

## Codeforces Round #642 (Div. 3)

### A. Most Unstable Array

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

You are given two integers  $n$  and  $m$ . You have to construct the array  $a$  of length  $n$  consisting of **non-negative integers** (i.e. integers greater than or equal to zero) such that the sum of elements of this array is **exactly**  $m$  and the value  $\sum_{i=1}^{n-1} |a_i - a_{i+1}|$  is the maximum possible. Recall that  $|x|$  is the absolute value of  $x$ .

In other words, you have to maximize the sum of absolute differences between adjacent (consecutive) elements. For example, if the array  $a = [1, 3, 2, 5, 5, 0]$  then the value above for this array is  $|1 - 3| + |3 - 2| + |2 - 5| + |5 - 5| + |5 - 0| = 2 + 1 + 3 + 0 + 5 = 11$ . Note that this example **doesn't show the optimal answer** but it shows how the required value for some array is calculated.

You have to answer  $t$  independent test cases.

#### Input

The first line of the input contains one integer  $t$  ( $1 \leq t \leq 10^4$ ) — the number of test cases. Then  $t$  test cases follow.

The only line of the test case contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 10^9$ ) — the length of the array and its sum correspondingly.

#### Output

For each test case, print the answer — the maximum possible value of  $\sum_{i=1}^{n-1} |a_i - a_{i+1}|$  for the array  $a$  consisting of  $n$  non-negative integers with the sum  $m$ .

#### Example

input
5 1 100 2 2 5 5 2 1000000000 1000000000 1000000000
output
0 2 10 1000000000 2000000000

#### Note

In the first test case of the example, the only possible array is  $[100]$  and the answer is obviously 0.

In the second test case of the example, one of the possible arrays is  $[2, 0]$  and the answer is  $|2 - 0| = 2$ .

In the third test case of the example, one of the possible arrays is  $[0, 2, 0, 3, 0]$  and the answer is  $|0 - 2| + |2 - 0| + |0 - 3| + |3 - 0| = 10$ .

### B. Two Arrays And Swaps

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

You are given two arrays  $a$  and  $b$  both consisting of  $n$  positive (greater than zero) integers. You are also given an integer  $k$ .

In one move, you can choose two indices  $i$  and  $j$  ( $1 \leq i, j \leq n$ ) and swap  $a_i$  and  $b_j$  (i.e.  $a_i$  becomes  $b_j$  and vice versa). Note that  $i$  and  $j$  can be equal or different (in particular, swap  $a_2$  with  $b_2$  or swap  $a_3$  and  $b_9$  both are acceptable moves).

Your task is to find the **maximum** possible sum you can obtain in the array  $a$  if you can do no more than (i.e. at most)  $k$  such moves (swaps).

You have to answer  $t$  independent test cases.

Input

The first line of the input contains one integer  $t$  ( $1 \leq t \leq 200$ ) — the number of test cases. Then  $t$  test cases follow.

The first line of the test case contains two integers  $n$  and  $k$  ( $1 \leq n \leq 30; 0 \leq k \leq n$ ) — the number of elements in  $a$  and  $b$  and the maximum number of moves you can do. The second line of the test case contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq 30$ ), where  $a_i$  is the  $i$ -th element of  $a$ . The third line of the test case contains  $n$  integers  $b_1, b_2, \dots, b_n$  ( $1 \leq b_i \leq 30$ ), where  $b_i$  is the  $i$ -th element of  $b$ .

Output

For each test case, print the answer — the **maximum** possible sum you can obtain in the array  $a$  if you can do no more than (i.e. at most)  $k$  swaps.

Example

input
5 2 1 1 2 3 4 5 5 5 5 6 6 5 1 2 5 4 3 5 3 1 2 3 4 5 10 9 10 10 9 4 0 2 2 4 3 2 4 2 3 4 4 1 2 2 1 4 4 5 4
output
6 27 39 11 17

Note

In the first test case of the example, you can swap  $a_1 = 1$  and  $b_2 = 4$ , so  $a = [4, 2]$  and  $b = [3, 1]$ .

In the second test case of the example, you don't need to swap anything.

In the third test case of the example, you can swap  $a_1 = 1$  and  $b_1 = 10$ ,  $a_3 = 3$  and  $b_3 = 10$  and  $a_2 = 2$  and  $b_4 = 10$ , so  $a = [10, 10, 10, 4, 5]$  and  $b = [1, 9, 3, 2, 9]$ .

