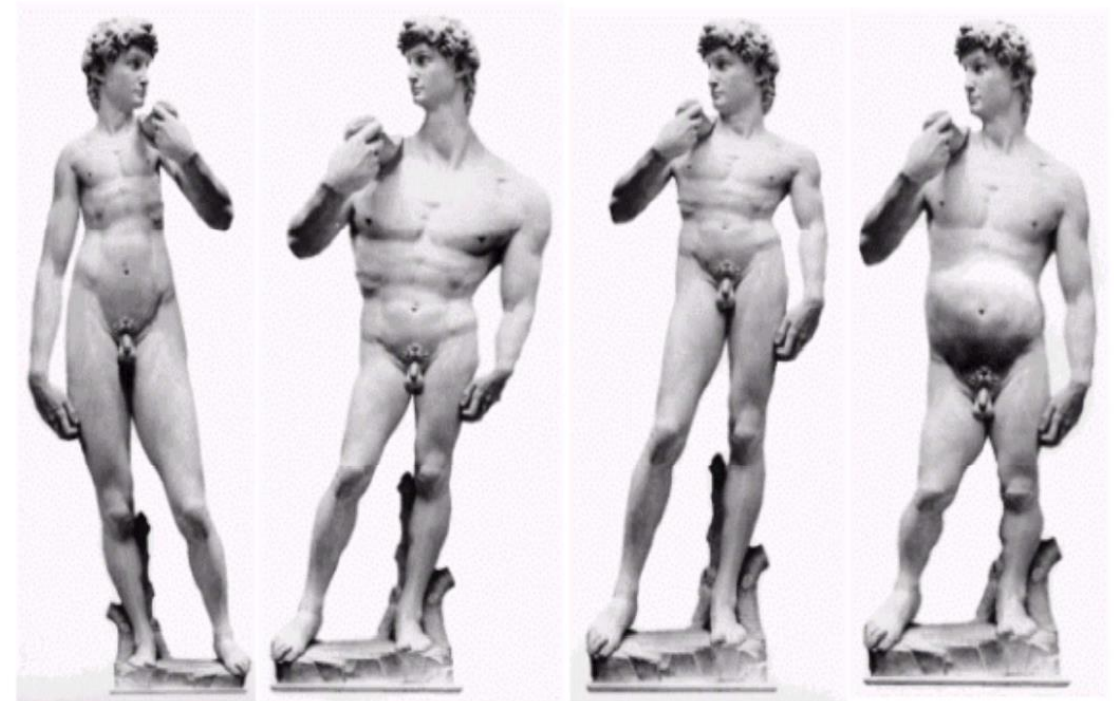
# What about the quality of the model ? – Right Shank length

```
>> PostProcessingKinematic_Anthropo
```



# What about the quality of the model ?






For a same size, segment lengths can vary between subjects.



# Pre-Work

Go in `Examples\1_Walking_Kinematic\POC0980A_normal_Geometric_Calibration`

It contains :

|   |                  |             |
|---|------------------|-------------|
|  Marche.c3d                            | 16/12/2019 11:28 | Fichier C3D |
|  PostProcessingCalibration.m           | 28/11/2018 18:20 | MATLAB Code |
|  PostProcessingKinematic_Calibration.m | 16/12/2019 14:02 | MATLAB Code |
|  PostProcessingShankLength.m           | 28/11/2018 21:58 | MATLAB Code |
|  ROM01.c3d                             | 30/01/2019 09:38 | Fichier C3D |

We will add a geometric calibration step

Same previous steps, except for AnalysisParameters.

# Geometrical Calibration step

- Frames used
  - Selection method of frames : **UniformlyDistributed**
  - Number of frames : **20**
- Body length
  - Homothetic factors of Clavicles are linked to homothetic factor of the Thorax
- Marker Position
  - Direction of markers to optimize in local frames ( Z is medio-lateral )
- Axis of rotation
  - Orientation of Joint axis can be optimized to fit subject-specific joint axis.
  - For example knee axis. Two rotation angles have to be introduced.



# What is CusToM Doing ?

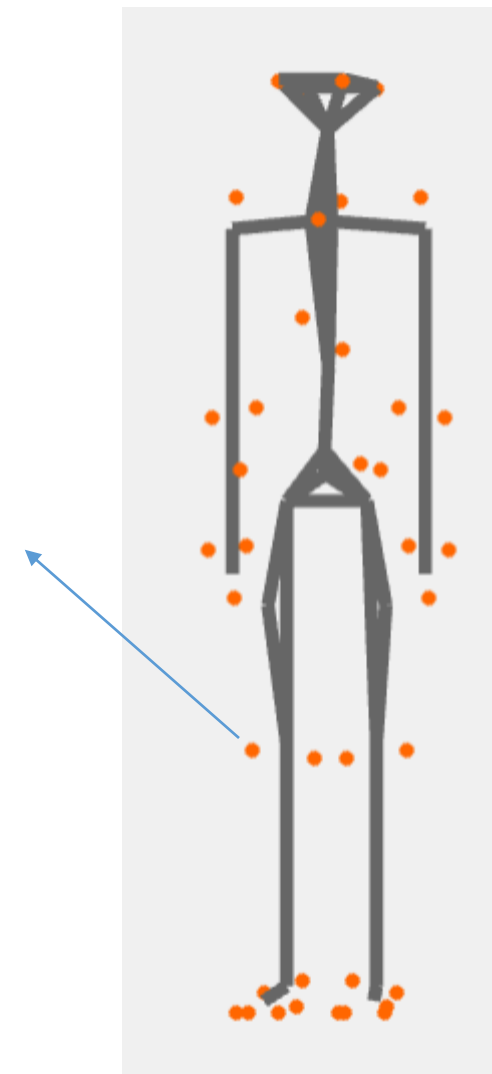
Geometrical Calibration ...

... Geometrical Calibration done

A priori known location of anatomical landmarks are computed in the global reference frame  $R_0$ , function of:

- joint coordinates  $\mathbf{q}$ ,
- homothetic factors  $\mathbf{k}$ ,
- variation of marker position  $\Delta\mathbf{p}$ ,
- rotation of joint axis  $\alpha$ .

$${}^{R_0}\mathbf{X}_{marker} = f(\mathbf{q}, \mathbf{k}, \Delta\mathbf{p}, \alpha)$$

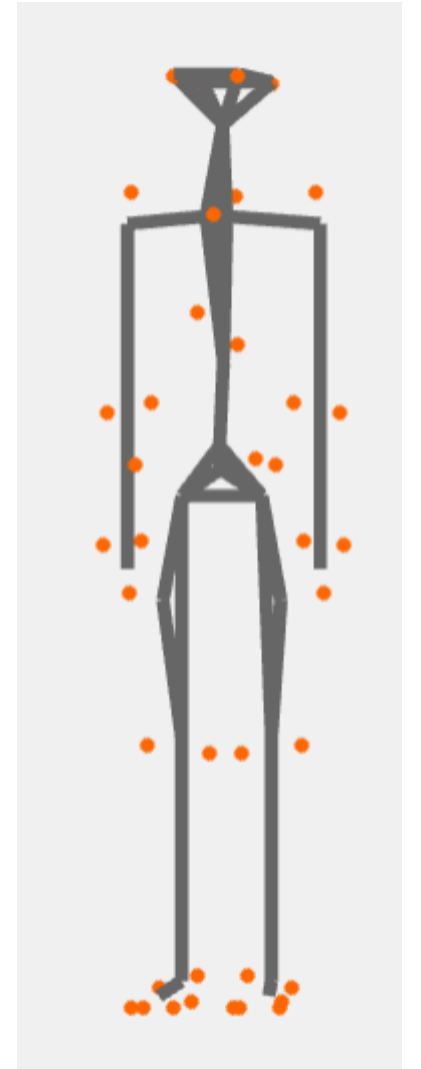


# What is CusToM Doing ?

```
Geometrical Calibration ...  
... Geometrical Calibration done
```

## Uniformly distributed frames

Frames are chosen equally spaced in ROM.c3d



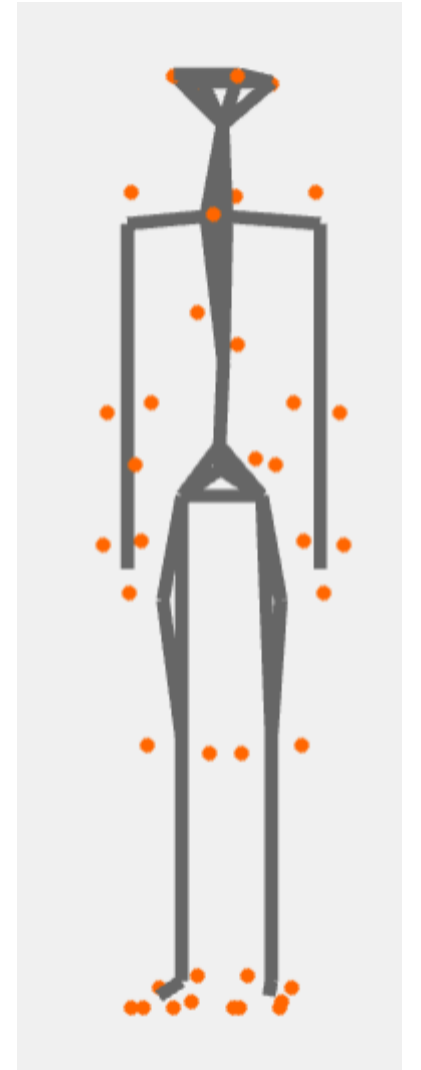
# What is CusToM Doing ?

|  |           |                                     |
|--|-----------|-------------------------------------|
| <input type="text" value="RClavicle"/> | Linked to | <input type="text" value="Thorax"/> |
| <input type="text" value="LClavicle"/> | Linked to | <input type="text" value="Thorax"/> |

## Body Length

Linear Constraints of homothetic factors.

$$\begin{cases} k_{RClavicle} - k_{Thorax} = 0 \\ k_{LClavicle} - k_{Thorax} = 0 \end{cases}$$



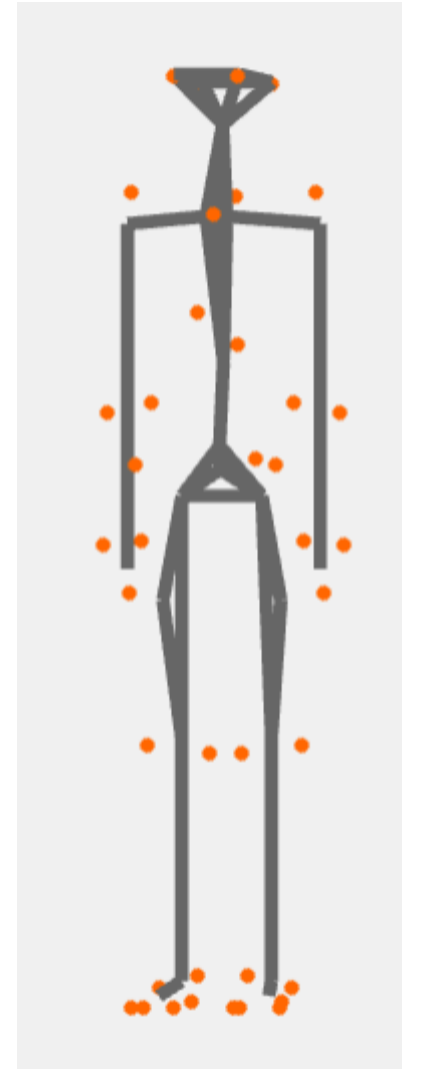
# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$



# What is CusToM Doing ?

Geometrical Calibration ...

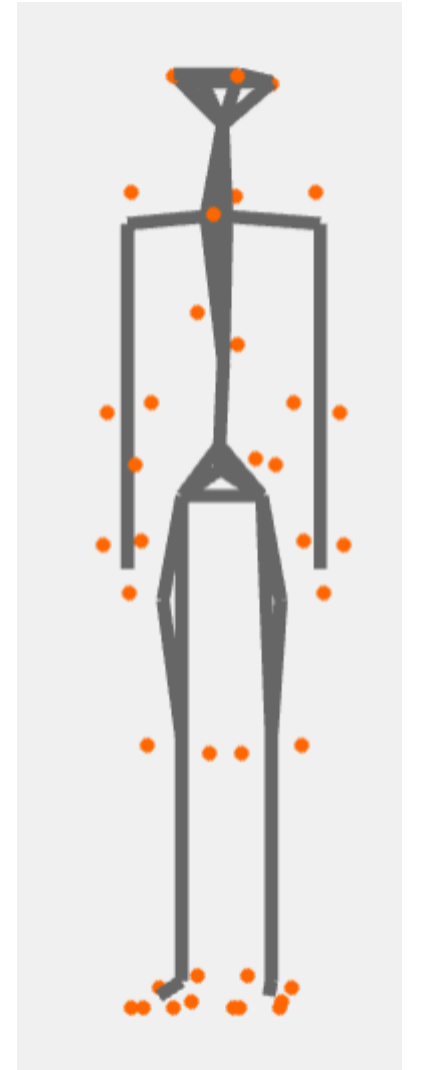
... Geometrical Calibration done

**Axis of rotation**

$${}^{R_i}\mathbf{X}_{marker} = {}^{R_i}\mathbf{p}_A + {}^{R_i}\Delta\mathbf{p}$$

Some location of markers are optimized

In this case :



# What is CusToM Doing ?

Geometrical Calibration ...

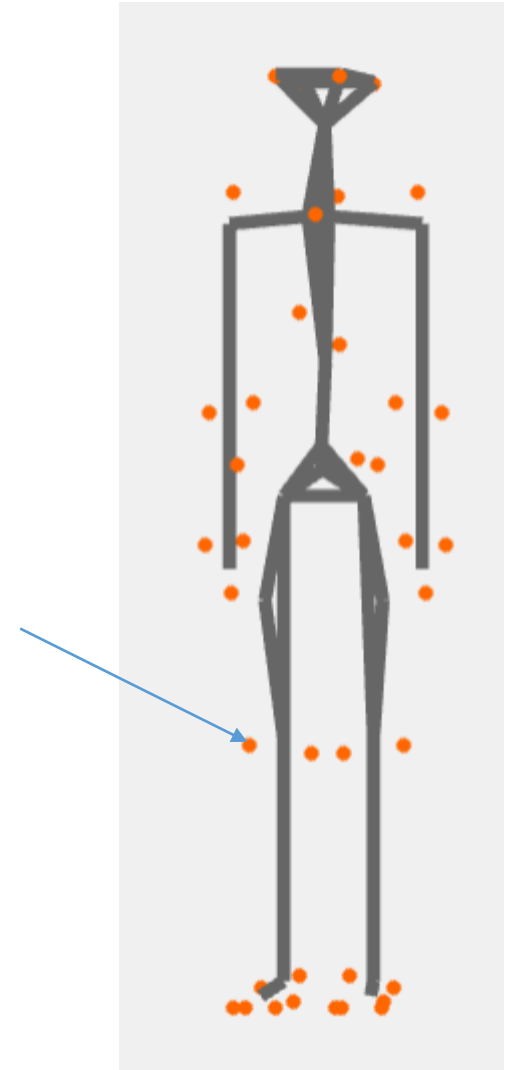
... Geometrical Calibration done

**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

Some location of markers are optimized

In this case :



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

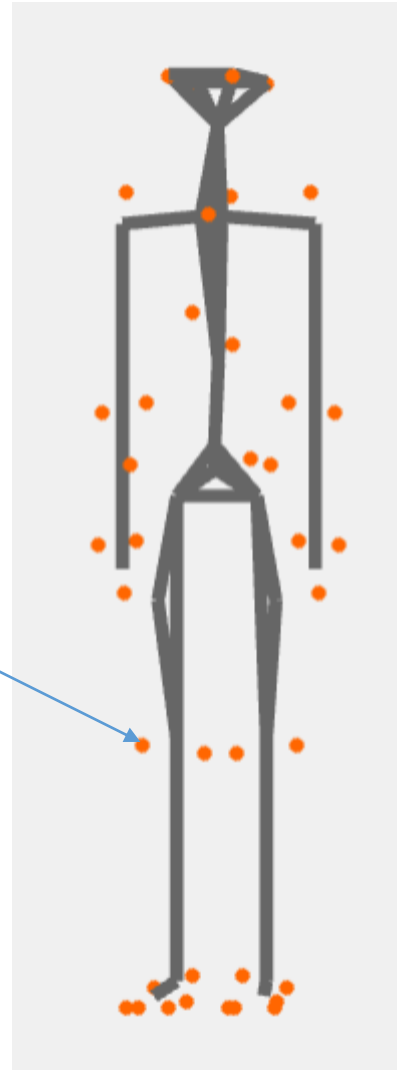
**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

Some location of markers are optimized

In this case :

