

## Codeforces Round #628 (Div. 2)

### A. EhAb AnD gCd

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

You are given a positive integer  $x$ . Find **any** such 2 positive integers  $a$  and  $b$  such that  $GCD(a, b) + LCM(a, b) = x$ .

As a reminder,  $GCD(a, b)$  is the greatest integer that divides both  $a$  and  $b$ . Similarly,  $LCM(a, b)$  is the smallest integer such that both  $a$  and  $b$  divide it.

It's guaranteed that the solution always exists. If there are several such pairs  $(a, b)$ , you can output any of them.

#### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 100$ ) — the number of testcases.

Each testcase consists of one line containing a single integer,  $x$  ( $2 \leq x \leq 10^9$ ).

#### Output

For each testcase, output a pair of positive integers  $a$  and  $b$  ( $1 \leq a, b \leq 10^9$ ) such that  $GCD(a, b) + LCM(a, b) = x$ . It's guaranteed that the solution always exists. If there are several such pairs  $(a, b)$ , you can output any of them.

#### Example

input	
2	
2	
14	
output	
1 1	
6 4	

#### Note

In the first testcase of the sample,  $GCD(1, 1) + LCM(1, 1) = 1 + 1 = 2$ .

In the second testcase of the sample,  $GCD(6, 4) + LCM(6, 4) = 2 + 12 = 14$ .

### B. CopyCopyCopyCopyCopy

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

Ehab has an array  $a$  of length  $n$ . He has just enough free time to make a new array consisting of  $n$  copies of the old array, written back-to-back. What will be the length of the new array's longest increasing subsequence?

A sequence  $a$  is a subsequence of an array  $b$  if  $a$  can be obtained from  $b$  by deletion of several (possibly, zero or all) elements. The longest increasing subsequence of an array is the longest subsequence such that its elements are ordered in strictly increasing order.

#### Input

The first line contains an integer  $t$  — the number of test cases you need to solve. The description of the test cases follows.

The first line of each test case contains an integer  $n$  ( $1 \leq n \leq 10^5$ ) — the number of elements in the array  $a$ .

The second line contains  $n$  space-separated integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq 10^9$ ) — the elements of the array  $a$ .

**The sum of  $n$  across the test cases doesn't exceed  $10^5$ .**

#### Output

For each testcase, output the length of the longest increasing subsequence of  $a$  if you concatenate it to itself  $n$  times.

#### Example

input	
2	
3	

3 2 1 6 3 1 4 1 5 9
<b>output</b>
3 5

**Note**

In the first sample, the new array is [3, 2, **1**, 3, **2**, 1, **3**, 2, 1]. The longest increasing subsequence is marked in bold.

In the second sample, the longest increasing subsequence will be [1, 3, 4, 5, 9].

### C. Ehab and Path-etic MEXs

time limit per test: 1 second  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given a tree consisting of  $n$  nodes. You want to write some labels on the tree's edges such that the following conditions hold:

- Every label is an integer between 0 and  $n - 2$  inclusive.
- All the written labels are distinct.
- The largest value among  $MEX(u, v)$  over all pairs of nodes  $(u, v)$  is as small as possible.

Here,  $MEX(u, v)$  denotes the smallest non-negative integer that isn't written on any edge on the unique simple path from node  $u$  to node  $v$ .

#### Input

The first line contains the integer  $n$  ( $2 \leq n \leq 10^5$ ) — the number of nodes in the tree.

Each of the next  $n - 1$  lines contains two space-separated integers  $u$  and  $v$  ( $1 \leq u, v \leq n$ ) that mean there's an edge between nodes  $u$  and  $v$ . It's guaranteed that the given graph is a tree.

#### Output

Output  $n - 1$  integers. The  $i^{th}$  of them will be the number written on the  $i^{th}$  edge (in the input order).

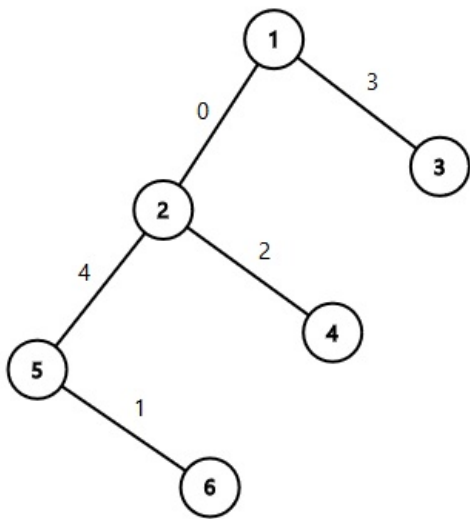
#### Examples

<b>input</b>
3 1 2 1 3
<b>output</b>
0 1

<b>input</b>
6 1 2 1 3 2 4 2 5 5 6
<b>output</b>
0 3 2 4 1

**Note**

The tree from the second sample:



## D. Ehab the Xorcist

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

Given 2 integers  $u$  and  $v$ , find the shortest array such that **bitwise-xor** of its elements is  $u$ , and the sum of its elements is  $v$ .

### Input

The only line contains 2 integers  $u$  and  $v$  ( $0 \leq u, v \leq 10^{18}$ ).

### Output

If there's no array that satisfies the condition, print "-1". Otherwise:

The first line should contain one integer,  $n$ , representing the length of the desired array. The next line should contain  $n$  **positive** integers, the array itself. If there are multiple possible answers, print any.

### Examples

<b>input</b>
2 4
<b>output</b>
2 3 1
<b>input</b>
1 3
<b>output</b>
3 1 1 1
<b>input</b>
8 5
<b>output</b>
-1
<b>input</b>
0 0
<b>output</b>
0

### Note

In the first sample,  $3 \oplus 1 = 2$  and  $3 + 1 = 4$ . There is no valid array of smaller length.

Notice that in the fourth sample the array is empty.

## E. Ehab's REAL Number Theory Problem

time limit per test: 3 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given an array  $a$  of length  $n$  that has a special condition: every element in this array has at most 7 divisors. Find the length of the shortest non-empty subsequence of this array product of whose elements is a perfect square.

A sequence  $a$  is a subsequence of an array  $b$  if  $a$  can be obtained from  $b$  by deletion of several (possibly, zero or all) elements.

### Input

The first line contains an integer  $n$  ( $1 \leq n \leq 10^5$ ) — the length of  $a$ .

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq 10^6$ ) — the elements of the array  $a$ .

### Output

Output the length of the shortest non-empty subsequence of  $a$  product of whose elements is a perfect square. If there are several shortest subsequences, you can find any of them. If there's no such subsequence, print "-1".

### Examples

input
3 1 4 6
output
1
input
4 2 3 6 6
output
2
input
3 6 15 10
output
3
input
4 2 3 5 7
output
-1

### Note

In the first sample, you can choose a subsequence  $[1]$ .

In the second sample, you can choose a subsequence  $[6, 6]$ .

In the third sample, you can choose a subsequence  $[6, 15, 10]$ .

In the fourth sample, there is no such subsequence.

## F. Ehab's Last Theorem

time limit per test: 1 second  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

It's the year 5555. You have a graph, and you want to find a long cycle and a huge independent set, just because you can. But for now, let's just stick with finding either.

Given a connected graph with  $n$  vertices, you can choose to either:

- find an independent set that has **exactly**  $\lceil \sqrt{n} \rceil$  vertices.
- find a **simple** cycle of length **at least**  $\lceil \sqrt{n} \rceil$ .

An independent set is a set of vertices such that no two of them are connected by an edge. A simple cycle is a cycle that doesn't contain any vertex twice. I have a proof you can always solve one of these problems, but it's too long to fit this margin.

### Input

The first line contains two integers  $n$  and  $m$  ( $5 \leq n \leq 10^5, n - 1 \leq m \leq 2 \cdot 10^5$ ) — the number of vertices and edges in the graph.

Each of the next  $m$  lines contains two space-separated integers  $u$  and  $v$  ( $1 \leq u, v \leq n$ ) that mean there's an edge between vertices  $u$  and  $v$ . It's guaranteed that the graph is connected and doesn't contain any self-loops or multiple edges.

**Output**

If you choose to solve the first problem, then on the first line print "1", followed by a line containing  $\lceil \sqrt{n} \rceil$  distinct integers not exceeding  $n$ , the vertices in the desired independent set.

If you, however, choose to solve the second problem, then on the first line print "2", followed by a line containing one integer,  $c$ , representing the length of the found cycle, followed by a line containing  $c$  distinct integers not exceeding  $n$ , the vertices in the desired cycle, **in the order they appear in the cycle**.

**Examples**

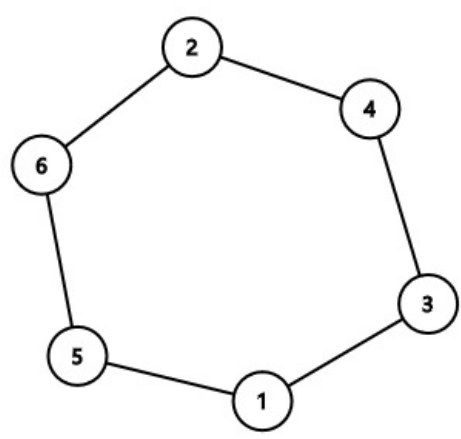
input
6 6 1 3 3 4 4 2 2 6 5 6 5 1
output
1 1 6 4

input
6 8 1 3 3 4 4 2 2 6 5 6 5 1 1 4 2 5
output
2 4 1 5 2 4

input
5 4 1 2 1 3 2 4 2 5
output
1 3 4 5

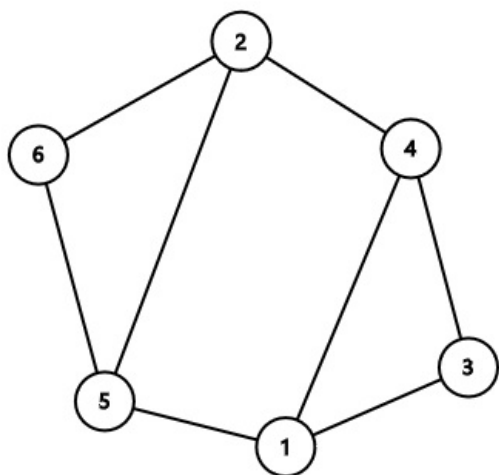
**Note**

In the first sample:



Notice that you can solve either problem, so printing the cycle  $2 - 4 - 3 - 1 - 5 - 6$  is also acceptable.

In the second sample:



Notice that if there are multiple answers you can print any, so printing the cycle  $2 - 5 - 6$ , for example, is acceptable.

In the third sample:

