大数据计算及应用(十二)

Mining Data Streams

Agenda

High dim. data

Locality sensitive hashing

Clustering

Dimensiona lity reduction

Graph data

PageRank, SimRank

Community Detection

Spam Detection

Infinite data

Filtering data streams

Web advertising

Queries on streams

Machine learning

SVM

Decision Trees

Perceptron, kNN

Apps

Recommen der systems

Association Rules

Duplicate document detection

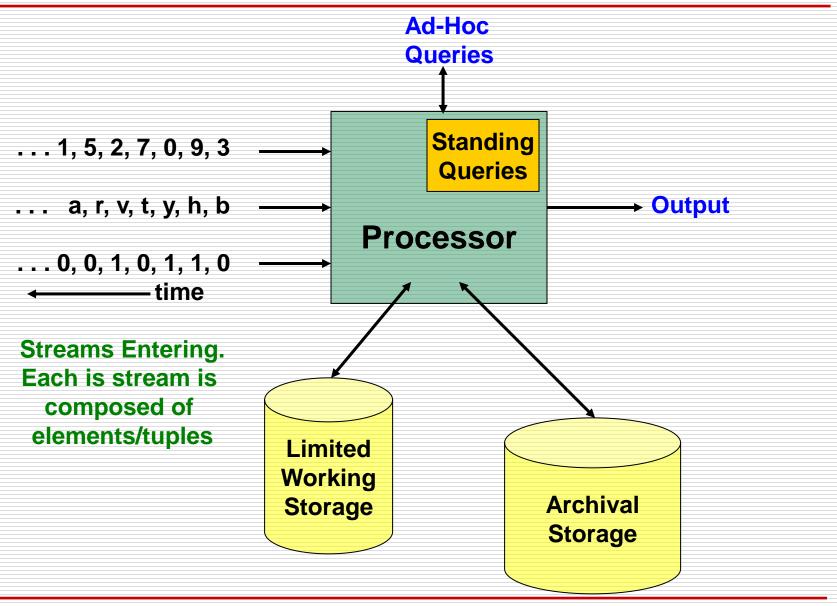
Data Streams

- In many data mining situations, we do not know the entire data set in advance
- Stream Management is important when the input rate is controlled externally:
 - Google queries
 - Twitter or Facebook status updates
- We can think of the data as infinite and non-stationary (the distribution changes over time)

The Stream Model

- Input elements enter at a rapid rate, at one or more input ports (i.e., streams)
 - We call elements of the stream tuples
- The system cannot store the entire stream accessibly
- Q: How do you make critical calculations about the stream using a limited amount of (secondary) memory?

General Stream Processing Model



Problems on Data Streams

- □ Types of queries one wants to answer on a data stream:
 - Sampling data from a stream
 - Construct a random sample
 - Queries over sliding windows
 - Number of items of type x in the last k elements of the stream

Applications (1)

☐ Mining query streams

 Google wants to know what queries are more frequent today than yesterday

■ Mining click streams

Yahoo wants to know which of its pages are getting an unusual number of hits in the past hour

■ Mining social network news feeds

E.g., look for trending topics on Twitter, Facebook

Applications (2)

Sensor Networks

Many sensors feeding into a central controller

☐ Telephone call records

 Data feeds into customer bills as well as settlements between telephone companies

□ IP packets monitored at a switch

- Gather information for optimal routing
- Detect denial-of-service attacks

Sampling from a Data Stream: Sampling a fixed proportion

As the stream grows the sample also gets bigger

Sampling from a Data Stream

- Since we can not store the entire stream, one obvious approach is to store a sample
- ☐ Two different problems:
 - (1) Sample a fixed proportion of elements in the stream (say 1 in 10)
 - (2) Maintain a random sample of fixed size over a potentially infinite stream
 - □ At any "time" k we would like a random sample of s elements
 - What is the property of the sample we want to maintain? For all time steps *k*, each of *k* elements seen so far has equal prob. of being sampled