**RKNE**



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

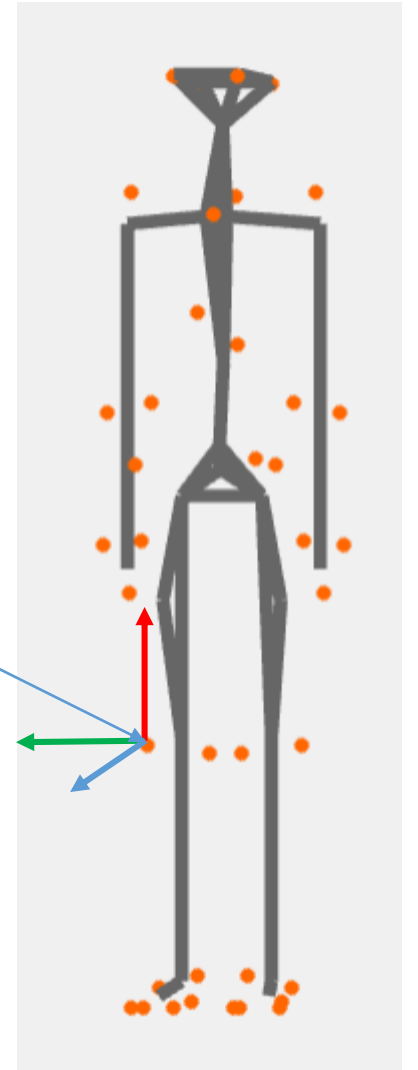
**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

Some location of markers are optimized

In this case :

**RKNE**





# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

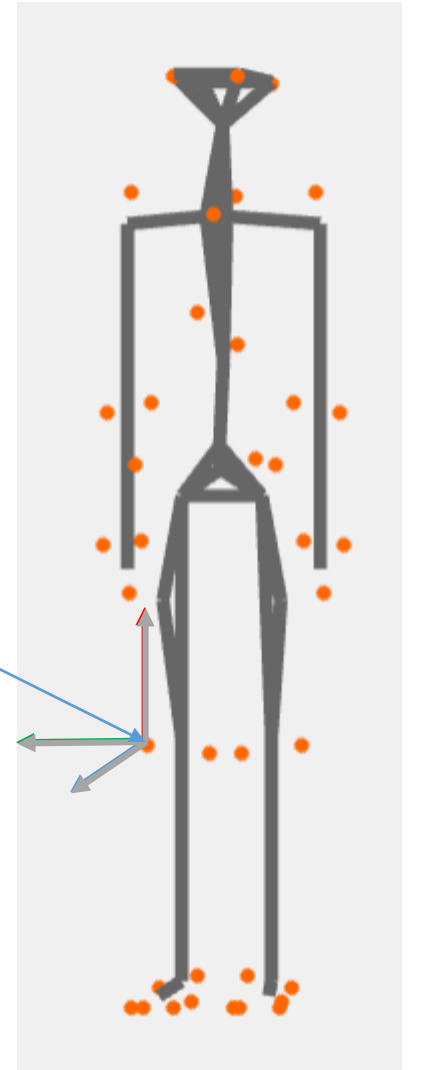
**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

Some location of markers are optimized

In this case :

**RKNE**



# What is CusToM Doing ?

Geometrical Calibration ...

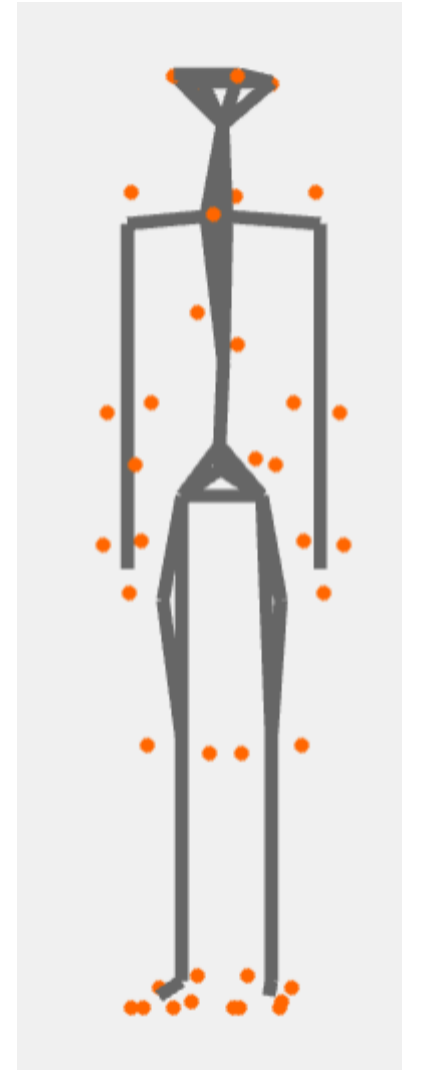
... Geometrical Calibration done

**Axis of rotation**

$${}^{R_i}\mathbf{X}_{marker} = {}^{R_i}\mathbf{p}_A + {}^{R_i}\Delta\mathbf{p}$$

Some location of markers are optimized

In this case :



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

**Axis of rotation**

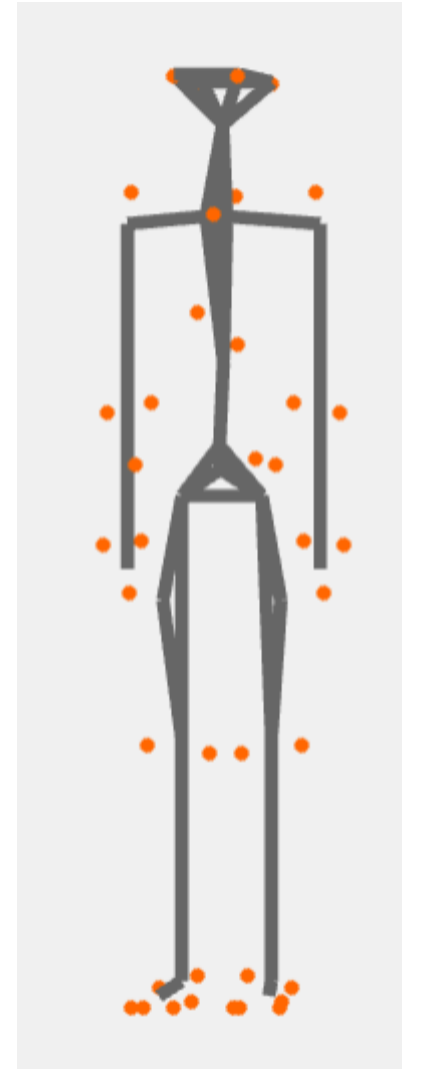
$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

Some location of markers are optimized

In this case :

- RKNE is trusted for x,y,z direction

RKNE

☐☐☐

# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

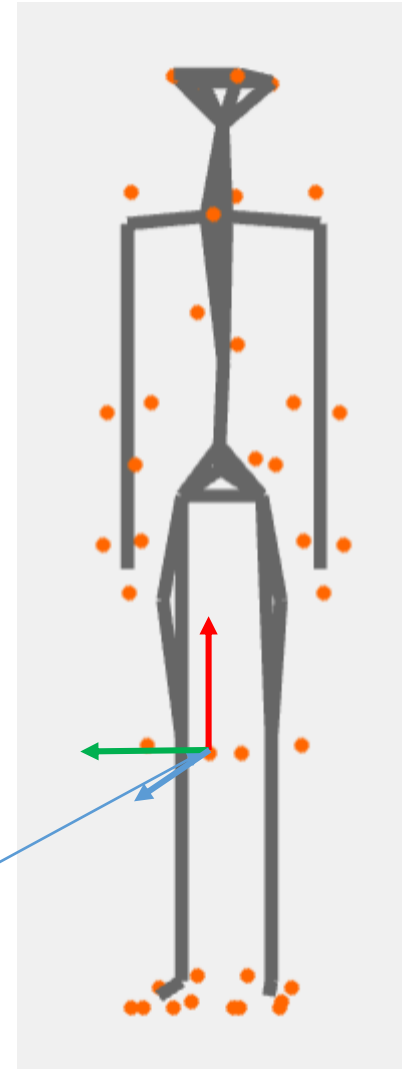
Some location of markers are optimized

In this case :

- RKNE is trusted for x,y,z direction

RKNE ☐ ☐ ☐

**RKNI**



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

**Axis of rotation**

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

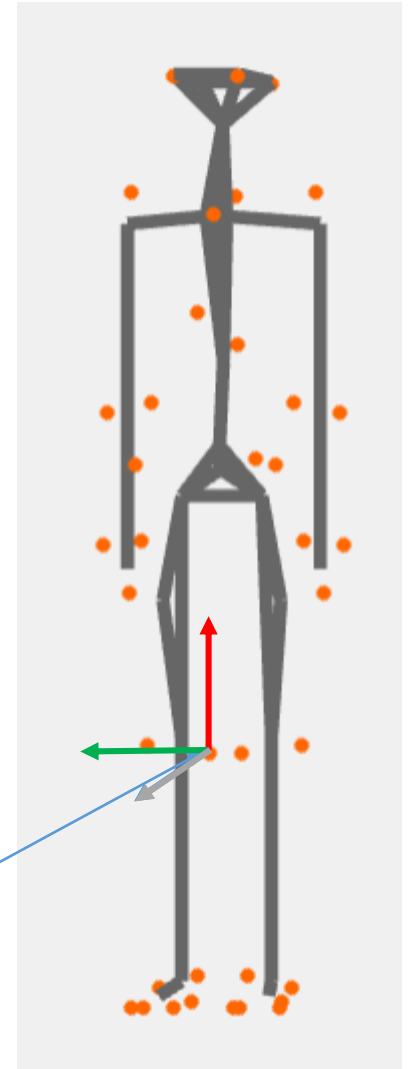
Some location of markers are optimized

In this case :

- RKNE is trusted for x,y,z direction

RKNE ☐ ☐ ☐

**RKNI**



# What is CusToM Doing ?

```
Geometrical Calibration ...  
... Geometrical Calibration done
```

## Axis of rotation

$${}^{R_i}X_{marker} = {}^{R_i}p_A + {}^{R_i}\Delta p$$

Some location of markers are optimized

In this case :

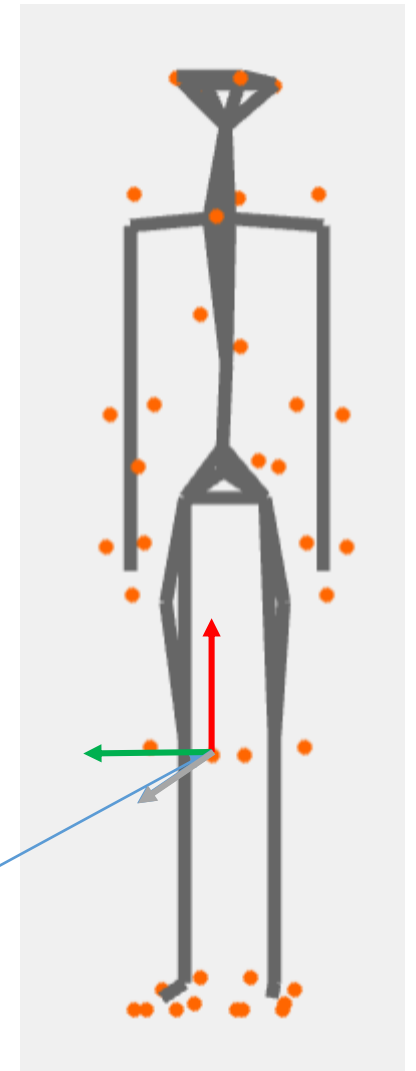
- RKNE is trusted for x,y,z direction

RKNE ☐ ☐ ☐

- RKNI is trusted for x direction and optimized for y and z direction

RKNI ☐ ☒ ☒

RKNI



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

## Axis of rotation

$$\overrightarrow{a_z'} = Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * \overrightarrow{a_z'}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

|          |                  |                          |                                     |                                     |
|----------|------------------|--------------------------|-------------------------------------|-------------------------------------|
|          | Axis of rotation | X                        | Y                                   | Z                                   |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

## Axis of rotation

$$\overrightarrow{a_z'} = Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * \overrightarrow{a_z'}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

|          |                  |                          |                                     |                                     |
|----------|------------------|--------------------------|-------------------------------------|-------------------------------------|
|          | Axis of rotation | X                        | Y                                   | Z                                   |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |





# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

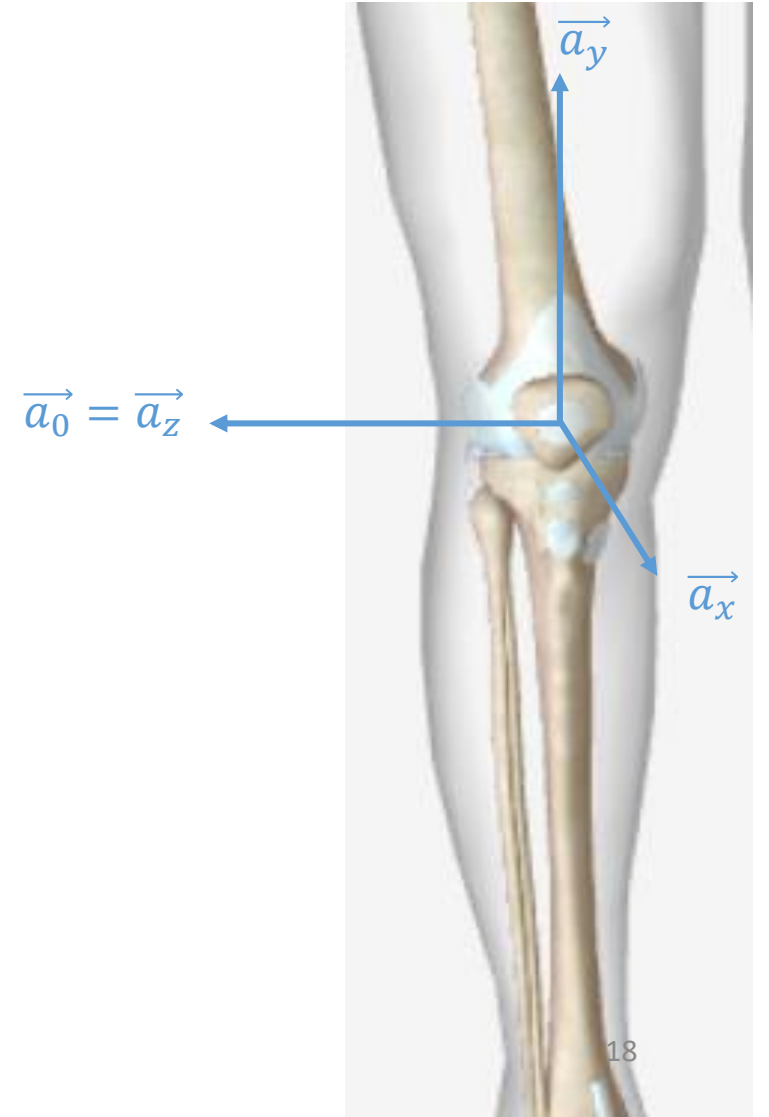
## Axis of rotation

$$\overrightarrow{a_z'} = Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * \overrightarrow{a_z'}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

|          |                  |                          |                                     |                                     |
|----------|------------------|--------------------------|-------------------------------------|-------------------------------------|
|          | Axis of rotation | X                        | Y                                   | Z                                   |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

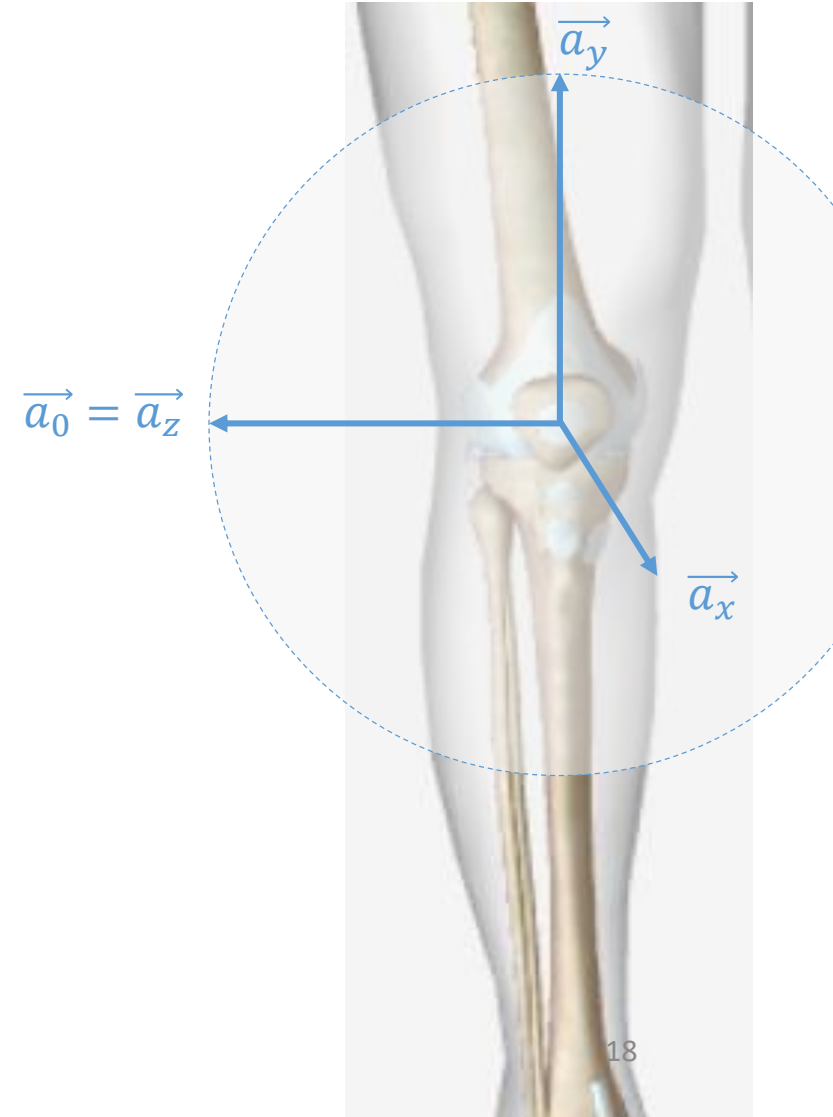
## Axis of rotation

$$\vec{a}_z' = Rot(\alpha_1, \vec{a}_x) * \vec{a}_0$$

$$\vec{a}_z'' = Rot(\alpha_2, \vec{a}_y') * \vec{a}_z'$$

$$\vec{a}_z'' = Rot(\alpha_2, \vec{a}_y') * Rot(\alpha_1, \vec{a}_x) * \vec{a}_0$$

|          |                  |                          |                                     |                                     |
|----------|------------------|--------------------------|-------------------------------------|-------------------------------------|
|          | Axis of rotation | X                        | Y                                   | Z                                   |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

