Al Hackathon Challenge - Optimal Control of Microgrid

Hackathon team 9

Erling Syversveen Lie og Martin Borge Heir

April, 2020

Sections

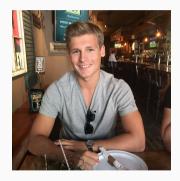
Team

Solution choice

Result

This is us

Erling Syversveen Lie



Martin Borge Heir



Both are third year cybernetics students

Sections

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Solution choice

Result

MPC

- We have chosen to solve the problem with MPC
- MPC is a control method for controlling a system while satisfying constraints

We modeled the system with the following states and inputs

$$\mathbf{x}_{t} = \begin{bmatrix} B_{t} \\ H_{t} \\ G_{t} \end{bmatrix}, \ \mathbf{u}_{t} = \begin{bmatrix} B_{charge} \\ B_{discharge} \\ H_{charge} \\ H_{discharge} \end{bmatrix}$$
(1)

 We modeled two different cost functions. P_{spot} is a diagonal matrix of the prices over different time steps. G is a vector of the grid usage.

$$Cost_1 = \mathbf{G}^T \mathbf{P}_{spot} \mathbf{G} \tag{2}$$

$$Cost_2 = \mathbf{G}^T \mathbf{P}_{spot} \mathbf{G} + 49 * max(\mathbf{G})$$
 (3)

This gave the following equation for charging the battery and hydrogen

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \mathbf{x}_{t+1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \mathbf{x}_t + \begin{bmatrix} 0.85 & -1 & 0 & 0 \\ 0 & 0 & 0.325 & -1 \end{bmatrix} \mathbf{u}_t$$
 (4)

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• Equation for constraint on grid

$$G_t = \begin{bmatrix} 1 & -1 & 1 & -1 \end{bmatrix} \mathbf{u}_t - P\hat{V}_t - \hat{W}_t + \hat{C}_t$$
 (5)

• Inequality constraints:

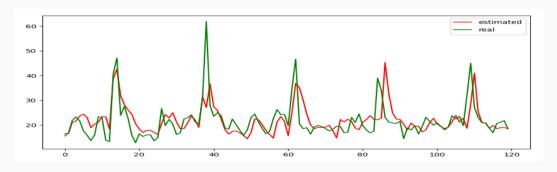
$$\begin{bmatrix} 1 & 0 & 0 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -1 & 0 \end{bmatrix} \mathbf{x}_{t} + \begin{bmatrix} 0.85 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0.325 & 0 \\ 0 & 0 & 01 \end{bmatrix} \mathbf{u}_{t} < \begin{bmatrix} 500 \\ 0 \\ 1670 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 \end{bmatrix} \qquad \begin{bmatrix} 400 \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} < \mathbf{u}_t < \begin{bmatrix} 400 \\ 400 \\ 55 \\ 100 \end{bmatrix} \tag{7}$$

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- We estimated consumption with an AR(48) model.
 - AR models are representations of stochastic processes that predicts the next timestep as linearly dependent on the signals own previous values

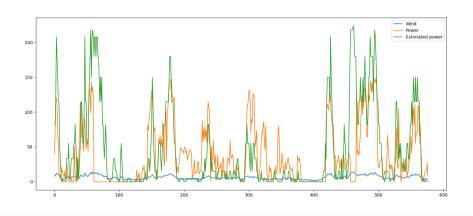


 $\textbf{Figure 1:} \ \, \mathsf{True} \, \, \mathsf{vs} \, \, \mathsf{estimated} \, \, \mathsf{consumption} \, \,$

• We estimated wind production simply by applying the wind power curve

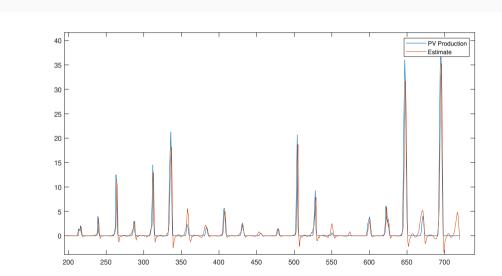


Figure 2: Ideal wind power curve



 $\textbf{Figure 3:} \ \, \mathsf{True} \, \, \mathsf{vs} \, \, \mathsf{estimated} \, \, \mathsf{wind} \, \, \mathsf{production} \, \,$

■ PV we also modeled as an AR(48) process



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Results

Result without prediction

- The system worked well when we tested with the actual stochastic values.
- On the training set, starting from 01/02-2020 we achieved a reward of 1811.
- On the test set, which starts at 01/02-2021 we achieved a reward of 11174.