Sampling a Fixed Proportion

- □ Problem 1: Sampling fixed proportion
- Scenario: Search engine query stream
 - Stream of tuples: (user, query, time)
 - Answer questions such as: How often did a user run the same query in a single day
 - Have space to store 1/10th of query stream
- Naïve solution:
 - Generate a random integer in [0..9] for each query
 - Store the query if the integer is 0, otherwise discard

Problem with Naïve Approach

- □ Simple question: What fraction of queries by an average search engine user are duplicates?
 - Suppose each user issues x queries once and d queries twice (total of x+2d queries)
 - □ Correct answer: d/(x+d)
 - Proposed solution: We keep 10% of the queries
 - □ Sample will contain x/10 of the singleton queries and
 2d/10 of the duplicate queries at least once
 - ☐ But only **d/100** pairs of duplicates
 - d/100 = $1/10 \cdot 1/10 \cdot d$
 - ☐ Of *d* "duplicates" *18d/100* appear exactly once
 - $18d/100 = ((1/10 \cdot 9/10) + (9/10 \cdot 1/10)) \cdot d$
 - So the sample-based answer is $\frac{\frac{a}{100}}{\frac{x}{10} + \frac{d}{100} + \frac{18d}{100}} = \frac{d}{10x + 19d}$

Solution: Sample Users

Solution:

- ☐ Pick **1/10**th of **users** and take all their searches in the sample
- Use a hash function that hashes the user name or user id uniformly into 10 buckets

Generalized Solution

- ☐ Stream of tuples with keys:
 - Key is some subset of each tuple's components
 - e.g., tuple is (user, search, time); key is user
 - Choice of key depends on application
- \square To get a sample of a/b fraction of the stream:
 - Hash each tuple's key uniformly into b buckets
 - Pick the tuple if its hash value is at most a



Hash table with b buckets, pick the tuple if its hash value is at most a. How to generate a 30% sample?

Hash into b=10 buckets, take the tuple if it hashes to one of the first 3 buckets

Sampling from a Data Stream: Sampling a fixed-size sample

As the stream grows, the sample is of fixed size

Maintaining a fixed-size sample

- ☐ Problem 2: Fixed-size sample
- □ Suppose we need to maintain a random sample S of size exactly s tuples
 - E.g., main memory size constraint
- Why? Don't know length of stream in advance
- ☐ Suppose at time *n* we have seen *n* items
 - Each item is in the sample S with equal prob. s/n

How to think about the problem: say s = 2

Stream: a x c y z k c d e g...

At n= 5, each of the first 5 tuples is included in the sample S with equal prob.

At n= 7, each of the first 7 tuples is included in the sample S with equal prob.

Impractical solution would be to store all the *n* tuples seen so far and out of them pick *s* at random

Solution: Fixed Size Sample

- ☐ Algorithm (a.k.a. Reservoir Sampling)
 - Store all the first s elements of the stream to S
 - Suppose we have seen n elements, and now the n+1th element arrives (n+1>s)
 - \square With probability s/(n+1), keep the $n+1^{th}$ element, else discard it
 - If we picked the n+1th element, then it replaces one of the s elements in the sample s, picked uniformly at random
- Claim: This algorithm maintains a sample S with the desired property:
 - After n elements, the sample contains each element seen so far with probability s/n

Proof: By Induction

■ We prove this by induction:

- Assume that after n elements, the sample contains each element seen so far with probability s/n
- We need to show that after seeing element n+1 the sample maintains the property
 - □ Sample contains each element seen so far with probability s/(n+1)

☐ Base case:

- After we see n=s elements the sample S has the desired property
 - Each out of n=s elements is in the sample with probability s/s = 1

