ENG1005 S2 2024 Workshop 1 Concentrated solar thermal (CST)

18 marks total

This problem set is intended for you to apply the mathematical skills you are learning. It is also designed to practice communicating your work clearly.

It is expected that you will use the workshop to develop (rough) solutions. During the workshop, you should discuss the problems with your peers and the academic staff who are there to assist you. In particular, if you are uncertain about what the problems are asking or you are stuck on a particular point, this is the time to get assistance. The time between the end of the workshop and when the solutions are due is only meant to be for writing up your solutions and for this you should not need more than an hour or two at most.

General submission information:

- 1. Electronic submission of your solutions is due on Moodle by 11:55 pm on Sunday of the same week.
- 2. Your solutions should include a description/explanation of what you are doing at each step and relevant working. Without these you will receive limited marks. The description should be in complete English sentences. All mathematics should be appropriately laid out and with appropriate notation. Your writing should be similar in style to the worked solutions from the Applied Class problem sheets, not the annotations from the videos. For more information and advice, please read the "Guidelines for writing in mathematics" document posted under the "Additional information and resources" section of the ENG1005 Moodle page.
- 3. Your solutions may be typed or handwritten and scanned (the latter is encouraged). The final document should be submitted as a <u>single pdf file</u> that is clearly and easily legible. If the marker is unable to read it (or any part of it) you may lose marks.

Academic integrity:

You can (and should!) discuss your solutions with the other students, but **you must write up your solutions by yourself**. Copying solutions is serious academic misconduct and will be penalised according to Monash University guidelines. Other examples of academic misconduct include asking a personal tutor to do any of your assessments and posting your assessments to a "homework" website. Please refer back to your Academic Integrity module if you are in any doubt about what constitutes academic misconduct. **Your integrity is an important part of who you are. It is much more important than any grade you could receive.**

Concentrated solar thermal (CST)

Concentrated solar thermal is one approach to combat the problem of intermittency in solar power generation. The idea is to focus the sun's rays from a broad area onto a single collector to heat molten salt (or another material). This heat can then be stored for later use to generate steam and drive turbines when the sun isn't shining, complementing the use of photovoltaics. In this workshop, you will explore how the sun's rays can be focused onto a collector using an array of plane mirrors (as shown in the image below; a similar plant is being developed near Port Augusta, SA, and others are planned around Australia)



By National Renewable Energy Laboratory https://commons.wikimedia.org/w/index.php?curid=1455806

The physical laws for reflection in a mirror are the following:

- The reflected light ray is in the same plane as the incident (i.e. incoming) ray and the normal to the mirror.
- The angle between the reflected ray and the normal to the mirror (the angle of reflection) is the same as that between the incident ray and the normal to the mirror (the angle of incidence). This is usually stated as "the angle of reflection is equal to the angle of incidence".

If $\hat{\mathbf{a}}_i$ is a unit vector in the direction of an *incoming* light ray onto a plane mirror with normal $\hat{\mathbf{n}}$, then the mirror reflection law says that the direction of the reflected ray $\hat{\mathbf{a}}_r$ is given by

$$\hat{\mathbf{a}}_r = \hat{\mathbf{a}}_i - 2(\hat{\mathbf{a}}_i \cdot \hat{\mathbf{n}})\hat{\mathbf{n}}.$$

Here both $\hat{\mathbf{a}}_i$ and $\hat{\mathbf{a}}_r$ are pointing in the direction that the light ray is travelling towards, and $\hat{\mathbf{n}}$ is the unit normal vector pointing away from the surface of the mirror.

- Q1: Make a diagram that illustrates the physical setup which includes the mirror, the light ray before and after reflection. Clearly label the vectors $\hat{\mathbf{n}}$, $\hat{\mathbf{a}}_i$ and $\hat{\mathbf{a}}_r$ on your diagram. [2 marks]
- **Q2**: On the same diagram, clearly label the angle of incidence θ_i and the angle of reflection θ_r . [1 mark]
- Q3: Verify that if $\hat{\mathbf{a}}_r$ is given by the above formula, then the two physical laws are satisfied. [4 marks]

As the sun travels across the sky, the mirrors need to be rotated to ensure that they continue to reflect the light onto the collector. You will now investigate how to adjust the position of an individual mirror.

Choose the coordinate system such that the x-axis is aligned due East, the y-axis due North, the z-axis vertically upwards, and the centre of the mirror is located at the origin. In its initial resting position, the mirror has its normal pointing due East. Suppose that in this coordinate system, the sun appears to be in the direction of the vector (10, 2, 11).

- Q4 Write down the unit normal vector $\hat{\mathbf{n}}$ to the mirror in its resting position. [1 mark]
- Q5 Write down the unit vector $\hat{\mathbf{a}}_i$ of the *incoming* sunlight. [1 mark]
- Q6 Calculate the unit vector $\hat{\mathbf{a}}_r$ of the reflected light ray. [2 marks]
- **Q7** Suppose the collector is located at the position (-100, 100, 50), will the reflected light ray hit the collector? Justify your answer. [1 mark]
- Q8 The mirror is rotated so that the reflected light ray will hit the collector. Calculate the unit normal vector $\hat{\mathbf{n}}$ to the mirror in this position. [4 marks]

There is also 1 additional mark given for the quality of the English and 1 additional mark for correct mathematical notation. These marks are easy to obtain but the markers will be instructed to be strict in awarding these marks.