

Meetup



Friendly Environment Policy



Berlin Code of Conduct

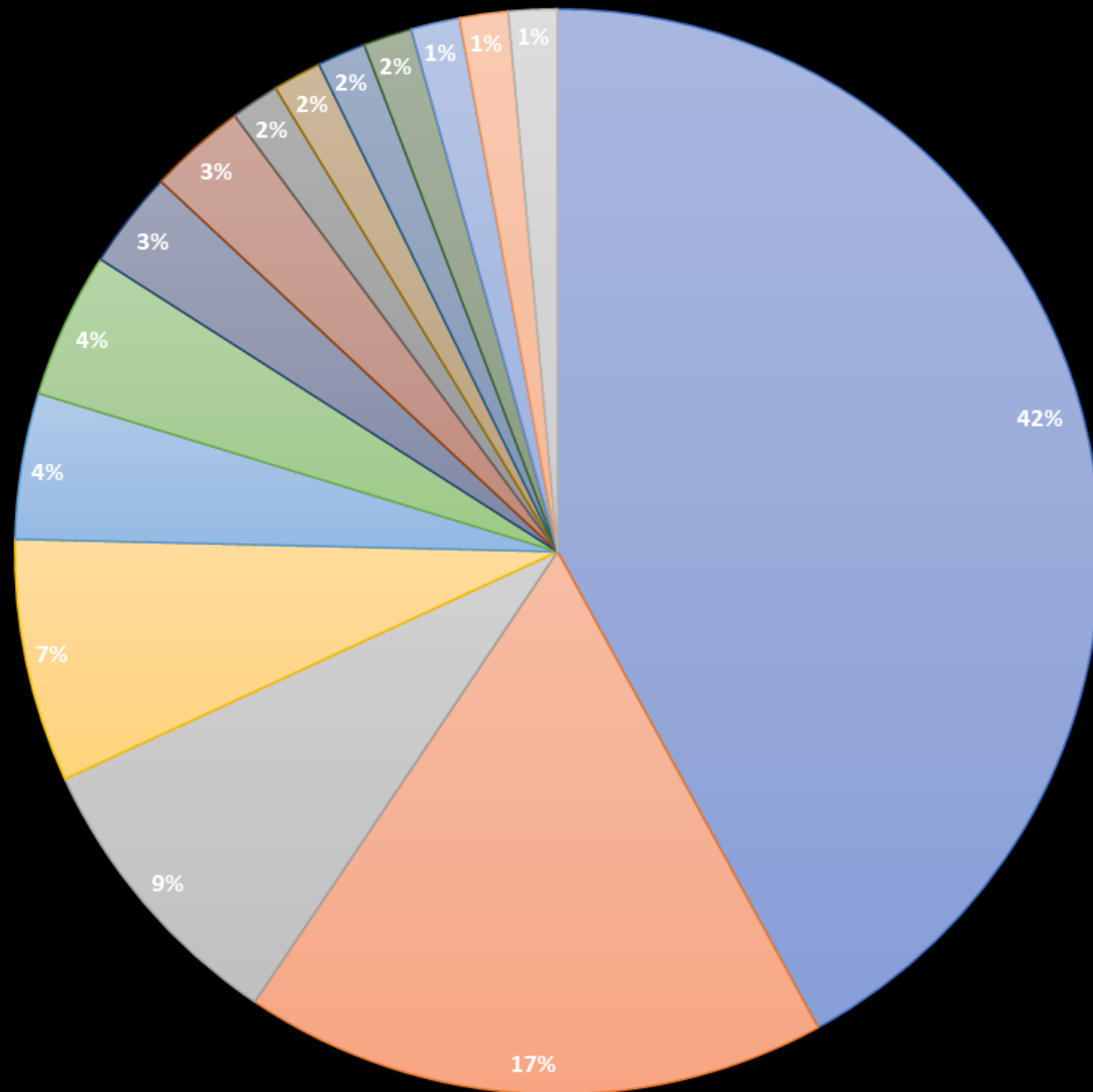


**CATEGORY THEORY
FOR PROGRAMMERS**



Bartosz Milewski

**Category
Theory
for
Programmers
Chapter 2:
Types & Functions**



- C++
- Python
- Rust
- Java
- Dart
- Haskell
- F#
- Go
- Swift
- Elixir
- Ruby
- R
- Clojure
- Ocaml
- Erlang

2	Types and Functions	11
2.1	Who Needs Types?	11
2.2	Types Are About Composability	13
2.3	What Are Types?	14
2.4	Why Do We Need a Mathematical Model?	17
2.5	Pure and Dirty Functions	20
2.6	Examples of Types	21
2.7	Challenges	25

THE CATEGORY OF TYPES AND FUNCTIONS plays an important role in programming, so let's talk about what types are and why we need them.