In the fourth test case of the example, you cannot swap anything.

In the fifth test case of the example, you can swap arrays  $a$  and  $b$ , so  $a = [4, 4, 5, 4]$  and  $b = [1, 2, 2, 1]$ .

C. Board Moves

time limit per test: 1 second  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given a board of size  $n \times n$ , where  $n$  is **odd** (not divisible by 2). Initially, each cell of the board contains one figure.

In one move, you can select **exactly one figure** presented in some cell and move it to one of the cells **sharing a side or a corner with the current cell**, i.e. from the cell  $(i, j)$  you can move the figure to cells:

- $(i - 1, j - 1);$
- $(i - 1, j);$
- $(i - 1, j + 1);$
- $(i, j - 1);$
- $(i, j + 1);$
- $(i + 1, j - 1);$
- $(i + 1, j);$
- $(i + 1, j + 1);$

Of course, you **can not** move figures to cells out of the board. It is allowed that after a move there will be several figures in one cell.

Your task is to find the minimum number of moves needed to get **all the figures** into **one** cell (i.e.  $n^2 - 1$  cells should contain 0 figures and one cell should contain  $n^2$  figures).

You have to answer  $t$  independent test cases.

Input

The first line of the input contains one integer  $t$  ( $1 \leq t \leq 200$ ) — the number of test cases. Then  $t$  test cases follow.

The only line of the test case contains one integer  $n$  ( $1 \leq n < 5 \cdot 10^5$ ) — the size of the board. It is guaranteed that  $n$  is odd (not divisible by 2).

It is guaranteed that the sum of  $n$  over all test cases does not exceed  $5 \cdot 10^5$  ( $\sum n \leq 5 \cdot 10^5$ ).

Output

For each test case print the answer — the minimum number of moves needed to get **all the figures** into **one** cell.

Example

input
3 1 5 499993
output
0 40 41664916690999888

D. Constructing the Array

time limit per test: 1 second  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given an array  $a$  of length  $n$  consisting of zeros. You perform  $n$  actions with this array: during the  $i$ -th action, the following sequence of operations appears:

1. Choose the maximum by length subarray (**continuous subsegment**) consisting **only** of zeros, among all such segments choose the **leftmost** one;
2. Let this segment be  $[l; r]$ . If  $r - l + 1$  is odd (not divisible by 2) then assign (set)  $a[\frac{l+r}{2}] := i$  (where  $i$  is the number of the current action), otherwise (if  $r - l + 1$  is even) assign (set)  $a[\frac{l+r-1}{2}] := i$ .

Consider the array  $a$  of length 5 (initially  $a = [0, 0, 0, 0, 0]$ ). Then it changes as follows:

1. Firstly, we choose the segment  $[1; 5]$  and assign  $a[3] := 1$ , so  $a$  becomes  $[0, 0, 1, 0, 0]$ ;
2. then we choose the segment  $[1; 2]$  and assign  $a[1] := 2$ , so  $a$  becomes  $[2, 0, 1, 0, 0]$ ;
3. then we choose the segment  $[4; 5]$  and assign  $a[4] := 3$ , so  $a$  becomes  $[2, 0, 1, 3, 0]$ ;
4. then we choose the segment  $[2; 2]$  and assign  $a[2] := 4$ , so  $a$  becomes  $[2, 4, 1, 3, 0]$ ;
5. and at last we choose the segment  $[5; 5]$  and assign  $a[5] := 5$ , so  $a$  becomes  $[2, 4, 1, 3, 5]$ .

Your task is to find the array  $a$  of length  $n$  after performing all  $n$  actions. **Note that the answer exists and unique.**

You have to answer  $t$  independent test cases.

Input

The first line of the input contains one integer  $t$  ( $1 \leq t \leq 10^4$ ) — the number of test cases. Then  $t$  test cases follow.

The only line of the test case contains one integer  $n$  ( $1 \leq n \leq 2 \cdot 10^5$ ) — the length of  $a$ .

It is guaranteed that the sum of  $n$  over all test cases does not exceed  $2 \cdot 10^5$  ( $\sum n \leq 2 \cdot 10^5$ ).

