

Computed torque control (one method to control a robot)

Consider a typical model for a robot manipulator.

$$\underbrace{M(q)}_{\text{inertia matrix}} \ddot{q} + \underbrace{C(q, \dot{q})}_{\text{Coriolis and centrifugal terms}} + \underbrace{g(q)}_{\text{gravity terms}} = \tau$$

inertia
matrix

Coriolis and
centrifugal terms

gravity
terms

← torque applied

e.g. simple pendulum

$$\frac{ml^2}{3} \ddot{\theta} + \frac{mgl \cos \theta}{2} = \tau$$

$$q = \theta \quad M(q) = \frac{ml^2}{3} \quad C(q, \dot{q}) = 0 \quad g(q) = \frac{mgl \cos \theta}{2}$$

To do computed torque control:

given the current position q , velocity \dot{q} , and desired acceleration \ddot{q}_d , compute the torque that will produce \ddot{q}_d

If we have a regression model we can compute the torque

$$\tau = w^T \phi(q, \dot{q}, \ddot{q})$$

You probably need feedback to make it work in real life.

$$\tau = w^T \phi(q, \dot{q}, \ddot{q}) + \underset{\substack{\uparrow \\ \text{Proportional} \\ \text{gain}}}{K_p} (\underset{\substack{\uparrow \\ \text{measure}}}{q_d} - \underset{\substack{\uparrow \\ \text{measure}}}{q}) + \underset{\substack{\uparrow \\ \text{derivative} \\ \text{gain}}}{K_d} (\underset{\substack{\uparrow \\ \text{measure}}}{\dot{q}_d} - \underset{\substack{\uparrow \\ \text{measure}}}{\dot{q}})$$