2.1 Who Needs Types?

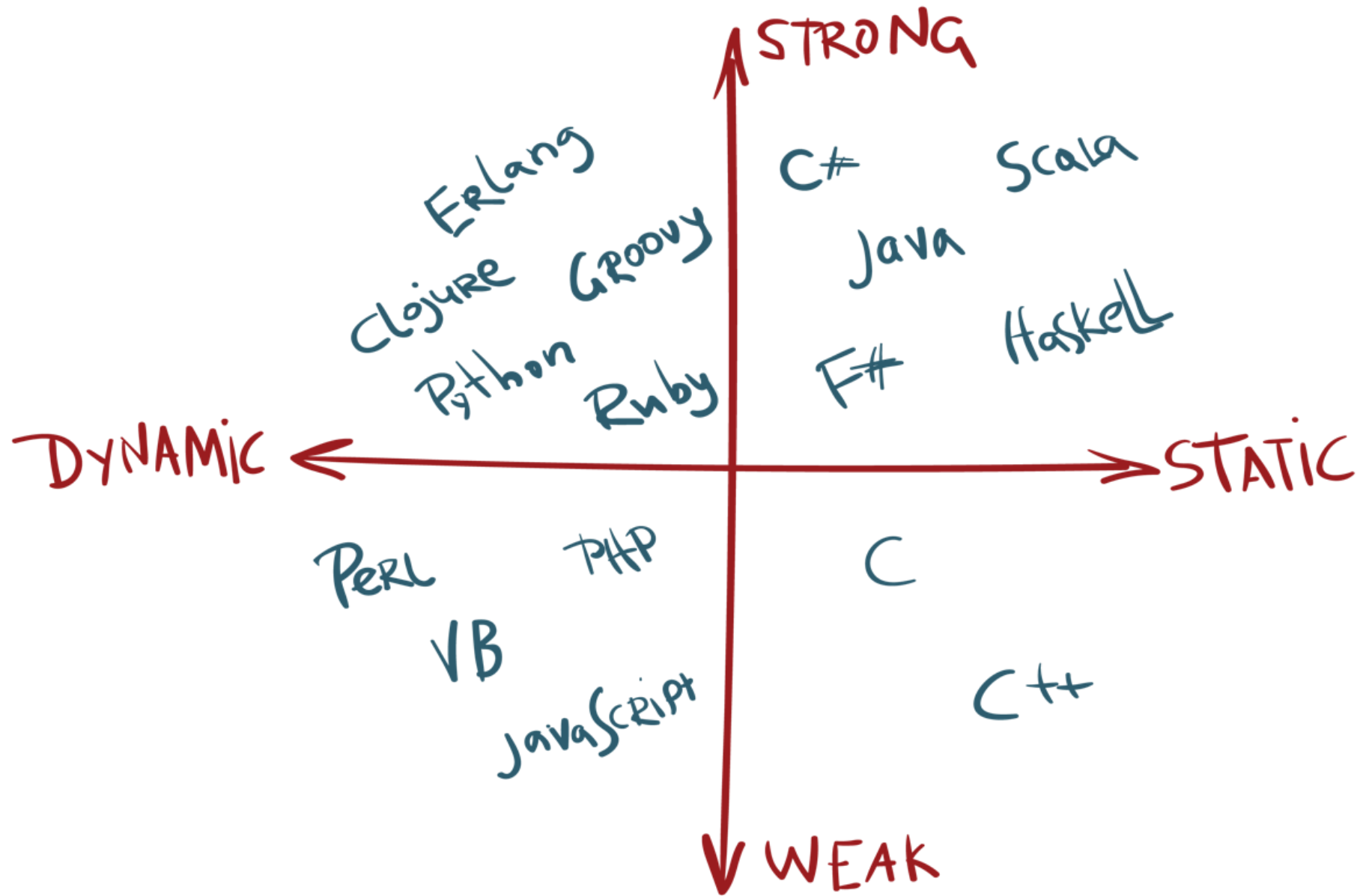
There seems to be some controversy about the advantages of static vs. dynamic and strong vs. weak typing.

