

Lecture 2: Supervised Machine Learning

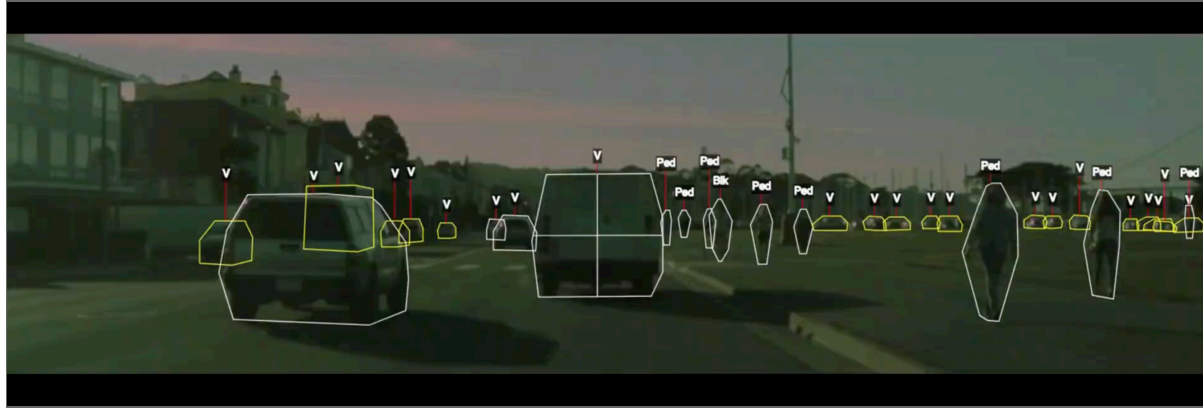
Applied Machine Learning

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Recall: Supervised Learning

The most common approach to machine learning is supervised learning.



1. First, we collect a dataset of labeled training examples.
2. We train a model to output accurate predictions on this dataset.
3. When the model sees new, similar data, it will also be accurate.

Part 1: A First Supervised Machine Learning Problem

Let's start with a simple example of a supervised learning problem: predicting diabetes risk.

Suppose we have a dataset of diabetes patients.

- For each patient we have access to measurements from their medical record and an estimate of diabetes risk.
- We are interested in understanding how the measurements affect an individual's diabetes risk.

Three Components of A Supervised Machine Learning Problem

At a high level, a supervised machine learning problem has the following structure:

$$\text{Dataset} + \text{Algorithm} \rightarrow \text{Predictive Model}$$

The predictive model is chosen to model the relationship between inputs and targets. For instance, it can predict future targets.

A Supervised Learning Dataset

Let's return to our example: predicting diabetes risk. What would a dataset look like?

We will use the UCI Diabetes Dataset; it's a toy dataset that's often used to demonstrate machine learning algorithms.

- For each patient we have access to a measurement of their body mass index (BMI) and a quantitative diabetes risk score (from 0-400).
- We are interested in understanding how BMI affects an individual's diabetes risk.

In [2]:

```

import numpy as np
import pandas as pd
from sklearn import datasets

# Load the diabetes dataset
diabetes_X, diabetes_y = datasets.load_diabetes(return_X_y=True, as_frame=True)

# Use only the BMI feature
diabetes_X = diabetes_X.loc[:, ['bmi']]

# The BMI is zero-centered and normalized; we recenter it for ease of presentation
diabetes_X = diabetes_X * 30 + 25

# Collect 20 data points
diabetes_X_train = diabetes_X.iloc[-20:]
diabetes_y_train = diabetes_y.iloc[-20:]

# Display some of the data points
pd.concat([diabetes_X_train, diabetes_y_train], axis=1).head()

```

Out [2]:

| | bmi | target |
|-----|-----------|--------|
| 422 | 27.335902 | 233.0 |
| 423 | 23.811456 | 91.0 |
| 424 | 25.331171 | 111.0 |
| 425 | 23.779122 | 152.0 |
| 426 | 23.973128 | 120.0 |

We can also visualize this two-dimensional dataset.

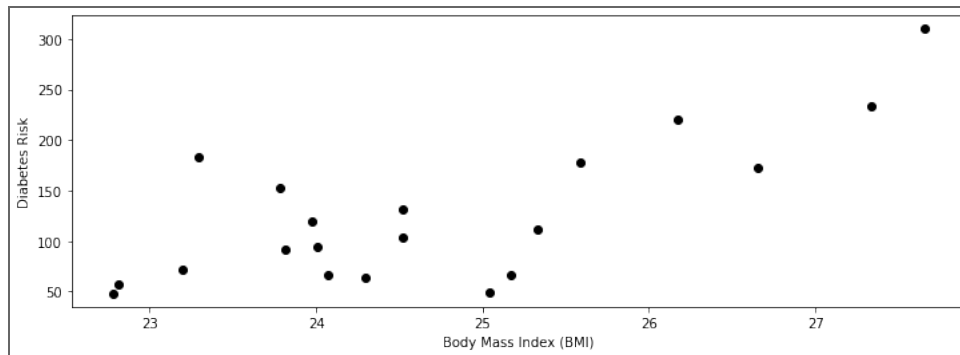
In [3]:

```
%matplotlib inline
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [12, 4]

plt.scatter(diabetes_X_train, diabetes_y_train, color='black')
plt.xlabel('Body Mass Index (BMI)')
plt.ylabel('Diabetes Risk')
```

Out[3]:

```
Text(0, 0.5, 'Diabetes Risk')
```



A Supervised Learning Algorithm (Part 1)

What is the relationship between BMI and diabetes risk?