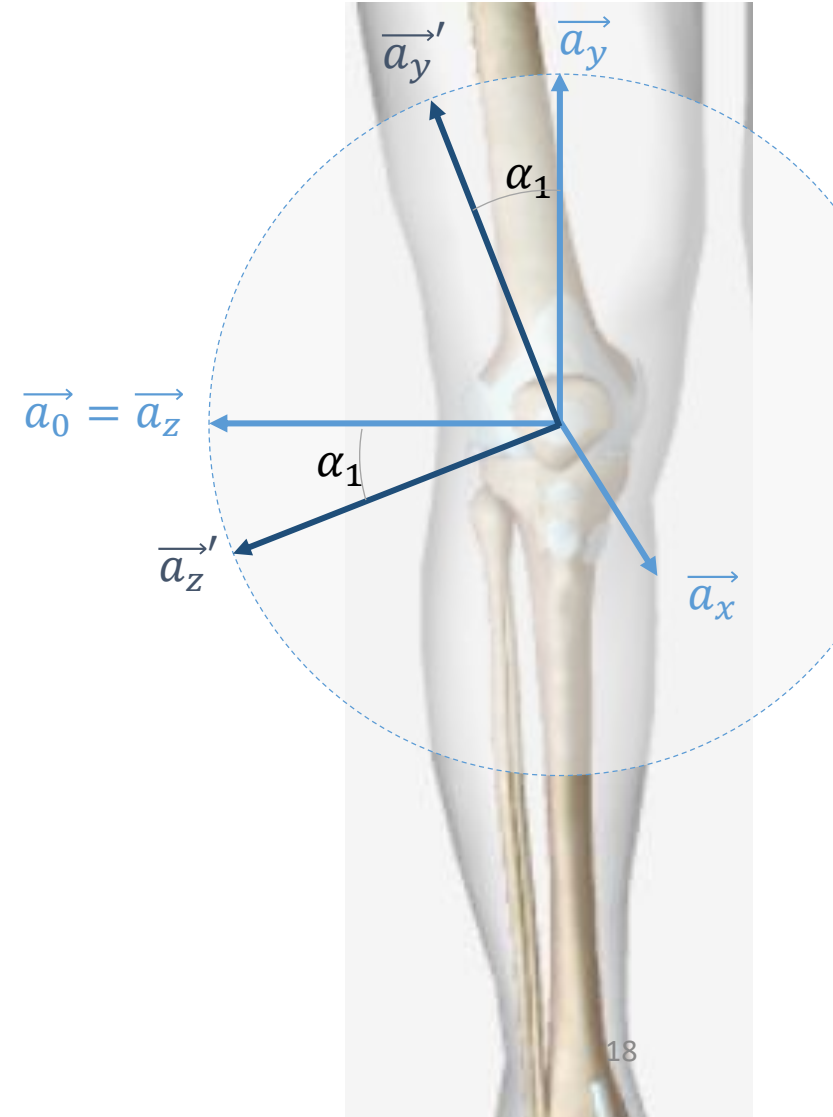
## Axis of rotation

$$\vec{a}_z' = \text{Rot}(\alpha_1, \vec{a}_x) * \vec{a}_0$$

$$\vec{a}_z'' = \text{Rot}(\alpha_2, \vec{a}_y') * \vec{a}_z'$$

$$\vec{a}_z'' = \text{Rot}(\alpha_2, \vec{a}_y') * \text{Rot}(\alpha_1, \vec{a}_x) * \vec{a}_0$$

|          |                  |  |
|----------|------------------|--|
|          | Axis of rotation | X Y Z  |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> <input checked="" type="checkbox"/> <input checked="" type="checkbox"/> |



# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

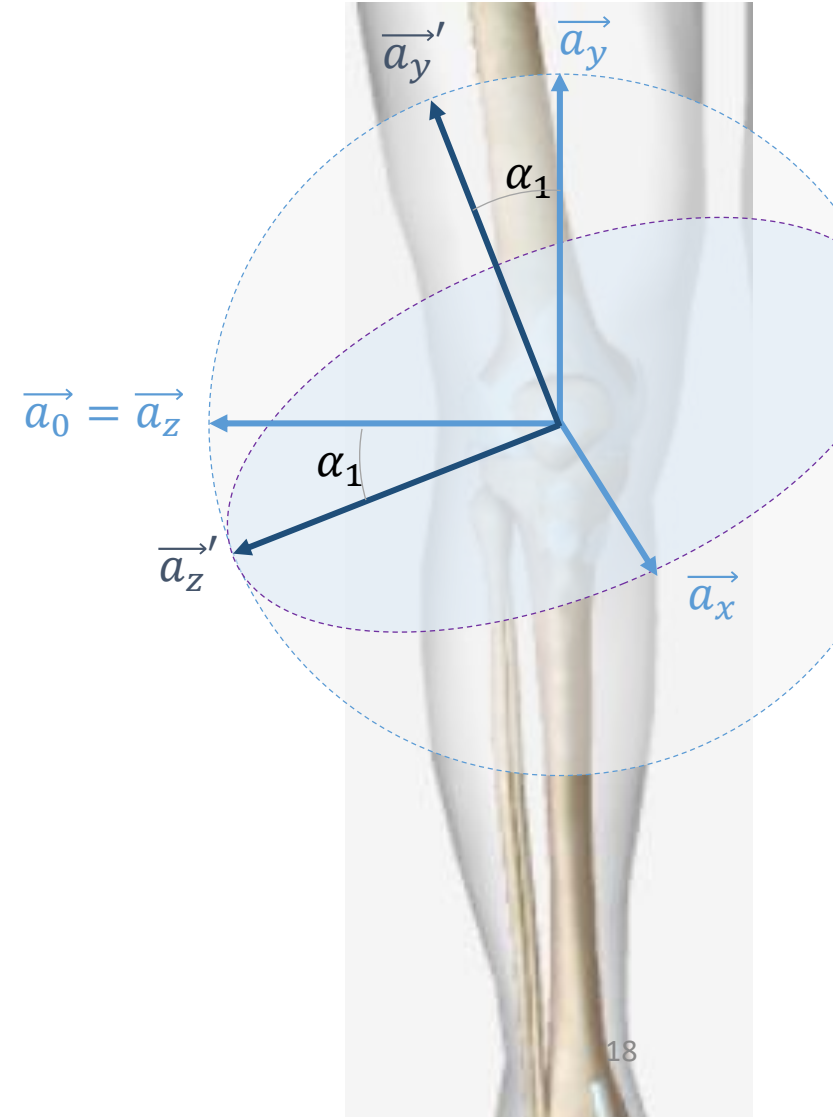
## Axis of rotation

$$\vec{a}_z' = \text{Rot}(\alpha_1, \vec{a}_x) * \vec{a}_0$$

$$\vec{a}_z'' = \text{Rot}(\alpha_2, \vec{a}_y') * \vec{a}_z'$$

$$\vec{a}_z'' = \text{Rot}(\alpha_2, \vec{a}_y') * \text{Rot}(\alpha_1, \vec{a}_x) * \vec{a}_0$$

|          |                  |  |
|----------|------------------|--|
|          | Axis of rotation | X Y Z  |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> <input checked="" type="checkbox"/> <input checked="" type="checkbox"/> |



# What is CusToM Doing ?

Geometrical Calibration ...

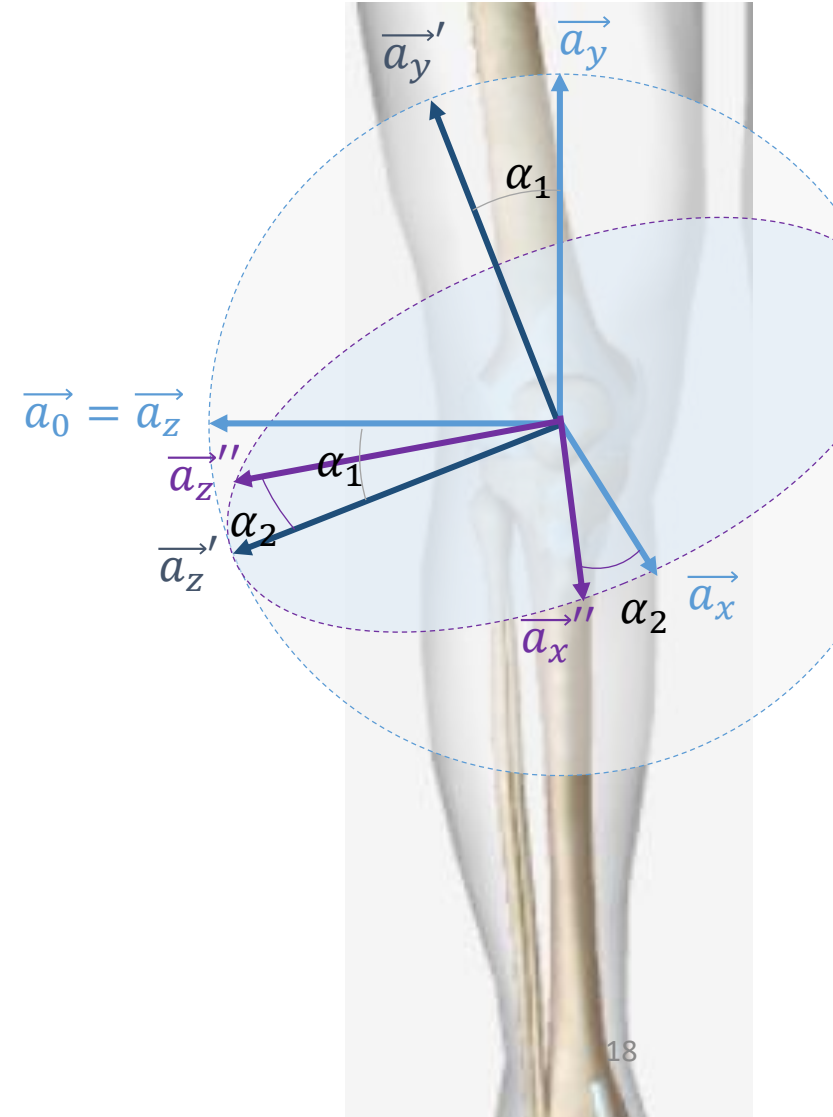
... Geometrical Calibration done

## Axis of rotation

$$\vec{a}_z' = \text{Rot}(\alpha_1, \vec{a}_x) * \vec{a}_0$$

$$\vec{a}_z'' = \text{Rot}(\alpha_2, \vec{a}_y') * \vec{a}_z'$$

$$\vec{a}_z'' = \text{Rot}(\alpha_2, \vec{a}_y') * \text{Rot}(\alpha_1, \vec{a}_x) * \vec{a}_0$$



|          |                  |  |
|----------|------------------|--|
|          | Axis of rotation | X Y Z  |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> <input checked="" type="checkbox"/> <input checked="" type="checkbox"/> |

# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

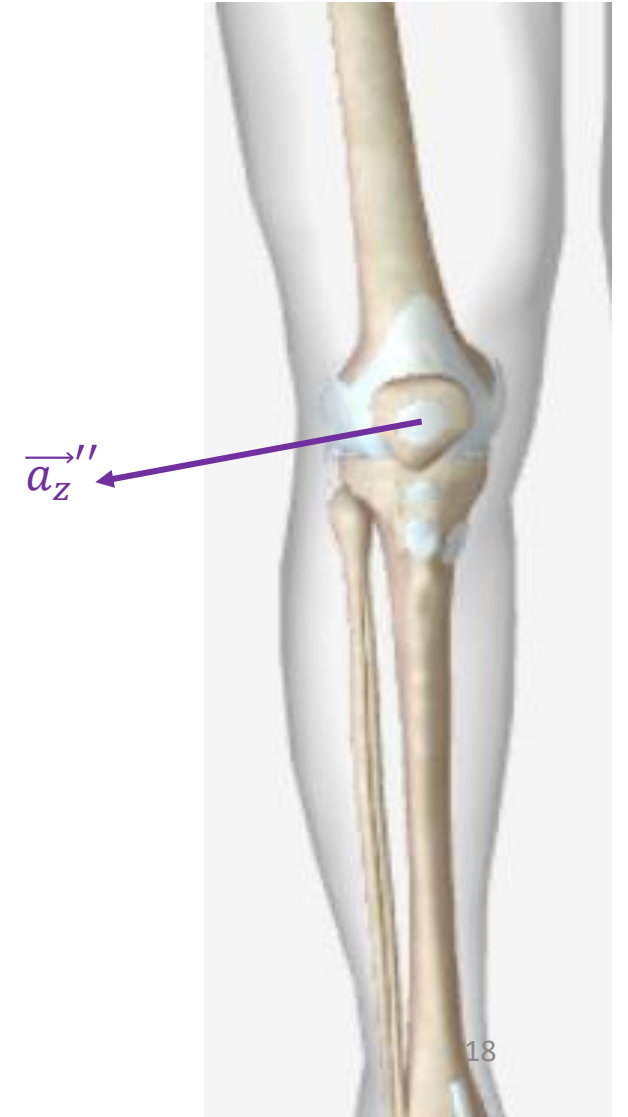
## Axis of rotation

$$\overrightarrow{a_z'} = Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * \overrightarrow{a_z'}$$

$$\overrightarrow{a_z''} = Rot(\alpha_2, \overrightarrow{a_y'}) * Rot(\alpha_1, \overrightarrow{a_x}) * \overrightarrow{a_0}$$

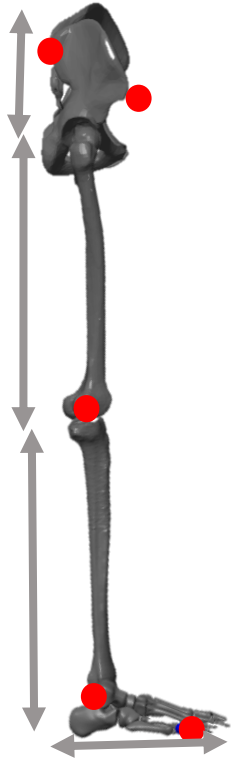
|          |                  |                          |                                     |                                     |
|----------|------------------|--------------------------|-------------------------------------|-------------------------------------|
|          | Axis of rotation | X                        | Y                                   | Z                                   |
| RShank ▼ | 0 0 1            | <input type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |



# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done

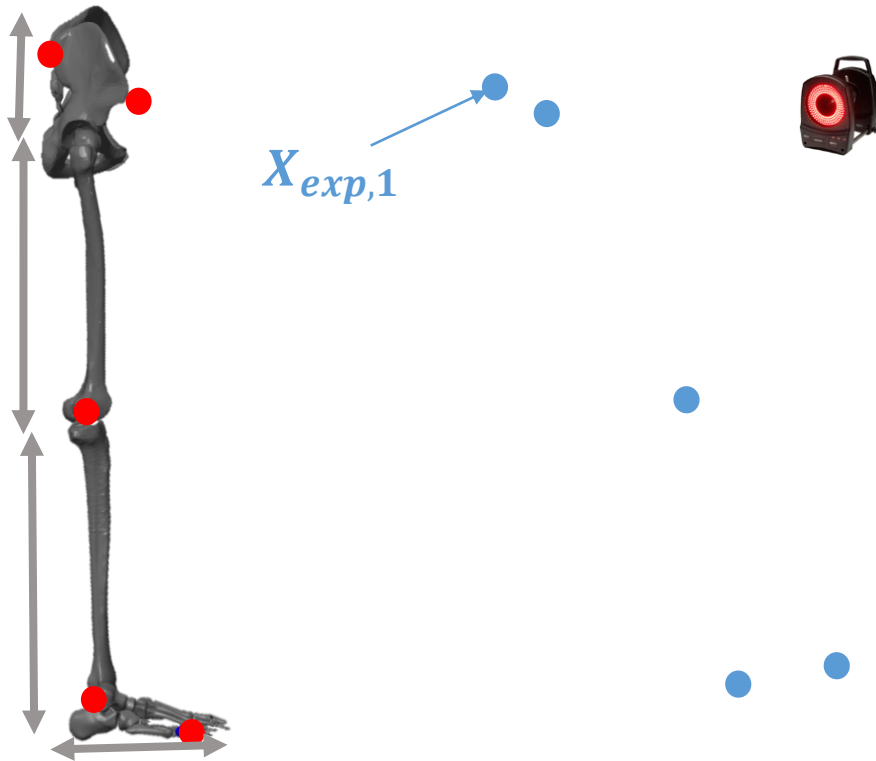


Regression method  
Based on height  
RM

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done

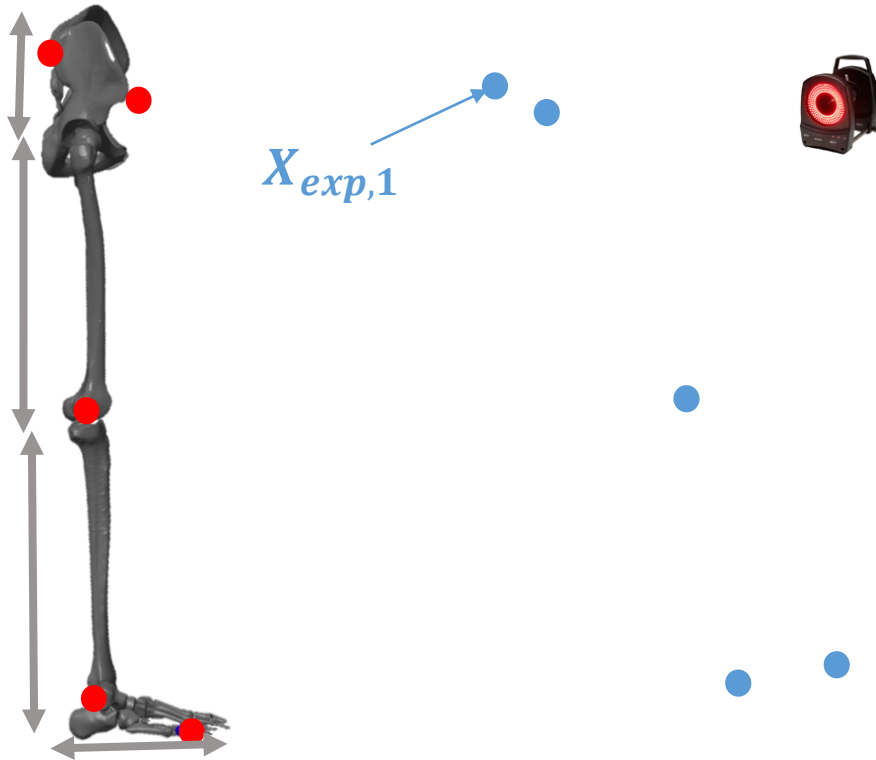




# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

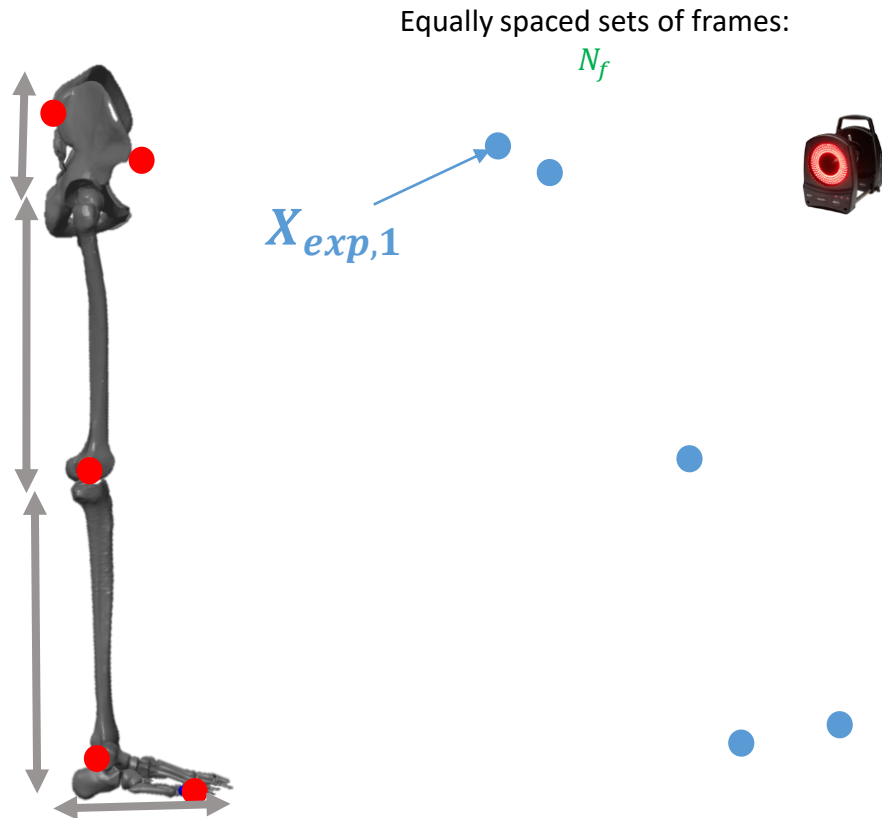
... Geometrical Calibration done



# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

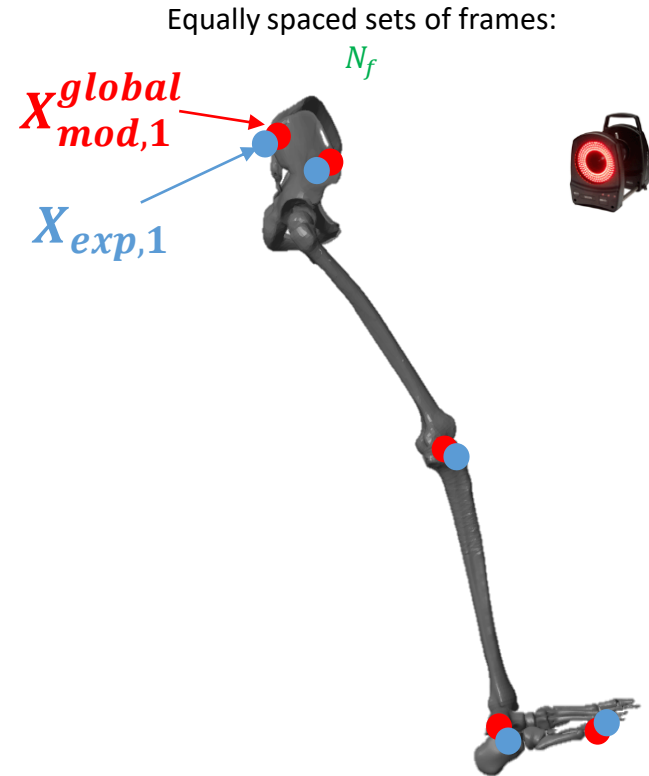
... Geometrical Calibration done



# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

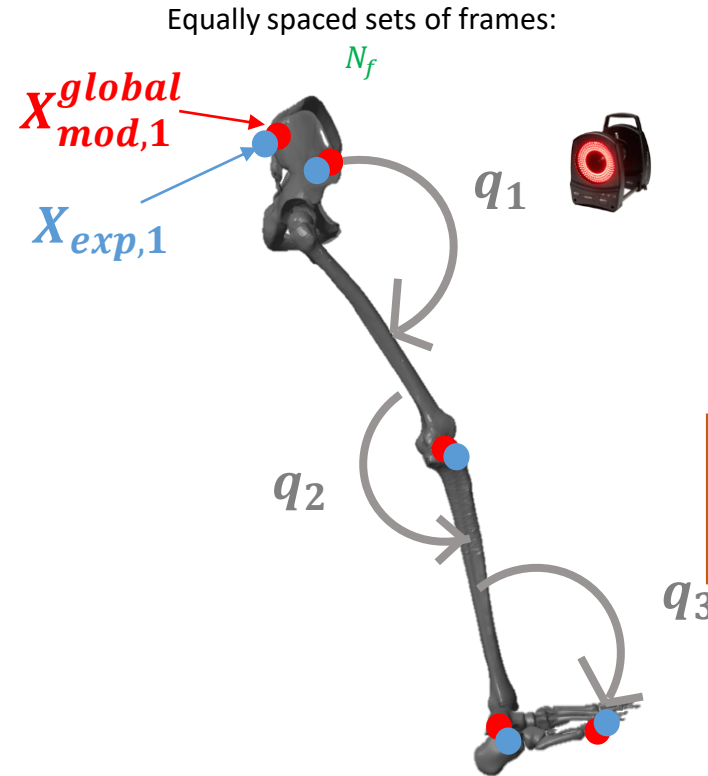
... Geometrical Calibration done



# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



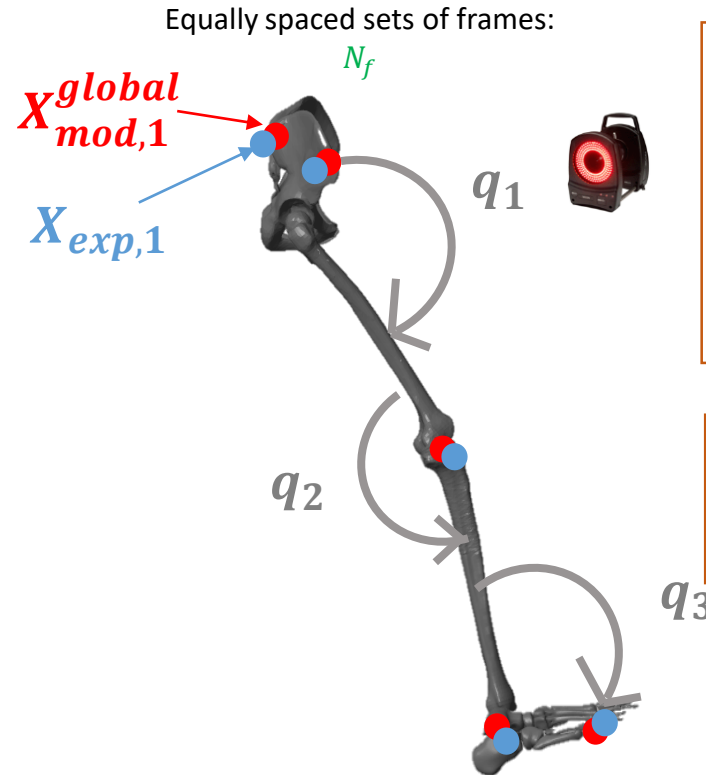
Inverse kinematics

*Lu and O'Connor et al. 1999*

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration i

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

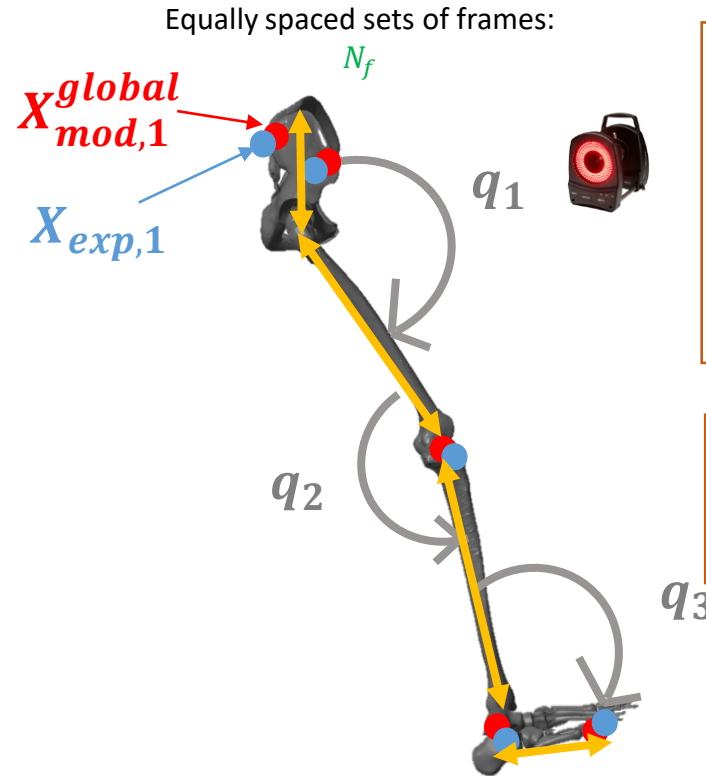
## Inverse kinematics

Lu and O'Connor et al. 1999

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration  $i$

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

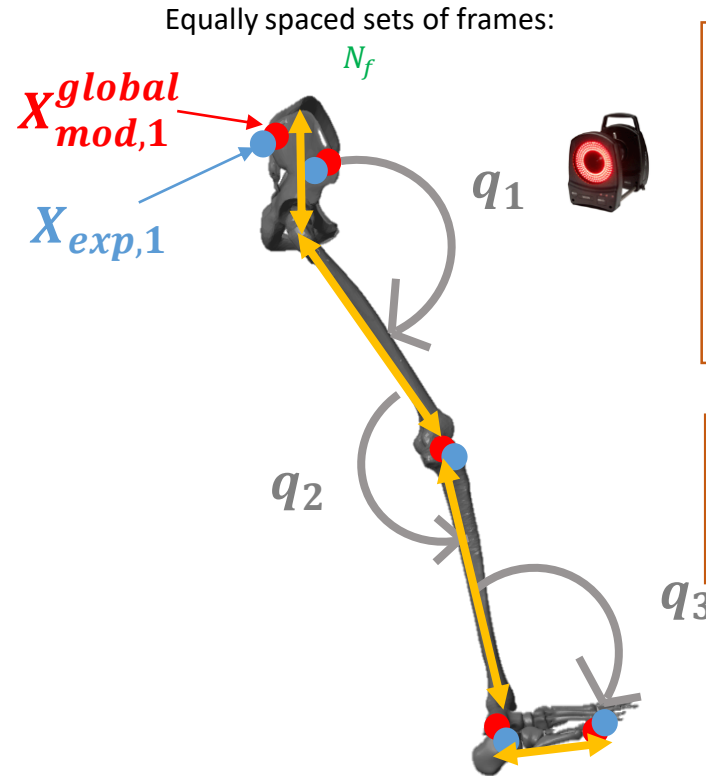
## Inverse kinematics

Lu and O'Connor et al. 1999

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration  $i$

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

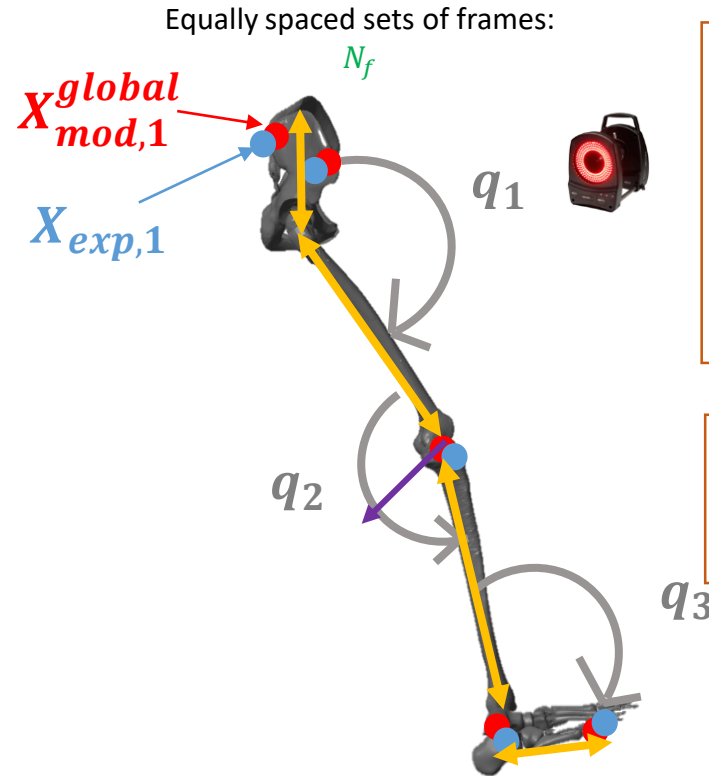
## Inverse kinematics

Lu and O'Connor et al. 1999

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration  $i$

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

## Inverse kinematics

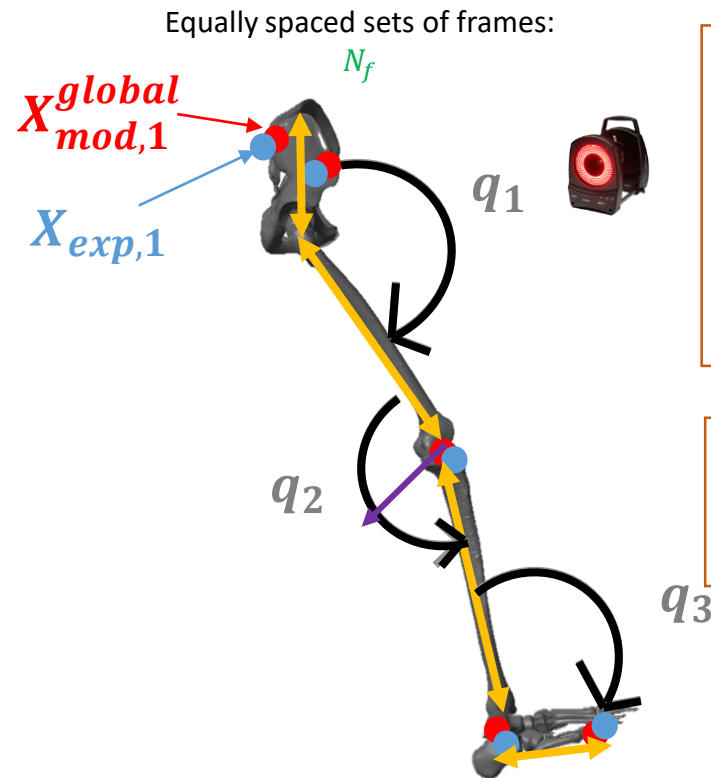
Lu and O'Connor et al. 1999



# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration i

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

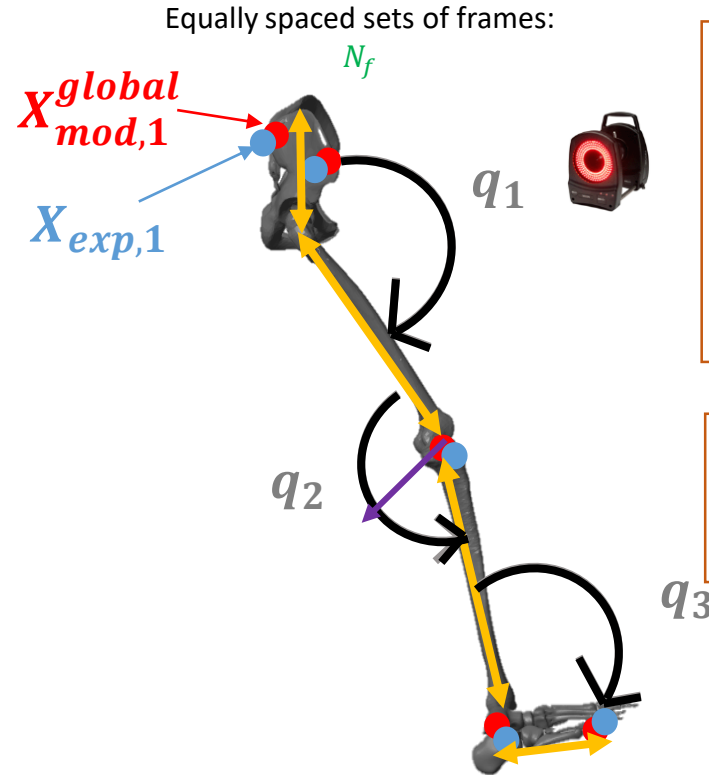
## Inverse kinematics

Lu and O'Connor et al. 1999

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration i

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

## Inverse kinematics

Lu and O'Connor et al. 1999

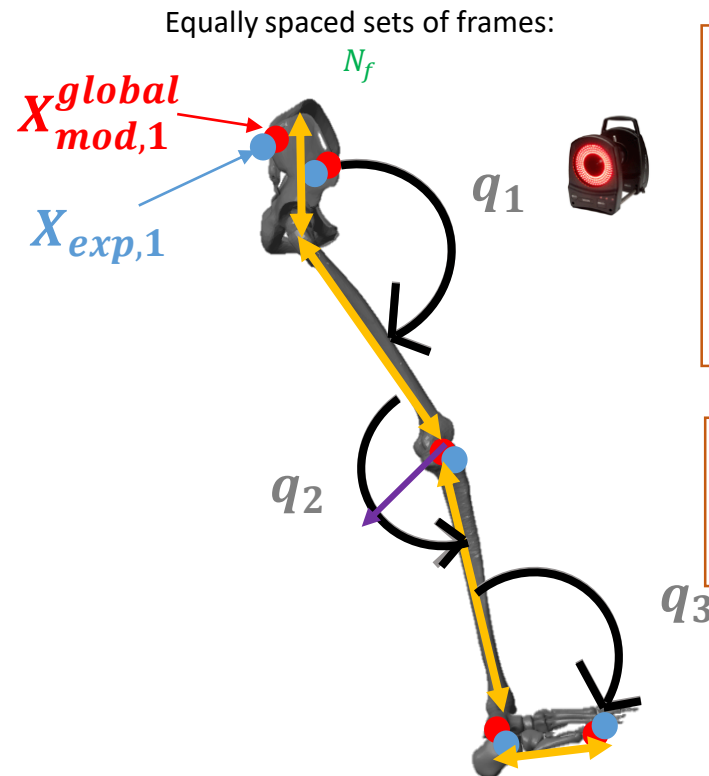
Criterion satisfied ?

$$\frac{\phi_i - \phi_{i-1}}{\phi_{i-1}} < 5\%$$

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration  $i$

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

## Inverse kinematics

Lu and O'Connor et al. 1999

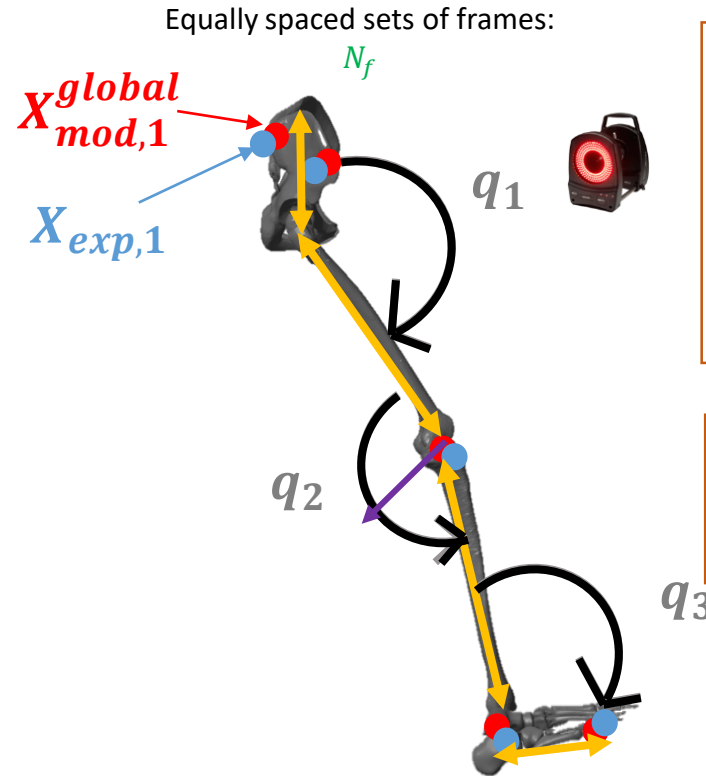
Criterion satisfied ?

$$\frac{\phi_i - \phi_{i-1}}{\phi_{i-1}} < 5\% \quad \text{No}$$

# What is CusToM Doing ? – Geometrical Calibration Process

Geometrical Calibration ...

