

## Codeforces Round #710 (Div. 3)

### A. Strange Table

time limit per test: 2 seconds  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

Polycarp found a rectangular table consisting of  $n$  rows and  $m$  columns. He noticed that each cell of the table has its number, obtained by the following algorithm **"by columns"**:

- cells are numbered starting from one;
- cells are numbered from left to right by columns, and inside each column from top to bottom;
- number of each cell is an integer one greater than in the previous cell.

For example, if  $n = 3$  and  $m = 5$ , the table will be numbered as follows:

```

1  4  7 10 13
2  5  8 11 14
3  6  9 12 15
  
```

However, Polycarp considers such numbering inconvenient. He likes the numbering **"by rows"**:

- cells are numbered starting from one;
- cells are numbered from top to bottom by rows, and inside each row from left to right;
- number of each cell is an integer one greater than the number of the previous cell.

For example, if  $n = 3$  and  $m = 5$ , then Polycarp likes the following table numbering:

```

1  2  3  4  5
6  7  8  9 10
11 12 13 14 15
  
```

Polycarp doesn't have much time, so he asks you to find out what would be the cell number in the numbering **"by rows"**, if in the numbering **"by columns"** the cell has the number  $x$ ?

#### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 10^4$ ). Then  $t$  test cases follow.

Each test case consists of a single line containing three integers  $n, m, x$  ( $1 \leq n, m \leq 10^6, 1 \leq x \leq n \cdot m$ ), where  $n$  and  $m$  are the number of rows and columns in the table, and  $x$  is the cell number.

Note that the numbers in some test cases do not fit into the 32-bit integer type, so you must use at least the 64-bit integer type of your programming language.

#### Output

For each test case, output the cell number in the numbering **"by rows"**.

#### Example

input
5 1 1 1 2 2 3 3 5 11 100 100 7312 1000000 1000000 1000000000000
output
1 2 9 1174 10000000000000

### B. Partial Replacement

time limit per test: 2 seconds  
 memory limit per test: 256 megabytes  
 input: standard input

output: standard output

You are given a number  $k$  and a string  $s$  of length  $n$ , consisting of the characters '.' and '\*'. You want to replace some of the '\*' characters with 'x' characters so that the following conditions are met:

- The first character '\*' in the original string should be replaced with 'x';
- The last character '\*' in the original string should be replaced with 'x';
- The distance between two neighboring replaced characters 'x' must not exceed  $k$  (more formally, if you replaced characters at positions  $i$  and  $j$  ( $i < j$ ) and at positions  $[i + 1, j - 1]$  there is no "x" symbol, then  $j - i$  must be no more than  $k$ ).

For example, if  $n = 7$ ,  $s = .**.***$  and  $k = 3$ , then the following strings will satisfy the conditions above:

- .xx.\*xx;
- .x\*.x\*x;
- .xx.xxx.

But, for example, the following strings will not meet the conditions:

- .\*\*.\*xx (the first character '\*' should be replaced with 'x');
- .x\*.xx\* (the last character '\*' should be replaced with 'x');
- .x\*.\*\*xx (the distance between characters at positions 2 and 6 is greater than  $k = 3$ ).

Given  $n$ ,  $k$ , and  $s$ , find the minimum number of '\*' characters that must be replaced with 'x' in order to meet the above conditions.

### Input

The first line contains one integer  $t$  ( $1 \leq t \leq 500$ ). Then  $t$  test cases follow.

The first line of each test case contains two integers  $n$  and  $k$  ( $1 \leq k \leq n \leq 50$ ).

The second line of each test case contains a string  $s$  of length  $n$ , consisting of the characters '.' and '\*'.

It is guaranteed that there is at least one '\*' in the string  $s$ .

It is guaranteed that the distance between any two neighboring '\*' characters does not exceed  $k$ .

### Output

For each test case output the minimum number of '\*' characters that must be replaced with 'x' characters in order to satisfy the conditions above.

### Example

input
5 7 3 .**.*** 5 1 ..*.. 5 2 *.*.* 3 2 *.* 1 1 *
output
3 1 3 2 1

## C. Double-ended Strings

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

You are given the strings  $a$  and  $b$ , consisting of lowercase Latin letters. You can do any number of the following operations in any order:

- if  $|a| > 0$  (the length of the string  $a$  is greater than zero), delete the first character of the string  $a$ , that is, replace  $a$  with  $a_2a_3 \dots a_n$ ;
- if  $|a| > 0$ , delete the last character of the string  $a$ , that is, replace  $a$  with  $a_1a_2 \dots a_{n-1}$ ;
- if  $|b| > 0$  (the length of the string  $b$  is greater than zero), delete the first character of the string  $b$ , that is, replace  $b$  with  $b_2b_3 \dots b_n$ ;
- if  $|b| > 0$ , delete the last character of the string  $b$ , that is, replace  $b$  with  $b_1b_2 \dots b_{n-1}$ .

Note that after each of the operations, the string  $a$  or  $b$  may become empty.

For example, if  $a = \text{"hello"}$  and  $b = \text{"icpc"}$ , then you can apply the following sequence of operations:

- delete the first character of the string  $a \Rightarrow a = \text{"ello"}$  and  $b = \text{"icpc"}$ ;
- delete the first character of the string  $b \Rightarrow a = \text{"ello"}$  and  $b = \text{"cpc"}$ ;
- delete the first character of the string  $b \Rightarrow a = \text{"ello"}$  and  $b = \text{"pc"}$ ;
- delete the last character of the string  $a \Rightarrow a = \text{"ell"}$  and  $b = \text{"pc"}$ ;
- delete the last character of the string  $b \Rightarrow a = \text{"ell"}$  and  $b = \text{"p"}$ .

For the given strings  $a$  and  $b$ , find the minimum number of operations for which you can make the strings  $a$  and  $b$  equal. Note that empty strings are also equal.

**Input**

The first line contains a single integer  $t$  ( $1 \leq t \leq 100$ ). Then  $t$  test cases follow.

The first line of each test case contains the string  $a$  ( $1 \leq |a| \leq 20$ ), consisting of lowercase Latin letters.

The second line of each test case contains the string  $b$  ( $1 \leq |b| \leq 20$ ), consisting of lowercase Latin letters.

**Output**

For each test case, output the minimum number of operations that can make the strings  $a$  and  $b$  equal.

**Example**

input
5 a a abcd bc hello codeforces hello helo dhjakjsnasjhfksafasd adjsnasjhfksvdafdser
output
0 2 13 3 20

D. Epic Transformation

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given an array  $a$  of length  $n$  consisting of integers. You can apply the following operation, consisting of several steps, on the array  $a$  **zero** or more times:

- you select two **different** numbers in the array  $a_i$  and  $a_j$ ;
- you remove  $i$ -th and  $j$ -th elements from the array.

For example, if  $n = 6$  and  $a = [1, 6, 1, 1, 4, 4]$ , then you can perform the following sequence of operations:

- select  $i = 1, j = 5$ . The array  $a$  becomes equal to  $[6, 1, 1, 4]$ ;
- select  $i = 1, j = 2$ . The array  $a$  becomes equal to  $[1, 4]$ .

What can be the minimum size of the array after applying some sequence of operations to it?

**Input**

The first line contains a single integer  $t$  ( $1 \leq t \leq 10^4$ ). Then  $t$  test cases follow.

The first line of each test case contains a single integer  $n$  ( $1 \leq n \leq 2 \cdot 10^5$ ) is length of the array  $a$ .

The second line of each test case contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq 10^9$ ).

It is guaranteed that the sum of  $n$  over all test cases does not exceed  $2 \cdot 10^5$ .

**Output**

For each test case, output the minimum possible size of the array after applying some sequence of operations to it.

**Example**

input
5 6

1 6 1 1 4 4 2 1 2 2 1 1 5 4 5 4 5 4 6 2 3 2 1 3 1
output
0 0 2 1 0

E. Restoring the Permutation

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

A permutation is a sequence of  $n$  integers from 1 to  $n$ , in which all numbers occur exactly once. For example,  $[1]$ ,  $[3, 5, 2, 1, 4]$ ,  $[1, 3, 2]$  are permutations, and  $[2, 3, 2]$ ,  $[4, 3, 1]$ ,  $[0]$  are not.

Polycarp was presented with a permutation  $p$  of numbers from 1 to  $n$ . However, when Polycarp came home, he noticed that in his pocket, the permutation  $p$  had turned into an array  $q$  according to the following rule:

- $q_i = \max(p_1, p_2, \dots, p_i)$ .

Now Polycarp wondered what lexicographically minimal and lexicographically maximal permutations could be presented to him.

An array  $a$  of length  $n$  is lexicographically smaller than an array  $b$  of length  $n$  if there is an index  $i$  ( $1 \leq i \leq n$ ) such that the first  $i - 1$  elements of arrays  $a$  and  $b$  are the same, and the  $i$ -th element of the array  $a$  is less than the  $i$ -th element of the array  $b$ . For example, the array  $a = [1, 3, 2, 3]$  is lexicographically smaller than the array  $b = [1, 3, 4, 2]$ .

For example, if  $n = 7$  and  $p = [3, 2, 4, 1, 7, 5, 6]$ , then  $q = [3, 3, 4, 4, 7, 7, 7]$  and the following permutations could have been as  $p$  initially:

- $[3, 1, 4, 2, 7, 5, 6]$  (lexicographically minimal permutation);
- $[3, 1, 4, 2, 7, 6, 5]$ ;
- $[3, 2, 4, 1, 7, 5, 6]$ ;
- $[3, 2, 4, 1, 7, 6, 5]$  (lexicographically maximum permutation).

For a given array  $q$ , find the lexicographically minimal and lexicographically maximal permutations that could have been originally presented to Polycarp.

Input

The first line contains one integer  $t$  ( $1 \leq t \leq 10^4$ ). Then  $t$  test cases follow.

The first line of each test case contains one integer  $n$  ( $1 \leq n \leq 2 \cdot 10^5$ ).

The second line of each test case contains  $n$  integers  $q_1, q_2, \dots, q_n$  ( $1 \leq q_i \leq n$ ).

It is guaranteed that the array  $q$  was obtained by applying the rule from the statement to some permutation  $p$ .

It is guaranteed that the sum of  $n$  over all test cases does not exceed  $2 \cdot 10^5$ .

Output

For each test case, output two lines:

- on the first line output  $n$  integers — lexicographically **minimal** permutation that could have been originally presented to Polycarp;
- on the second line print  $n$  integers — lexicographically **maximal** permutation that could have been originally presented to Polycarp;

Example

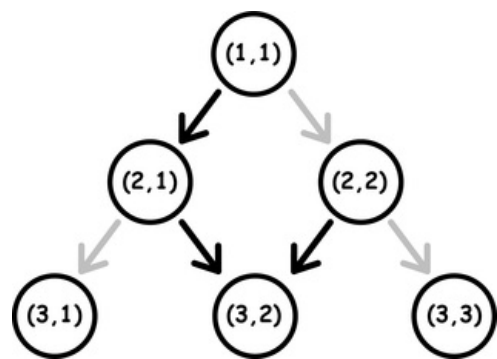
input
4 7 3 3 4 4 7 7 7 4 1 2 3 4 7 3 4 5 5 5 7 7 1 1

output
3 1 4 2 7 5 6 3 2 4 1 7 6 5 1 2 3 4 1 2 3 4 3 4 5 1 2 7 6 3 4 5 2 1 7 6 1 1

F. Triangular Paths

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Consider an infinite triangle made up of layers. Let's number the layers, starting from one, from the top of the triangle (from top to bottom). The  $k$ -th layer of the triangle contains  $k$  points, numbered from left to right. Each point of an infinite triangle is described by a pair of numbers  $(r, c)$  ( $1 \leq c \leq r$ ), where  $r$  is the number of the layer, and  $c$  is the number of the point in the layer. From each point  $(r, c)$  there are two **directed** edges to the points  $(r + 1, c)$  and  $(r + 1, c + 1)$ , but only one of the edges is activated. If  $r + c$  is even, then the edge to the point  $(r + 1, c)$  is activated, otherwise the edge to the point  $(r + 1, c + 1)$  is activated. Look at the picture for a better understanding.



Activated edges are colored in black. Non-activated edges are colored in gray.

From the point  $(r_1, c_1)$  it is possible to reach the point  $(r_2, c_2)$ , if there is a path between them only from **activated** edges. For example, in the picture above, there is a path from  $(1, 1)$  to  $(3, 2)$ , but there is no path from  $(2, 1)$  to  $(1, 1)$ .

Initially, you are at the point  $(1, 1)$ . For each turn, you can:

- Replace activated edge for point  $(r, c)$ . That is if the edge to the point  $(r + 1, c)$  is activated, then **instead of it**, the edge to the point  $(r + 1, c + 1)$  becomes activated, otherwise if the edge to the point  $(r + 1, c + 1)$ , then **instead if it**, the edge to the point  $(r + 1, c)$  becomes activated. This action increases the cost of the path by 1;
- Move from the current point to another by following the activated edge. This action **does not increase** the cost of the path.

You are given a sequence of  $n$  points of an infinite triangle  $(r_1, c_1), (r_2, c_2), \dots, (r_n, c_n)$ . Find the minimum cost path from  $(1, 1)$ , passing through all  $n$  points in **arbitrary** order.

Input

The first line contains one integer  $t$  ( $1 \leq t \leq 10^4$ ) is the number of test cases. Then  $t$  test cases follow.

Each test case begins with a line containing one integer  $n$  ( $1 \leq n \leq 2 \cdot 10^5$ ) is the number of points to visit.

The second line contains  $n$  numbers  $r_1, r_2, \dots, r_n$  ( $1 \leq r_i \leq 10^9$ ), where  $r_i$  is the number of the layer in which  $i$ -th point is located.

The third line contains  $n$  numbers  $c_1, c_2, \dots, c_n$  ( $1 \leq c_i \leq r_i$ ), where  $c_i$  is the number of the  $i$ -th point in the  $r_i$  layer.

It is guaranteed that all  $n$  points are distinct.

It is guaranteed that there is always at least one way to traverse all  $n$  points.

It is guaranteed that the sum of  $n$  over all test cases does not exceed  $2 \cdot 10^5$ .

Output

For each test case, output the minimum cost of a path passing through all points in the corresponding test case.

Example

input
4 3 1 4 2 1 3 1 2 2 4 2 3

```

2
1 1000000000
1 1000000000
4
3 10 5 8
2 5 2 4

```

**output**

```

0
1
9999999999
2

```

## G. Maximize the Remaining String

time limit per test: 2.5 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given a string  $s$ , consisting of lowercase Latin letters. While there is at least one character in the string  $s$  that is **repeated at least twice**, you perform the following operation:

- you choose the index  $i$  ( $1 \leq i \leq |s|$ ) such that the character at position  $i$  occurs **at least two** times in the string  $s$ , and delete the character at position  $i$ , that is, replace  $s$  with  $s_1 s_2 \dots s_{i-1} s_{i+1} s_{i+2} \dots s_n$ .

For example, if  $s = \text{"codeforces"}$ , then you can apply the following sequence of operations:

- $i = 6 \Rightarrow s = \text{"codefrces"}$ ;
- $i = 1 \Rightarrow s = \text{"odefrces"}$ ;
- $i = 7 \Rightarrow s = \text{"odefrcs"}$ ;

Given a given string  $s$ , find the lexicographically maximum string that can be obtained after applying a certain sequence of operations after which all characters in the string **become unique**.

A string  $a$  of length  $n$  is lexicographically less than a string  $b$  of length  $m$ , if:

- there is an index  $i$  ( $1 \leq i \leq \min(n, m)$ ) such that the first  $i - 1$  characters of the strings  $a$  and  $b$  are the same, and the  $i$ -th character of the string  $a$  is less than  $i$ -th character of string  $b$ ;
- or** the first  $\min(n, m)$  characters in the strings  $a$  and  $b$  are the same and  $n < m$ .

For example, the string  $a = \text{"aezakmi"}$  is lexicographically less than the string  $b = \text{"aezus"}$ .

### Input

The first line contains one integer  $t$  ( $1 \leq t \leq 10^4$ ). Then  $t$  test cases follow.

Each test case is characterized by a string  $s$ , consisting of lowercase Latin letters ( $1 \leq |s| \leq 2 \cdot 10^5$ ).

It is guaranteed that the sum of the lengths of the strings in all test cases does not exceed  $2 \cdot 10^5$ .

### Output

For each test case, output the lexicographically maximum string that can be obtained after applying a certain sequence of operations after which all characters in the string **become unique**.

### Example

**input**

```

6
codeforces
aezakmi
abacaba
convexhull
swfldjgpaxs
myneocktxqpjz

```

**output**

```

odfrces
ezakmi
cba
convexhul
wfldjgpaxs
myneocktxqpjz

```