We could assume that risk is a linear function of BMI. In other words, for some unknown $\theta_0, \theta_1 \in \mathbb{R}$, we have

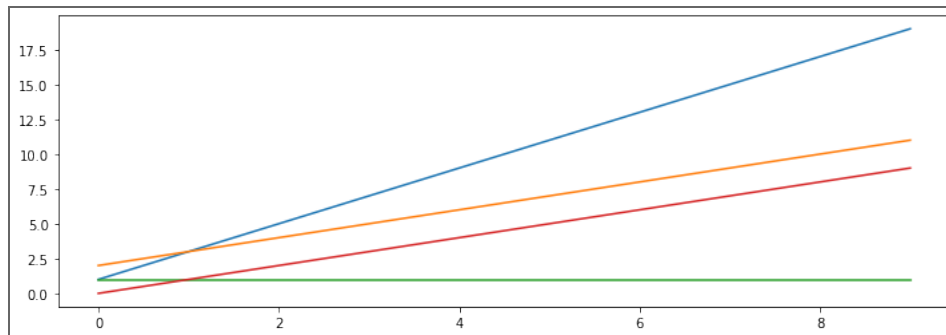
$$y = \theta_1 \cdot x + \theta_0,$$

where x is the BMI (also called the dependent variable), and y is the diabetes risk score (the independent variable).

Note that θ_1, θ_0 are the slope and the intercept of the line relates x to y . We call them *parameters*.

We can visualize this for a few values of θ_1, θ_0 .

```
In [4]:  
theta_list = [(1, 2), (2, 1), (1, 0), (0, 1)]  
for theta0, theta1 in theta_list:  
    x = np.arange(10)  
    y = theta1 * x + theta0  
    plt.plot(x, y)
```



A Supervised Learning Algorithm (Part 2)

Assuming that x, y follow the above linear relationship, the goal of the **supervised learning algorithm** is to find a good set of parameters consistent with the data.

We will see many algorithms for this task. For now, let's call the `sklearn.linear_model` library to find a θ_1, θ_0 that fit the data well.

```
In [6]:  
from sklearn import linear_model  
from sklearn.metrics import mean_squared_error  
  
# Create linear regression object  
regr = linear_model.LinearRegression()  
  
# Train the model using the training sets  
regr.fit(diabetes_X_train, diabetes_y_train.values)  
  
# Make predictions on the training set  
diabetes_y_train_pred = regr.predict(diabetes_X_train)  
  
# The coefficients  
print('Slope (theta1): \t', regr.coef_[0])  
print('Intercept (theta0): \t', regr.intercept_)
```

```
Slope (theta1):          37.378842160517664  
Intercept (theta0):     -797.0817390342369
```

A Supervised Learning Model

The supervised learning algorithm gave us a pair of parameters θ_1^*, θ_0^* . These define the *predictive model* f^* , defined as

$$f(x) = \theta_1^* \cdot x + \theta_0^*,$$

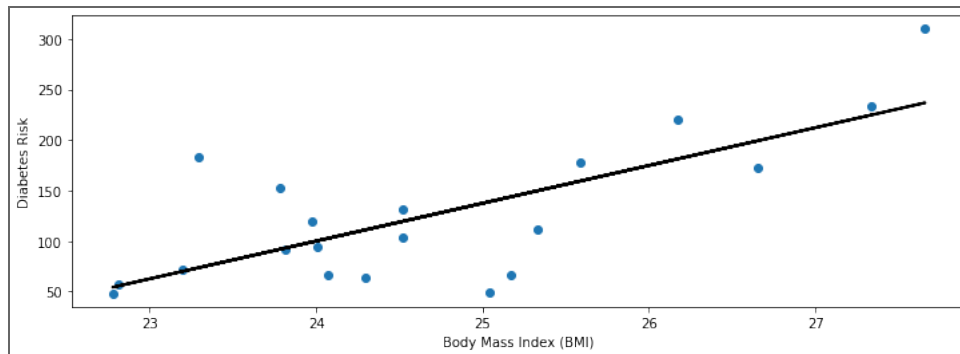
where again x is the BMI, and y is the diabetes risk score.

We can visualize the linear model that fits our data.

```
In [7]:  
plt.xlabel('Body Mass Index (BMI)')  
plt.ylabel('Diabetes Risk')  
plt.scatter(diabetes_X_train, diabetes_y_train)  
plt.plot(diabetes_X_train, diabetes_y_train_pred, color='black', linewidth=2)
```

Out [7]:

```
[<matplotlib.lines.Line2D at 0x1253f9240>]
```



Predictions Using Supervised Learning

Given a new dataset of patients with a known BMI, we can use this model to estimate their diabetes risk.

