

Given function,  $f(x) = x^3 + 2x^2 - x - 2$

$$(1) \quad x^3 + 2x^2 - x - 2 = 0$$

$$\Rightarrow x = x^3 + 2x^2 - 2$$

$$\Rightarrow g(x) = x^3 + 2x^2 - 2$$

$$(2) \quad g(x) = x^3 + 2x^2 - 2$$

Starting from  $x_0 = 0$ , we get,

$$g(0) = -2$$

$$g(-2) = -2$$

$$(3) \quad \text{error} = |-2 - (-2)| = |-2 + 2| = 0$$

P.T.D



④

$$g(x) = x^3 + 2x^2 - 2$$

$$\Rightarrow g'(x) = 3x^2 + 4x$$

$$\begin{aligned}\Rightarrow g'(-2) &= 3(-2)^2 + 4(-2) \\ &= 4\end{aligned}$$

⑤  $g(x) = \frac{2}{x^2 + 2x - 1}$

$$\Rightarrow g'(x) = -\frac{4(x+1)}{(x^2 + 2x - 1)^2}$$

$$\begin{aligned}\Rightarrow g'(-1) &= -\frac{4(-1+1)}{\{(-1)^2 + 2(-1) - 1\}^2} \\ &= 0\end{aligned}$$

And hence, we got a super linear convergence