



# Codeforces Round #514 (Div. 2)

## A. Cashier

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

Vasya has recently got a job as a cashier at a local store. His day at work is L minutes long. Vasya has already memorized n regular customers, the i-th of which comes after  $t_i$  minutes after the beginning of the day, and his service consumes  $l_i$  minutes. It is guaranteed that no customer will arrive while Vasya is servicing another customer.

Vasya is a bit lazy, so he likes taking smoke breaks for a minutes each. Those breaks may go one after another, but Vasya must be present at work during all the time periods he must serve regular customers, otherwise one of them may alert his boss. What is the maximum number of breaks Vasya can take during the day?

#### Input

The first line contains three integers n, L and a ( $0 \le n \le 10^5$ ,  $1 \le L \le 10^9$ ,  $1 \le a \le L$ ).

The i-th of the next n lines contains two integers  $t_i$  and  $l_i$  ( $0 \le t_i \le L-1$ ,  $1 \le l_i \le L$ ). It is guaranteed that  $t_i + l_i \le t_{i+1}$  and  $t_n + l_n \le L$ .

## Output

Output one integer  $\,-\,$  the maximum number of breaks.

#### **Examples**

input			
2 11 3 0 1 1 1			
output			
3			

input 0 5 2	
0 5 2	
output	
2	

input
1 3 2 1 2
output

# **Note**

In the first sample Vasya can take 3 breaks starting after 2, 5 and 8 minutes after the beginning of the day.

In the second sample Vasya can take 2 breaks starting after 0 and 2 minutes after the beginning of the day.

In the third sample Vasya can't take any breaks.

# B. Forgery

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

Student Andrey has been skipping physical education lessons for the whole term, and now he must somehow get a passing grade on this subject. Obviously, it is impossible to do this by legal means, but Andrey doesn't give up. Having obtained an empty certificate from a local hospital, he is going to use his knowledge of local doctor's handwriting to make a counterfeit certificate of illness. However, after writing most of the certificate, Andrey suddenly discovered that doctor's signature is impossible to forge. Or is it?

For simplicity, the signature is represented as an  $n \times m$  grid, where every cell is either filled with ink or empty. Andrey's pen can fill a  $3 \times 3$  square without its central cell if it is completely contained inside the grid, as shown below.

XXX X.X XXX

Determine whether is it possible to forge the signature on an empty  $n \times m$  grid.

## Input

The first line of input contains two integers n and m ( $3 \le n, m \le 1000$ ).

Then n lines follow, each contains m characters. Each of the characters is either '.', representing an empty cell, or '#', representing an ink filled cell.

## **Output**

If Andrey can forge the signature, output "YES". Otherwise output "N0".

You can print each letter in any case (upper or lower).

## **Examples**

```
input
3 3
###
#.#
###

output

YES
```

```
input

3 3

###
###

output

NO
```

```
input

4 3
###
###
###
###

output

YES
```

# Note

In the first sample Andrey can paint the border of the square with the center in (2,2).

In the second sample the signature is impossible to forge.

In the third sample Andrey can paint the borders of the squares with the centers in (2,2) and (3,2):

1. we have a clear paper:

...

2. use the pen with center at (2,2).

3. use the pen with center at (3,2).

### ### ###

###

In the fourth sample Andrey can paint the borders of the squares with the centers in (3,3) and (3,5).

# C. Sequence Transformation

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

Let's call the following process a transformation of a sequence of length n.

If the sequence is empty, the process ends. Otherwise, append the greatest common divisor (GCD) of all the elements of the sequence to the result and remove one arbitrary element from the sequence. Thus, when the process ends, we have a sequence of n integers: the greatest common divisors of all the elements in the sequence before each deletion.

You are given an integer sequence  $1, 2, \ldots, n$ . Find the lexicographically maximum result of its transformation.

A sequence  $a_1, a_2, \ldots, a_n$  is lexicographically larger than a sequence  $b_1, b_2, \ldots, b_n$ , if there is an index i such that  $a_j = b_j$  for all j < i, and  $a_i > b_i$ .