Train - February 2020

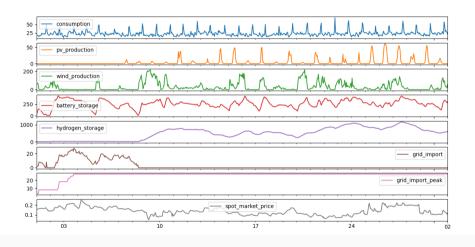


Figure 5: Performance on February 2020

Test - February 2021

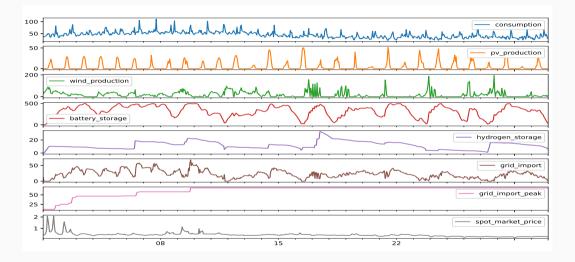


Figure 6: Performance on February 2020

Result with prediction

- When we include prediction our model unfortunately performs bad
- On the test set with estimated stochastic values we reached a reward of 18032 NOK with the MPC model
- No action at all gives 14385 NOK reward
- We felt we had to at least provide a model that performs better than no action. So we propose a solution called Night and Day model
 - Discharge battery with a rate of 25 kWh between 15 and 19 each day.
 - Charge battery with a rate of 3.57 kWh between 19 and 15.
- The Night-and-Day model achieves 13421 NOK reward on the test set.

Test with prediction - February 2021

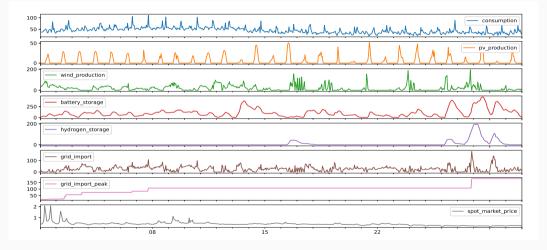


Figure 7: States for test set with predicted stochastic values

Test with prediction - February 2021

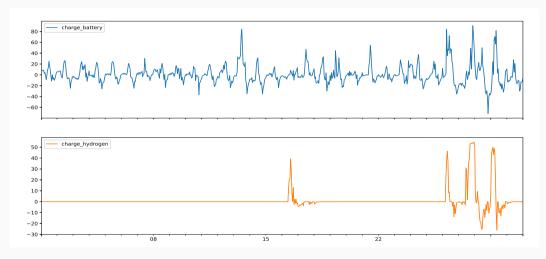


Figure 8: Actions for test set with predicted stochastic values

Test Night and day - February 2021

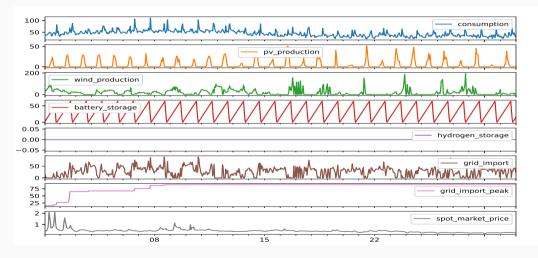
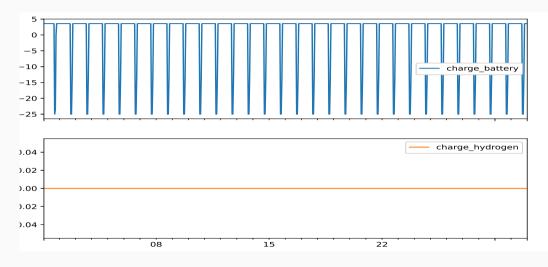


Figure 9: States for test set with night and day model

Test Night and day - February 2021



 $\textbf{Figure 10:} \ \, \textbf{Action for test set with night and day model}$