



#### **Kotlin Heroes 5: ICPC Round**

# A. Selling Hamburgers

time limit per test: 2 seconds memory limit per test: 512 megabytes input: standard input output: standard output

There are n customers in the cafeteria. Each of them wants to buy a hamburger. The i-th customer has  $a_i$  coins, and they will buy a hamburger if it costs at most  $a_i$  coins.

Suppose the cost of the hamburger is m. Then the number of coins the cafeteria earns is m multiplied by the number of people who buy a hamburger if it costs m. Your task is to calculate the maximum number of coins the cafeteria can earn.

#### Input

The first line contains one integer t ( $1 \le t \le 100$ ) — the number of test cases.

Each test case consists of two lines. The first line contains one integer n ( $1 \le n \le 100$ ) — the number of customers.

The second line contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_i \le 10^{12}$ ), where  $a_i$  is the number of coins the i-th customer has.

#### **Output**

For each test case, print one integer — the maximum number of coins the cafeteria can earn.

#### **Example**

#### Note

Explanations for the test cases of the example:

- 1. the best price for the hamburger is m=1, so 3 hamburgers are bought, and the cafeteria earns 3 coins;
- 2. the best price for the hamburger is m=4, so 1 hamburger is bought, and the cafeteria earns 4 coins;
- 3. the best price for the hamburger is m=2, so 3 hamburgers are bought, and the cafeteria earns 6 coins;
- 4. the best price for the hamburger is m=4, so 5 hamburgers are bought, and the cafeteria earns 20 coins;
- 5. the best price for the hamburger is  $m=10^{12}$ , so 1 hamburger is bought, and the cafeteria earns  $10^{12}$  coins;
- 6. the best price for the hamburger is  $m=10^{12}-1$ , so 2 hamburgers are bought, and the cafeteria earns  $2\cdot 10^{12}-2$  coins.

## B. Polycarp and the Language of Gods

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

Polycarp has just finished writing down the lecture on elvish languages. The language this week was "VwV" (pronounced as "uwu"). The writing system of this language consists of only two lowercase Latin letters: 'v' and 'w'.

Unfortunately, Polycarp has written all the lecture in cursive and without any spaces, so the notes look like a neverending sequence of squiggles. To be exact, Polycarp can't tell 'w' apart from 'vv' in his notes as both of them consist of the same two squiggles.

Luckily, his brother Monocarp has better writing habits, so Polycarp managed to take his notes and now wants to make his own

notes more readable. To do that he can follow the notes of Monocarp and underline some letters in his own notes in such a way that there is no more ambiguity. If he underlines a 'v', then it can't be mistaken for a part of some 'w', and if the underlines a 'w', then it can't be mistaken for two adjacent letters 'v'.

What is the minimum number of letters Polycarp should underline to make his notes unambiguous?

#### Input

The first line contains a single integer t ( $1 \le t \le 100$ ) — the number of testcases.

Each of the next t lines contains a non-empty string in VwV language, which consists only of lowercase Latin letters 'v' and 'w'. The length of the string does not exceed 100.

## **Output**

For each testcase print a single integer: the minimum number of letters Polycarp should underline so that there is no ambiguity in his notes.

#### **Example**

| input    |  |
|----------|--|
| 5        |  |
| vv       |  |
| v        |  |
| W        |  |
| vwv      |  |
| vwvvwv   |  |
| output   |  |
| 1        |  |
| <b>0</b> |  |
| 1        |  |
| 1        |  |
| 3        |  |

#### Note

In the first testcase it's enough to underline any of the two letters 'v'.

In the second testcase the letter 'v' is not ambiguous by itself already, so you don't have to underline anything.

In the third testcase you have to underline 'w', so that you don't mix it up with two letters 'v'.

In the fourth testcase you can underline 'w' to avoid all the ambiguity.

In the fifth testcase you can underline both letters 'w' and any of the two letters 'v' between them.

# C. Black Friday

time limit per test: 2 seconds memory limit per test: 256 megabytes input: standard input output: standard output

There is a local shop in your area getting prepared for the great holiday of Black Friday. There are n items with prices  $p_1, p_2, \ldots, p_n$  on the display. They are ordered by price, so  $p_1 \leq p_2 \leq \cdots \leq p_n$ .

The shop has a prechosen discount value k. The Black Friday discount is applied in the following way: for a single purchase of x items, you get the cheapest  $\lfloor \frac{x}{k} \rfloor$  items of them for free ( $\lfloor \frac{x}{k} \rfloor$  is x divided by k rounded down to the nearest integer). You can include each item in your purchase no more than once.

For example, if there are items with prices [1,1,2,2,2,3,4,5,6] in the shop, and you buy items with prices [1,2,2,4,5], and k=2, then you get the cheapest  $\lfloor \frac{5}{2} \rfloor = 2$  for free. They are items with prices 1 and 2.

So you, being the naive customer, don't care about how much money you spend. However, you want the total price of the items you get for free to be as large as possible.

What is the maximum total price of the items you can get for free on a single purchase?

#### Input

The first line contains a single integer t (1  $\leq t \leq$  500) — the number of testcases.

Then the description of t testcases follows.

The first line of each testcase contains two integers n and k ( $1 \le n \le 200$ ;  $1 \le k \le n$ ) — the number of items in the shop and the discount value, respectively.

The second line of each testcase contains n integers  $p_1, p_2, \ldots, p_n$  ( $1 \le p_i \le 10^6$ ) — the prices of the items on the display of the shop. The items are ordered by their price, so  $p_1 \le p_2 \le \cdots \le p_n$ .

#### Output

Print a single integer for each testcase: the maximum total price of the items you can get for free on a single purchase.

## Example

| Example               |  |
|-----------------------|--|
| input                 |  |
| 5<br>5 2<br>1 3 4 6 7 |  |
| 5 2                   |  |
| 1 3 4 6 7             |  |
| 6 3                   |  |
| 1 2 3 4 5 6           |  |
| 6 3                   |  |
| 3 3 4 4 5 5           |  |
| 1 1                   |  |
| 1 1 7                 |  |
| 4 4                   |  |
| 4 4<br>1 3 3 7        |  |
| output                |  |
| 7                     |  |
| 4                     |  |
| 6                     |  |
| 7                     |  |
| 1                     |  |
| T -                   |  |

## D. Used Markers

time limit per test: 3 seconds memory limit per test: 256 megabytes input: standard input output: standard output

Your University has a large auditorium and today you are on duty there. There will be n lectures today — all from different lecturers, and your current task is to choose in which order ord they will happen.

Each lecturer will use one marker to write something on a board during their lecture. Unfortunately, markers become worse the more you use them and lecturers may decline using markers which became too bad in their opinion.

Formally, the i-th lecturer has their acceptance value  $a_i$  which means they will not use the marker that was used at least in  $a_i$  lectures already and will ask for a replacement. More specifically:

- before the first lecture you place a new marker in the auditorium;
- before the  $ord_j$ -th lecturer (in the order you've chosen) starts, they check the quality of the marker and if it was used in at least  $a_{ord_j}$  lectures before, they will ask you for a new marker;
- if you were asked for a new marker, then you throw away the old one, place a new one in the auditorium, and the lecturer gives a lecture.

You know: the better the marker — the easier for an audience to understand what a lecturer has written, so you want to **maximize the number of used markers**. Unfortunately, the higher-ups watch closely how many markers were spent, so you can't just replace markers before each lecture. So, you have to replace markers only when you are asked by a lecturer. The marker is considered used if at least one lecturer used it for their lecture.

You can choose the order ord in which lecturers will give lectures. Find such order that leads to the maximum possible number of the used markers.

## Input

The first line contains one integer t ( $1 \le t \le 100$ ) — the number of independent tests.

The first line of each test case contains one integer n ( $1 \le n \le 500$ ) — the number of lectures and lecturers.

The second line of each test case contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_i \le n$ ) — acceptance values of each lecturer.

## Output

For each test case, print n integers — the order ord of lecturers which maximizes the number of used markers. The lecturers are numbered from 1 to n in the order of the input. If there are multiple answers, print any of them.