#### Input

The first and only line of input contains one integer n ( $1 \le n \le 10^6$ ).

#### Output

Output n integers — the lexicographically maximum result of the transformation.

## **Examples**

input	
3	
output	
1 1 3	

nput	
output	
. 2	

input	
1	
output	
1	

## Note

In the first sample the answer may be achieved this way:

- Append GCD(1,2,3)=1, remove 2.
- Append GCD(1,3) = 1, remove 1.
- Append GCD(3) = 3, remove 3.

We get the sequence [1, 1, 3] as the result.

# D. Nature Reserve

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

There is a forest that we model as a plane and live n rare animals. Animal number i has its lair in the point  $(x_i, y_i)$ . In order to protect them, a decision to build a nature reserve has been made.

The reserve must have a form of a circle containing all lairs. There is also a straight river flowing through the forest. All animals drink from this river, therefore it must have at least one common point with the reserve. On the other hand, ships constantly sail along the river, so the reserve must not have more than one common point with the river.

For convenience, scientists have made a transformation of coordinates so that the river is defined by y=0. Check whether it is possible to build a reserve, and if possible, find the minimum possible radius of such a reserve.

#### Input

The first line contains one integer n ( $1 \le n \le 10^5$ ) — the number of animals.

Each of the next n lines contains two integers  $x_i$ ,  $y_i$  ( $-10^7 \le x_i, y_i \le 10^7$ ) — the coordinates of the i-th animal's lair. It is guaranteed that  $y_i \ne 0$ . No two lairs coincide.

#### **Output**

If the reserve cannot be built, print -1. Otherwise print the minimum radius. Your answer will be accepted if absolute or relative error does not exceed  $10^{-6}$ .

Formally, let your answer be a, and the jury's answer be b. Your answer is considered correct if  $\frac{|a-b|}{\max{(1,|b|)}} \leq 10^{-6}$ .

#### **Examples**

input	
1 0 1	
output 0.5	

```
input

3
0 1
0 2
0 -3

output
-1
```

input		
2 0 1 1 1		
output 0.625		
0.625		

## Note

In the first sample it is optimal to build the reserve with the radius equal to 0.5 and the center in (0, 0.5).

In the second sample it is impossible to build a reserve.

In the third sample it is optimal to build the reserve with the radius equal to  $\frac{5}{8}$  and the center in  $(\frac{1}{2}, \frac{5}{8})$ .

# E. Split the Tree

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

You are given a rooted tree on n vertices, its root is the vertex number 1. The i-th vertex contains a number  $w_i$ . Split it into the minimum possible number of vertical paths in such a way that each path contains no more than L vertices and the sum of integers  $w_i$  on each path does not exceed S. Each vertex should belong to exactly one path.

A vertical path is a sequence of vertices  $v_1, v_2, \ldots, v_k$  where  $v_i$  ( $i \geq 2$ ) is the parent of  $v_{i-1}$ .

#### Input

The first line contains three integers n, L, S ( $1 \le n \le 10^5$ ,  $1 \le L \le 10^5$ ,  $1 \le S \le 10^{18}$ ) — the number of vertices, the maximum number of vertices in one path and the maximum sum in one path.

The second line contains n integers  $w_1, w_2, \ldots, w_n$  ( $1 \le w_i \le 10^9$ ) — the numbers in the vertices of the tree.

The third line contains n-1 integers  $p_2, \ldots, p_n$  ( $1 \le p_i < i$ ), where  $p_i$  is the parent of the i-th vertex in the tree.

### Output

Output one number — the minimum number of vertical paths. If it is impossible to split the tree, output -1.

## **Examples**

input		
3 1 3 1 2 3 1 1		
output		
3		

input	
3 3 6 1 2 3 1 1	
output	
2	

input		
1 1 10000 10001		
output		
-1		

## Note

In the first sample the tree is split into  $\{1\}, \{2\}, \{3\}.$ 

In the second sample the tree is split into  $\{1,\ 2\},\ \{3\}$  or  $\{1,\ 3\},\ \{2\}.$ 

In the third sample it is impossible to split the tree.

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