Given a new x' , we can output a predicted y' as

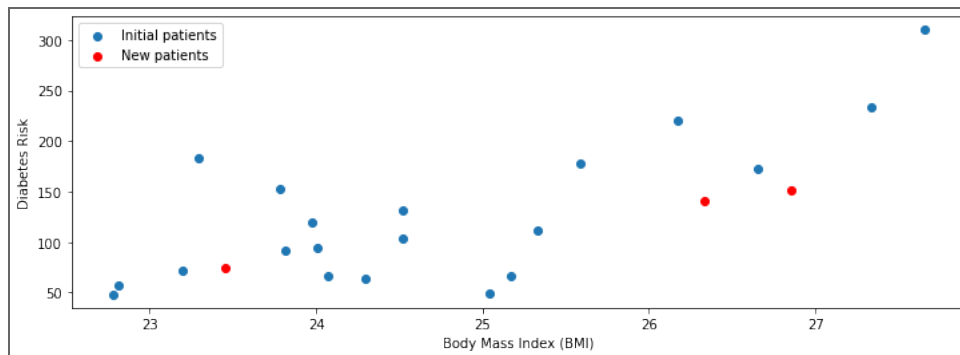
$$y' = f(x') = \theta_1^* \cdot x' + \theta_0.$$

Let's start by loading more data. We will load three new patients (shown in red below) that we haven't seen before.

```
In [8]:  
# Collect 3 data points  
diabetes_X_test = diabetes_X.iloc[:3]  
diabetes_y_test = diabetes_y.iloc[:3]  
  
plt.scatter(diabetes_X_train, diabetes_y_train)  
plt.scatter(diabetes_X_test, diabetes_y_test, color='red')  
plt.xlabel('Body Mass Index (BMI)')  
plt.ylabel('Diabetes Risk')  
plt.legend(['Initial patients', 'New patients'])
```

Out [8]:

<matplotlib.legend.Legend at 0x1259cd390>



Our linear model provides an estimate of the diabetes risk for these patients.

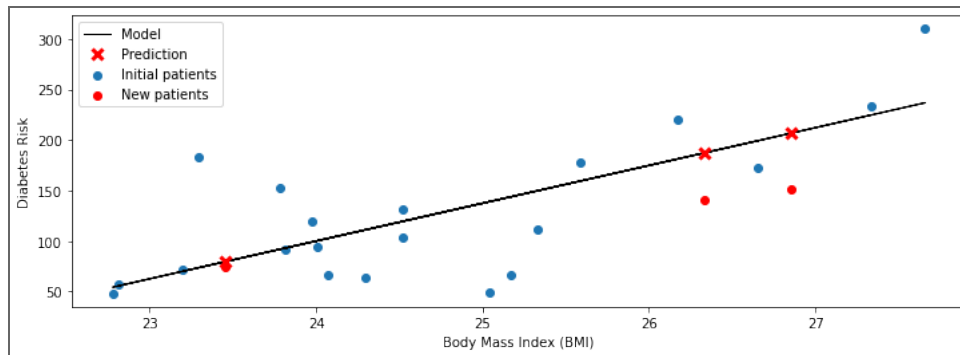
In [9]:

```
# generate predictions on the new patients
diabetes_y_test_pred = regr.predict(diabetes_X_test)

# visualize the results
plt.xlabel('Body Mass Index (BMI)')
plt.ylabel('Diabetes Risk')
plt.scatter(diabetes_X_train, diabetes_y_train)
plt.scatter(diabetes_X_test, diabetes_y_test, color='red', marker='o')
plt.plot(diabetes_X_train, diabetes_y_train_pred, color='black', linewidth=1)
plt.plot(diabetes_X_test, diabetes_y_test_pred, 'x', color='red', mew=3, markersize=8)
plt.legend(['Model', 'Prediction', 'Initial patients', 'New patients'])
```

Out [9]:

<matplotlib.legend.Legend at 0x125bfb048>



Why Supervised Learning?

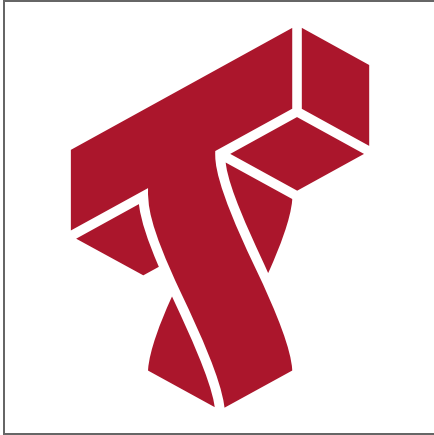
Supervised learning can be useful in many ways.

- Making predictions on new data.
- Understanding the mechanisms through which input variables affect targets.

Applications of Supervised Learning

Many of the most important applications of machine learning are supervised:

- Classifying medical images.
- Translating between pairs of languages.
- Detecting objects in a self-driving car.



Part 2: Anatomy of a Supervised Learning Problem: Datasets

We have seen a simple example of a supervised machine learning problem and an algorithm for solving this problem.

Let's now look at what a general supervised learning problem looks like.

Recall: Three Components of A Supervised Machine Learning Problem

At a high level, a supervised machine learning problem has the following structure:

$$\text{Dataset} + \text{Algorithm} \rightarrow \text{Predictive Model}$$

The predictive model is chosen to model the relationship between inputs and targets. For instance, it can predict future targets.