... Geometrical Calibration done



Muller et al. 2015

## Parameters identification

At each iteration  $i$

$$\min_{k, \Delta p, \alpha} \phi_i = \sum_f^{N_f} \sum_m^{N_m} \|X_{exp,m}(t_f) - X_{mod,m}^{global}(t_f, k, \Delta p, \alpha)\|^2$$

## Inverse kinematics

Lu and O'Connor et al. 1999

Criterion satisfied ?

$$\frac{\phi_i - \phi_{i-1}}{\phi_{i-1}} < 5\%$$

No

Yes

Stop

# What is CusToM Doing ?

Geometrical Calibration ...

... Geometrical Calibration done

$$\Phi = \sum_f^{N_f} \sum_m^{N_m} \|\mathbf{X}_{exp,m}(t_f) - \mathbf{X}_{mod,m}^{R_{global}}(\mathbf{q}(t_f), \mathbf{k}, \alpha, \Delta \mathbf{p})\|^2$$

$$\min_{\mathbf{k}, \alpha, \Delta \mathbf{p}} \quad \Phi(\mathbf{q}(t_f), \mathbf{k}, \alpha, \Delta \mathbf{p})$$

$$\text{s.t.} \quad \forall s \in \llbracket 1; N_s \rrbracket, \quad \left| \frac{k_s}{k_s^0} - 1 \right| < 20 \%$$

$$\forall a \in \llbracket 1; N_\alpha \rrbracket, \quad \alpha_{a,min} < \alpha_a < \alpha_{a,max}$$

$$\forall m \in \llbracket 1; N_m \rrbracket, \quad |\Delta p_m| < 0.05 \text{ m}$$

$$\epsilon = \frac{\Phi_i - \Phi_{i-1}}{\Phi_{i-1}}$$

# Geometrical Calibration Results

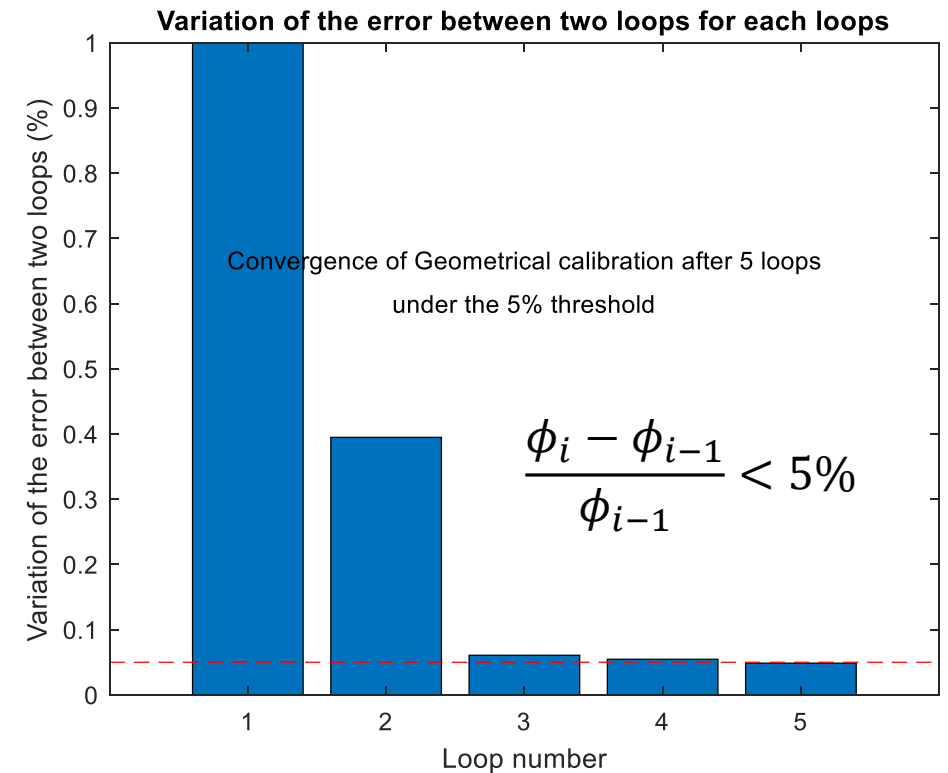
```
>> PostProcessingCalibration
```

All contained in a struct :

| BiomechanicalModel.GeometricalCalibration |                                 |
|---|---------------------------------|
| Field ▲                                   | Value                           |
| frame_calib                               | 1x20 double                     |
| crit                                      | [1 0.4682 0.0703 0.0989 0.0414] |
| errorm                                    | 1x5 cell                        |
| k_calib                                   | 48x1 double                     |
| p_calib                                   | 126x1 double                    |
| alpha_calib                               | []                              |

```
BiomechanicalModel.GeometricalCalibration
```

```
« .Crit »
```




# Geometrical Calibration Results

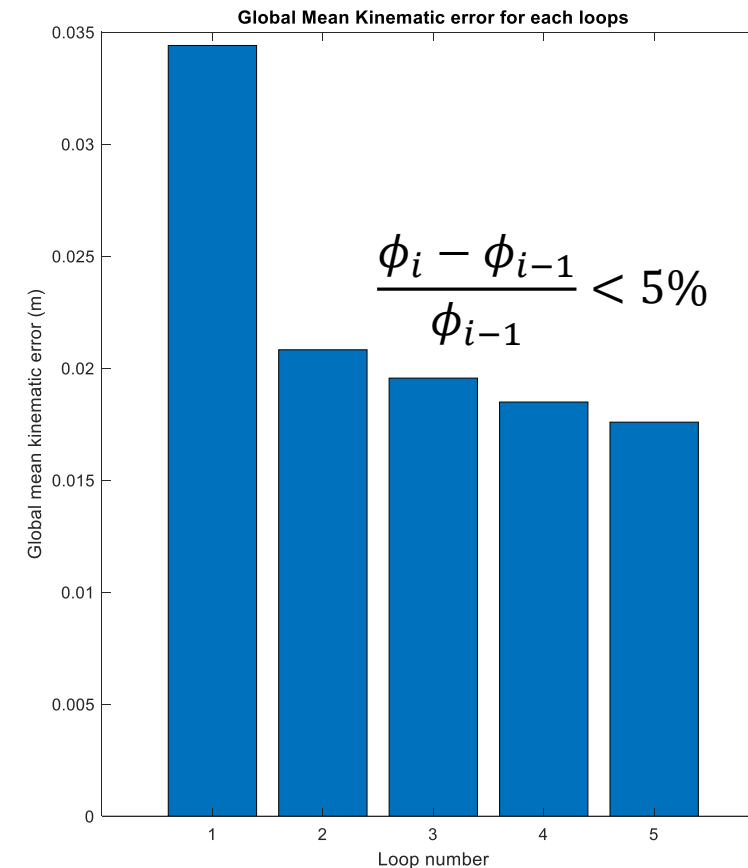
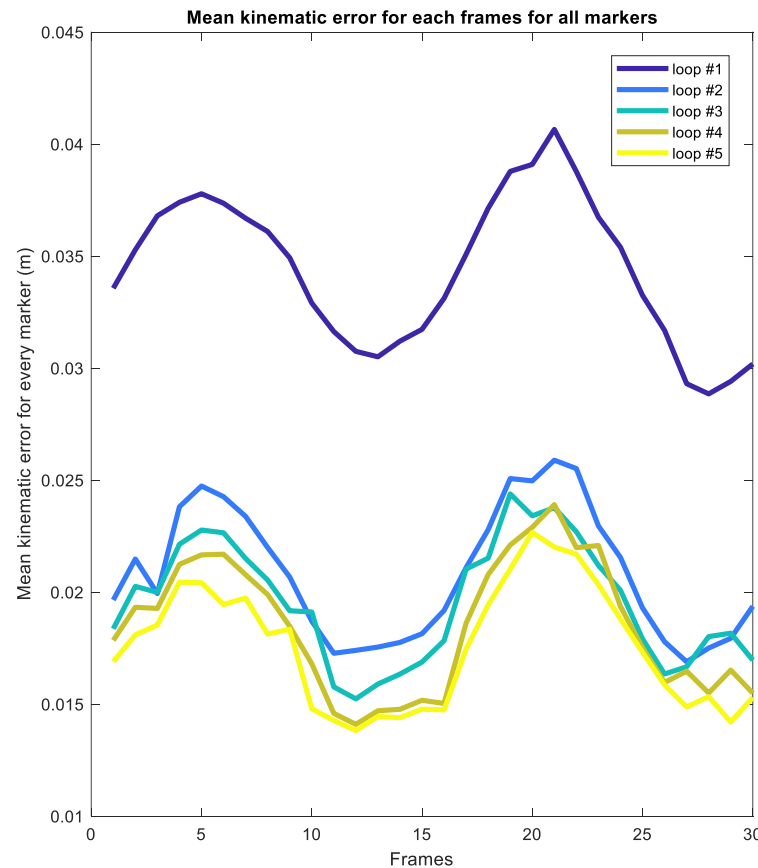
```
>> PostProcessingCalibration
```

```
BiomechanicalModel.GeometricalCalibration
```

```
« .error »
```

 error

1x5 cell



# Geometrical Calibration Results

```
>> PostProcessingCalibration|
```

```
BiomechanicalModel.GeometricalCalibration  
« .calib_k »
```

Variation of the homothetic coefficient from the anthropometric estimation.

Reminder:

$$k_0 = \frac{\textit{size of the subject}}{\textit{size of the cadaver}}$$

From the initial musculoskeletal model:

$$k_{final} = k_0 * k_{calib}$$

k\_calib

48x1 double

BiomechanicalModel.GeometricalCalibration.k\_calib

|    | 1      | 2 | 3 | 4 |
|----|--------|---|---|---|
| 1  | 0.9646 |   |   |   |
| 2  | 1      |   |   |   |
| 3  | 1      |   |   |   |
| 4  | 1      |   |   |   |
| 5  | 1      |   |   |   |
| 6  | 1      |   |   |   |
| 7  | 0.9487 |   |   |   |
| 8  | 1      |   |   |   |
| 9  | 1      |   |   |   |
| 10 | 0.9487 |   |   |   |
| 11 | 1      |   |   |   |
| 12 | 1      |   |   |   |
| 13 | 0.9487 |   |   |   |
| 14 | 1      |   |   |   |
| 15 | 1      |   |   |   |
| 16 | 0.9336 |   |   |   |

BiomechanicalModel.OsteoArticularModel

| Fields | name            | sister | child |
|--------|-----------------|--------|-------|
| 1      | 'PelvisSacr...  | 0      | 2     |
| 2      | 'LowerTrun...   | 17     | 3     |
| 3      | 'LowerTrun...   | 0      | 4     |
| 4      | 'LowerTrunk'    | 0      | 5     |
| 5      | 'UpperTrun...   | 0      | 6     |
| 6      | 'UpperTrun...   | 0      | 7     |
| 7      | 'Thorax'        | 0      | 8     |
| 8      | 'RClavicle_J... | 11     | 9     |
| 9      | 'RClavicle_J... | 0      | 10    |
| 10     | 'RClavicle'     | 0      | 29    |
| 11     | 'LClavicle_J1'  | 14     | 12    |
| 12     | 'LClavicle_J2'  | 0      | 13    |
| 13     | 'LClavicle'     | 0      | 36    |
| 14     | 'ThoraxSkul...  | 0      | 15    |
| 15     | 'ThoraxSkul...  | 0      | 16    |



# Geometrical Calibration Results

```
>> PostProcessingCalibration|
```

BiomechanicalModel.GeometricalCalibration  
« .calib\_p »

Displacement of the marker in local frames.

p\_calib

126x1 double

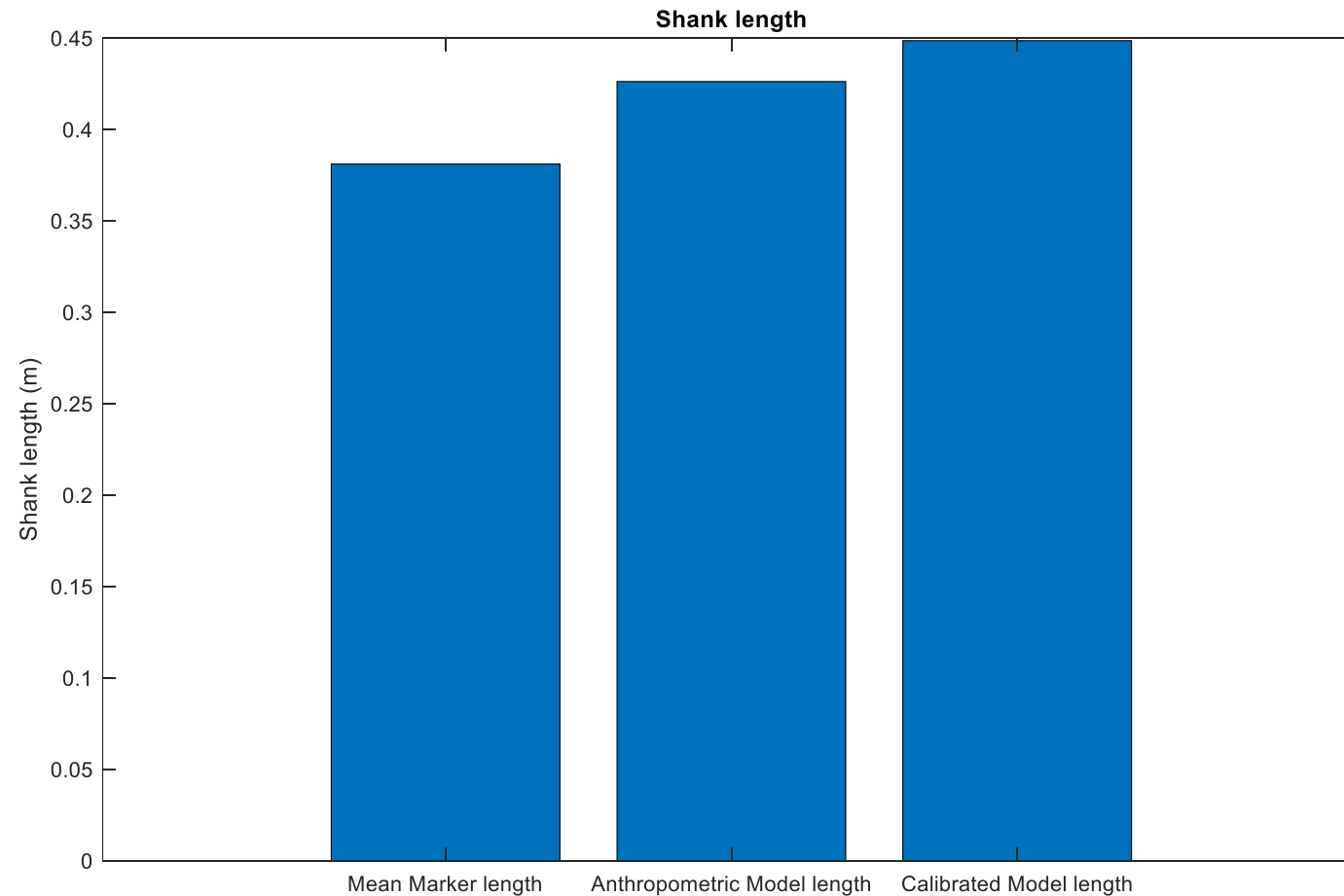
| BiomechanicalModel.GeometricalCalibration.p_calib |            |   |   |   |
|---|------------|---|---|---|
|   | 1          | 2   | 3 | 4 |
| 1   | 0          | $\left. \begin{matrix} \vec{x} \\ \vec{y} \\ \vec{z} \end{matrix} \right\}$ |   |   |
| 2   | -0.0037    |   |   |   |
| 3   | 0          |   |   |   |
| 4   | 0.0210     |   |   |   |
| 5   | 0          |   |   |   |
| 6   | 0          |   |   |   |
| 7   | 0          |   |   |   |
| 8   | -0.0271    |   |   |   |
| 9   | 0          |   |   |   |
| 10  | -0.0181    |   |   |   |
| 11  | -0.0111    |   |   |   |
| 12  | 0          |   |   |   |
| 13  | 2.8682e-04 |   |   |   |
| 14  | 0          |   |   |   |
| 15  | 0.0218     |   |   |   |
| 16  | 0.0067     |   |   |   |

BiomechanicalModel.Markers

| Field's | name   | anat_position | calib_   |
|---------|--------|---------------|----------|
| 1       | 'STRN' | 'STRN'        | 3x1 cell |
| 2       | 'CLAV' | 'CLAV'        | 3x1 cell |
| 3       | 'T10'  | 'T10'         | 3x1 cell |
| 4       | 'C7'   | 'C7'          | 3x1 cell |
| 5       | 'RSHO' | 'RSHO'        | 3x1 cell |
| 6       | 'LSHO' | 'LSHO'        | 3x1 cell |
| 7       | 'RFTW' | 'RFTW'        | 3x1 cell |
| 8       | 'LFTW' | 'LFTW'        | 3x1 cell |
| 9       | 'RBWT' | 'RBWT'        | 3x1 cell |
| 10      | 'LBWT' | 'LBWT'        | 3x1 cell |
| 11      | 'RFHD' | 'RFHD'        | 3x1 cell |
| 12      | 'LFHD' | 'LFHD'        | 3x1 cell |
| 13      | 'RBHD' | 'RBHD'        | 3x1 cell |
| 14      | 'LBHD' | 'LBHD'        | 3x1 cell |
| 15      | 'RKNE' | 'RKNE'        | 3x1 cell |
| 16      | 'RANE' | 'RANE'        | 3x1 cell |

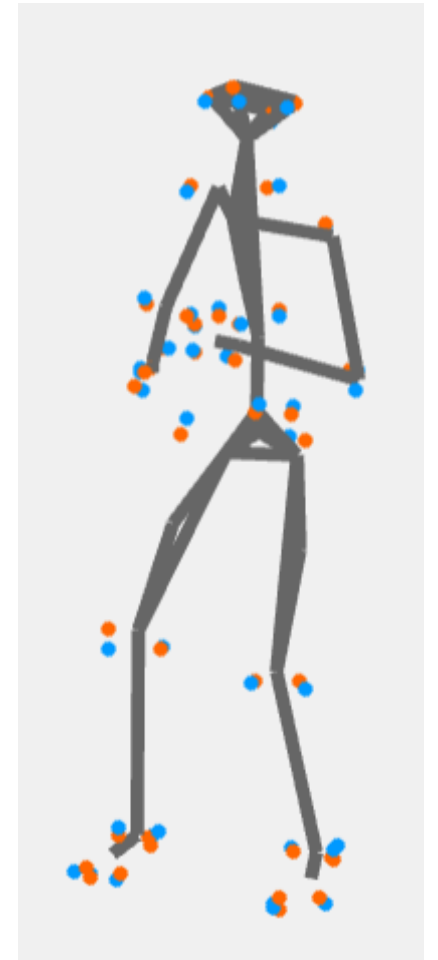
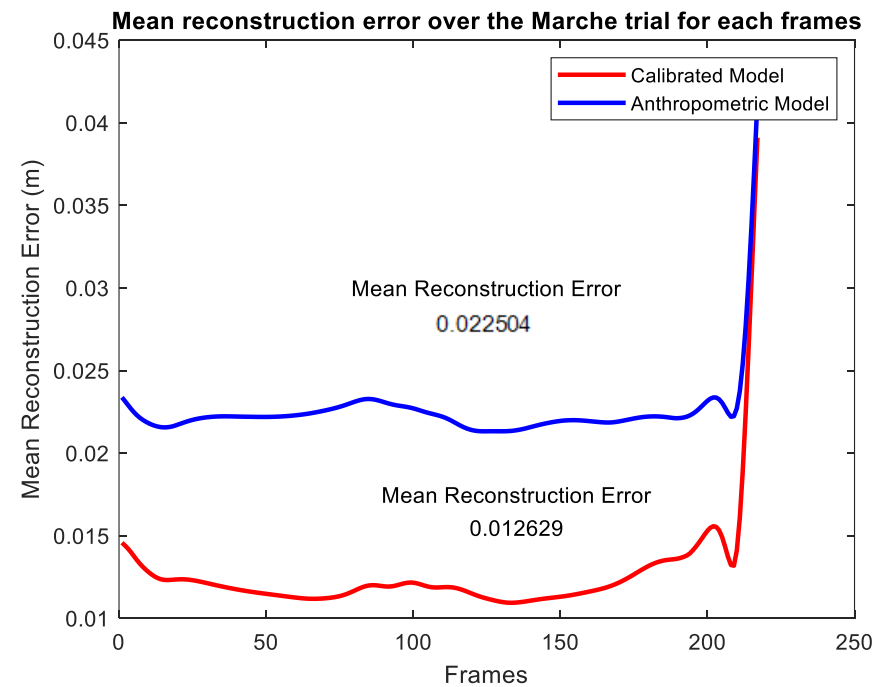
# What about the quality of the model ?

## Geometrical Calibration Results - Right Shank length

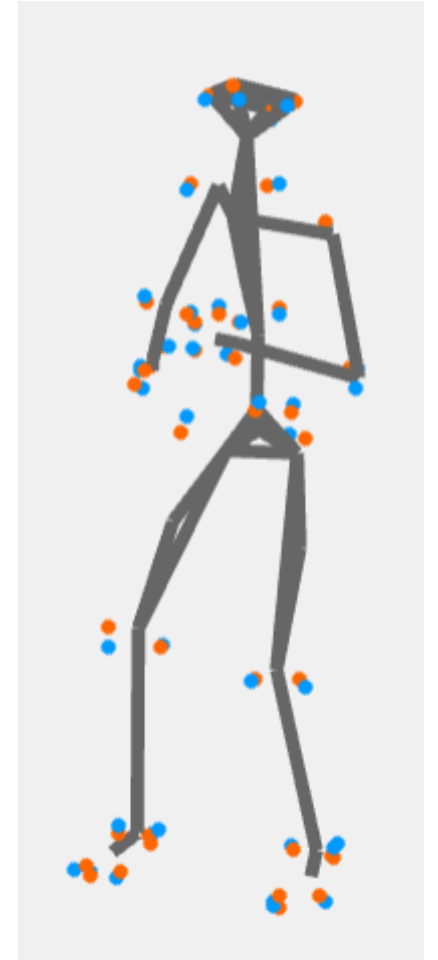
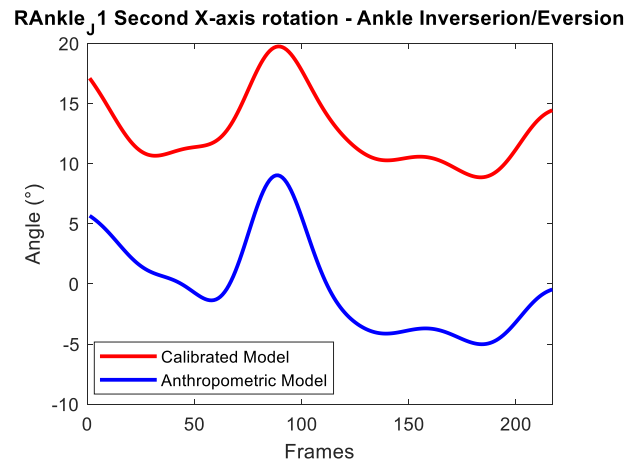
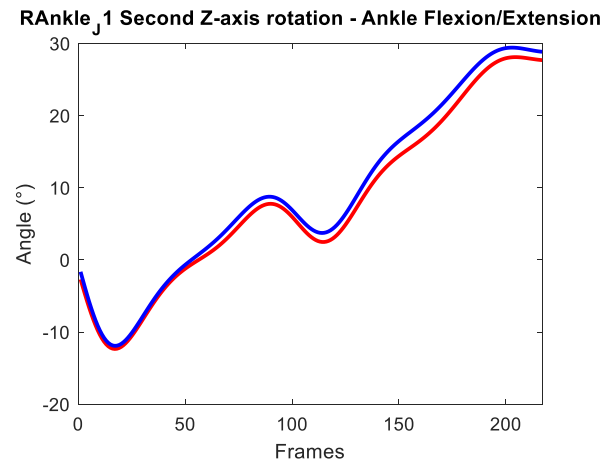
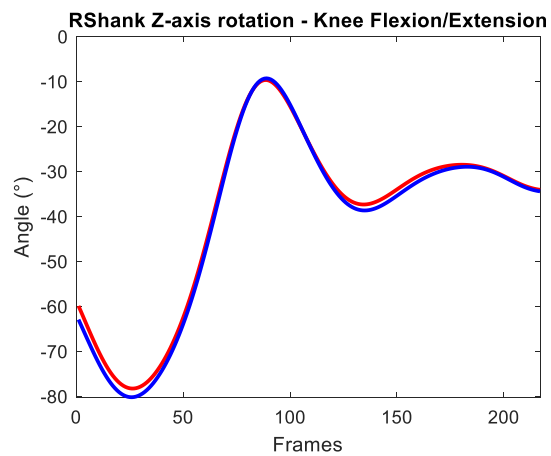
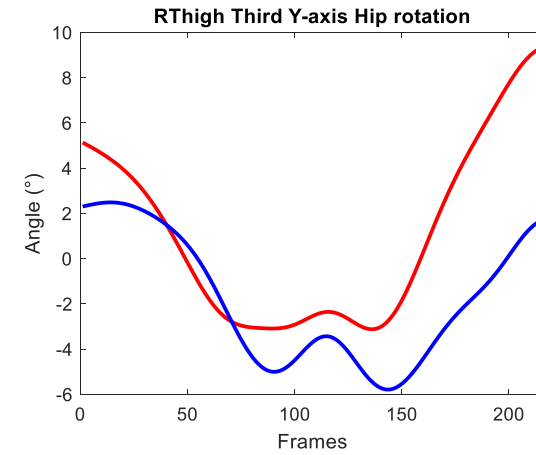
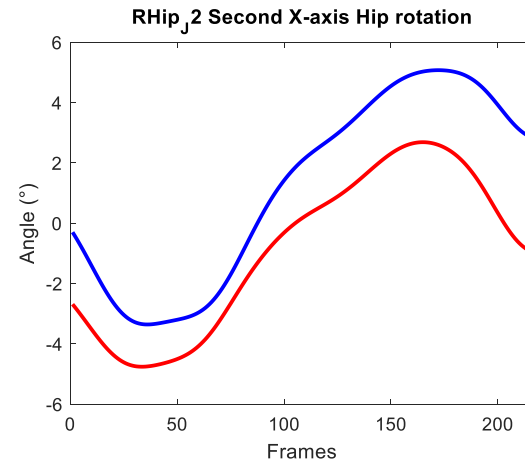
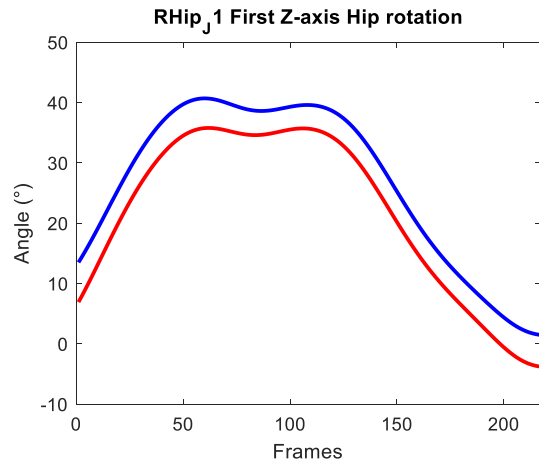


# Kinematical Results

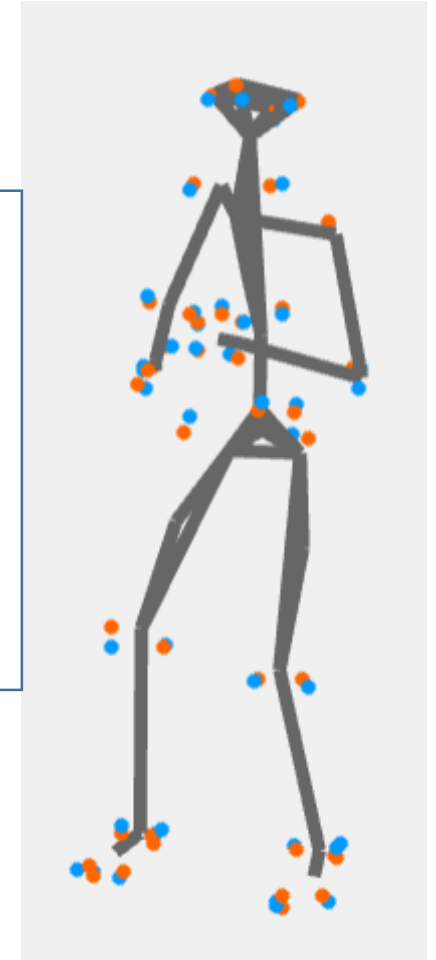
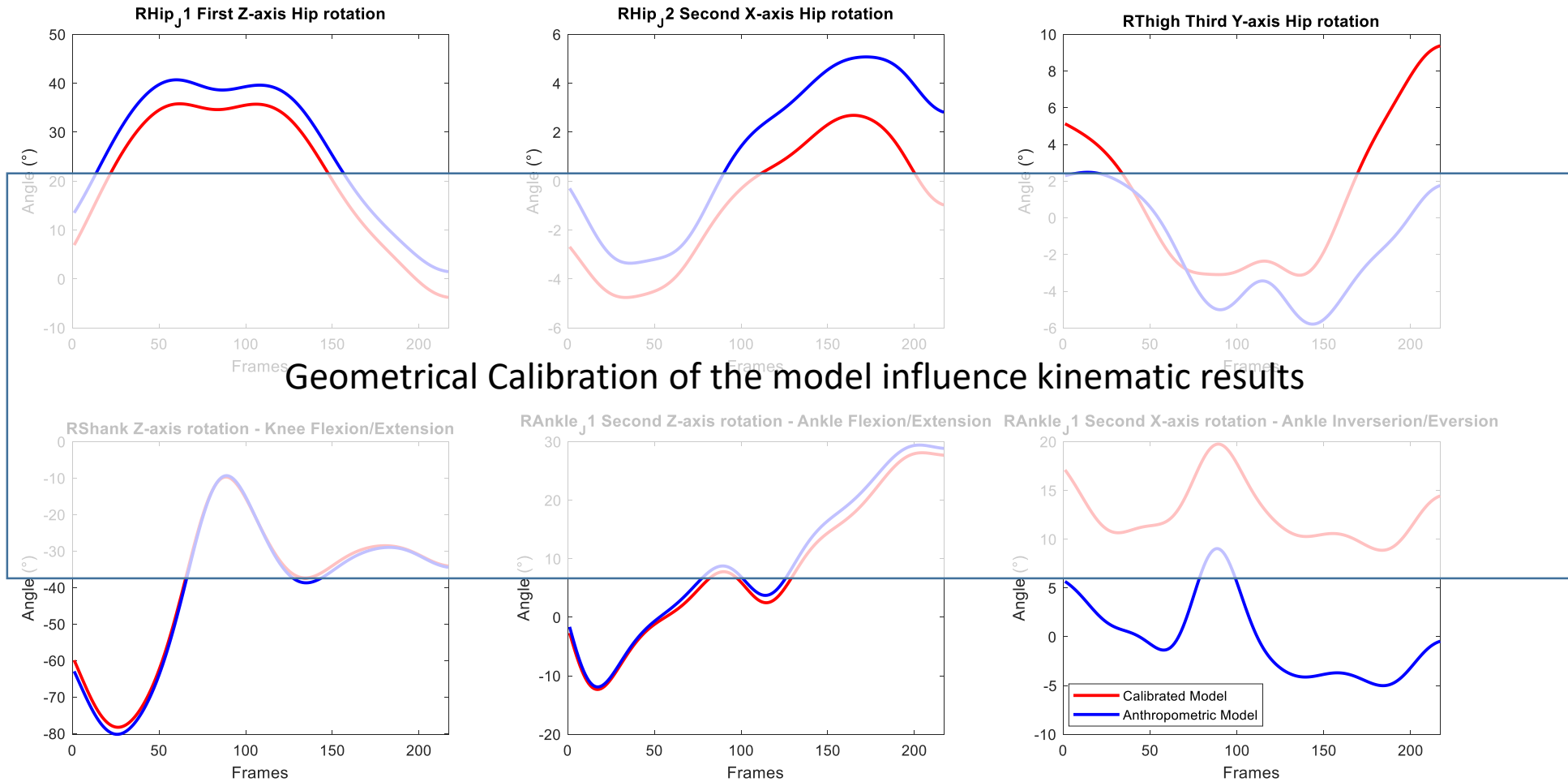
Decreasing of the mean reconstruction error over the walking trial.



# Kinematical Results



# Kinematical Results



# Take home message

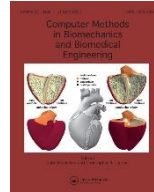
## To ensure the quality of the model and kinematic results

- Check your reconstruction errors
  - on your calibration trial
  - on your inverse kinematic trials
  - 4 to 40 mm reconstruction error mean have been reported. [Begon et al. 2017]

*Begon, M., Andersen, M.S., Dumas, R., 2017. Multibody kinematic optimization for the estimation of upper and lower limb human joint kinematics: a systematic review. J. Biomech. Eng. 140, 1–11.*

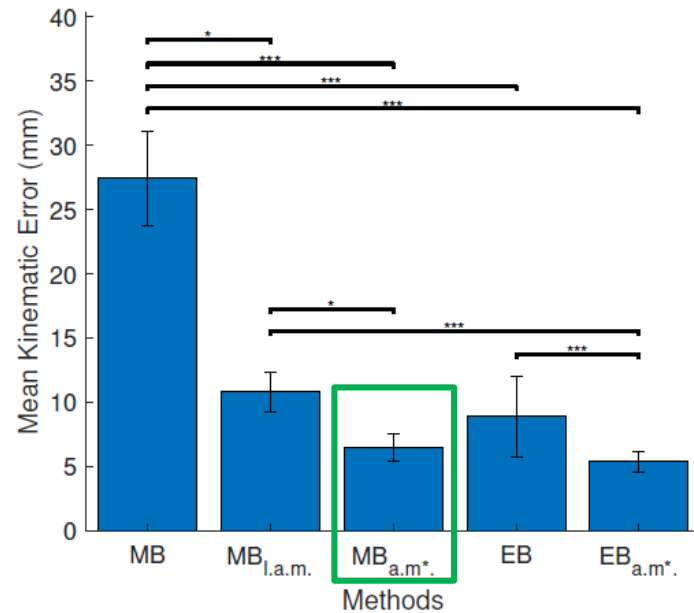
- Be sure you chose the right constraints to ensure the geometrical calibration
  - Enough frames (20-100)
  - Homothetic constraints (equality)
  - Displacement of markers
  - Rotation of joint axis

# Perspectives for scaling in CusToM



Accuracy and kinematics consistency of marker-based scaling approaches on a lower limb model: a comparative study with imagery data

P.Puchaud<sup>a,b,c</sup>, C. Sauret<sup>d</sup>, A. Muller<sup>a,e</sup>, N. Bideau<sup>b</sup>, G. Dumont<sup>a</sup>, H. Pillet<sup>d</sup>, C. Pontonnier<sup>a,c</sup>



**Figure 5.** Kinematic errors (mean and standard deviation) on hip- and knee-joint functional movements with blue five models: HB, MB, MB<sub>l.a.m.</sub>, MB<sub>a.m\*</sub>, EB and EB<sub>a.m\*</sub>. \*, \*\*, \*\*\* indicated respective p-values < 0.05, < 0.005, < 0.001 with respect to Tukey's honest significant difference criterion.



Biplanar Radiographies



## STEPS

1. Scaled bones based on markers locations
2. Optimize marker locations and joint axis orientations




## BENEFITS

1. Consistent segment lengths (inter-hip distance, femur, shank) compared with radiographies
2. Low kinematic residuals consistent with EOS models
3. Joint angles consistent with EOS models

# Pre-Work

Go in `Examples\1_Walking_Kinematic\POC0980A_altered`

It contains :

|   |                  |             |
|---|------------------|-------------|
|  Marche.c3d                        | 16/12/2019 11:29 | Fichier C3D |
|  NormalizeAbscisseCurve100.m       | 30/01/2019 16:48 | MATLAB Code |
|  PostProcessingKinematic_Walking.m | 16/12/2019 17:39 | MATLAB Code |
|  ROM01.c3d                         | 28/01/2019 14:14 | Fichier C3D |



# Context – New Example

Ankle Sprain over the world

1 /10,000 people /day *Katcherian D. 1994*

# Context – New Example

Ankle Sprain over the world

1 /10,000 people /day *Katcherian D. 1994*

Treating the ankle sprain grade III:

- Immobilization

*Mohammadi et al. 2013*



# Context – New Example

Ankle Sprain over the world

1 /10,000 people /day *Katcherian D. 1994*

Treating the ankle sprain grade III:

- Immobilization
- Functional treatment *Mohammadi et al. 2013*



# Context – New Example

Ankle Sprain over the world

1 /10,000 people /day *Katcharian D. 1994*

Treating the ankle sprain grade III:

- Immobilization
- Functional treatment *Mohammadi et al. 2013*

A kinematic analysis  
with CusToM

Normal  
gait

vs

Altered  
gait

*with an ankle brace*



# Context – New Example

Ankle Sprain over the world

1 /10,000 people /day *Katcharian D. 1994*

Treating the ankle sprain grade III:

- Immobilization
- Functional treatment

*Mohammadi et al. 2013*

A kinematic analysis  
with CusToM

Normal  
gait

vs

Altered  
gait

*with an ankle brace*



Botimed

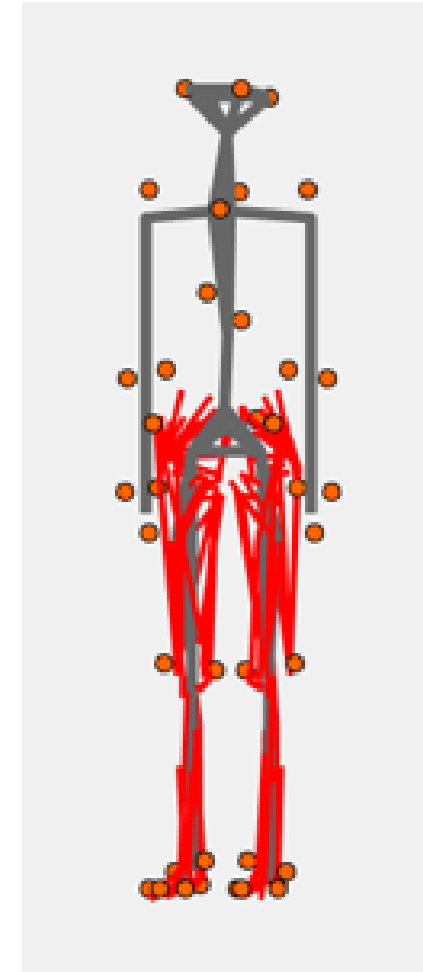
Research Question:

*What are the kinematical compensation strategies ?*

# Generate Parameters of the Model

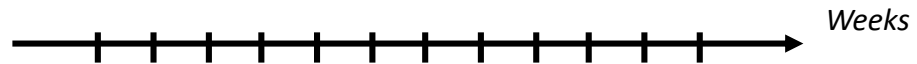
```
>> GenerateParameters|
```

- Size : 1.74 m
- **Mass : 62,5 Kg**
- Osteo-articular model – full body
  - **Leg – Leg without Ankle**
- Marker Set
  - MarkerSet\_2 (M2S makerset)
  - 1 markers on hand
- Muscles



# Data Collection

1 subject



# Data Collection

1 subject



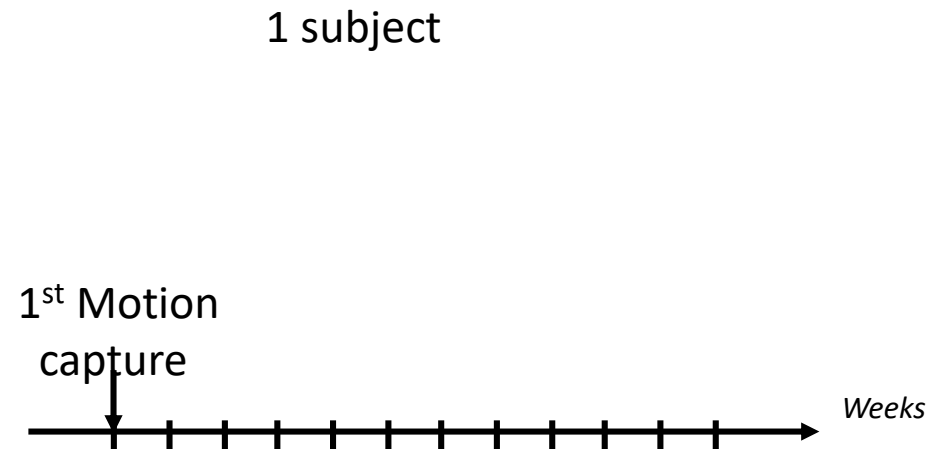


# Data Collection

1 subject



# Data Collection

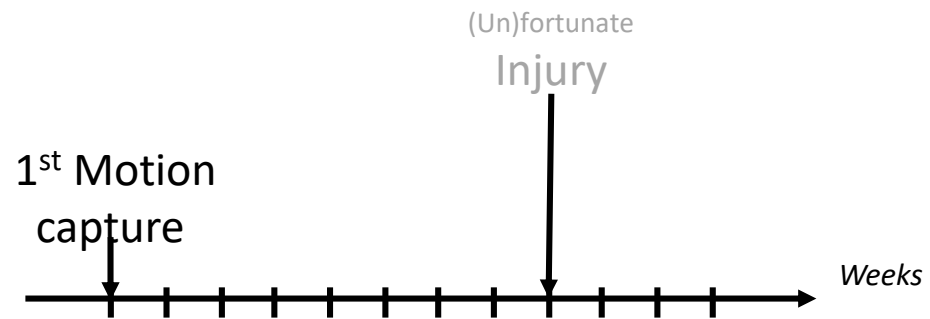


A modified plug-in-gait markerset

45 reflective markers

# Data Collection

1 subject



Complete tear  
of  
right lateral  
ankle  
ligament

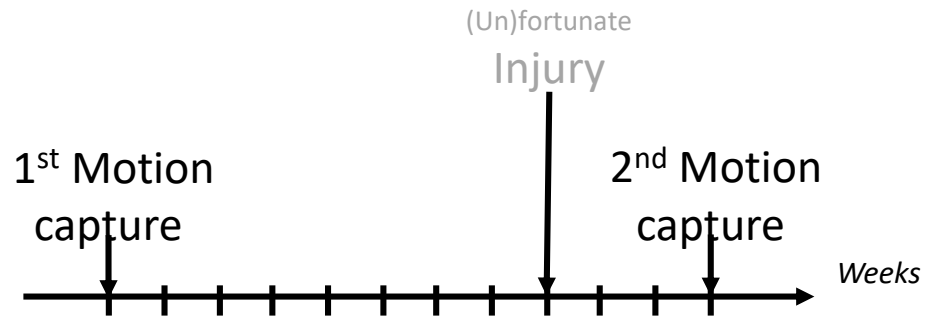


A modified plug-in-gait markerset

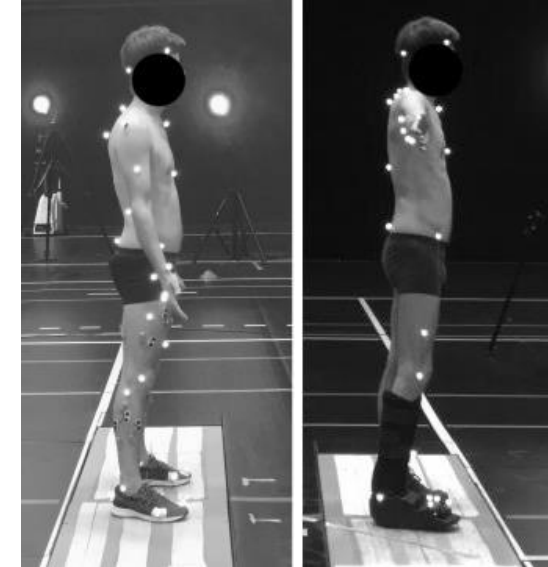
45 reflective markers

# Data Collection

1 subject



Complete tear  
of  
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ligament