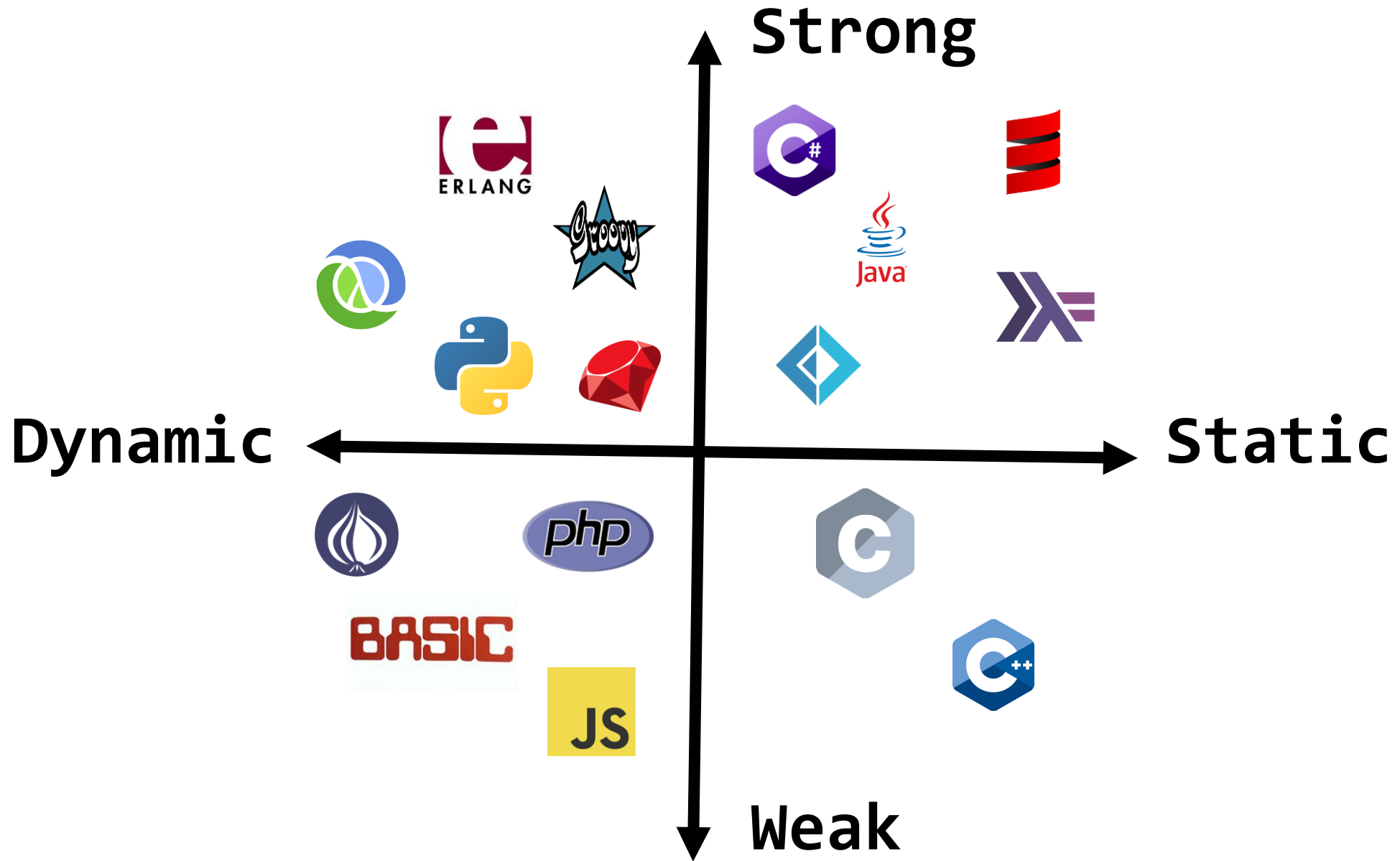
Anyone know any lazy-by-default, dynamically typed functional programming languages?