Output

For each test case, print the answer — the array  $a$  of length  $n$  after performing  $n$  actions described in the problem statement. **Note that the answer exists and unique.**

Example

input
6 1 2 3 4 5 6
output
1 1 2 2 1 3 3 1 2 4 2 4 1 3 5

## E. K-periodic Garland

time limit per test: 1 second  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given a garland consisting of  $n$  lamps. States of the lamps are represented by the string  $s$  of length  $n$ . The  $i$ -th character of the string  $s_i$  equals '0' if the  $i$ -th lamp is turned off or '1' if the  $i$ -th lamp is turned on. You are also given a positive integer  $k$ .

In one move, you can choose **one lamp** and change its state (i.e. turn it on if it is turned off and vice versa).

The garland is called  $k$ -periodic if the distance between **each pair of adjacent turned on lamps** is **exactly**  $k$ . Consider the case  $k = 3$ . Then garlands "00010010", "1001001", "00010" and "0" are good but garlands "00101001", "1000001" and "01001100" are not. Note that **the garland is not cyclic**, i.e. the first turned on lamp is not going after the last turned on lamp and vice versa.

Your task is to find the **minimum** number of moves you need to make to obtain  $k$ -periodic garland from the given one.

You have to answer  $t$  independent test cases.

### Input

The first line of the input contains one integer  $t$  ( $1 \leq t \leq 25\,000$ ) — the number of test cases. Then  $t$  test cases follow.

The first line of the test case contains two integers  $n$  and  $k$  ( $1 \leq n \leq 10^6$ ;  $1 \leq k \leq n$ ) — the length of  $s$  and the required period. The second line of the test case contains the string  $s$  consisting of  $n$  characters '0' and '1'.

It is guaranteed that the sum of  $n$  over all test cases does not exceed  $10^6$  ( $\sum n \leq 10^6$ ).

### Output

For each test case, print the answer — the **minimum** number of moves you need to make to obtain  $k$ -periodic garland from the given one.

### Example

input
6 9 2 010001010 9 3 111100000 7 4 1111111 10 3 1001110101 1 1 1 1 1 0
output
1 2 5 4 0 0

## F. Decreasing Heights

time limit per test: 2.5 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are playing one famous sandbox game with the three-dimensional world. The map of the world can be represented as a matrix of size  $n \times m$ , where the height of the cell  $(i, j)$  is  $a_{i,j}$ .

You are in the cell  $(1, 1)$  right now and want to get in the cell  $(n, m)$ . You can move only down (from the cell  $(i, j)$  to the cell  $(i + 1, j)$ ) or right (from the cell  $(i, j)$  to the cell  $(i, j + 1)$ ). There is an additional **restriction**: if the height of the current cell is  $x$  then you can move only to the cell with height  $x + 1$ .

**Before the first move** you can perform several operations. During one operation, you can decrease the height of **any** cell by one. I.e. you choose some cell  $(i, j)$  and assign (set)  $a_{i,j} := a_{i,j} - 1$ . Note that you **can** make heights **less than or equal to zero**. Also note that you **can** decrease the height of the cell  $(1, 1)$ .

Your task is to find the **minimum** number of operations you have to perform to obtain at least one suitable path from the cell  $(1, 1)$  to the cell  $(n, m)$ . It is guaranteed that the answer exists.

You have to answer  $t$  independent test cases.

**Input**

The first line of the input contains one integer  $t$  ( $1 \leq t \leq 100$ ) — the number of test cases. Then  $t$  test cases follow.

The first line of the test case contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 100$ ) — the number of rows and the number of columns in the map of the world. The next  $n$  lines contain  $m$  integers each, where the  $j$ -th integer in the  $i$ -th line is  $a_{i,j}$  ( $1 \leq a_{i,j} \leq 10^{15}$ ) — the height of the cell  $(i, j)$ .

It is guaranteed that the sum of  $n$  (as well as the sum of  $m$ ) over all test cases does not exceed 100 ( $\sum n \leq 100; \sum m \leq 100$ ).

**Output**

For each test case, print the answer — the **minimum** number of operations you have to perform to obtain at least one suitable path from the cell  $(1, 1)$  to the cell  $(n, m)$ . It is guaranteed that the answer exists.

**Example**

input
5 3 4 1 2 3 4 5 6 7 8 9 10 11 12 5 5 2 5 4 8 3 9 10 11 5 1 12 8 4 2 5 2 2 5 4 1 6 8 2 4 2 2 2 100 10 10 1 1 2 123456789876543 987654321234567 1 1 42
output
9 49 111 864197531358023 0