A Supervised Learning Dataset

We are going to dive deeper into what's a supervised learning dataset. As an example, consider the full version of the UCI Diabetes Dataset seen earlier.

Previously, we only looked at the patients' BMI, but this dataset actually records many additional measurements.

The UCI dataset contains many additional data columns besides `bmi`, including age, sex, and blood pressure. We can ask `sklearn` to give us more information about this dataset.

```
In [10]:
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [12, 4]
from sklearn import datasets

# Load the diabetes dataset
diabetes = datasets.load_diabetes(as_frame=True)
print(diabetes.DESCR)
```

```
.. _diabetes_dataset:
```

Diabetes dataset

Ten baseline variables, age, sex, body mass index, average blood pressure, and six blood serum measurements were obtained for each of $n = 442$ diabetes patients, as well as the response of interest, a quantitative measure of disease progression one year after baseline.

****Data Set Characteristics:****

:Number of Instances: 442

:Number of Attributes: First 10 columns are numeric predictive values

:Target: Column 11 is a quantitative measure of disease progression one year after baseline

:Attribute Information:

- age age in years
- sex
- bmi body mass index
- bp average blood pressure

- s1 tc, T-Cells (a type of white blood cells)
- s2 ldl, low-density lipoproteins
- s3 hdl, high-density lipoproteins
- s4 tch, thyroid stimulating hormone
- s5 ltg, lamotrigine
- s6 glu, blood sugar level

Note: Each of these 10 feature variables have been mean centered and scaled by the standard deviation times ``n_samples`` (i.e. the sum of squares of each column totals 1).

Source URL:

<https://www4.stat.ncsu.edu/~boos/var.select/diabetes.html>

For more information see:

Bradley Efron, Trevor Hastie, Iain Johnstone and Robert Tibshirani (2004) "Least Angle Regression," Annals of Statistics (with discussion), 407-499.

(https://web.stanford.edu/~hastie/Papers/LARS/LeastAngle_2002.pdf)

A Supervised Learning Dataset: Notation

We say that a training dataset of size n (e.g., n patients) is a set

$$\mathcal{D} = \{(x^{(i)}, y^{(i)}) \mid i = 1, 2, \dots, n\}$$

Each $x^{(i)}$ denotes an input (e.g., the measurements for patient i), and each $y^{(i)} \in \mathcal{Y}$ is a target (e.g., the diabetes risk).

Together, $(x^{(i)}, y^{(i)})$ form a *training example*.

We can look at the diabetes dataset in this form.

```
In [11]:
# Load the diabetes dataset
diabetes_X, diabetes_y = diabetes.data, diabetes.target

# Print part of the dataset
diabetes_X.head()
```

Out [11]:

| | age | sex | bmi | bp | s1 | s2 | s3 | s4 | |
|---|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|----------|
| 0 | 0.038076 | 0.050680 | 0.061696 | 0.021872 | -0.044223 | -0.034821 | -0.043401 | -0.002592 | 0.01990 |
| 1 | -0.001882 | -0.044642 | -0.051474 | -0.026328 | -0.008449 | -0.019163 | 0.074412 | -0.039493 | -0.06833 |
| 2 | 0.085299 | 0.050680 | 0.044451 | -0.005671 | -0.045599 | -0.034194 | -0.032356 | -0.002592 | 0.00286 |
| 3 | -0.089063 | -0.044642 | -0.011595 | -0.036656 | 0.012191 | 0.024991 | -0.036038 | 0.034309 | 0.02269 |
| 4 | 0.005383 | -0.044642 | -0.036385 | 0.021872 | 0.003935 | 0.015596 | 0.008142 | -0.002592 | -0.03199 |

Training Dataset: Inputs

More precisely, an input $x^{(i)} \in \mathcal{X}$ is a d -dimensional vector of the form

$$x^{(i)} = \begin{bmatrix} x_1^{(i)} \\ x_2^{(i)} \\ \vdots \\ x_d^{(i)} \end{bmatrix}$$

For example, it could be the measurements the values of the d features for patient i . The set \mathcal{X} is called the feature space. Often, we have, $\mathcal{X} = \mathbb{R}^d$.

Let's look at data for one patient.

```
In [12]:  
diabetes_X.iloc[0]
```

Out[12]:

```
age      0.038076  
sex      0.050680  
bmi      0.061696  
bp       0.021872  
s1      -0.044223  
s2      -0.034821  
s3      -0.043401  
s4      -0.002592  
s5       0.019908  
s6      -0.017646  
Name: 0, dtype: float64
```

Training Dataset: Attributes

We refer to the numerical variables describing the patient as *attributes*. Examples of attributes include:

- The age of a patient.
- The patient's gender.
- The patient's BMI.

Note that the attributes in the above example have been mean-centered at zero and re-scaled to have a variance of one.

Training Dataset: Features

Often, an input object has many attributes, and we want to use these attributes to define more complex descriptions of the input.

- Is the patient old and a man? (Useful if old men are at risk).
- Is the BMI above the obesity threshold?

We call these custom attributes *features*.