Proof: By Induction

- □ Inductive hypothesis: After n elements, the sample S contains each element seen so far with prob. s/n
- Now element n+1 arrives
- ☐ Inductive step: For elements already in S, probability that the algorithm keeps it in S is:

$$\left(1 - \frac{s}{n+1}\right) + \left(\frac{s}{n+1}\right)\left(\frac{s-1}{s}\right) = \frac{n}{n+1}$$

Element n+1 discarded

Element n+1 Element in the not discarded sample not picked

- So, at time *n*, tuples in *S* were there with prob. s/n
- \square Time $n \rightarrow n+1$, tuple stayed in S with prob. n/(n+1)
- \square So prob. tuple is in **S** at time $n+1 = \frac{s}{n} \cdot \frac{n}{n+1} = \frac{s}{n+1}$

Queries over a (long) Sliding Window

Sliding Windows

- A useful model of stream processing is that queries are about a window of length N – the N most recent elements received
- ☐ Interesting case: N is so large that the data cannot be stored in memory, or even on disk
 - Or, there are so many streams that windows for all cannot be stored
- ☐ Amazon example:
 - For every product X we keep 0/1 stream of whether that product was sold in the n-th transaction
 - We want answer queries, how many times have we sold
 X in the last k sales

Sliding Window: 1 Stream

☐ Sliding window on a single stream:

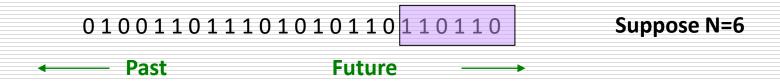
N = 6

Counting Bits (1)

- ☐ Problem:
 - Given a stream of 0s and 1s
 - Be prepared to answer queries of the form How many 1s are in the last k bits? where k ≤ N
- ☐ Obvious solution:

Store the most recent **N** bits

■ When new bit comes in, discard the **N+1**st bit

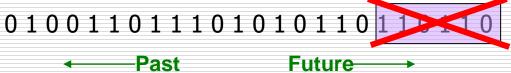


Counting Bits (2)

- ☐ You can not get an exact answer without storing the entire window
- ☐ Real Problem:

What if we cannot afford to store N bits?

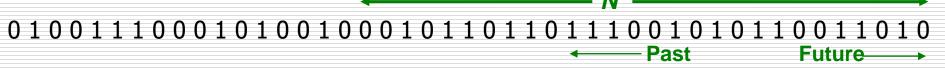
E.g., we're processing 1 billion streams andN = 1 billion



But we are happy with an approximate answer

An attempt: Simple solution

- Q: How many 1s are in the last N bits?
- A simple solution that does not really solve our problem: Uniformity assumption



- Maintain 2 counters:
 - **S**: number of 1s from the beginning of the stream
 - **Z**: number of 0s from the beginning of the stream
- ☐ How many 1s are in the last N bits? $N \cdot \frac{S}{S+Z}$
- But, what if stream is non-uniform?
 - What if distribution changes over time?

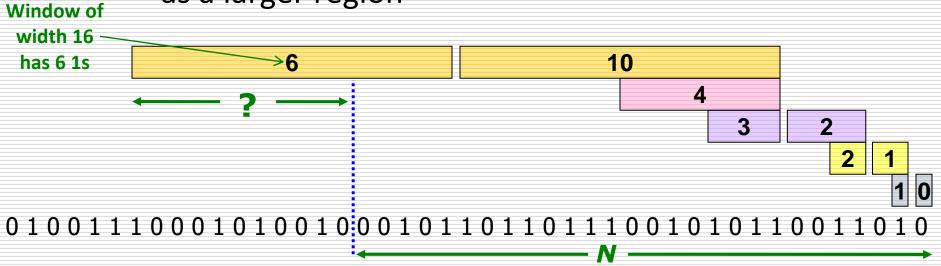
DGIM Method

[Datar, Gionis, Indyk, Motwani]