#functionalprogramming

@planetclojure @kotlin @fsharporg @erlang_org
@elixirlang @scala_lang @elm-lang @OCamlLang
@racketlang #haskell #lisp #schemelang #fsharp
#clojure #scala #elixir #kotlin







Cunningham's Law states "the best way to get the right answer on the internet is not to ask a question; it's to post the wrong answer."

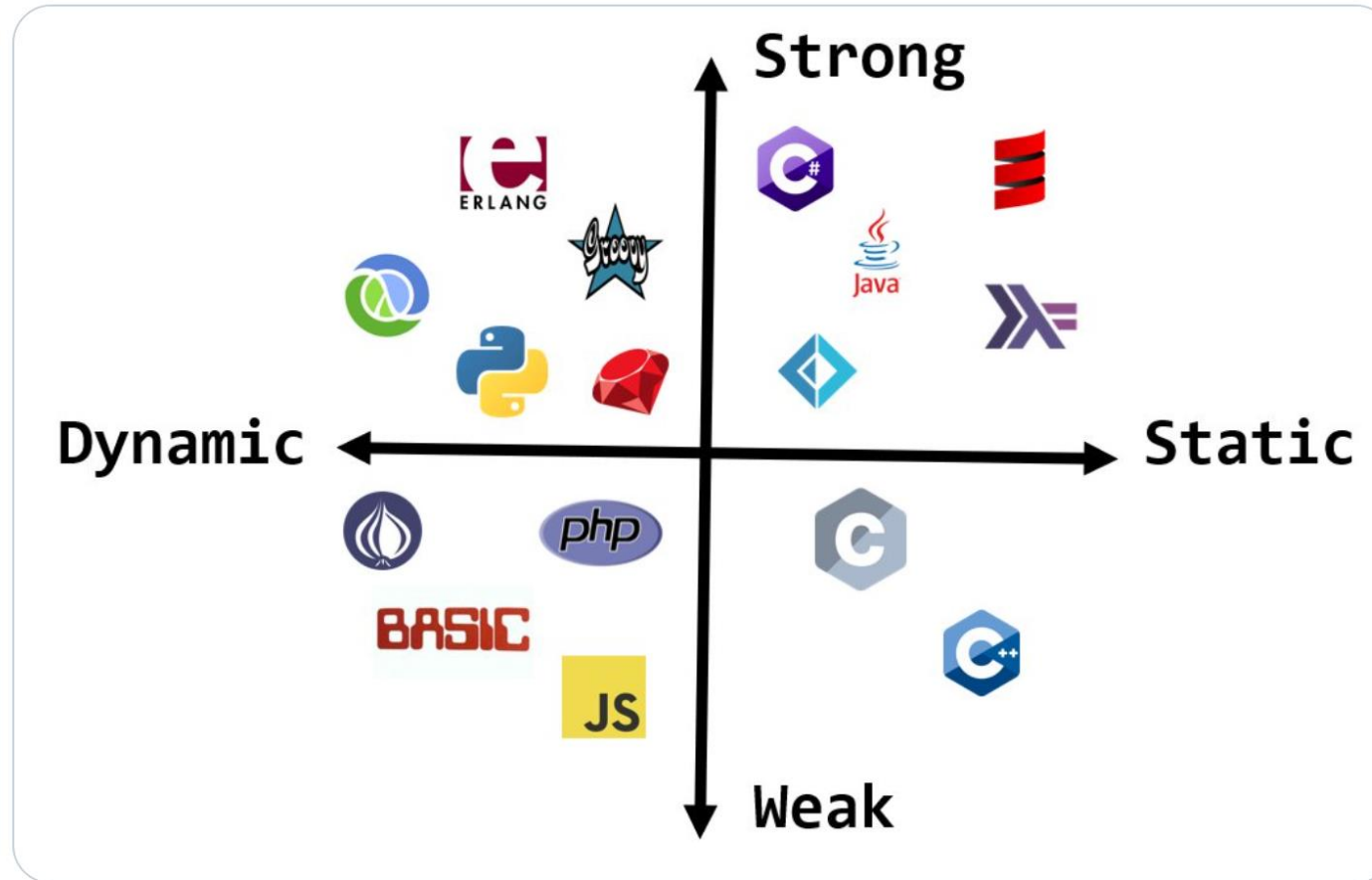


Programming Languages Virtual Meetup

@plvirtualmeetup

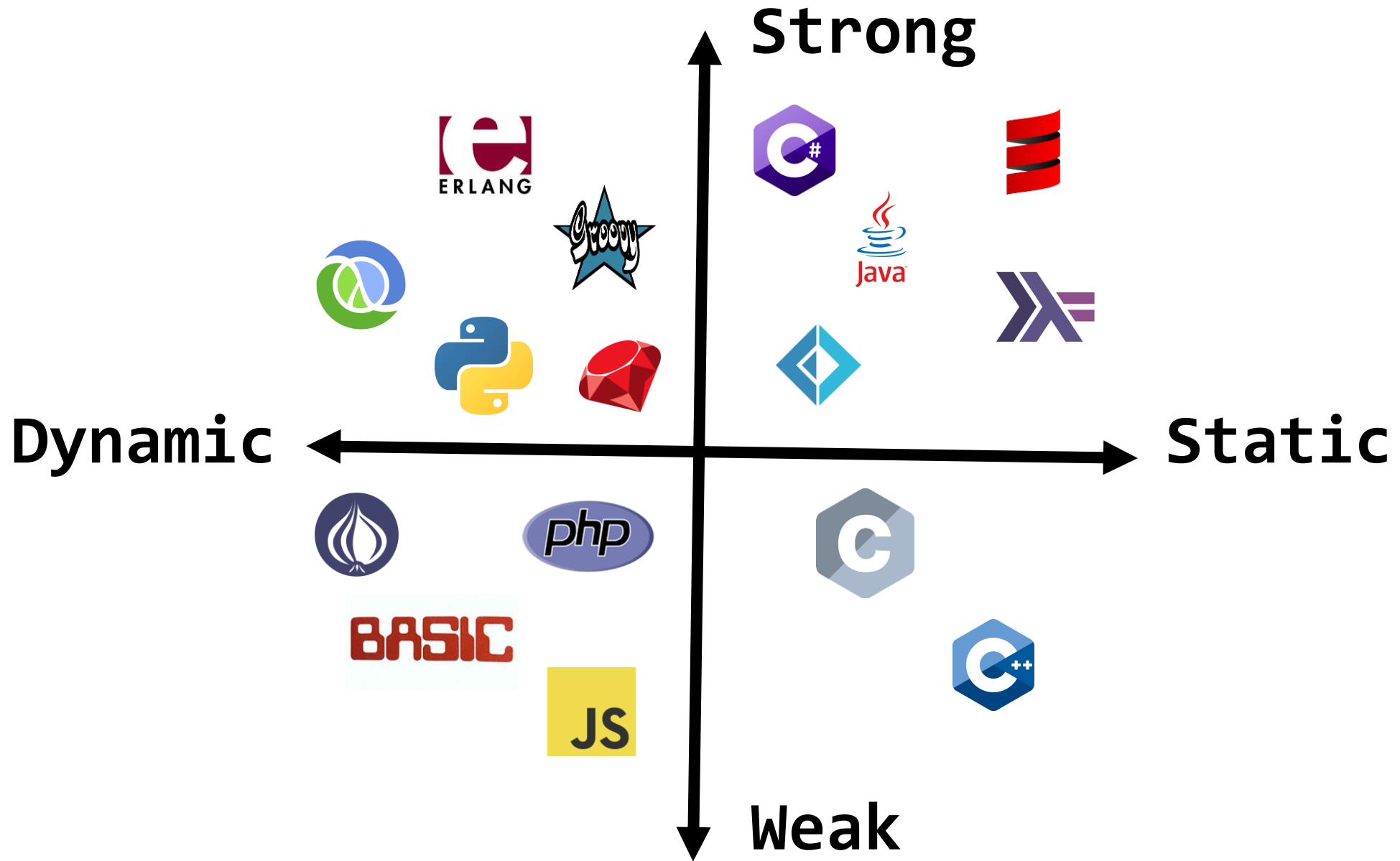


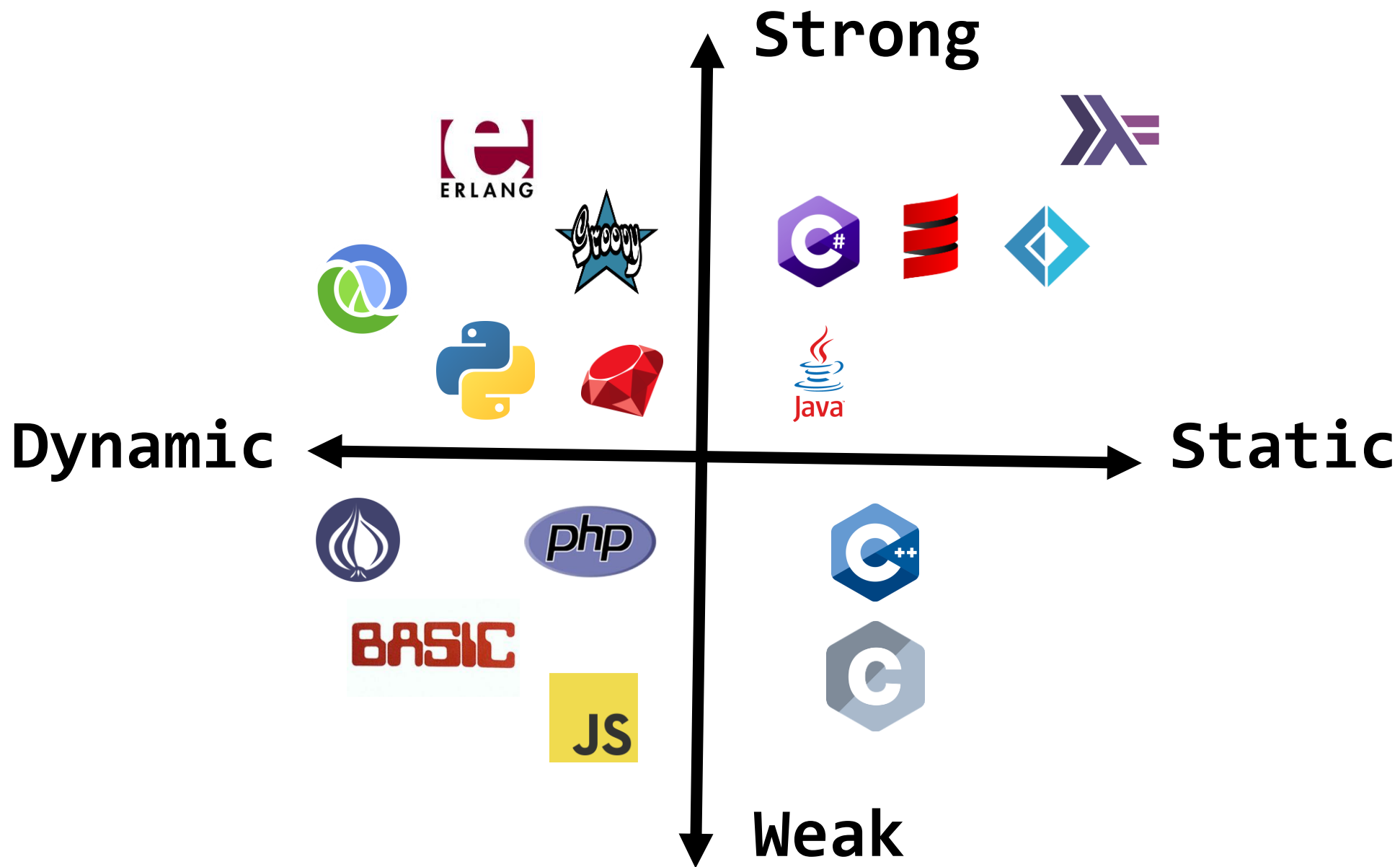
What [#programminglanguages](#) are missing and where do they go?



5:42 PM · Feb 5, 2021 · Twitter Web App

4 Retweets 1 Quote Tweet 19 Likes





2.3 What Are Types?

The simplest intuition for types is that they are sets of values. The type `Bool` (remember, concrete types start with a capital letter in Haskell) is a two-element set of `True` and `False`. Type `Char` is a set of all Unicode characters like `a` or `ą`.