Let's create an "old man" feature.

```
In [13]:
diabetes_X['old_man'] = (diabetes_X['sex'] > 0) & (diabetes_X['age'] > 0.05)
diabetes_X.head()
```

Out [13]:

| | age | sex | bmi | bp | s1 | s2 | s3 | s4 | |
|---|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|----------|
| 0 | 0.038076 | 0.050680 | 0.061696 | 0.021872 | -0.044223 | -0.034821 | -0.043401 | -0.002592 | 0.01990 |
| 1 | -0.001882 | -0.044642 | -0.051474 | -0.026328 | -0.008449 | -0.019163 | 0.074412 | -0.039493 | -0.06833 |
| 2 | 0.085299 | 0.050680 | 0.044451 | -0.005671 | -0.045599 | -0.034194 | -0.032356 | -0.002592 | 0.00286 |
| 3 | -0.089063 | -0.044642 | -0.011595 | -0.036656 | 0.012191 | 0.024991 | -0.036038 | 0.034309 | 0.02269 |
| 4 | 0.005383 | -0.044642 | -0.036385 | 0.021872 | 0.003935 | 0.015596 | 0.008142 | -0.002592 | -0.03199 |

Training Dataset: Features

More formally, we can define a function $\phi : \mathcal{X} \rightarrow \mathbb{R}^p$ that takes an input $x^{(i)} \in \mathcal{X}$ and outputs a p -dimensional vector

$$\phi(x^{(i)}) = \begin{bmatrix} \phi(x^{(i)})_1 \\ \phi(x^{(i)})_2 \\ \vdots \\ \phi(x^{(i)})_p \end{bmatrix}$$

We say that $\phi(x^{(i)})$ is a *featurized* input, and each $\phi(x^{(i)})_j$ is a *feature*.

Features vs Attributes

In practice, the terms attribute and features are often used interchangeably. Most authors refer to $x^{(i)}$ as a vector of features (i.e., they've been precomputed).

We will follow this convention and use attribute only when there is ambiguity between features and attributes.

Features: Discrete vs. Continuous

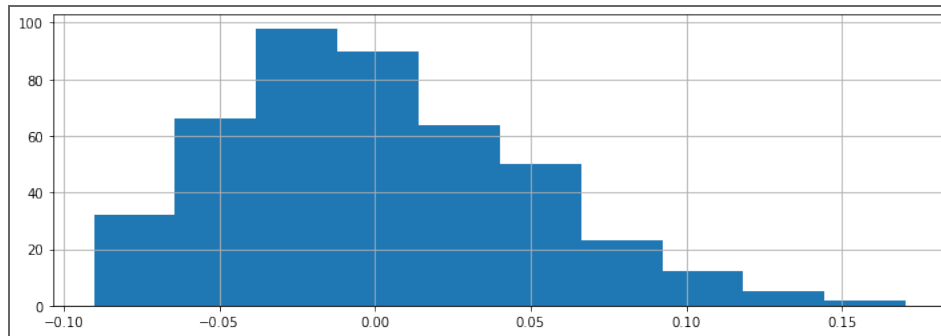
Features can be either discrete or continuous. We will see later that they may be handled differently by ML algorithms.

The BMI feature that we have seen earlier is an example of a continuous feature. We can visualize its distribution.

```
In [14]:  
diabetes_X.loc[:, 'bmi'].hist()
```

Out[14]:

<AxesSubplot:>



Other features take on one of a finite number of discrete values. The `sex` column is an example of a categorical feature.

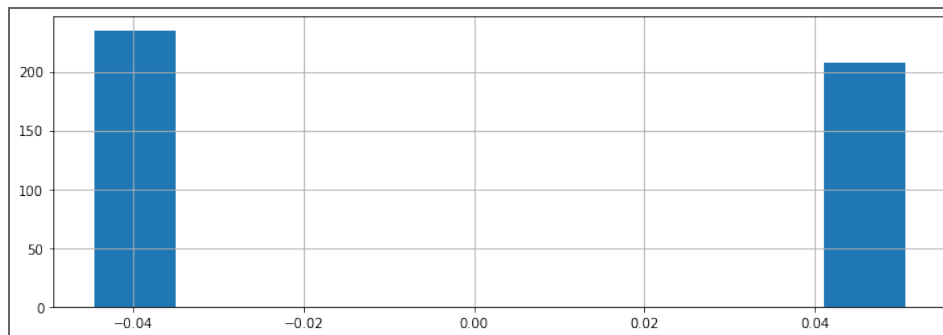
In this example, the dataset has been pre-processed such that the two values happen to be `0.05068012` and `-0.04464164`.

```
In [15]:  
print(diabetes_X.loc[:, 'sex'].unique())  
diabetes_X.loc[:, 'sex'].hist()
```

```
[ 0.05068012 -0.04464164]
```

Out[15]:

<AxesSubplot:>



Training Dataset: Targets

For each patient, we are interested in predicting a quantity of interest, the *target*. In our example, this is the patient's diabetes risk.