- □ DGIM solution that does <u>not</u> assume uniformity
- \square We store $O(\log^2 N)$ bits per stream
- □ Solution gives approximate answer, never off by more than 50%
 - Error factor can be reduced to any fraction > 0, with more complicated algorithm and proportionally more stored bits

Idea: Exponential Windows

- ☐ Solution that doesn't (quite) work:
 - Summarize exponentially increasing regions of the stream, looking backward
 - Drop small regions if they begin at the same point as a larger region



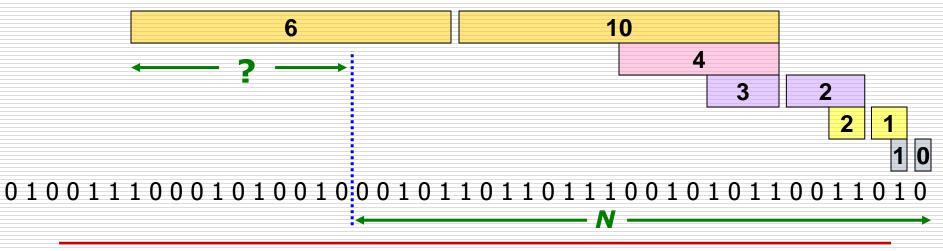
We can reconstruct the count of the last N bits, except we are not sure how many of the last 6 1s are included in the N

What's Good?

- ☐ Easy update as more bits enter
- ☐ Error in count no greater than the number of **1s** in the "**unknown**" area

What's Not So Good?

- As long as the 1s are fairly evenly distributed, the error due to the unknown region is small – no more than 50%
- But it could be that all the 1s are in the unknown area at the end
- □ In that case, the error is unbounded!



Fixup: DGIM method

[Datar, Gionis, Indyk, Motwani]

- Idea: Instead of summarizing fixed-length blocks, summarize blocks with specific number of 1s:
 - Let the block sizes (number of 1s) increase exponentially
- □ When there are few 1s in the window, block sizes stay small, so errors are small

DGIM: Timestamps

- Each bit in the stream has a timestamp, starting 1, 2, ...
- \square Record timestamps modulo N (the window size), so we can represent any relevant timestamp in $O(log_2N)$ bits

DGIM: Buckets

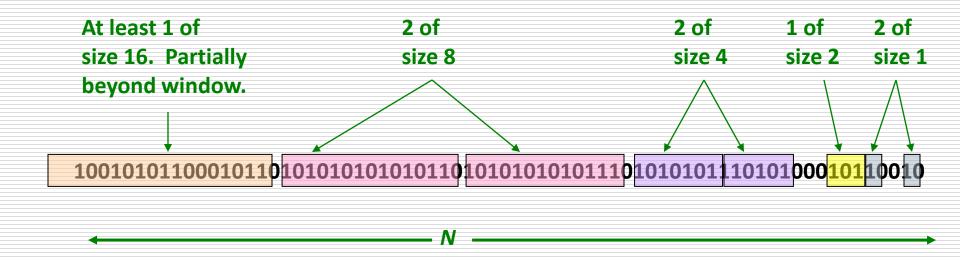
- A bucket in the DGIM method is a record consisting of:
 - (A) The timestamp of its end [O(log N) bits]
 - (B) The number of 1s between its beginning and end [O(log log N) bits]
- Constraint on buckets:
 - Number of 1s must be a power of 2
 - That explains the O(log log N) in (B) above



Representing a Stream by Buckets

- □ Either one or two buckets with the same power-of-2 number of 1s
- Buckets do not overlap in timestamps
- Buckets are sorted by size
 - Earlier buckets are not smaller than later buckets
- Buckets disappear when their end-time is > N time units in the past

Example: Bucketized Stream



Three properties of buckets that are maintained:

- Either one or two buckets with the same power-of-2 number of 1s
- Buckets do not overlap in timestamps
- Buckets are sorted by size

Updating Buckets (1)

- □ When a new bit comes in, drop the last (oldest) bucket if its end-time is prior to N time units before the current time
- 2 cases: Current bit is 0 or 1
- ☐ If the current bit is 0: no other changes are needed

Updating Buckets (2)

- ☐ If the current bit is 1:
 - (1) Create a new bucket of size 1, for just this bit End timestamp = current time
 - (2) If there are now three buckets of size 1, combine the oldest two into a bucket of size 2
 - (3) If there are now three buckets of size 2, combine the oldest two into a bucket of size 4
 - (4) And so on ...

Example: Updating Buckets

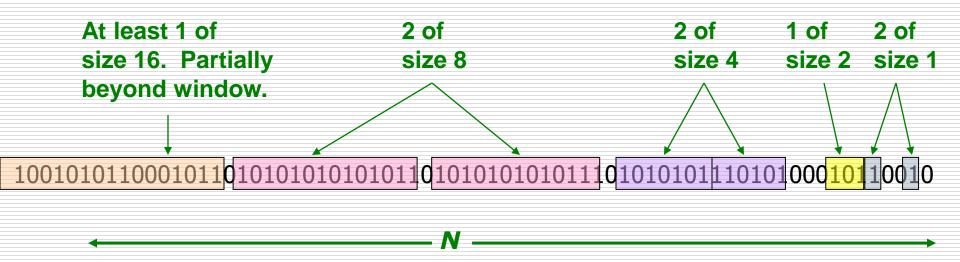
Current state of the stream: Bit of value 1 arrives Two orange buckets get merged into a yellow bucket Next bit 1 arrives, new grey bucket is created, then 0 comes, then 1: Buckets get merged... State of the buckets after merging

How to Query?

- □ To estimate the number of 1s in the most recent N bits:
 - 1. Sum the sizes of all buckets but the last (note "size" means the number of 1s in the bucket)
 - 2. Add half the size of the last bucket

Remember: We do not know how many 1s of the last bucket are still within the wanted window

Example: Bucketized Stream



Error Bound: Proof

- ☐ Why is error 50%? Let's prove it!
- ☐ Suppose the last bucket has size **2**^r
- ☐ Then by assuming 2^{r-1} (i.e., half) of its 1s are still within the window, we make an error of at most 2^{r-1}
- \square Since there is at least one bucket of each of the sizes less than 2^r , the true sum is at least

$$1 + 2 + 4 + ... + 2^{r-1} = 2^r - 1$$

☐ Thus, error at most **50**%

At least 16 1s

Further Reducing the Error

- Instead of maintaining $\mathbf{1}$ or $\mathbf{2}$ of each size bucket, we allow either $r-\mathbf{1}$ or r buckets (r > 2)
 - Except for the largest size buckets; we can have any number between 1 and r of those
- \square Error is at most O(1/r)
- By picking r appropriately, we can tradeoff between number of bits we store and the error

Extensions

- \square Can we use the same trick to answer queries How many 1's in the last k? where k < N?
 - A: Find earliest bucket B that at overlaps with k. Number of 1s is the sum of sizes of more recent buckets + ½ size of B

□ Can we handle the case where the stream is not bits, but integers, and we want the sum of the last *k* elements? 课堂作业

Extensions

- ☐ Stream of positive integers
- \square We want the sum of the last k elements
 - Amazon: Avg. price of last k sales
- ☐ Solution:
 - If you know all have at most m bits
 - Treat m bits of each integer as a separate stream
 - Use DGIM to count 1s in each integer
 - \square The sum is $=\sum_{i=0}^{m-1} c_i 2^i$ c_i ... estimated count for i-th bit

Summary

- Sampling a fixed proportion of a stream
 - Sample size grows as the stream grows
- Sampling a fixed-size sample
 - Reservoir sampling
- Counting the number of 1s in the last N elements
 - Exponentially increasing windows
 - Extensions:
 - Number of 1s in any last k (k < N) elements</p>
 - Sums of integers in the last N elements

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