But there is an alternative. It's called *denotational semantics* and it's based on math. In denotational semantics every programming construct is given its mathematical interpretation. With that, if you want to prove a property of a program, you just prove a mathematical theorem.



fact n = product [1 .. n]



```
int fact ( int n) {  
    int result = 1;  
    for (int i = 2; i <= n; ++ i)  
        result *= i;  
    return result;  
}
```



```
using namespace std::ranges;
```

```
auto fact(int n) -> int {  
    auto vals = views::iota(1, n);  
    return std::reduce(begin(vals), end(vals), 1, std::multiplies{});  
}
```



```
using namespace std::ranges;
```

```
auto fact(int n) -> int {  
    return views::iota(1, n) | fold(1, std::multiplies{});  
}
```



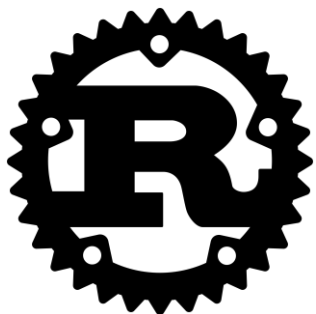
```
fn fact(n: i32) -> i32 {  
    (1..  
    =n).product()  
}
```



```
fact n = product [1 .. n]
```



```
auto fact(int n) -> int {  
    auto vals = views::iota(1, n);  
    return std::reduce(begin(vals), end(vals), 1, std::multiplies{});  
}
```



```
fn fact(n: i32) -> i32 {  
    (1..=n).product()  
}
```



Conor Hoekstra
@code_report

...

"I've been referring to it [Rust] 🦀 as a love child between Haskell and C++."

- quote from @roeschinc on Episode 77 of @fngeekery
Another awesome episode! #Haskell #cplusplus
@rustlang

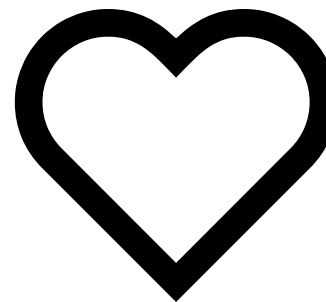
12:45 PM · Aug 26, 2019 from Sunnyvale, CA · Twitter for Android



+



+



=



?

In programming languages, functions that always produce the same result given the same input and have no side effects are called *pure functions*. In a pure functional language like Haskell all functions are pure.

Functions that can be implemented with the same formula for any type are called parametrically polymorphic.

Functions to `Bool` are called *predicates*. For instance, the Haskell library `Data.Char` is full of predicates like `isAlpha` or `isDigit`.



1. Define a higher-order function (or a function object) `memoize` in your favorite language. This function takes a pure function `f` as an argument and returns a function that behaves almost exactly like `f`, except that it only calls the original function once for every argument, stores the result internally, and subsequently returns this stored result every time it's called with the same argument. You can tell the memoized function from the original by watching its performance. For instance, try to memoize a function that takes a long time to evaluate. You'll have to wait for the result the first time you call it, but on subsequent calls, with the same argument, you should get the result immediately.



```
auto memoize(auto fn) {  
    return [done = std::map<int,int>{}, fn](auto n) mutable {  
        if (auto it = done.find(n); it != done.end())  
            return it->second;  
        auto const val = fn(n);  
        done[n] = val;  
        return val;  
    };  
}
```



```
auto memoize(auto fn) {  
    return [done = std::map<int,int>{}, fn](auto n) mutable {  
        if (auto it = done.find(n); it != done.end())  
            return it->second;  
        return done[n] = fn(n);  
    };  
}
```



5. How many different functions are there from `Bool` to `Bool`? Can you implement them all?



```
auto same_(bool b) -> bool { return b;      }  
auto diff_(bool b) -> bool { return !b;     }  
auto true_(bool b) -> bool { return true;   }  
auto fals_(bool b) -> bool { return false; }
```



same	←	⊢
diff	←	~
true	←	1 ∘ ⊢
false	←	0 ∘ ⊢



Bartosz Milewski

19.8K subscribers

SUBSCRIBE

HOME

VIDEOS

PLAYLISTS

COMMUNITY

CHANNELS

ABOUT



Uploads PLAY ALL

≡ SORT BY



Category Theory III 7.2,
Coends

4.1K views • 2 years ago



Category Theory III 7.1,
Natural transformations as...

2.6K views • 2 years ago



Category Theory III 6.2, Ends

2.3K views • 2 years ago



Category Theory III 6.1,
Profunctors

2.5K views • 2 years ago



Category Theory III 5.2,
Lawvere Theories

2.3K views • 2 years ago



Category Theory III 5.1,
Eilenberg Moore and Lawvere

2.5K views • 2 years ago



Category Theory III 4.2,
Monad algebras part 3

1.7K views • 2 years ago



Category Theory III 4.1,
Monad algebras part 2

1.8K views • 2 years ago



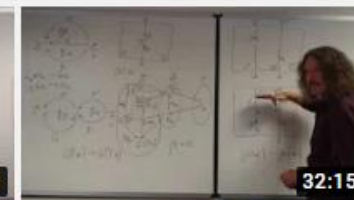
Category Theory III 3.2,
Monad Algebras

2.6K views • 2 years ago



Category Theory III 3.1,
Adjunctions and monads

2.8K views • 2 years ago



Category Theory III 2.2, String
Diagrams part 2

2.8K views • 2 years ago



Category Theory III 2.1:
String Diagrams part 1

3.9K views • 2 years ago



Category Theory III 1.2:
Overview part 2

2.8K views • 2 years ago



Category Theory III 1.1:
Overview part 1

8.6K views • 2 years ago



Category Theory II 9.2:
Lenses categorically

3.8K views • 3 years ago



Category Theory II 9.1:
Lenses

4.9K views • 3 years ago



Category Theory II 8.2:
Catamorphisms and...

4.4K views • 3 years ago



Category Theory II 8.1: F-
Algebras, Lambek's lemma

5.7K views • 3 years ago

$\text{Void} \longleftrightarrow \text{false}$

$\text{absurd} :: \text{Void} \rightarrow a$

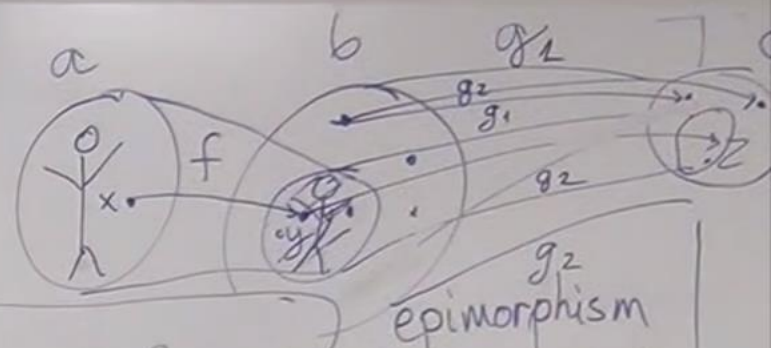
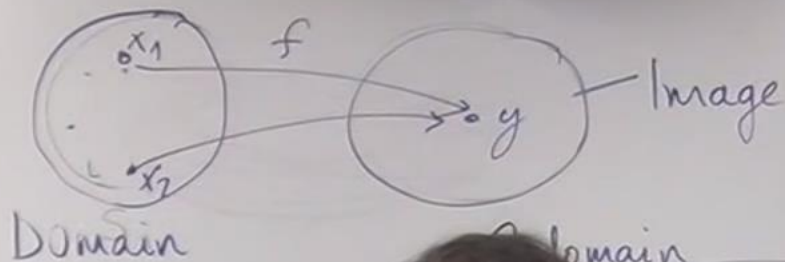
$\text{id}_{\text{Void}} :: \text{Void} \rightarrow \text{Void}$

$\text{Unit} \quad () :: () \longleftrightarrow \text{True}$

$\text{unit} :: a \rightarrow ()$

$\text{one} :: () \rightarrow \text{Int}$

two



$\forall c. \forall g_1, g_2. g_1 \circ f = g_2 \circ f \Rightarrow g_1 = g_2$ **surjective** **epic**

~~$g_1 \circ f = g_2 \circ f$~~



Meetup