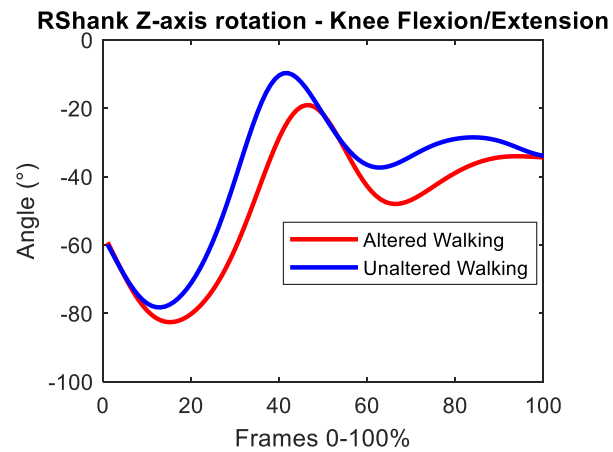
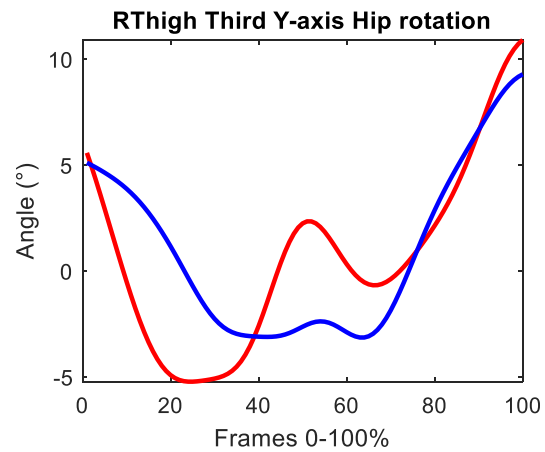
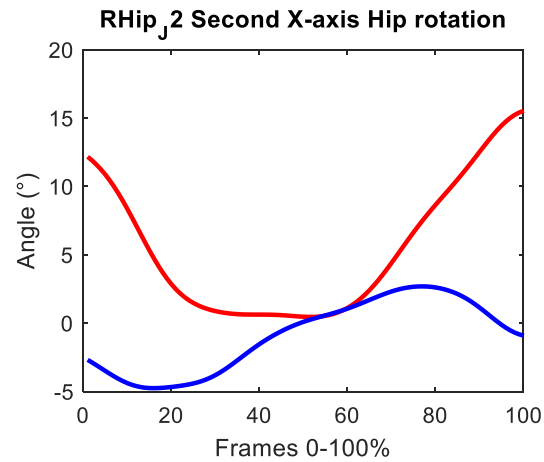
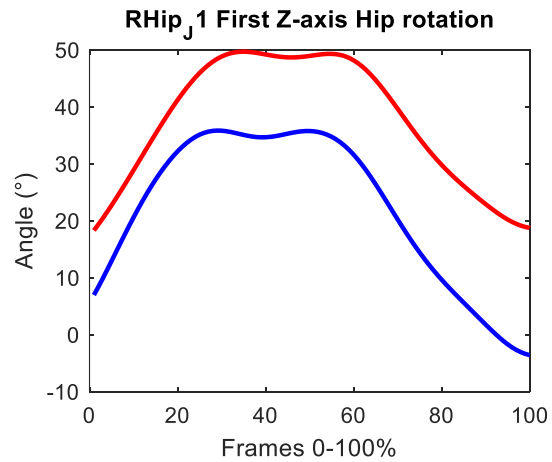


A modified plug-in-gait markerset

45 reflective markers

# Altered and normal gait comparison

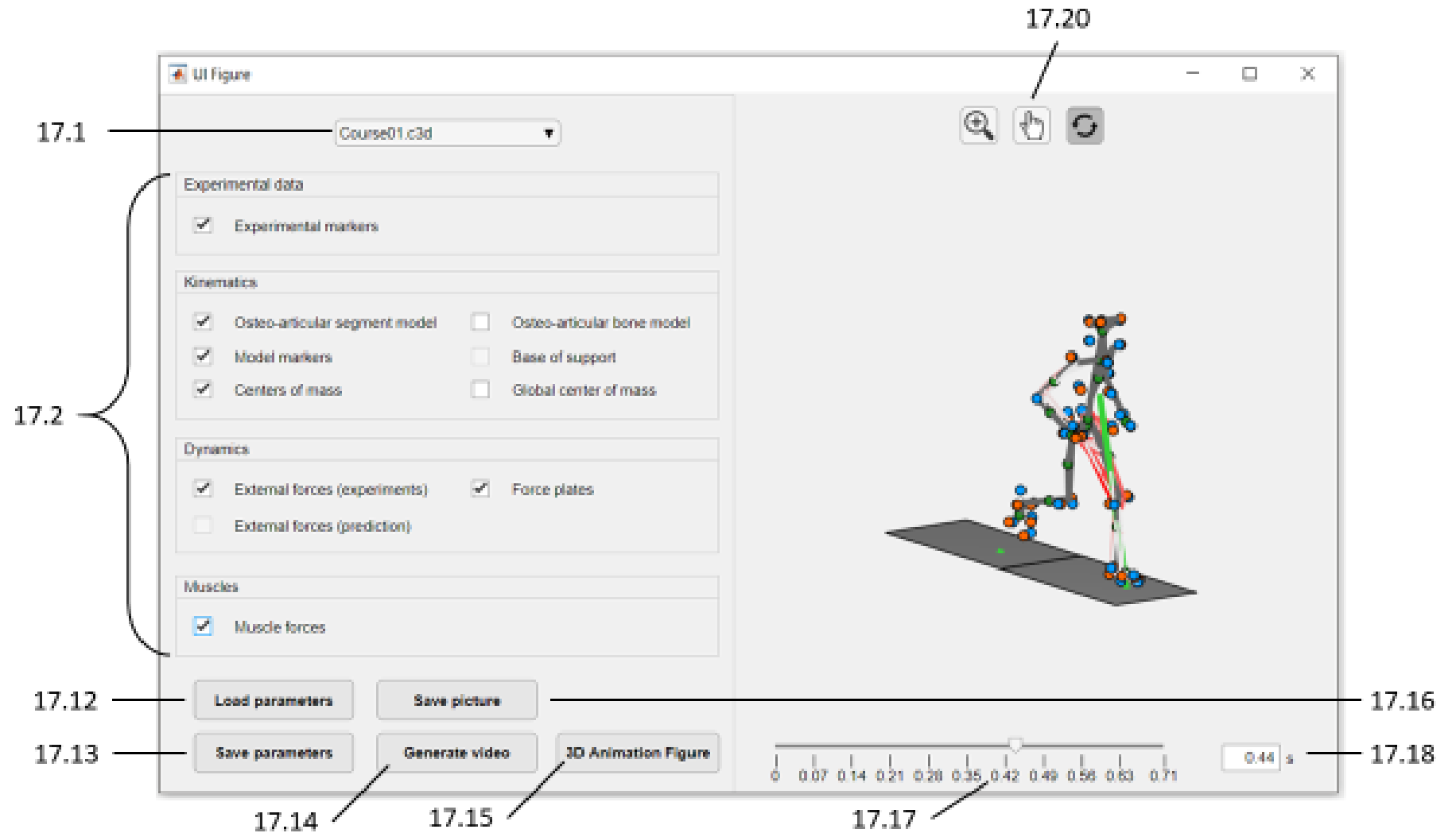
```
>> PostProcessingKinematic_Walking
```



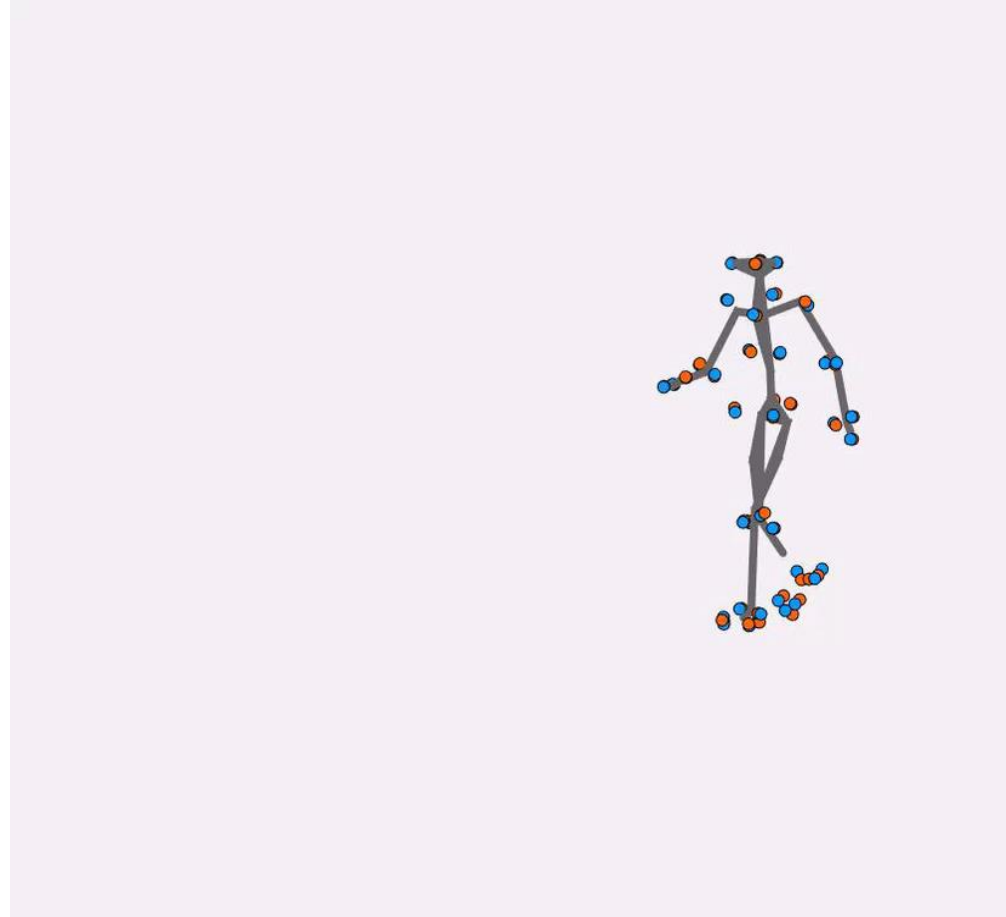
→ Hip circumduction

# Visualization Tutorial

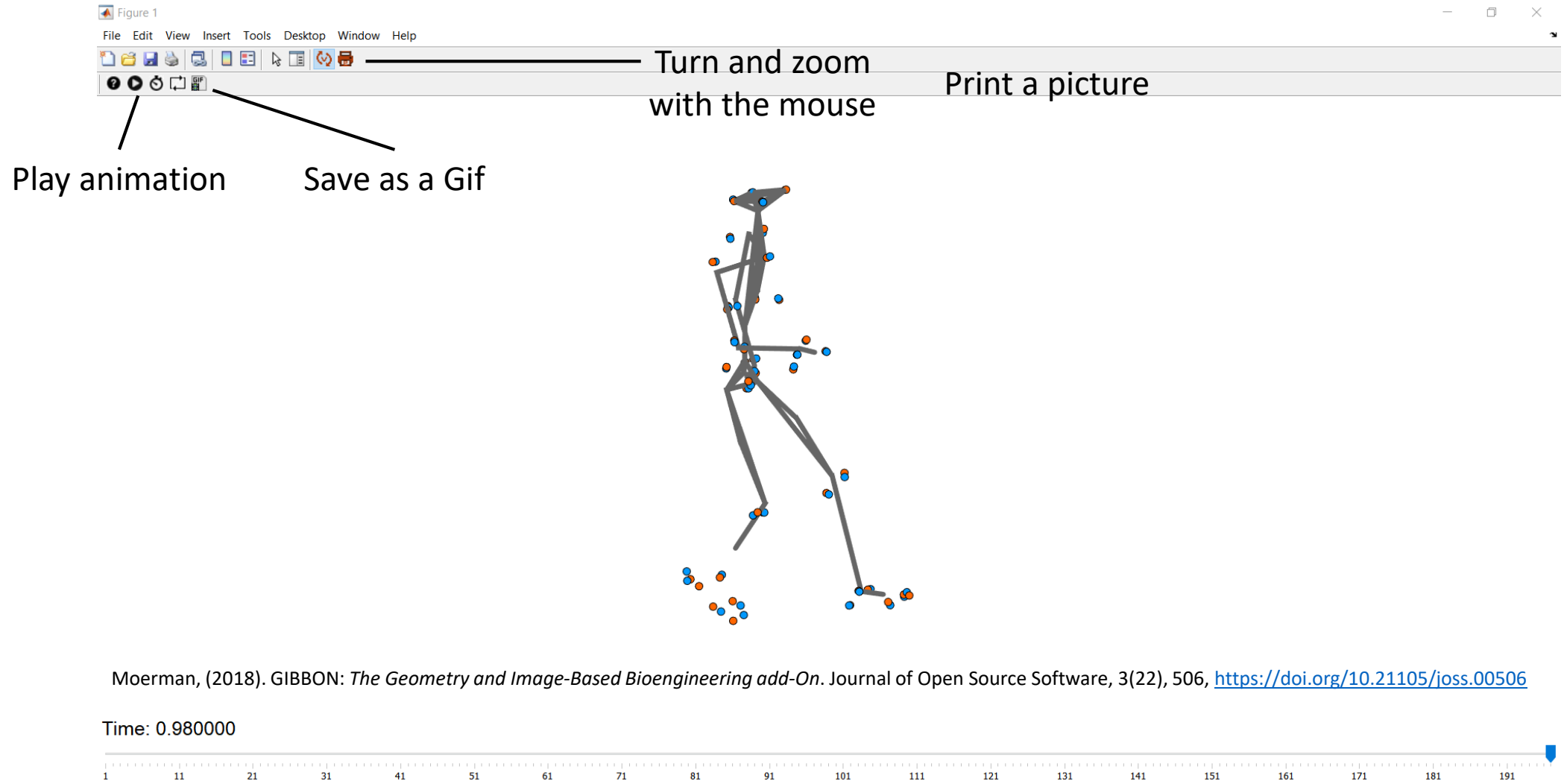
>> GenerateAnimate



# Video



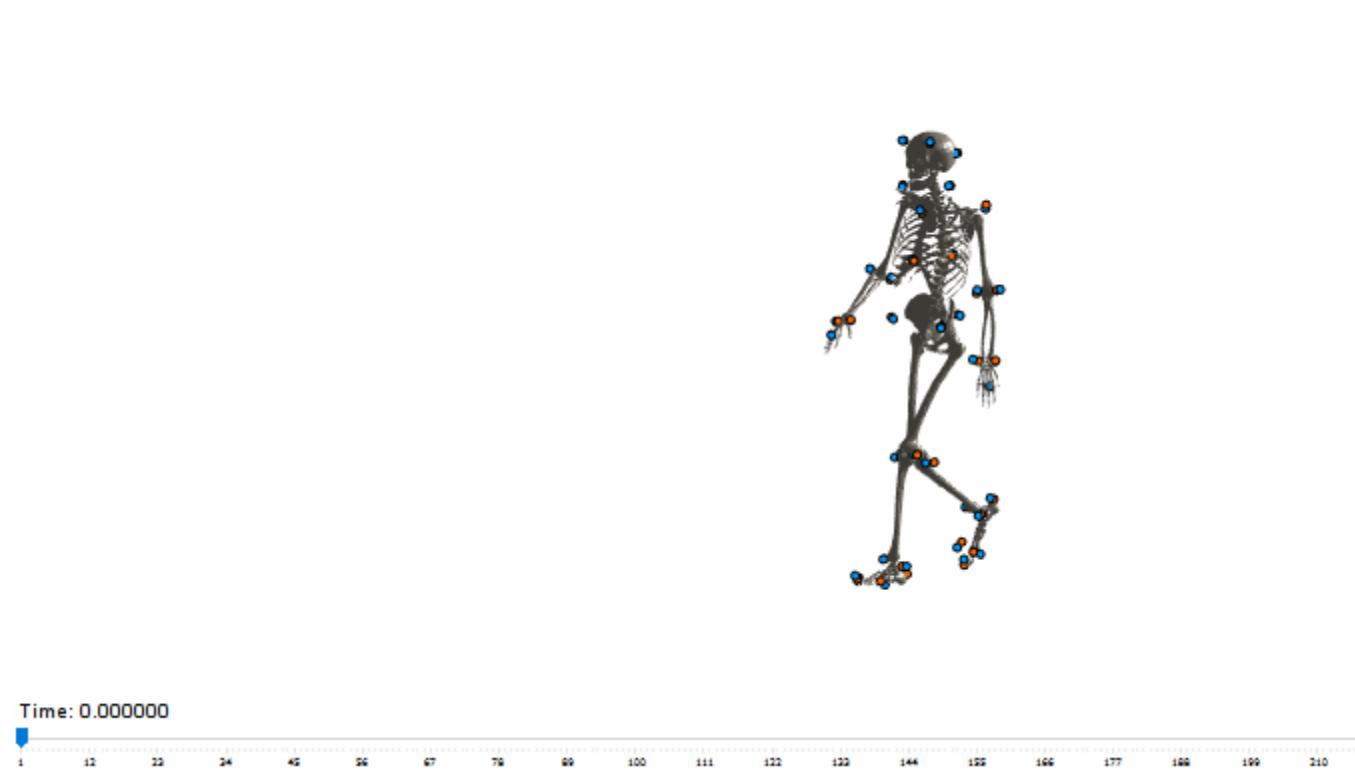
# 3D Animation Figure



Moerman, (2018). GIBBON: *The Geometry and Image-Based Bioengineering add-On*. Journal of Open Source Software, 3(22), 506, <https://doi.org/10.21105/joss.00506>



# .Gif Export



Moerman, (2018). GIBBON: *The Geometry and Image-Based Bioengineering add-On*. Journal of Open Source Software, 3(22), 506, <https://doi.org/10.21105/joss.00506>