# Example

4321

# input 4 4 1 2 1 2 2 2 1 3 1 1 1 4 2 3 1 3 output 4 1 3 2 1 2 3 1 2

#### Note

In the first test case, one of the optimal orders is the following:

- 1. the 4-th lecturer comes first. The marker is new, so they don't ask for a replacement;
- 2. the 1-st lecturer comes next. The marker is used once and since  $a_1 = 1$  the lecturer asks for a replacement;
- 3. the 3-rd lecturer comes next. The second marker is used once and since  $a_3=1$  the lecturer asks for a replacement;
- 4. the 2-nd lecturer comes last. The third marker is used once but  $a_2=2$  so the lecturer uses this marker.

In total, 3 markers are used.

In the second test case, 2 markers are used.

In the third test case, 3 markers are used.

In the fourth test case, 3 markers are used.

## E. Chess Match

time limit per test: 2 seconds memory limit per test: 512 megabytes input: standard input output: standard output

The final of Berland Chess Team Championship is going to be held soon. Two teams consisting of n chess players each will compete for first place in the tournament. The skill of the i-th player in the first team is  $a_i$ , and the skill of the i-th player in the second team is  $b_i$ . The match will be held as follows: each player of the first team will play a game against one player from the second team in such a way that every player has exactly one opponent. Formally, if the player i from the first team opposes the player  $p_i$  from the second team, then  $[p_1, p_2, \ldots, p_n]$  is a permutation (a sequence where each integer from i to i0 appears exactly once).

Whenever two players of almost equal skill play a game, it will likely result in a tie. Chess fans don't like ties, so the organizers of the match should distribute the players in such a way that ties are unlikely.

Let the unfairness of the match be the following value:  $\min_{i=1}^{n} |a_i - b_{p_i}|$ . Your task is to assign each player from the first team an opponent from the second team so that the unfairness is maximum possible (the greater it is, the smaller the probability of ties is, that's why you should maximize it).

#### Input

The first line contains one integer t (1  $\leq t \leq 3000$ ) — the number of test cases.

Each test case consists of three lines. The first line contains one integer n ( $1 \le n \le 3000$ ) — the number of players in each team.

The second line contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_1 \le a_2 \le \cdots \le a_n \le 10^6$ ) — the skills of players of the first team.

The third line contains n integers  $b_1, b_2, \ldots, b_n$  ( $1 \le b_1 \le b_2 \le \cdots \le b_n \le 10^6$ ) — the skills of players of the second team.

It is guaranteed that the sum of n over all test cases does not exceed 3000.

## Output

For each test case, output the answer as follows:

Print n integers  $p_1, p_2, \ldots, p_n$  on a separate line. All integers from 1 to n should occur among them exactly once. The value of  $\min_{i=1}^n |a_i - b_{p_i}|$  should be maximum possible. If there are multiple answers, print any of them.

## Example

2 1 5 4 2 3 1

```
input

4
4
1 2 3 4
1 2 3 4
2
1 1 100
100 101
2
1 1 100
50 51
5
1 1 1 1 1
3 3 3 3 3

output

3 4 1 2
1 2
```

memory limit per test: 256 megabytes input: standard input output: standard output

You want to train a neural network model for your graduation work. There are n images in the dataset, the i-th image's size is  $a_i$  bytes.

You don't have any powerful remote servers to train this model so you have to do it on your local machine. But there is a problem: the total size of the dataset is too big for your machine, so you decided to remove some images — though you don't want to make the dataset too weak so you can remove **no more than** k images from it. Note that you can only remove images, you **can't change their order**.

You want to remove these images optimally so you came up with a metric (you're a data scientist after all) that allows to measure the result of removals. Consider the array  $b_1, b_2, \ldots, b_m$  after removing at most k images  $(n-k \le m \le n)$ . The data from this array will be uploaded to the machine in blocks of x **consecutive** elements each. More precisely:

- elements with indices from 1 to x ( $b_1, b_2, \ldots, b_x$ ) belong to the first block;
- elements with indices from x+1 to 2x  $(b_{x+1},b_{x+2},\ldots,b_{2x})$  belong to the second block;
- elements with indices from 2x+1 to 3x ( $b_{2x+1},b_{2x+2},\ldots,b_{3x}$ ) belong to the third block;
- and so on

There will be  $cnt = \lceil \frac{m}{x} \rceil$  blocks in total. Note that if m is not divisible by x then the last block contains less than x elements, and it's okay.

Let w(i) be the total size of the i-th block — that is, the sum of sizes of images inside this block. For example, the size of the first block w(1) is  $b_1+b_2+\ldots+b_x$ , the size of the second block w(2) is  $b_{x+1}+b_{x+2}+\ldots+b_{2x}$ .

The value of the metric you came up with is the **maximum** block size over the blocks of the resulting dataset. In other words, the value of the metric is  $\max_{i=1}^{cnt} w(i)$ .

You don't want to overload your machine too much, so you have to remove at most k images in a way that **minimizes** the value of the metric described above.

#### Input

The first line of the input contains three integers n, k and x ( $1 \le n \le 10^5$ ;  $1 \le k, x \le n$ ) — the number of images in the dataset, the maximum number of images you can remove and the length of each block (except maybe for the last one), respectively.

The second line of the input contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_i \le 10^5$ ), where  $a_i$  is the size of the i-th image.

#### **Output**

Print one integer: the minimum possible value of the metric described in the problem statement after removing no more than k images from the dataset.

#### **Examples**

| input                            |  |
|----------------------------------|--|
| <pre>input 5 5 4 1 1 5 4 5</pre> |  |
| output                           |  |
| 0                                |  |

| input                        |  |
|------------------------------|--|
| <b>input</b> 5 2 4 6 1 5 5 6 |  |
| output                       |  |
| 11                           |  |

| nput        |  |
|-------------|--|
| 14<br>31312 |  |
| output      |  |
|             |  |

| input                |  |
|----------------------|--|
| 6 1 3<br>2 2 1 2 2 1 |  |
| output               |  |
|                      |  |

#### Note

In the first example, you can remove the whole array so the answer is 0.

In the second example, you can remove the first and the last elements of a and obtain b = [1, 5, 5]. The size of the first (and the only) block is 11. So the answer is 11.

In the third example, you can remove the second element of a and obtain b = [3, 1, 3, 1, 2]. The size of the first block is 8 and the size of the second block is 2. So the answer is 8.

In the fourth example, you can keep the array a unchanged and obtain b = [2, 2, 1, 2, 2, 1]. The size of the first block is 5 as well as the size of the second block. So the answer is 5.

## G. Number Deletion Game

time limit per test: 2 seconds memory limit per test: 512 megabytes input: standard input output: standard output

Alice and Bob play a game. They have a set that initially consists of n integers. The game is played in k turns. During each turn, the following events happen:

- 1. firstly, Alice chooses an integer from the set. She can choose any integer **except for the maximum one**. Let the integer chosen by Alice be *a*;
- 2. secondly, Bob chooses an integer from the set. He can choose any integer **that is greater than** a. Let the integer chosen by Bob be b;
- 3. finally, both a and b are erased from the set, and the value of b-a is added to the score of the game.

Initially, the score is 0. Alice wants to maximize the resulting score, Bob wants to minimize it. Assuming that both Alice and Bob play optimally, calculate the resulting score of the game.

#### Input

The first line contains two integers n and k ( $2 \le n \le 400$ ,  $1 \le k \le \lfloor \frac{n}{2} \rfloor$ ) — the initial size of the set and the number of turns in the game.

The second line contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_i \le 10^6$ ) — the initial contents of the set. These integers are pairwise distinct.

#### **Output**

Print one integer — the resulting score of the game (assuming that both Alice and Bob play optimally).

## **Examples**

| input            |  |
|------------------|--|
| 5 2<br>3 4 1 5 2 |  |
| output           |  |
| 4                |  |

## input

101 108 200 1 201 109 100

output

283

# H. Rogue-like Game

time limit per test: 4 seconds memory limit per test: 256 megabytes input: standard input output: standard output

Marina plays a new rogue-like game. In this game, there are n different character species and m different classes. The game is played in runs; for each run, Marina has to select a species and a class for her character. If she selects the i-th species and the j-th class, she will get  $c_{i,j}$  points for this run.

Initially, some species and classes are unlocked, all others are locked. To unlock the i-th species, Marina has to get at least  $a_i$  points in total for previous runs — that is, as soon as her total score for played runs is at least  $a_i$ , this species is unlocked. Similarly, to unlock the j-th class, she has to get at least  $b_j$  points in total for previous runs. If  $a_i=0$  for some i, then this species is unlocked initially (the same applies to classes with  $b_j=0$ ).

Marina wants to unlock all species and classes in the minimum number of runs. Before playing the game, she can read **exactly one guide** on some combination of species and class, and reading a guide will increase the score she gets for **all runs with that combination** by k (formally, before playing the game, she can increase **exactly one** value of  $c_{i,j}$  by k).

What is the minimum number of runs she has to play to unlock all species and classes if she chooses the combination to read a

guide on optimally?

## Input

The first line contains three integers n, m and k ( $1 \le n, m \le 1500$ ;  $0 \le k \le 10^9$ ).

The second line contains n integers  $a_1$ ,  $a_2$ , ...,  $a_n$  ( $0 = a_1 \le a_2 \le \cdots \le a_n \le 10^{12}$ ), where  $a_i$  is the number of points required to unlock the i-th species (or 0, if it is unlocked initially). **Note that**  $a_1 = 0$ , **and these values are non-descending**.

The third line contains m integers  $b_1$ ,  $b_2$ , ...,  $b_m$  ( $0=b_1\leq b_2\leq \cdots \leq b_m\leq 10^{12}$ ), where  $b_i$  is the number of points required to unlock the i-th class (or 0, if it is unlocked initially). **Note that**  $b_1=0$ , **and these values are non-descending**.

Then n lines follow, each of them contains m integers. The j-th integer in the i-th line is  $c_{i,j}$  ( $1 \le c_{i,j} \le 10^9$ ) — the score Marina gets for a run with the i-th species and the j-th class.

#### **Output**

Print one integer — the minimum number of runs Marina has to play to unlock all species and all classes if she can read exactly one guide before playing the game.

## **Examples**

```
input

3 4 2
0 5 7
0 2 6 10
2 5 5 2
5 3 4 4
3 4 2 4

output

3
```

```
input

4 2 1
0 3 9 9
0 2
3 3
5 1
1 3
2 3

output
2
```

```
input

3 3 5
0 8 11
0 0 3
3 1 3
1 2 1
1 1 3

output

2
```

### Note

The explanation for the first test:

- 1. Marina reads a guide on the combination of the 1-st species and the 2-nd class. Thus,  $c_{1,2}$  becomes 7. Initially, only the 1-st species and the 1-st class are unlocked.
- 2. Marina plays a run with the 1-st species and the 1-st class. Her score becomes 2, and she unlocks the 2-nd class.
- 3. Marina plays a run with the 1-st species and the 2-nd class. Her score becomes 9, and she unlocks everything except the 4-th class
- 4. Marina plays a run with the 3-rd species and the 3-rd class. Her score becomes 11, and she unlocks the 4-th class. She has unlocked everything in 3 runs.

Note that this way to unlock everything is not the only one.

The explanation for the second test:

- 1. Marina reads a guide on the combination of the 2-nd species and the 1-st class. Thus,  $c_{2,1}$  becomes 6. Initially, only the 1-st species and the 1-st class are unlocked.
- 2. Marina plays a run with the 1-st species and the 1-st class. Her score becomes 3, and she unlocks the 2-nd species and the 2-nd class.
- 3. Marina plays a run with the 2-nd species and the 1-st class. Her score becomes 9, and she unlocks the 3-rd species and the 4-th species. She has unlocked everything in 2 runs.

As in the 1-st example, this is not the only way to unlock everything in 2 runs.

# I. Cyclic Shifts

time limit per test: 3 seconds memory limit per test: 512 megabytes input: standard input output: standard output

You are given a matrix consisting of n rows and m columns. The matrix contains lowercase letters of the Latin alphabet.

You can perform the following operation any number of times you want to: choose two integers i ( $1 \le i \le m$ ) and k (0 < k < n), and shift every column j such that  $i \le j \le m$  cyclically by k. The shift is performed upwards.