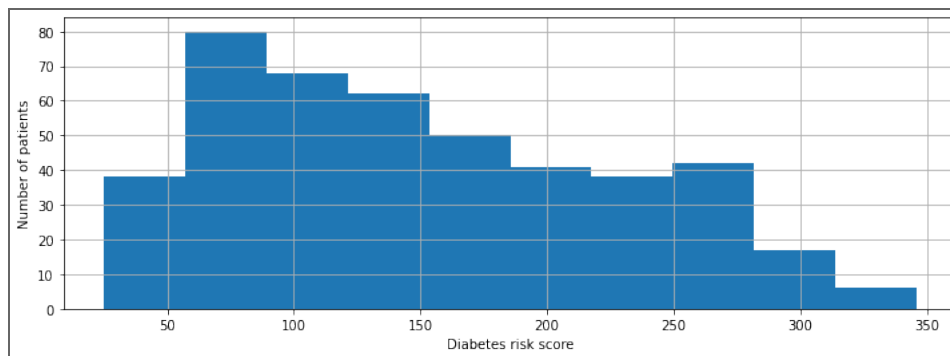
Formally, when $(x^{(i)}, y^{(i)})$ form a *training example*, each $y^{(i)} \in \mathcal{Y}$ is a target. We call \mathcal{Y} the target space.

We plot the distribution of risk scores below.

```
In [16]:  
plt.xlabel('Diabetes risk score')  
plt.ylabel('Number of patients')  
diabetes_y.hist()
```

Out[16]:

```
<AxesSubplot: xlabel='Diabetes risk score', ylabel='Number of patients'>
```



Targets: Regression vs. Classification

We distinguish between two broad types of supervised learning problems that differ in the form of the target variable.

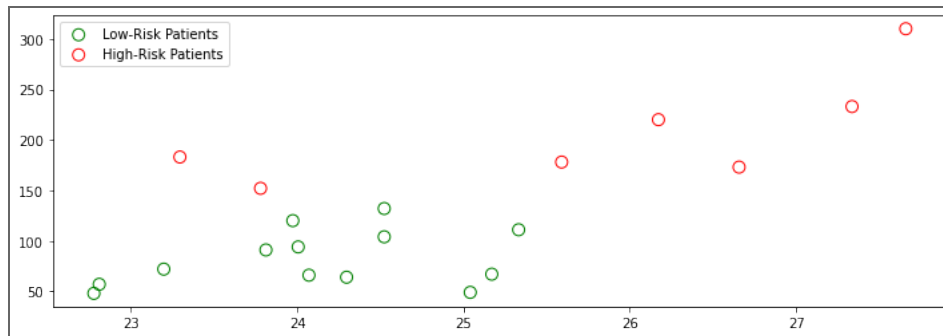
1. **Regression:** The target variable y is continuous. We are fitting a curve in a high-dimensional feature space that approximates the shape of the dataset.
2. **Classification:** The target variable y is discrete. Each discrete value corresponds to a *class* and we are looking for a hyperplane that separates the different classes.

We can easily turn our earlier regression example into classification by discretizing the diabetes risk scores into high or low.

```
In [17]:  
# Discretize the targets  
diabetes_y_train_discr = np.digitize(diabetes_y_train, bins=[150])  
  
# Visualize it  
plt.scatter(diabetes_X_train[diabetes_y_train_discr==0], diabetes_y_train[diabetes_y_train_discr==0], marker='o', s=80, facecolors='none', edgecolors='g')  
plt.scatter(diabetes_X_train[diabetes_y_train_discr==1], diabetes_y_train[diabetes_y_train_discr==1], marker='o', s=80, facecolors='none', edgecolors='r')  
plt.legend(['Low-Risk Patients', 'High-Risk Patients'])
```

Out[17]:

<matplotlib.legend.Legend at 0x125ffc240>



Let's try to generate predictions for this dataset.

```
In [18]:
# Create logistic regression object (note: this is actually a classification algorithm!)
clf = linear_model.LogisticRegression()

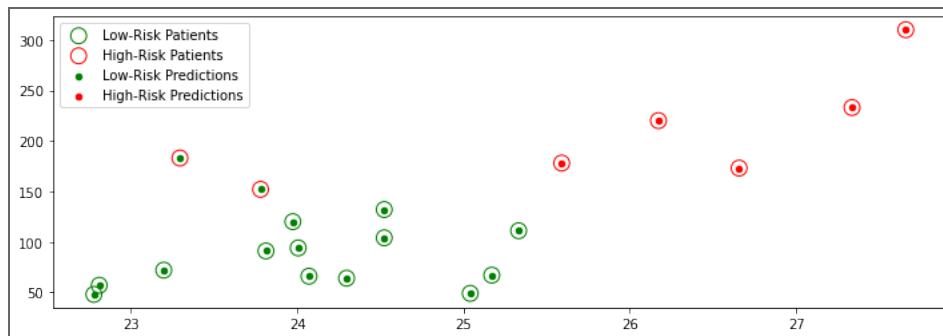
# Train the model using the training sets
clf.fit(diabetes_X_train, diabetes_y_train_discr)

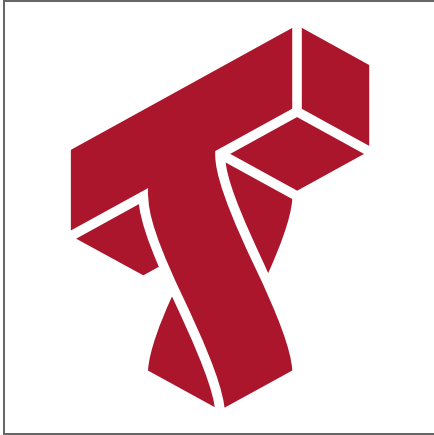
# Make predictions on the training set
diabetes_y_train_pred = clf.predict()

# Visualize it
plt.scatter(diabetes_X_train[diabetes_y_train_discr==0], diabetes_y_train[diabetes_y_train_discr==0], marker='o', s=140, facecolors='none', edgecolors='g')
plt.scatter(diabetes_X_train[diabetes_y_train_discr==1], diabetes_y_train[diabetes_y_train_discr==1], marker='o', s=140, facecolors='none', edgecolors='r')
plt.scatter(diabetes_X_train[diabetes_y_train_pred==0], diabetes_y_train[diabetes_y_train_pred==0], color='g', s=20)
plt.scatter(diabetes_X_train[diabetes_y_train_pred==1], diabetes_y_train[diabetes_y_train_pred==1], color='r', s=20)
plt.legend(['Low-Risk Patients', 'High-Risk Patients', 'Low-Risk Predictions', 'High-Risk Predictions'])
```

Out [18]:

<matplotlib.legend.Legend at 0x11847d320>





Part 3: Anatomy of a Supervised Learning Problem: Learning Algorithm

Let's now look at what a general supervised learning algorithm looks like.

Recall: Three Components of A Supervised Machine Learning Problem

At a high level, a supervised machine learning problem has the following structure:

$$\text{Dataset} + \text{Algorithm} \rightarrow \text{Predictive Model}$$

The predictive model is chosen to model the relationship between inputs and targets. For instance, it can predict future targets.

The Components of A Supervised Machine Learning Algorithm

We can also define the high-level structure of a supervised learning algorithm as consisting of three components:

- A **model class**: the set of possible models we consider.
- An **objective** function, which defines how good a model is.
- An **optimizer**, which finds the best predictive model in the model class according to the objective function

Let's look again at our diabetes dataset for an example.

```
In [19]:
import numpy as np
import pandas as pd
from sklearn import datasets
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [12, 4]

# Load the diabetes dataset
diabetes = datasets.load_diabetes(as_frame=True)
diabetes_X, diabetes_y = diabetes.data, diabetes.target

# Print part of the dataset
diabetes_X.head()
```

Out [19]:

| | age | sex | bmi | bp | s1 | s2 | s3 | s4 | |
|---|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|----------|
| 0 | 0.038076 | 0.050680 | 0.061696 | 0.021872 | -0.044223 | -0.034821 | -0.043401 | -0.002592 | 0.01990 |
| 1 | -0.001882 | -0.044642 | -0.051474 | -0.026328 | -0.008449 | -0.019163 | 0.074412 | -0.039493 | -0.06833 |
| 2 | 0.085299 | 0.050680 | 0.044451 | -0.005671 | -0.045599 | -0.034194 | -0.032356 | -0.002592 | 0.00286 |
| 3 | -0.089063 | -0.044642 | -0.011595 | -0.036656 | 0.012191 | 0.024991 | -0.036038 | 0.034309 | 0.02269 |
| 4 | 0.005383 | -0.044642 | -0.036385 | 0.021872 | 0.003935 | 0.015596 | 0.008142 | -0.002592 | -0.03199 |

Model: Notation

We'll say that a model is a function

$$f : \mathcal{X} \rightarrow \mathcal{Y}$$

that maps inputs $x \in \mathcal{X}$ to targets $y \in \mathcal{Y}$.

Often, models have *parameters* $\theta \in \Theta$ living in a set Θ . We will then write the model as

$$f_{\theta} : \mathcal{X} \rightarrow \mathcal{Y}$$

to denote that it's parametrized by θ .

Model Class: Notation

Formally, the model class is a set

$$\mathcal{M} \subseteq \{f \mid f: \mathcal{X} \rightarrow \mathcal{Y}\}$$

of possible models that map input features to targets.

When the models f_θ are parametrized by *parameters* $\theta \in \Theta$ living in some set Θ . Thus we can also write

$$\mathcal{M} = \{f_\theta \mid f: \mathcal{X} \rightarrow \mathcal{Y}; \theta \in \Theta\}.$$

Model Class: Example

One simple approach is to assume that x and y are related by a linear model of the form

$$y = \theta_0 + \theta_1 \cdot x_1 + \theta_2 \cdot x_2 + \dots + \theta_d \cdot x_d$$

where x is a featurized output and y is the target.

The θ_j are the *parameters* of the model.

Objectives: Notation

To capture this intuition, we define an *objective function* (also called a *loss function*)

$$J(f) : \mathcal{M} \rightarrow [0, \infty),$$

which describes the extent to which f "fits" the data $\mathcal{D} = \{(x^{(i)}, y^{(i)}) \mid i = 1, 2, \dots, n\}$.

When f is parametrized by $\theta \in \Theta$, the objective becomes a function $J(\theta) : \Theta \rightarrow [0, \infty)$.

