```
1 //
   2 const double PI = acos(-1.0);
   3 const double deg rad = PI / 180.0;
   5 class Qua {//Quaterion
  6 public:
   7
                       Qua() {}
  8
  9
                       Qua(double t, double x, double y, double z) : t(t), x(x)
          ), y(y), z(z) {}
10
11
                       double t, x, y, z;
12
13
                       Qua inv() {
14
                                     return Qua(t, -x, -y, -z);
15
16
17
                       friend Qua operator*(Qua l, Qua r) {
18
                                    Qua ans;
                                    ans.t = l.t * r.t - l.x * r.x - l.y * r.y - l.z * r
19
          .Z;
20
                                    ans.x = l.t * r.x + l.x * r.t + l.y * r.z - l.z * r
          у,
21
                                    ans.y = l.t * r.y + l.y * r.t + l.z * r.x - l.x * r
          .Z;
22
                                    ans.z = l.t * r.z + l.z * r.t + l.x * r.y - l.y * r
          .х,
23
                                    return ans;
24
                       }
25
26 };
27
28
29 class Point3 {
30 public:
31
                       Point3() {}
32
33
                       Point3(double x, double y, double z) : x(x), y(y), z(z)
             {}
34
35
                       double x, y, z;
36
37
                       double dis to(Point3 b) {
                                     return sqrt((x - b.x) * (x - b.x) + (y - b.y) * (y
38
                b_y) + (z - b_z) * (z - b_z);
39
40
41
                       double length() {
                                     return dis_to(Point3(0, 0, 0));
42
43
                       }
```

```
44
45
       friend Point3 operator+(Point3 l, Point3 r) {
46
           return Point3(l.x + r.x, l.y + r.y, l.z + r.z);
47
       };
48
49
       friend Point3 operator-(Point3 l, Point3 r) {
50
           return Point3(l.x - r.x, l.y - r.y, l.z - r.z);
51
       };
52
53
       Point3 operator*(double b) {
54
           return Point3(x * b, y * b, z * b);
55
       }
56
57
       friend double operator*(Point3 l, Point3 r) {
58
           return l.x * r.x + l.y * r.y + l.z * r.z;
59
       };
60
61
       //叉乘
62
       Point3 cross(Point3 r) {
           return Point3(y * r_1z - z * r_1y, z * r_1x - x * r_1z,
63
    x * r_{y} - y * r_{x};
       }
64
65
66
       Point3 unit() {
67
           double len = length();
68
           return Point3(x / len, y / len, z / len);
       }
69
70
71
       void debug() {
72
           printf("(%lf,\t%lf,\t%lf)\n", x, y, z);
73
       }
74
75 };
76
77 class Segment {
78 public:
79
80
       Point3 u, v;
81
82
       Segment() {};
83
84
       Segment(Point3 u, Point3 v) : u(u), v(v) {};
85
       double dis_to(Point3 x) {
86
           if (((x - u) * (v - u)) * ((x - v) * (v - u)) <= 0)
87
    {
88
               return ((x - u).cross(v - u)).length() / (v - u)
   ).length();
89
           } else {
90
               return min(x.dis_to(u), x.dis_to(v));
```

```
91
 92
        }
 93
 94
        double dis_to(Segment b){
 95
            if((v-u).cross(b.v-b.u).length()<=EPS){</pre>
 96
 97
            }
        }
 98
99
100 };
101
102 class Point3r {
103 public:
104
        Point3r() {}
105
106
        Point3r(double phi, double theta, double r) : phi(phi)
    , theta(theta), r(r) {}
107
108
        double phi, theta, r;//x-axis[-pi,pi] z-axis[0,pi]
    radius
109
110
        Point3 to_xyz() {
111
            Point3 re;
112
            re.z = cos(theta) * r;
113
            double xy = sin(theta) * r;
            re.x = cos(phi) * xy;
114
115
            re_y = sin(phi) * xy;
116
            return re;
117
        }
118 };
119
120 class Point3jw {
121 public:
122
        Point3jw() {}
123
124
        Point3jw(double lo, double la, double r) : lo(lo), la(
    la), r(r) {}
125
126
        double lo, la, r;//longitude[-180,180] latitude[-90,90
    ] radius
127
128
        Point3 to_xyz() {
129
            Point3 re:
            re_z = cos((90 - la) * deg_rad) * r;
130
            double xy = sin((90 - la) * deg_rad) * r;
131
            re.x = cos(lo * deg rad) * xy;
132
133
            re.y = sin(lo * deg_rad) * xy;
134
            return re;
135
        }
136 };
```