For example, if you have a matrix

$$\begin{pmatrix}
a & b & c \\
d & e & f \\
g & h & i
\end{pmatrix}$$

and perform an operation with i=2, k=1, then it becomes:

$$\left(egin{matrix} a & e & f \ d & h & i \ g & b & c \end{array}
ight)$$

You have to process q queries. Each of the queries is a string of length m consisting of lowercase letters of the Latin alphabet. For each query, you have to calculate the minimum number of operations described above you have to perform so that at least one row of the matrix is equal to the string from the query. Note that all queries are independent, that is, the operations you perform in a query don't affect the initial matrix in other queries.

## Input

The first line contains three integers n, m, q ( $2 \le n$ , m,  $q \le 2.5 \cdot 10^5$ ;  $n \cdot m \le 5 \cdot 10^5$ ;  $q \cdot m \le 5 \cdot 10^5$ ) — the number of rows and columns in the matrix and the number of queries, respectively.

The next n lines contains m lowercase Latin letters each — elements of the matrix.

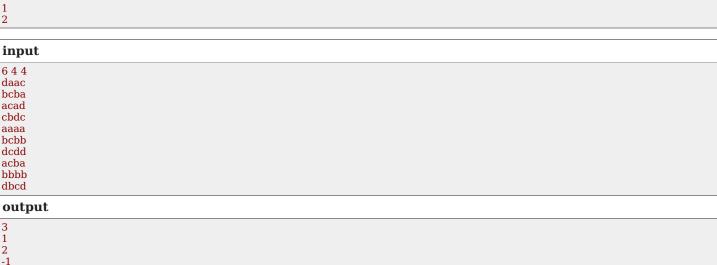
The following q lines contains a description of queries — strings of length m consisting of lowercase letters of the Latin alphabet.

## Output

Print q integers. The i-th integer should be equal to the minimum number of operations you have to perform so that the matrix contains a string from the i-th query or -1 if the specified string cannot be obtained.

## **Examples**

| The second secon |  |
|--|--|
| out  |  |
| 4 cc coa can can can can can can can can can ca  |  |
| put  |  |
|  |  |



| input  |  |
|--|--|
| 5 10 5   |  |
| ltjksdyfgg                                       |  |
| chhpsereqn                                       |  |
| 5 10 5<br>ltjksdyfgg<br>cbhpsereqn<br>ijndtzbzcf |  |

| ı | ghgcgeadep   |
|---|--|
| ı | bfzdgxqmqe   |
| ı | ibgcgzyfep   |
| ı | bbhdgxqmqg   |
| ı | ltgcgxrzep   |
| ı | ljnpseldgn   |
|   | ghgcgeadep<br>bfzdgxqmqe<br>ibgcgzyfep<br>bbhdgxqmqg<br>ltgcgxrzep<br>ljnpseldgn<br>ghhpseyzcf |
|   |  |
| н | output   |
|   | output   |
|   | output   |
|   | output   |
|   |  |

# J. Zero-XOR Array

time limit per test: 6 seconds memory limit per test: 256 megabytes input: standard input output: standard output

You are given an array of integers a of size n. This array is non-decreasing, i. e.  $a_1 \leq a_2 \leq \cdots \leq a_n$ .

You have to find arrays of integers b of size 2n-1, such that:

- $b_{2i-1} = a_i \ (1 \le i \le n);$
- array b is non-decreasing;
- $b_1 \oplus b_2 \oplus \cdots \oplus b_{2n-1} = 0$  ( $\oplus$  denotes bitwise XOR operation: https://en.wikipedia.org/wiki/Exclusive\_or. In Kotlin, it is xor function).

Calculate the number of arrays that meet all the above conditions, modulo 998244353.

## Input

The first line contains a single integer n ( $2 \le n \le 17$ ) — the size of the array a.

The second line contains n integers ( $0 \le a_i \le 2^{60} - 1$ ;  $a_i \le a_{i+1}$ ) — elements of the array a.

#### Output

Print a single integer — the number of arrays that meet all the above conditions, modulo 998244353.

## **Examples**

| input      |  |
|------------|--|
| 3<br>0 1 3 |  |
| output     |  |
| 2          |  |

| input        |  |
|--------------|--|
| 4<br>0 3 6 7 |  |
| output       |  |
| 6            |  |

| input            |  |
|------------------|--|
| 5<br>1 5 9 10 23 |  |
| output           |  |
| 20               |  |

```
input

10
39 62 64 79 81 83 96 109 120 122

output

678132
```