Objective: Examples

What would be some possible objective functions? We will see many, but here are a few examples:

- Mean squared error:

$$J(\theta) = \frac{1}{2n} \sum_{i=1}^n \left(f_{\theta}(x^{(i)}) - y^{(i)} \right)^2$$

- Absolute (L1) error:

$$J(\theta) = \frac{1}{n} \sum_{i=1}^n |f_{\theta}(x^{(i)}) - y^{(i)}|$$

These are defined for a dataset $\mathcal{D} = \{(x^{(i)}, y^{(i)}) \mid i = 1, 2, \dots, n\}$.

```
In [60]:  
         from sklearn.metrics import mean_squared_error, mean_absolute_error  
  
y1 = np.array([1, 2, 3, 4])  
y2 = np.array([-1, 1, 3, 5])  
  
print('Mean squared error: %.2f' % mean_squared_error(y1, y2))  
print('Mean absolute error: %.2f' % mean_absolute_error(y1, y2))
```

```
Mean squared error: 1.50  
Mean absolute error: 1.00
```

Optimizer: Notation

At a high-level an optimizer takes an objective J and a model class \mathcal{M} and finds a model $f \in \mathcal{M}$ with the smallest value of the objective J .

$$\min_{f \in \mathcal{M}} J(f)$$

Intuitively, this is the function that bests "fits" the data on the training dataset.

When f is parametrized by $\theta \in \Theta$, the optimizer minimizes a function $J(\theta)$ over all $\theta \in \Theta$.

Optimizer: Example

We will see that behind the scenes, the `sklearn.linear_models.LinearRegression` algorithm optimizes the MSE loss.

$$\min_{\theta \in \mathbb{R}} \frac{1}{2n} \sum_{i=1}^n \left(f_{\theta}(x^{(i)}) - y^{(i)} \right)^2$$

We can easily measure the quality of the fit on the training set and the test set.

Let's run the above algorithm on our diabetes dataset.

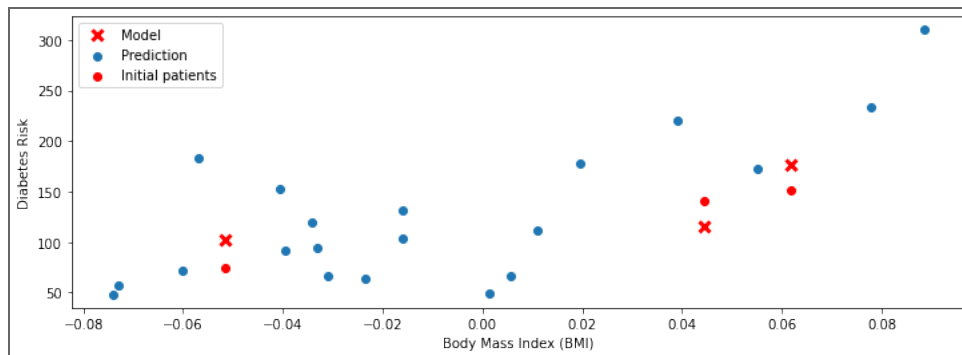
```
In [54]:  
# Collect 20 data points for training  
diabetes_X_train = diabetes_X.iloc[-20:]  
diabetes_y_train = diabetes_y.iloc[-20:]  
  
# Create linear regression object  
regr = linear_model.LinearRegression()  
  
# Train the model using the training sets  
regr.fit(diabetes_X_train, diabetes_y_train.values)  
  
# Make predictions on the training set  
diabetes_y_train_pred = regr.predict(diabetes_X_train)  
  
# Collect 3 data points for testing  
diabetes_X_test = diabetes_X.iloc[:3]  
diabetes_y_test = diabetes_y.iloc[:3]  
  
# generate predictions on the new patients  
diabetes_y_test_pred = regr.predict(diabetes_X_test)
```

The algorithm returns a predictive model. We can visualize its predictions below.

```
In [55]:  
# visualize the results  
plt.xlabel('Body Mass Index (BMI)')  
plt.ylabel('Diabetes Risk')  
plt.scatter(diabetes_X_train.loc[:, 'bmi'], diabetes_y_train)  
plt.scatter(diabetes_X_test.loc[:, 'bmi'], diabetes_y_test, color='red', marker='o')  
# plt.scatter(diabetes_X_train.loc[:, 'bmi'], diabetes_y_train_pred, color='black', linewidth=1)  
plt.plot(diabetes_X_test.loc[:, 'bmi'], diabetes_y_test_pred, 'x', color='red', mew=3, markersize=8)  
plt.legend(['Model', 'Prediction', 'Initial patients', 'New patients'])
```

Out [55]:

<matplotlib.legend.Legend at 0x12f6a46a0>



Summary: Components of A Supervised Machine Learning Problem

At a high level, a supervised machine learning problem has the following structure:

$$\text{Dataset} + \underbrace{\text{Algorithm}}_{\text{Model Class} + \text{Objective} + \text{Optimizer}} \rightarrow \text{Predictive Model}$$

The predictive model is chosen to model the relationship between inputs and targets. For instance, it can predict future targets.

In []: