

### A. Dawid and Bags of Candies

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

Dawid has four bags of candies. The  $i$ -th of them contains  $a_i$  candies. Also, Dawid has two friends. He wants to give each bag to one of his two friends. Is it possible to distribute the bags in such a way that each friend receives the same amount of candies in total?

Note, that you can't keep bags for yourself or throw them away, each bag should be given to one of the friends.

#### Input

The only line contains four integers  $a_1, a_2, a_3$  and  $a_4$  ( $1 \leq a_i \leq 100$ ) — the numbers of candies in each bag.

#### Output

Output YES if it's possible to give the bags to Dawid's friends so that both friends receive the same amount of candies, or NO otherwise. Each character can be printed in any case (either uppercase or lowercase).

#### Examples

<b>input</b>
1 7 11 5
<b>output</b>
YES
<b>input</b>
7 3 2 5
<b>output</b>
NO

#### Note

In the first sample test, Dawid can give the first and the third bag to the first friend, and the second and the fourth bag to the second friend. This way, each friend will receive 12 candies.

In the second sample test, it's impossible to distribute the bags.

### B. Ania and Minimizing

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

Ania has a large integer  $S$ . Its decimal representation has length  $n$  and doesn't contain any leading zeroes. Ania is allowed to change at most  $k$  digits of  $S$ . She wants to do it in such a way that  $S$  still won't contain any leading zeroes and it'll be minimal possible. What integer will Ania finish with?

#### Input

The first line contains two integers  $n$  and  $k$  ( $1 \leq n \leq 200\,000$ ,  $0 \leq k \leq n$ ) — the number of digits in the decimal representation of  $S$  and the maximum allowed number of changed digits.

The second line contains the integer  $S$ . It's guaranteed that  $S$  has exactly  $n$  digits and doesn't contain any leading zeroes.

#### Output

Output the minimal possible value of  $S$  which Ania can end with. Note that the resulting integer should also have  $n$  digits.

#### Examples

<b>input</b>
5 3 51528
<b>output</b>
10028
<b>input</b>
3 2 102
<b>output</b>
100
<b>input</b>
1 1 1
<b>output</b>
0

#### Note

A number has leading zeroes if it consists of at least two digits and its first digit is 0. For example, numbers 00, 00069 and 0101 have leading zeroes, while 0, 3000 and 1010 don't have leading zeroes.

### C. Increasing Matrix

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

In this problem, a  $n \times m$  rectangular matrix  $a$  is called *increasing* if, for each row of  $i$ , when go from left to right, the values strictly increase (that is,  $a_{i,1} < a_{i,2} < \dots < a_{i,m}$ ) and for each column  $j$ , when go from top to bottom, the values strictly increase (that is,  $a_{1,j} < a_{2,j} < \dots < a_{n,j}$ ).

In a given matrix of non-negative integers, it is necessary to replace each value of 0 with some positive integer so that the resulting matrix is increasing and the sum of its elements is maximum, or find that it is impossible.

It is guaranteed that in a given value matrix all values of 0 are contained only in internal cells (that is, not in the first or last row and not in the first or last column).

### Input

The first line contains integers  $n$  and  $m$  ( $3 \leq n, m \leq 500$ ) — the number of rows and columns in the given matrix  $a$ .

The following lines contain  $m$  each of non-negative integers — the values in the corresponding row of the given matrix:  $a_{i,1}, a_{i,2}, \dots, a_{i,m}$  ( $0 \leq a_{i,j} \leq 8000$ ).

It is guaranteed that for all  $a_{i,j} = 0$ ,  $1 < i < n$  and  $1 < j < m$  are true.

### Output

If it is possible to replace all zeros with positive numbers so that the matrix is increasing, print the maximum possible sum of matrix elements. Otherwise, print -1.

### Examples

<b>input</b>
4 5 1 3 5 6 7 3 0 7 0 9 5 0 0 0 10 8 9 10 11 12
<b>output</b>
144
<b>input</b>
3 3 1 2 3 2 0 4 4 5 6
<b>output</b>
30
<b>input</b>
3 3 1 2 3 3 0 4 4 5 6
<b>output</b>
-1
<b>input</b>
3 3 1 2 3 2 3 4 3 4 2
<b>output</b>
-1

### Note

In the first example, the resulting matrix is as follows:

1 3 5 6 7  
3 6 7 8 9  
5 7 8 9 10  
8 9 10 11 12

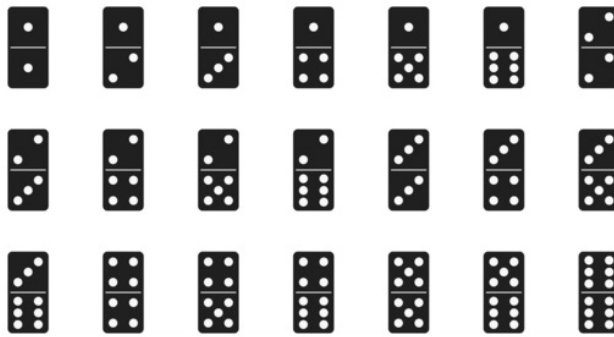
In the second example, the value 3 must be put in the middle cell.

In the third example, the desired resultant matrix does not exist.

## D. Anadi and Domino

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Anadi has a set of dominoes. Every domino has two parts, and each part contains some dots. For every  $a$  and  $b$  such that  $1 \leq a \leq b \leq 6$ , there is exactly one domino with  $a$  dots on one half and  $b$  dots on the other half. The set contains exactly 21 dominoes. Here is an exact illustration of his set:



Also, Anadi has an undirected graph without self-loops and multiple edges. He wants to choose some dominoes and place them on the edges of this graph. He can use at most one domino of each type. Each edge can fit at most one domino. It's not necessary to place a domino on each edge of the graph.

When placing a domino on an edge, he also chooses its direction. In other words, one half of any placed domino must be directed toward one of the endpoints of the edge and the other half must be directed toward the other endpoint. There's a catch: if there are multiple halves of dominoes directed toward the same vertex, each of these halves must contain the same number of dots.

How many dominoes at most can Anadi place on the edges of his graph?

### Input

The first line contains two integers  $n$  and  $m$  ( $1 \leq n \leq 7, 0 \leq m \leq \frac{n(n-1)}{2}$ ) — the number of vertices and the number of edges in the graph.

The next  $m$  lines contain two integers each. Integers in the  $i$ -th line are  $a_i$  and  $b_i$  ( $1 \leq a, b \leq n, a \neq b$ ) and denote that there is an edge which connects vertices  $a_i$  and  $b_i$ .

The graph might be disconnected. It's however guaranteed that the graph doesn't contain any self-loops, and that there is at most one edge between any pair of vertices.

### Output

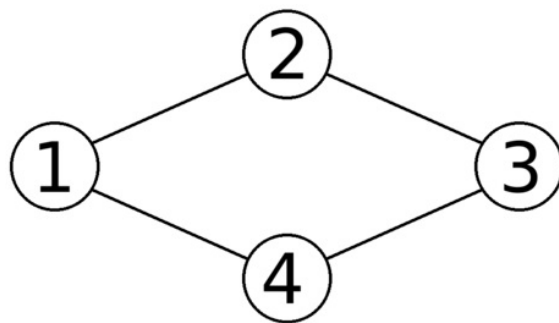
Output one integer which denotes the maximum number of dominoes which Anadi can place on the edges of the graph.

### Examples

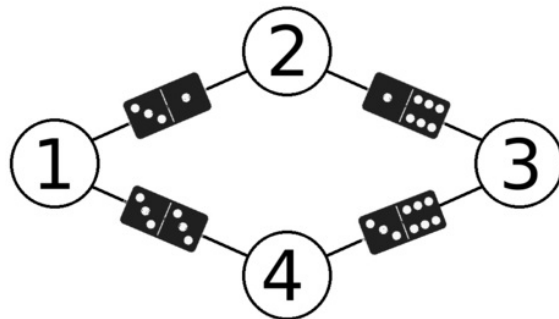
input
4 4 1 2 2 3 3 4 4 1
output
4
input
7 0
output
0
input
3 1 1 3
output
1
input
7 21 1 2 1 3 1 4 1 5 1 6 1 7 2 3 2 4 2 5 2 6 2 7 3 4 3 5 3 6 3 7 4 5 4 6 4 7 5 6 5 7 6 7
output
16

### Note

Here is an illustration of Anadi's graph from the first sample test:



And here is one of the ways to place a domino on each of its edges:



Note that each vertex is faced by the halves of dominoes with the same number of dots. For instance, all halves directed toward vertex 1 have three dots.

### E. Middle-Out

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

*The problem was inspired by Pied Piper story. After a challenge from Hooli's compression competitor Nucleus, Richard pulled an all-nighter to invent a new approach to compression: middle-out.*

You are given two strings  $s$  and  $t$  of the same length  $n$ . Their characters are numbered from 1 to  $n$  from left to right (i.e. from the beginning to the end).

In a single move you can do the following sequence of actions:

- choose any valid index  $i$  ( $1 \leq i \leq n$ ),
- move the  $i$ -th character of  $s$  from its position to the beginning of the string or move the  $i$ -th character of  $s$  from its position to the end of the string.

Note, that the moves don't change the length of the string  $s$ . You can apply a move only to the string  $s$ .

For example, if  $s = \text{"test"}$  in one move you can obtain:

- if  $i = 1$  and you move to the beginning, then the result is  $\text{"test"}$  (the string doesn't change),
- if  $i = 2$  and you move to the beginning, then the result is  $\text{"etst"}$ ,
- if  $i = 3$  and you move to the beginning, then the result is  $\text{"stet"}$ ,
- if  $i = 4$  and you move to the beginning, then the result is  $\text{"ttes"}$ ,
- if  $i = 1$  and you move to the end, then the result is  $\text{"estt"}$ ,
- if  $i = 2$  and you move to the end, then the result is  $\text{"tste"}$ ,
- if  $i = 3$  and you move to the end, then the result is  $\text{"tets"}$ ,
- if  $i = 4$  and you move to the end, then the result is  $\text{"test"}$  (the string doesn't change).

You want to make the string  $s$  equal to the string  $t$ . What is the minimum number of moves you need? If it is impossible to transform  $s$  to  $t$ , print -1.

#### Input

The first line contains integer  $q$  ( $1 \leq q \leq 100$ ) — the number of independent test cases in the input.

Each test case is given in three lines. The first line of a test case contains  $n$  ( $1 \leq n \leq 100$ ) — the length of the strings  $s$  and  $t$ . The second line contains  $s$ , the third line contains  $t$ . Both strings  $s$  and  $t$  have length  $n$  and contain only lowercase Latin letters.

There are no constraints on the sum of  $n$  in the test (i.e. the input with  $q = 100$  and all  $n = 100$  is allowed).

#### Output

For every test print minimum possible number of moves, which are needed to transform  $s$  into  $t$ , or -1, if it is impossible to do.

#### Examples

input
<pre> 3 9 iredppipe piedpiper 4 estt test 4 tste test </pre>
output
<pre> 2 1 2 </pre>

input
4 1 a z 5 adhas dasha 5 aashd dasha 5 aahsd dasha
output
-1 2 2 3

**Note**

In the first example, the moves in one of the optimal answers are:

- for the first test case  $s = \text{"iredppipe"}, t = \text{"piedpiper"}$ :  $\text{"iredppipe"} \rightarrow \text{"iedppiper"} \rightarrow \text{"piedpiper"}$ ;
- for the second test case  $s = \text{"estt"}, t = \text{"test"}$ :  $\text{"estt"} \rightarrow \text{"test"}$ ;
- for the third test case  $s = \text{"tste"}, t = \text{"test"}$ :  $\text{"tste"} \rightarrow \text{"etst"} \rightarrow \text{"test"}$ .

F. Marcin and Training Camp

time limit per test: 3 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Marcin is a coach in his university. There are  $n$  students who want to attend a training camp. Marcin is a smart coach, so he wants to send only the students that can work calmly with each other.

Let's focus on the students. They are indexed with integers from 1 to  $n$ . Each of them can be described with two integers  $a_i$  and  $b_i$ ;  $b_i$  is equal to the skill level of the  $i$ -th student (the higher, the better). Also, there are 60 known algorithms, which are numbered with integers from 0 to 59. If the  $i$ -th student knows the  $j$ -th algorithm, then the  $j$ -th bit ( $2^j$ ) is set in the binary representation of  $a_i$ . Otherwise, this bit is not set.

Student  $x$  thinks that he is better than student  $y$  if and only if  $x$  knows some algorithm which  $y$  doesn't know. Note that two students can think that they are better than each other. A group of students can work together calmly if no student in this group thinks that he is better than everyone else in this group.

Marcin wants to send a group of at least two students which will work together calmly and will have the maximum possible sum of the skill levels. What is this sum?

**Input**

The first line contains one integer  $n$  ( $1 \leq n \leq 7000$ ) — the number of students interested in the camp.

The second line contains  $n$  integers. The  $i$ -th of them is  $a_i$  ( $0 \leq a_i < 2^{60}$ ).

The third line contains  $n$  integers. The  $i$ -th of them is  $b_i$  ( $1 \leq b_i \leq 10^9$ ).

**Output**

Output one integer which denotes the maximum sum of  $b_i$  over the students in a group of students which can work together calmly. If no group of at least two students can work together calmly, print 0.

**Examples**

input
4 3 2 3 6 2 8 5 10
output
15

input
3 1 2 3 1 2 3
output
0

input
1 0 1
output
0

**Note**

In the first sample test, it's optimal to send the first, the second and the third student to the camp. It's also possible to send only the first and the third student, but they'd have a lower sum of  $b_i$ .

In the second test, in each group of at least two students someone will always think that he is better than everyone else in the subset.

G. Kamil and Making a Stream

time limit per test: 4 seconds  
memory limit per test: 768 megabytes  
input: standard input

Kamil likes streaming the competitive programming videos. His MeTube channel has recently reached 100 million subscribers. In order to celebrate this, he posted a video with an interesting problem he couldn't solve yet. Can you help him?

You're given a tree — a connected undirected graph consisting of  $n$  vertices connected by  $n - 1$  edges. The tree is rooted at vertex 1. A vertex  $u$  is called an *ancestor* of  $v$  if it lies on the shortest path between the root and  $v$ . In particular, a vertex is an ancestor of itself.

Each vertex  $v$  is assigned its *beauty*  $x_v$  — a non-negative integer not larger than  $10^{12}$ . This allows us to define the beauty of a path. Let  $u$  be an ancestor of  $v$ . Then we define the beauty  $f(u, v)$  as the greatest common divisor of the beauties of all vertices on the shortest path between  $u$  and  $v$ . Formally, if  $u = t_1, t_2, t_3, \dots, t_k = v$  are the vertices on the shortest path between  $u$  and  $v$ , then  $f(u, v) = \gcd(x_{t_1}, x_{t_2}, \dots, x_{t_k})$ . Here,  $\gcd$  denotes the greatest common divisor of a set of numbers. In particular,  $f(u, u) = \gcd(x_u) = x_u$ .

Your task is to find the sum

$$\sum_{u \text{ is an ancestor of } v} f(u, v).$$

As the result might be too large, please output it modulo  $10^9 + 7$ .

Note that for each  $y$ ,  $\gcd(0, y) = \gcd(y, 0) = y$ . In particular,  $\gcd(0, 0) = 0$ .

**Input**

The first line contains a single integer  $n$  ( $2 \leq n \leq 100\,000$ ) — the number of vertices in the tree.

The following line contains  $n$  integers  $x_1, x_2, \dots, x_n$  ( $0 \leq x_i \leq 10^{12}$ ). The value  $x_v$  denotes the beauty of vertex  $v$ .

The following  $n - 1$  lines describe the edges of the tree. Each of them contains two integers  $a, b$  ( $1 \leq a, b \leq n, a \neq b$ ) — the vertices connected by a single edge.

**Output**

Output the sum of the beauties on all paths  $(u, v)$  such that  $u$  is ancestor of  $v$ . This sum should be printed modulo  $10^9 + 7$ .

**Examples**

input
5 4 5 6 0 8 1 2 1 3 1 4 4 5
output
42

input
7 0 2 3 0 0 0 0 1 2 1 3 2 4 2 5 3 6 3 7
output
30

**Note**

The following figure shows all 10 possible paths for which one endpoint is an ancestor of another endpoint. The sum of beauties of all these paths is equal to 42:

