



Physics Homework 2

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Group: DSAI-03

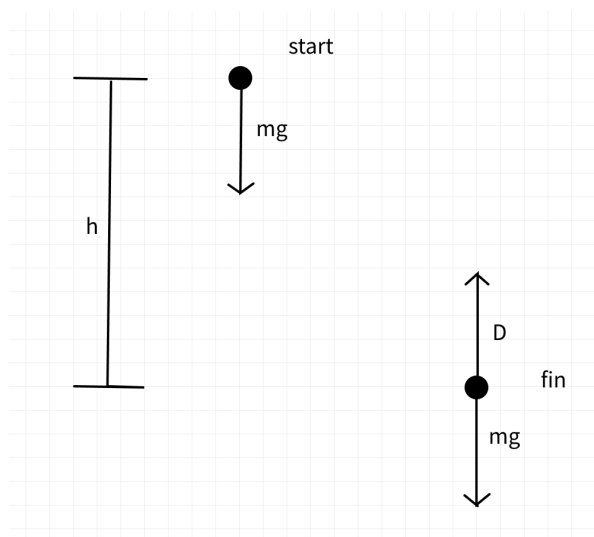
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Problem 1 (25 pts)

In the movie “Fast and Furious 7”, one particular scene features 5 parachute-equipped cars (Dom's 1968 Dodge Charger, Letty's 2015 Challenger SRT, Roman's 1968 Chevy Camaro Z/28, Brian's Subaru WRX STI, and Tej's Jeep Rubicon) being pushed out of a C-130 cargo airplane at the altitude of approximately 3500 meters. Some parameters of 3 of these cars are given in table below.

	Jeep Rubicon	Dodge Challenger SRT (2015)	Subaru WRX STi
Drag coefficient, C_d	0.5	0.38	0.33
Cross-sectional area, A (m ²)	2.58	2.41	2.225
Mass, m (kg)	2000	2450	1550

The air drag force is given by an equation $D = (1/2)C_d\rho A v^2$. Air density and the gravity constant are $\rho = 1.007 \text{ kg/m}^3$ and $g = 9.8 \text{ m/s}^2$, respectively. What would be the terminal velocities of each car (m/s, round to 1 decimal place), if they are performing a free-fall headfirst without tumbling in the air?

**Solution:**

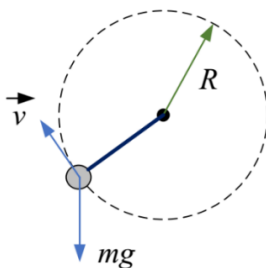
<p>Given:</p> <p>$g = 9.8 \text{ m/s}^2$</p> <p>$\rho = 1.007 \text{ kg/m}^3$</p> <p>$h = 3500 \text{ m}$</p>	<p>According to lecture slides.</p> <p>In some moment V will be constant and from this moment until falling down, because $mg - D = 0$; a will be 0;</p> <p>So let us find;</p> $mg - (1/2)C_d\rho A v^2 = 0$ $v^2 = 2mg / C_d\rho A$ $v = \sqrt{2mg / C_d\rho A}$ <p>Take only positive number cause velocity;</p> <p>Answer:</p> <p>1. Jeep Rubicon:</p> <p>$v = 173.7 \text{ m/s}$</p> <p>2. Dodge Challenger:</p> <p>$v = 228.2 \text{ m/s}$</p> <p>3. Subaru:</p> <p>$v = 202.7 \text{ m/s}$</p> <hr/> <p>Pin my second solution.</p> <p>So in the initial step let us write the law of conservation of energy. For this</p>
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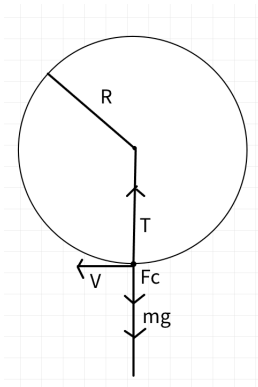
	<p>system. First is potential energy+kinetic energy+Energy that is given by air drag force.</p> $E_{gravity} + E_{kin} + E_{drag} = E_{full}$ <p>So when the car is falling our $E_{gravity}$ goes for overtaking E_{drag} and for increasing E_{kin}</p> <p>We can overwrite in this form. $E_{gravity} = mgh$; $E_{kin} = mv^2/2$;</p> $E_{drag} = D * h$ $mgh = mv^2/2 + D * h$ <p>We know D from the condition</p> $2hmg - Cd\rho Av^2h = mv^2$ $2hmg = v^2(m + Cd\rho Ah)$ $v = \sqrt{2hmg/(m + Cd\rho Ah)}$ <p>Jeep Rubicon: $v = 144.8 \text{ m/s}$ Dodge Challenger: $v = 172.1 \text{ m/s}$ Subaru: $v = 160.3 \text{ m/s}$</p>
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Problem 2 (25 pts)

An object of mass $m = 0.25 \text{ kg}$, rotating on a string along a circular path of radius $R = 0.7 \text{ m}$ in the vertical plane, subjects to gravitational force (see figure at the right). The maximum tension force that the string can sustain without breaking is 30 N . If the speed of the object is being slowly increased (it means that the tangential acceleration is negligibly small compared to centripetal one), and assuming $g = 9.8 \text{ m/s}^2$, answer the following:

- 2.1. Find the position of the mass on the circular trajectory (exactly) where the string has maximum tension at a given constant speed of the mass. (10 pts)
- 2.2. What is the maximum speed (m/s, round to 1 decimal place), when the string does not break for any position of the object on the whole circle trajectory? (15 pts)



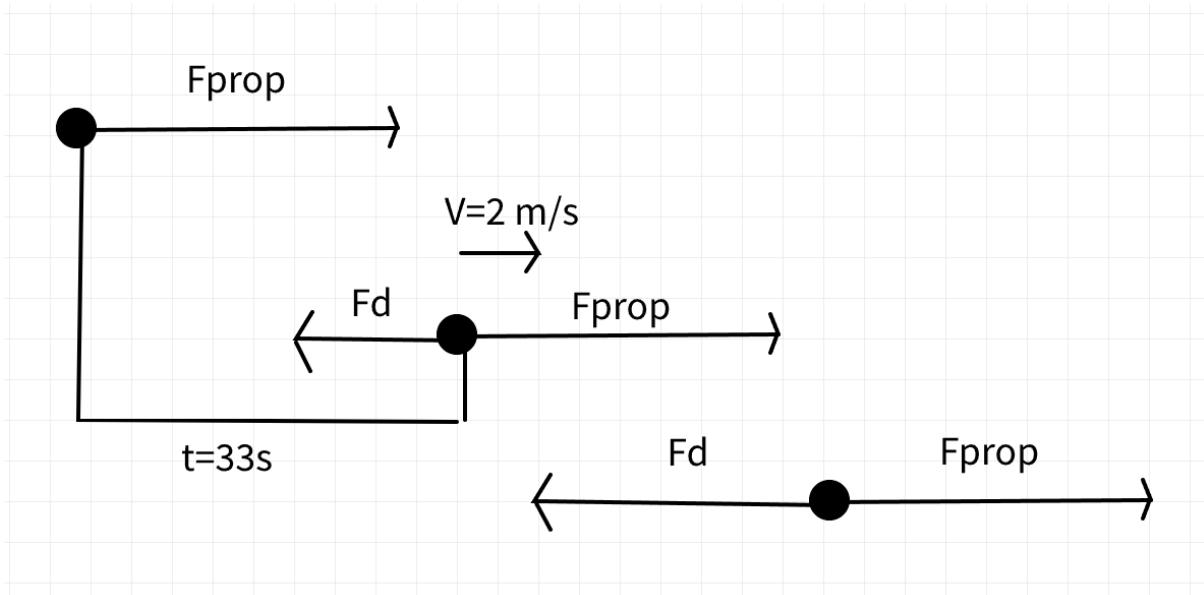
Solution:

<p>Given:</p> <p>$m=0.25 \text{ kg}$</p> <p>$R=0.7 \text{ m}$</p> <p>$T = 30 \text{ N}$</p> <p>$g = 9,8 \text{ m/s}^2$</p>	<p>1st part.</p> <p>We can write forces according to 2nd Newton law.</p> <p>We have 3 forces 1. T - thread tension force; 2. mg; 3. Centripetal force</p> <p>In vector form</p> <p>As our string is not breaking.</p> $T + mg + F_c > 0$
<p>Find:</p> <p>– V?</p>	<p>If we make projection</p> $T + mg(\text{projected somehow}) - F_c > 0$ <p>We can clearly see that T will have maximum value to correspond our equation if mg will be projected as -mg(opposite direction of T force)</p> $T > mg + F_c$ <p>This equation fits to case when object is in the lowest point(As I draw)</p> <p>2nd part</p> <p>Now let's look on case when string break;</p> <p>As we know it will be the first time in the lowest point.</p> <p>It will be broken if</p> <p>Vector form:</p> $T + mg + F_c \leq 0$ <p>With projection:</p> $T - mg - F_c \leq 0;$ <p>It will break if</p> $T - mg - F_c = 0;$ $T - mg - mv^2/R = 0;$ $v^2 = (T - mg) * R/m$ $v = \sqrt{(T - mg) * R/m}$ <p>Answer: $v = 8.8 \text{ m/s}$</p>

Problem 3 (25 pts)

A motorboat of mass $m = 3$ tons starts to move from rest. After 33 seconds, its velocity becomes 2 m/s. The engine force propelling the boat is constant throughout the whole period of the motion. Find the maximum velocity of the boat (m/s, round to 1 decimal place), if the drag force is given by the equation $F_d = -k\vec{v}$. Where \vec{v} denotes the boat velocity and $k = 100$ kg/s.

Solution:

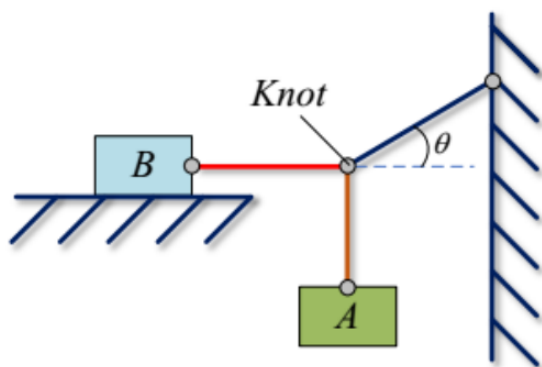


<p>Given:</p> <p>$m = 3 \text{ tons} = 3000\text{kg}$</p> <p>$v_{fin} = 2 \text{ m/s}$</p> <p>$t = 33 \text{ s}$</p> <p>$k = 100 \text{ kg/s}$</p>	<p>Start with 2nd Newton law:</p> $F_{prop} + F_d = ma$ <p>With projection on OX:</p> $F_{prop} - kv = ma$ <p>We know that a is dv/dt</p> $m * dv/dt = F_{prop} - kv$ <p>Divide both sides on $F_{prop} - kv$, m and mul on dt</p> $dv/(F_{prop} - kv) = dt/m;$
<p>Find:</p> <p>$v_{max} - ?$</p>	<p>Change dv; According to rule $f(u)'du = df(u)$</p> $d(F_{prop} - kv)/(F_{prop} - kv) = -k/m * dt$ <p>Integrate 2 parts first velocity from 0..2m/s second time from 0..33 s</p> $\int_0^2 d(F_{prop} - kv)/(F_{prop} - kv) = -k/m * \int_0^{33} dt$ $\ln F_{prop} - k2 - \ln F_{prop} = -k/m * 33$ $\ln (F_{prop} - 2 * k)/F_{prop} = -33k/m$ $(F_{prop} - 2 * k)/F_{prop} = e^{-33k/m}$ $1 - 2 * k/F_{prop} = e^{-33k/m}$ $F_{prop} = 2 * k/(1 - e^{-33k/m})$ <p>Next like in the first task, at some moment we will have acceleration equals to 0 when the speed will be max.</p> <p>2nd Newton law:</p> $F_{prop} - kv = 0$

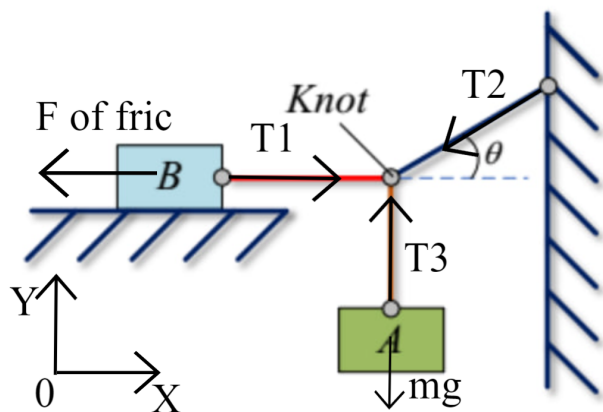
	$2 * k / (1 - e^{-33k/m}) - kv = 0$ $v = 2 / (1 - e^{-33k/m})$ $v = 3.0 \text{ m/s}$ <p>Answer: $v = 3.0 \text{ m/s}$</p>
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Problem 4 (25 pts)

Block B in figure (right) has the mass of 50 kg. The coefficient of static friction between the block and the table is 0.25; an angle θ is 30° ; assume that the cord between B and the knot is horizontal. Find the maximum mass of block A (kg, round to 1 decimal place), for which the system will be stationary. Assume $g = 9.8 \text{ m/s}^2$.



Solution:



<p>Given:</p> $m_b = 50 \text{ kg}$ $\mu = 0.25$ $\theta = 30^\circ$	<p>Write 2nd Newton law according to Knot. 3 Forces. T_1, T_2, mg</p> $T_1 + T_2 + T_3 = ma;$ <p>According to the problem. $a=0$ as system is stationary</p> $T_1 + T_2 + T_3 = 0;$ <p>Write 2nd Newton law according to B</p> $T_1 + \mu N = m_b a;$
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Find:
 m_a -?

The same with $a(a=0)$

$$T_1 + \mu N = 0;$$

Make projection on OX:

$$T_1 = \mu m_b g;$$

Make projection for the Knot on OX:

$$T_1 - T_2 \cos \theta = 0$$

Replace

$$\mu m_b g - T_2 \cos \theta = 0$$

$$\mu m_b g / \cos \theta = T_2$$

Write 2nd Newton law according to A:

$$T_3 + m_a g = m a;$$

The same with $a(a=0)$

$$T_3 + m_a g = 0$$

Make projection for the A on OY

$$T_3 = m_a g$$

Make projection for the Knot on OY:

$$- T_2 \sin \theta + T_3 = 0$$

Replace T3:

$$T_2 \sin \theta / g = m_a$$

Replace:

$$\mu m_b g * \sin \theta / (\cos \theta * g) = m_a$$

$$\mu m_b * \sin \theta / \cos \theta = m_a$$

$$m_a = 7.2 \text{ kg}$$

$$\text{Answer: } m_a = 7.2 \text{ kg}$$