

1. Convert Context Free Grammar to Chomsky Normal Form (CNF):

Given Grammar:

$VN = \{S, A, B\}$

$VT = \{a, b\}$

P:

$S \rightarrow a B$

$S \rightarrow B A$

$A \rightarrow a$

$A \rightarrow b B$

$A \rightarrow A a b B$

$B \rightarrow \epsilon$

$B \rightarrow b S$

$B \rightarrow a A B A$

Step 1: Eliminate ϵ -productions:

Replace $B \rightarrow \epsilon$ with $B \rightarrow SS \mid SB \mid BS \mid SA \mid AS$.

Step 2: Eliminate unit productions:

There are no unit productions in this grammar.

Step 3: Convert productions to have at most two symbols on the right side:

Rewrite long productions by introducing new non-terminals:

$$S \rightarrow BA \mid AB$$
$$A \rightarrow a$$
$$A \rightarrow bB$$
$$A \rightarrow AAB$$
$$B \rightarrow bS$$
$$B \rightarrow aAB \mid aBA$$

The CNF version of the grammar is now in the specified form.

2. Convert Grammar to Greibach Normal Form (GNF):

Given Grammar:

$$VN = \{S, A, B, C\}$$
$$VT = \{a, b\}$$

P:

$$S \rightarrow bB$$
$$A \rightarrow BA$$
$$B \rightarrow AC$$
$$A \rightarrow B$$

$A \rightarrow b$

$C \rightarrow a$

Step 1: Each production's right-hand side should start with a terminal symbol.

Rewrite the productions accordingly:

$S \rightarrow bB$

$A \rightarrow bA \mid BA$

$B \rightarrow aC$

$A \rightarrow B$

$A \rightarrow b$

$C \rightarrow a$

The grammar is now in Greibach Normal Form.

3. Construct Pushdown Automata for the language L:

The language $L = \{a^{(2m)} b^{(n)} a^{(n)} \mid m, n \in \mathbb{N}\}$ represents strings with twice as many 'a's followed by 'b's, and then followed by 'a's equal to the number of 'b's.

Pushdown Automaton (PDA):

States: $\{q_0, q_1, q_2, q_3\}$

Alphabet: $\{a, b\}$

Stack Alphabet: $\{Z_0, A\}$

Transition Rules:

$(q_0, a, Z_0) \rightarrow (q_0, AZ_0)$

$(q_0, a, A) \rightarrow (q_0, AA)$

$(q_0, \epsilon, A) \rightarrow (q_1, \epsilon)$

$(q_1, b, A) \rightarrow (q_2, \epsilon)$

$(q_2, \epsilon, Z_0) \rightarrow (q_3, \epsilon)$

Analysis of the Word:

For the word "aabbaa", the PDA would start at q_0 , pushing 'A' onto the stack for each 'a', transitioning to q_1 after reading all 'a's, then popping 'A' for each 'b' in q_2 , and finally transitioning to q_3 after reading all 'b's, where the stack becomes empty.

4. Matrix of Simple Precedence & Derivation Tree:

Given Grammar:

$VN = \{S, A, B, C, D\}$

$VT = \{a, b, c, d, e, f\}$

P:

$S \rightarrow A$

$A \rightarrow aD$

$D \rightarrow b$

$D \rightarrow bD$

$D \rightarrow Ac$

Matrix of Simple Precedence:

	b	c	d	e	f	
a		<	<	<	<	<
b	>	=	<	<	<	<
c						
d	>					
e						
f	>					

Analysis of "ababbc" and Derivation Tree:

Step 1: $S \rightarrow A$

Step 2: $A \rightarrow aD$

Step 3: $D \rightarrow b$

Step 4: $D \rightarrow bD$

Step 5: $D \rightarrow Ac$ (Apply this rule to generate the remaining 'c')

Derivation Tree:

S
|
A
/ | \
a D c
|
b
|
b