YAGS Yet Another Graph System GAP4 Package

Version 0.0.1 by

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Preface

1.1 Welcome to YAGS

Welcome to YAGS.
which is great and have a lot of work over the years.
Our motivation here was this and that.
Our Pourposes and Aim.
authors, contacts

1.2 Citing YAGS

Please cite us like this: \dots

1.3 More Information

web page, distribution list, github

1.4 License and Copyright

GPL V3

Getting Started

2.1 What is YAGS?

blah, blah, blah

2.2 Installing YAGS

blah, blah, blah

2.3 Testing the Installation

blah, blah, blah

2.4 A Gentle Tutorial

blah, blah, blah

2.5 An Overview of the Manual

blah, blah, blah

2.6 Cheatsheet

blah, blah, blah

2.7 ——- Old Sections Bellow —-

YAGS (Yet Another Graph System) is a system designed to aid in the study of graphs. Therefore it provides functions designed to help researchers in the field of graph theory. This chapter is intended as a gentle tutorial on working with YAGS (some knowledge of GAP and the basic use of a computer are assumed). The tutorial is divided as follows:

- Using YAGS
- Definition of a graph
- A taxonomy of graphs
- Creating graphs

gap> RequirePackage("yags");

2.8 Using YAGS

YAGS is a GAP package an as such the RequirePackage directive is used to start YAGS

```
Loading YAGS 0.0.1 (Yet Another Graph System),
by R. MacKinney, M.A. Pizana and R. Villarroel-Flores
```

rene@xamanek.izt.uam.mx, map@xamanek.izt.uam.mx, rvf0068@gmail.com

true

Once the package has been loaded help can be obtained at anytime using the GAP help facility. For instance get help on the function *PathGraph*:

2.9 Definition of graphs

A graph is defined as follows. A graph G is a set of vertices V and a set of edges (arrows) E, $G = \{V, E\}$. The set of edges is a set of tuples of vertices (v_i, v_j) that belong to $V, v_i, v_j \in V$ representing that v_i, v_j are adjacent.

For instance, $(\{1,2,3,4\},\{(1,3),(2,4),(3,2)\})$ is a graph with four vertices such that vertices 1 and 2 are adjacent to vertex 3 and vertex 2 is adjacent to vertex 4. Visually this can be seen as



The adjacencies can also be represented as a matrix. This would be a boolean matrix M where two vertices i, j are adjacent if M[i, j] = true and not adjacent otherwise.

Given two vertices i, j in graph G we will say that graph G has an **edge** $\{i, j\}$ if there is an arrow (i, j) and and arrow (j, i).

If a graph G has an arrow that starts and finishes on the same vertex we say that graph G has a loop.



YAGS handles graphs that have arrows, edges and loops. Graphs that, for instance, have multiple arrows between vertices are not handled by YAGS.



2.10 A taxonomy of graphs

There are several ways of characterizing graphs. YAGS uses a category system where any graph belongs to a specific category. The following is the list of graph categories in YAGS.

• Graphs: graphs with no particular property.



• Loopless: graphs with no loops.



• Undirected: graphs with no arrows but only edges.



• Oriented: graphs with no edges but only arrows.



• SimpleGraphs: graphs with no loops and only edges.



The following figure shows the relationships among categories.

Graphs

Loopless Undirected

Oriented Simple Graphs

Figure 1: Graph Categories

YAGS uses the category of a graph to normalize it. This is helpful, for instance, when we define an undirected graph and inadvertently forget an arrow in its definition. The category of a graph can be given explicitly or implicitly. To do it explicitly the category must be given when creating a graph, as can be seen in the section 2.11. If no category is given the category is assumed to be the *DefaultCategory*. The default category can be changed at any time using the *SetDefaultCategory* function.

Further information regarding categories can be found on chapter 4.

2.11 Creating Graphs

There exist several ways to create a graph in YAGS. First, a GAP record can be used. To do so the record has to have either of

- Adjacency List
- Adjacency Matrix

in the graph presented in Section 2.9 the adjacency list would be

and the adjacency matrix

To create a graph YAGS we also need the category the graph belongs to. We give this information to the *Graph* function. For instance to create the graph using the adjacency list we would use the following command:

```
gap> g:=Graph(rec(Category:=OrientedGraphs,Adjacencies:=[[],[4],[1,2],[]]));
Graph( Category := OrientedGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ ], [ 4 ], [ 1, 2 ], [ ] ])
```

This will create a graph g that represents the graph in Section 2.9.



Since the *DefaultCategory* is *SimpleGraphs* when YAGS starts up and the graph we have been using as an example is oriented we must explicitly give the category to YAGS. This is achieved using *Category:=OrientedGraphs* inside the record structure.

The same graph can be created using the function *GraphByAdjacencies* as in

```
gap> g:=GraphByAdjacencies([[],[4],[1,2],[]]:Category:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ ], [ 4 ], [ 1, 2 ], [ ] ] )
```

In this case to explicitly give the Category of the graph we use the construction : Category:=OrientedGraphs inside the function. This construction can be used in any function to explicitly give the category of a graph.

We said previously we can also use the adjacency matrix to create a graph. For instance the command

Creates the same graph. Note that we explicitly give the graph category as before. We also can use the command AdjMatrix as in

If we create the graph using any of the methods so far described omitting the graph category YAGS will create a graph normalized to the *DefaultCategory* which by default is *SimpleGraphs*

```
gap> g:=GraphByAdjacencies([[],[4],[1,2],[]];
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 3 ], [ 3, 4 ], [ 1, 2 ], [ 2 ] ] )
```

Which creates a graph with only edges



There are many functions to create graphs, some from existing graphs and some create interesting well known graphs.

Among the former we have the function AddEdges which adds edges to an existing graph

```
gap> g:=GraphByAdjacencies([[],[4],[1,2],[]]);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 3 ], [ 3, 4 ], [ 1, 2 ], [ 2 ] ] )
gap> h:=AddEdges(g,[[1,2]]);
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 3 ], [ 1, 3, 4 ], [ 1, 2 ], [ 2 ] ] )
```

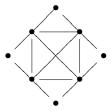
that yields the graph h



Among the latter we have the function SunGraph which takes an integer as argument and returns a fresh copy of a sun graph of the order given as argument.

```
gap> h:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size := 14, Adjacencies :=
[ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ], [ 2, 3, 5, 6, 8 ], [ 4, 6 ],
        [ 2, 4, 5, 7, 8 ], [ 6, 8 ], [ 1, 2, 4, 6, 7 ] ] )
```

that produces h as



Further information regarding constructing graphs can be found on chapter 7.3.

Cliques

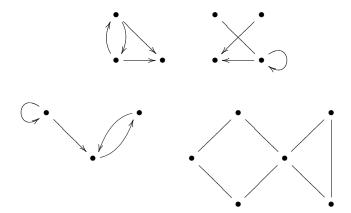
blah, blah, blah.

Categories

4.1 Graph Categories

Declaration of: Graphs

Among them we can find:



Declaration of: LooplessGraphs

A loop is an arrow that starts and finishes on the same vertex.



Loopless graphs have no such arrows.



Declaration of: UndirectedGraphs

Given two vertex i, j in graph G we will say that graph G has an **edge** $\{i, j\}$ if there is an arrow (i, j) and and arrow (j, i).

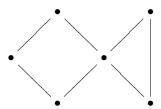
Undirected graphs have no arrows but only edges.

Declaration of: OrientedGraphs

Oriented graphs have no edges but only arrows.



Declaration of: SimpleGraphs



The following figure shows the relationships among categories.

Graphs

 $Loopless \ Undirected$

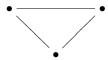
Oriented Simple Graphs

Figure 2: Graph Categories

This relationship is important because when a graph is created it is normalized to the category it belongs. For instance, if we create a graph such as



as a simple graph YAGS will normalize the graph as



For further examples see the following section.

4.2 Default Category

There are several ways to specify the category in which a new graph will be created. There exists a *Default-Category* which tells YAGS to which category belongs any new graph by default. The *DefaultCategory* can be changed using the following function.

Declaration of: SetDefaultGraphCategory

In order to handle graphs with different categories there two functions available.

Declaration of: GraphCategory

Declaration of: TargetGraphCategory

Finally we can test if a single graph belongs to a given category.

Declaration of: in

Morphisms of Graphs

There exists several classes of morphisms that can be found on graphs. Moreover, sometimes we want to find a combination of them. For this reason YAGS uses a unique mechanism for dealing with morphisms. This mechanisms allows to find any combination of morphisms using three underlying operations.

5.1 Core Operations

The following operations do all the work of finding morphisms that comply with all the properties given in a list. The list of checks that each function receives can have any of the following elements.

- CHK_METRIC Metric
- CHK_MONO Mono
- CHK_FULL Full
- CHK_EPI Epi
- CHK_CMPLT Complete
- CHK_ISO Iso

Additionally it must have at least one of the following.

- CHK_WEAK Weak
- CHK_MORPH Morph

These properties are detailed in the next section.

Declaration of: PropertyMorphism

Declaration of: PropertyMorphisms

Declaration of: NextPropertyMorphism

5.2 Morphisms

For all the definitions we assume we have a morphism $\varphi:G\to H\cdot$ The properties for creating morphisms are the following:

Metric A morphism is metric if the distance (see section 8) of any two vertices remains constant

$$d_G(x, y) = d_H(\varphi(x), \varphi(y))$$
.

Mono A morphism is mono if two different vertices in G map to two different vertices in H

$$x \neq y \implies \varphi(x) \neq \varphi(y)$$
.

Full A morphism is full if every edge in G is mapped to an edge in H.

$$|H| = |G|$$

Not yet implemented.

Epi A morphism is Epi if for each vertex in H exist a vertex in G that is mapped from.

$$\forall x \in H \exists x_0 \in G \bullet \varphi(x_0) = x$$

Complete A morphism is complete iff the inverse image of any complete of H is a complete of G.

Iso An isomorphism is a bimorphism which is also complete.

Aditionally they must be one of the following

Weak A morphism is weak if x adjacent to y in G means their mappings are adjacent in H

$$x, y \in G \land x \simeq y \Rightarrow \varphi(x) \simeq \varphi(y)$$
.

Morph This is equivalent to *strong*. A morphism is strong if two different vertices in G map to different vertices in H.

$$x, y \in G \land x \sim y \Rightarrow \varphi(x) \sim \varphi(y)$$
.

Note that $x \neq y \Rightarrow \varphi(x) \neq \varphi(y)$ unless there is a loop in G.

Backtrack

blah, blah, blah.

YAGS Functions by Topic

A complete list of all YAGS's functions by topic.

- 7.1 Most Common Functions
- 7.2 Drawing
- 7.3 Constructing Graphs
- 7.4 Families of Graphs
- 7.5 Attributes and Properties
- 7.6 Unary Operators
- 7.7 Binary Operators
- 7.8 Morphisms of Graphs
- 7.9 Graph Categories
- 7.10 Digraphs
- 7.11 Groups and Rings
- 7.12 Backtrack
- 7.13 Miscelaneous
- 7.14 Undocumented

YAGS Functions Reference

This chapter contains a complete list of all YAGS's functions, with definitions, in alphabetical order.

```
1 ► AddEdges( G, E )
```

Returns a new graph created from graph G by adding the edges in list E.

```
gap> g:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ])
gap> AddEdges(g,[[1,3]]);
Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3 ] ])
gap> AddEdges(g,[[1,3],[2,4]]);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ])
```

```
2 \triangleright AddVerticesByAdjacencies( G, NewAdjList )
```

O

Returns a new graph created from graph G by adding as many new vertices as Length (NewAdjList). Each entry in NewAdjList is also a list: the list of neighbors of the corresponding new vertex.

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> AddVerticesByAdjacencies(g,[[1,2],[4,5]]);
Graph( Category := SimpleGraphs, Order := 7, Size := 8, Adjacencies :=
[ [ 2, 6 ], [ 1, 3, 6 ], [ 2, 4 ], [ 3, 5, 7 ], [ 4, 7 ], [ 1, 2 ], [ 4, 5 ] ] )
gap> AddVerticesByAdjacencies(g,[[1,2,7],[4,5]]);
Graph( Category := SimpleGraphs, Order := 7, Size := 9, Adjacencies :=
[ [ 2, 6 ], [ 1, 3, 6 ], [ 2, 4 ], [ 3, 5, 7 ], [ 4, 7 ], [ 1, 2, 7 ], [ 4, 5, 6 ] ] )
```

Returns the adjacency lists of graph G.

```
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> Adjacencies(g);
[ [ 2 ], [ 1, 3 ], [ 2 ] ]
```

 $4 \triangleright Adjacency(G, x)$

 $3 \triangleright Adjacencies(G)$

Ο

O

Returns the adjacency list of vertex x in G.

```
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> Adjacency(g,1);
[ 2 ]
gap> Adjacency(g,2);
[ 1, 3 ]
```

 $5 \triangleright AdjMatrix(G)$

Α

V

Returns the adjacency matrix of graph G.

```
gap> AdjMatrix(CycleGraph(4));
[ [ false, true, false, true ], [ true, false, true, false ],
      [ false, true, false, true ], [ true, false, true, false ] ]
```

6► AGraph

A 4-cycle with two pendant vertices on consecutive vertices of the cycle.

```
gap> AGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 5 ], [ 2, 4 ], [ 3, 5 ], [ 2, 4, 6 ], [ 5 ] ] )
```

7► AntennaGraph

V

A HouseGraph with a pendant vertex (antenna) on the roof.

```
gap> AntennaGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 1, 4, 6 ], [ 5 ] ] )
```

```
8 \triangleright AutGroupGraph(G)
```

Α

Returns the group of automorphisms of the graph G. There is also a synonym for this attribute which is AutomorphismGroup(G).

```
gap> AutGroupGraph(Icosahedron);
Group([ (1,3,2,10,9,12,8,7,5,4)(6,11), (1,7,9)(2,4,12)(3,11,10)(5,8,6) ])
gap> AutomorphismGroup(Icosahedron);
Group([ (1,3,2,10,9,12,8,7,5,4)(6,11), (1,7,9)(2,4,12)(3,11,10)(5,8,6) ])
```

```
9 ► BackTrack( L, opts, chk, done, extra )
```

Ο

Generic, user-customizable backtracking algorithm.

A backtraking algorithm explores a decision tree in search for solutions to a combinatorial problem. The combinatorial problem and the search strategy are specified by the parameters:

L is just a list that BackTrack uses to keep track of solutions and partial solutions. It is usually set to the empty list as a starting point. After a solution is found, it is returned **and** stored in L. This value of L is then used as a starting point to search for the next solution in case BackTrack is called again. Partial solutions are also stored in L during the execution of BackTrack.

extra may be any object, list, record, etc. BackTrack only uses it to pass this data to the user-defined functions opts, chk and done, therefore offering you a way to share data between your functions.

opts:=function(L,extra) must return the list of continuation options (childs) one has after some partial solution (node) L has been reached within the decision tree (opts may use the extra data extra as needed).

O

Each of the values in the list returned by *opts*(L,extra) will be tried as possible continuations of the partial solution L. If *opts*(L,extra) always returns the same list, you can put that list in place of the parameter *opts*.

chk:=function(L,extra) must evaluate the partial solution L possibly using the extra data extra and must return false when it knows that L can not be extended to a solution of the problem. Otherwise it returns true. chk may assume that L[1..Length(L)-1] already passed the test.

done:=function(L,extra) returns true if L is already a complete solution and false otherwise. In many combinatorial problems, any partial solution of certain length N is also a solution (and viceversa), so if this is your case, you can put that length in place of the parameter done.

The following example uses BackTrack in its simplest form to compute derrangements (permutations of a set, where none of the elements appears in its original position).

```
gap> N:=4;;L:=[];;extra:=[];;opts:=[1..N];;done:=N;;
gap> chk:=function(L,extra) local i; i:=Length(L);
           return not L[i] in L{[1..i-1]} and L[i]<> i; end;;
gap> BackTrack(L,opts,chk,done,extra);
[2, 1, 4, 3]
gap> BackTrack(L,opts,chk,done,extra);
[2, 3, 4, 1]
gap> BackTrack(L,opts,chk,done,extra);
[2, 4, 1, 3]
gap> BackTrack(L,opts,chk,done,extra);
[3, 1, 4, 2]
gap> BackTrack(L,opts,chk,done,extra);
[3, 4, 1, 2]
gap> BackTrack(L,opts,chk,done,extra);
[3,4,2,1]
gap> BackTrack(L,opts,chk,done,extra);
[4, 1, 2, 3]
gap> BackTrack(L,opts,chk,done,extra);
[4,3,1,2]
gap> BackTrack(L,opts,chk,done,extra);
[4, 3, 2, 1]
gap> BackTrack(L,opts,chk,done,extra);
fail
```

10 ► BackTrackBag(opts, chk, done, extra)

Returns the list of all solutions that would be returned one at a time by Backtrack.

The following example computes all derrangements of order 4.

```
gap> N:=4;;
gap> chk:=function(L,extra) local i; i:=Length(L);
>         return not L[i] in L{[1..i-1]} and L[i]<> i; end;;
gap> BackTrackBag([1..N],chk,N,[]);
[[2, 1, 4, 3], [2, 3, 4, 1], [2, 4, 1, 3], [3, 1, 4, 2],
        [3, 4, 1, 2], [3, 4, 2, 1], [4, 1, 2, 3], [4, 3, 1, 2],
        [4, 3, 2, 1]]
```

O

```
11 \blacktriangleright Basement( G, KnG, x )

\blacktriangleright Basement( G, KnG, V )
```

Given a graph G, some iterated clique graph KnG of G and a vertex x of KnG, the operation returns the basement of x with respect to G [Piz04]. Loosely speaking, the basement of x is the set of vertices of G that constitutes the iterated clique x.

```
gap> g:=Icosahedron;;Cliques(g);
[ [ 1, 2, 3 ], [ 1, 2, 6 ], [ 1, 3, 4 ], [ 1, 4, 5 ], [ 1, 5, 6 ],
      [ 4, 5, 7 ], [ 4, 7, 11 ], [ 5, 7, 8 ], [ 7, 8, 12 ], [ 7, 11, 12 ],
      [ 5, 6, 8 ], [ 6, 8, 9 ], [ 8, 9, 12 ], [ 2, 6, 9 ], [ 2, 9, 10 ],
      [ 9, 10, 12 ], [ 2, 3, 10 ], [ 3, 10, 11 ], [ 10, 11, 12 ], [ 3, 4, 11 ] ]
gap> kg:=CliqueGraph(g);; k2g:=CliqueGraph(kg);;
gap> Basement(g,k2g,1);Basement(g,k2g,2);
[ 1, 2, 3, 4, 5, 6 ]
[ 1, 2, 3, 4, 6, 10 ]
```

In its second form, V is a set of vertices of KnG, in that case, the basement is simply the union of the basements of the vertices in V.

```
gap> Basement(g,k2g,[1,2]);
[ 1, 2, 3, 4, 5, 6, 10 ]
```

```
12 ▶ BoxProduct( G, H )
```

Returns the box product, $G \square H$, of two graphs G and H (also known as the cartesian product).

The box product is calculated as follows:

For each pair of vertices $g \in G, h \in H$ we create a vertex (g, h). Given two such vertices (g, h) and (g', h') they are adjacent iff g = g' and $h \sim h'$ or $g \sim g'$ and h = h'.

```
gap> g1:=PathGraph(3);g2:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> g1g2:=BoxProduct(g1,g2);
Graph( Category := SimpleGraphs, Order := 12, Size := 20, Adjacencies :=
[ [ 2, 4, 5 ], [ 1, 3, 6 ], [ 2, 4, 7 ], [ 1, 3, 8 ], [ 1, 6, 8, 9 ],
        [ 2, 5, 7, 10 ], [ 3, 6, 8, 11 ], [ 4, 5, 7, 12 ], [ 5, 10, 12 ],
        [ 6, 9, 11 ], [ 7, 10, 12 ], [ 8, 9, 11 ] ] )
gap> VertexNames(g1g2);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ],
        [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

```
13 \blacktriangleright BoxTimesProduct( G, H )
```

Returns the boxtimes product of two graphs G and H, $G \boxtimes H$ (also known as the strong product).

The boxtimes product is calculated as follows:

For each pair of vertices $g \in G, h \in H$ we create a vertex (g, h). Given two such vertices (g, h) and (g', h') such that $(g, h) \neq (g', h')$ they are adjacent iff $g \simeq g'$ and $h \simeq h'$.

```
gap> g1:=PathGraph(3);g2:=CycleGraph(4);
      Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
      [[2],[1,3],[2]])
      Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
      [[2, 4], [1, 3], [2, 4], [1, 3]])
      gap> g1g2:=BoxTimesProduct(g1,g2);
      Graph( Category := SimpleGraphs, Order := 12, Size := 36, Adjacencies :=
      [[2, 4, 5, 6, 8], [1, 3, 5, 6, 7], [2, 4, 6, 7, 8], [1, 3, 5, 7, 8],
        [1, 2, 4, 6, 8, 9, 10, 12], [1, 2, 3, 5, 7, 9, 10, 11],
        [2, 3, 4, 6, 8, 10, 11, 12], [1, 3, 4, 5, 7, 9, 11, 12],
        [5, 6, 8, 10, 12], [5, 6, 7, 9, 11], [6, 7, 8, 10, 12],
        [5, 7, 8, 9, 11])
      gap> VertexNames(g1g2);
      [[1,1],[1,2],[1,3],[1,4],[2,1],[2,2],[2,3],
        [2, 4], [3, 1], [3, 2], [3, 3], [3, 4]]
14► BullGraph
                                                                                        V
    A triangle with two pendant vertices (horns).
      gap> BullGraph;
      Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
      [[2],[1,3,4],[2,4],[2,3,5],[4]])
                                                                                       O
15 ► CayleyGraph( Grp, elms )
  ► CayleyGraph( Grp )
                                                                                        0
   Returns the graph G whose vertices are the elements of the group Grp such that x is adjacent to y iff
   x * q = y for some q in the list elms. if elms is not provided, then the generators of G are used instead.
      gap> grp:=Group((1,2,3),(1,2));
      Group([(1,2,3), (1,2)])
      gap> CayleyGraph(grp);
      Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
      [[3, 4, 5], [3, 5, 6], [1, 2, 6], [1, 5, 6], [1, 2, 4],
        [2, 3, 4]])
      gap> CayleyGraph(grp,[(1,2),(2,3)]);
      Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
      [[2, 3], [1, 5], [1, 4], [3, 6], [2, 6], [4, 5]])
16 ► ChairGraph
                                                                                        V
   A tree with degree sequence 3,2,1,1,1.
      gap> ChairGraph;
      Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
      [[2],[1,3,4],[2],[2,5],[4]])
17 \triangleright Circulant(n, jumps)
                                                                                        O
```

Returns the graph G whose vertices are [1..n] such that x is adjacent to y iff $x+z=y \mod n$ for some z the list of jumps

A

```
gap> Circulant(6,[1,2]);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 5, 6 ], [ 1, 3, 4, 6 ], [ 1, 2, 4, 5 ], [ 2, 3, 5, 6 ],
      [ 1, 3, 4, 6 ], [ 1, 2, 4, 5 ] ] )
```

18► ClawGraph V

The graph on 4 vertices, 3 edges, and maximum degree 3.

```
gap> ClawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1 ] ] )
```

Returns the intersection graph of all the (maximal) cliques of G.

The additional parameter MaxNumCli aborts the computation when MaxNumCli cliques are found, even if they are all the cliques of G. If the bound MaxNumCli is reached, fail is returned.

```
gap> CliqueGraph(Octahedron);
Graph( Category := SimpleGraphs, Order := 8, Size := 24, Adjacencies :=
[ [ 2, 3, 4, 5, 6, 7 ], [ 1, 3, 4, 5, 6, 8 ], [ 1, 2, 4, 5, 7, 8 ],
        [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 4, 5, 7, 8 ],
        [ 1, 3, 4, 5, 6, 8 ], [ 2, 3, 4, 5, 6, 7 ] ] )
gap> CliqueGraph(Octahedron,9);
Graph( Category := SimpleGraphs, Order := 8, Size := 24, Adjacencies :=
[ [ 2, 3, 4, 5, 6, 7 ], [ 1, 3, 4, 5, 6, 8 ], [ 1, 2, 4, 5, 7, 8 ],
        [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 4, 5, 7, 8 ],
        [ 1, 3, 4, 5, 6, 8 ], [ 2, 3, 4, 5, 6, 7 ] ] )
gap> CliqueGraph(Octahedron,8);
fail
```

```
20 ► CliqueNumber( G )
```

Returns the order, $\omega(G)$, of a maximum clique of G.

```
gap> g:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size := 14, Adjacencies :=
[ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ], [ 2, 3, 5, 6, 8 ], [ 4, 6 ],
        [ 2, 4, 5, 7, 8 ], [ 6, 8 ], [ 1, 2, 4, 6, 7 ] ] )
gap> CliqueNumber(g);
4
```

Returns the set of all (maximal) cliques of a graph G. A clique is a maximal complete subgraph. Here, we use the Bron-Kerbosch algorithm [BK73].

In the second form, It stops computing cliques after MaxNumCli of them have been found.

```
gap> Cliques(Octahedron);
[ [ 1, 3, 5 ], [ 1, 3, 6 ], [ 1, 4, 5 ], [ 1, 4, 6 ], [ 2, 3, 5 ],
      [ 2, 3, 6 ], [ 2, 4, 5 ], [ 2, 4, 6 ] ]
gap> Cliques(Octahedron,4);
[ [ 1, 3, 5 ], [ 1, 3, 6 ], [ 1, 4, 5 ], [ 1, 4, 6 ] ]
```

22 ► ComplementGraph(G)

Α

Computes the complement of graph G. The complement of a graph is created as follows: Create a graph G' with same vertices of G. For each $x, y \in G$ if $x \nsim y$ in G then $x \sim y$ in G'

```
gap> g:=ClawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2, 3, 4 ], [ 1 ], [ 1 ] ] )
gap> ComplementGraph(g);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ ], [ 3, 4 ], [ 2, 4 ], [ 2, 3 ] ] )
```

23 ► CompleteBipartiteGraph(n, m)

F

Returns the complete bipartite whose parts have order n and m respectively. This is the joint (Zykov sum) of two discrete graphs of order n and m.

```
gap> CompleteBipartiteGraph(2,3);
Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
[ [ 3, 4, 5 ], [ 3, 4, 5 ], [ 1, 2 ], [ 1, 2 ], [ 1, 2 ] ])
```

$24 \triangleright CompleteGraph(n)$

F

Returns the complete graph of order n. A complete graph is a graph where all vertices are connected to each other.

```
gap> CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

```
25 ► CompletelyParedGraph( G )
```

O

Returns the completely pared graph of G, which is obtained by repeatedly applying ParedGraph until no more dominated vertices remain.

```
gap> g:=PathGraph(6);
Graph( Category := SimpleGraphs, Order := 6, Size := 5, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4, 6 ], [ 5 ] ] )
gap> CompletelyParedGraph(g);
Graph( Category := SimpleGraphs, Order := 1, Size := 0, Adjacencies :=
[ [ ] ] )
```

```
26\,\blacktriangleright\, CompleteMultipartiteGraph( n1\,\text{,}\ n2 [, n3\ \dots] )
```

F

Returns the complete multipartite graph where the orders of the parts are n1, n2, ... It is also the Zykov sum of discrete graphs of order n1, n2, ...

```
gap> CompleteMultipartiteGraph(2,2,2);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
        [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

```
27 ► CompletesOfGivenOrder( G, Ord )
```

Ο

This operation finds all complete subgraphs of order Ord in graph G.

```
gap> g:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size := 14, Adjacencies :=
[ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ], [ 2, 3, 5, 6, 8 ], [ 4, 6 ],
        [ 2, 4, 5, 7, 8 ], [ 6, 8 ], [ 1, 2, 4, 6, 7 ] ] )
gap> CompletesOfGivenOrder(g,3);
[ [ 1, 2, 8 ], [ 2, 3, 4 ], [ 2, 4, 6 ], [ 2, 4, 8 ], [ 2, 6, 8 ],
        [ 4, 5, 6 ], [ 4, 6, 8 ], [ 6, 7, 8 ] ]
gap> CompletesOfGivenOrder(g,4);
[ [ 2, 4, 6, 8 ] ]
```

28 ► Composition(G, H)

Ο

Returns the composition G[H] of two graphs G and H.

A composition of graphs is obtained by calculating the GraphSum of G with Order(G) copies of H, G[H] = GraphSum(G, [H, ..., H]).

```
gap> g1:=CycleGraph(4);;g2:=DiscreteGraph(2);;
gap> Composition(g1,g2);
Graph( Category := SimpleGraphs, Order := 8, Size := 16, Adjacencies :=
[ [ 3, 4, 7, 8 ], [ 3, 4, 7, 8 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
        [ 3, 4, 7, 8 ], [ 3, 4, 7, 8 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ] ] )
```

29 ► Cone(G)

Returns the cone of graph G. The cone of G is the graph obtained from G by adding a new vertex which is adjacent to every vertex of G. The new vertex is the first one in the new graph.

```
gap> Cone(CycleGraph(4));
Graph( Category := SimpleGraphs, Order := 5, Size := 8, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 5 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 2, 4 ] ] )
```

$30 \triangleright \text{ConnectedComponents}(G)$

A

Returns the connected components of G.

```
31 \triangleright \text{Coordinates}(G)
```

Gets the coordinates of the vertices of G, which are used to draw G by $\mathsf{Draw}(\ G\)$. If the coordinates have not been previously set, $\mathsf{Coordinates}$ returns fail.

```
gap> g:=CycleGraph(4);;
gap> Coordinates(g);
fail
gap> SetCoordinates(g,[[-10,-10],[-10,20],[20,-10], [20,20]]);
gap> Coordinates(g);
[[-10,-10],[-10,20],[20,-10],[20,20]]
```

$32 \triangleright CopyGraph(G)$

O

Returns a fresh copy of graph G. Only the order and adjacency information is copied, all other known attributes of G are not. Mainly used to transform a graph from one category to another. The new graph will be forced to comply with the TargetGraphCategory.

```
gap> g:=CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> g1:=CopyGraph(g:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 3, 4 ], [ 4 ], [ ] ] )
gap> CopyGraph(g1:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

33 ► CuadraticRingGraph(Rng)

O

Returns the graph G whose vertices are the elements of Rng such that x is adjacent to y iff $x+z^2=y$ for some z in Rng

```
gap> CuadraticRingGraph(ZmodnZ(8));
Graph( Category := SimpleGraphs, Order := 8, Size := 12, Adjacencies :=
[ [ 2, 5, 8 ], [ 1, 3, 6 ], [ 2, 4, 7 ], [ 3, 5, 8 ], [ 1, 4, 6 ],
        [ 2, 5, 7 ], [ 3, 6, 8 ], [ 1, 4, 7 ] ] )
```

34 ► Cube V

The 1-skeleton of Plato's cube.

```
gap> Cube;
Graph( Category := SimpleGraphs, Order := 8, Size := 12, Adjacencies :=
[ [ 2, 3, 5 ], [ 1, 4, 6 ], [ 1, 4, 7 ], [ 2, 3, 8 ], [ 1, 6, 7 ],
        [ 2, 5, 8 ], [ 3, 5, 8 ], [ 4, 6, 7 ] ] )
```

```
35 ▶ CubeGraph( n )
```

F

Returns the hypercube of dimension n. This is the box product (cartesian product) of n copies of K_2 (an edge).

```
gap> CubeGraph(3);
Graph( Category := SimpleGraphs, Order := 8, Size := 12, Adjacencies :=
[ [ 2, 3, 5 ], [ 1, 4, 6 ], [ 1, 4, 7 ], [ 2, 3, 8 ], [ 1, 6, 7 ],
[ 2, 5, 8 ], [ 3, 5, 8 ], [ 4, 6, 7 ] ] )
```

```
36 ► CycleGraph( n )
```

F

Returns the cyclic graph on n vertices.

```
gap> CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
[ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
```

```
37 ► CylinderGraph( Base, Height)
```

F

Returns a cylinder of base Base and height Height. The order of this graph is $Base^*(Height+1)$ and it is constructed by taking Height+1 copies of the cyclic graph on Base vertices, ordering these cycles linearly and then joining consecutive cycles by a zigzagging 2^*Base -cycle. This graph is a triangulation of the cylinder where all internal vertices are of degree 6 and the border vertices are of degree 4.

F

```
gap> g:=CylinderGraph(4,1);
Graph( Category := SimpleGraphs, Order := 8, Size := 16, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3, 6, 7 ], [ 2, 4, 7, 8 ], [ 1, 3, 5, 8 ],
        [ 1, 4, 6, 8 ], [ 1, 2, 5, 7 ], [ 2, 3, 6, 8 ], [ 3, 4, 5, 7 ] ] )
gap> g:=CylinderGraph(4,2);
Graph( Category := SimpleGraphs, Order := 12, Size := 28, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3, 6, 7 ], [ 2, 4, 7, 8 ], [ 1, 3, 5, 8 ],
        [ 1, 4, 6, 8, 9, 10 ], [ 1, 2, 5, 7, 10, 11 ], [ 2, 3, 6, 8, 11, 12 ],
        [ 3, 4, 5, 7, 9, 12 ], [ 5, 8, 10, 12 ], [ 5, 6, 9, 11 ], [ 6, 7, 10, 12 ],
        [ 7, 8, 9, 11 ] ] )
```

38 ► DartGraph V

A diamond with a pending vertex and maximum degree 4.

```
gap> DartGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 4, 5 ], [ 2, 4, 5 ], [ 2, 3 ], [ 2, 3 ] ])
```

```
39 ► DeclareQtfyProperty( Name, Filter )
```

For internal use.

Declares a YAGS quantifiable property named *Name* for filter *Filter*. This in turns, declares a boolean GAP property *Name* and an integer GAP attribute *QtfyName*.

The user must provide the method Name(O, qtfy). If qtfy is false, the method must return a boolean indicating whether the property holds, otherwise, the method must return a non-negative integer quantifying how far is the object from satisfying the property. In the latter case, returning 0 actually means that the object does satisfy the property.

```
gap> DeclareQtfyProperty("Is2Regular",Graphs);
gap> InstallMethod(Is2Regular, "for graphs", true, [Graphs, IsBool], 0,
> function(G,qtfy)
    local x,count;
    count:=0;
    for x in Vertices(G) do
      if VertexDegree(G,x)<> 2 then
        if not qtfy then
          return false;
        fi;
>
          count:=count+1;
     fi;
    od;
    if not qtfy then return true; fi;
    return count;
> end);
gap> Is2Regular(CycleGraph(4));
true
gap> QtfyIs2Regular(CycleGraph(4));
gap> Is2Regular(DiamondGraph);
false
gap> QtfyIs2Regular(DiamondGraph);
```

 $40 \triangleright \text{Diameter}(G)$

Returns the maximum among the distances between pairs of vertices of G.

```
gap> g:=CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
[ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
gap> Diameter(g);
2
```

41 ► DiamondGraph

V

The graph on 4 vertices and 5 edges.

```
gap> DiamondGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3 ] ] )
```

$42 \blacktriangleright$ DiscreteGraph(n)

 \mathbf{F}

Returns the discrete graph of order n. A discrete graph is a graph without edges.

```
gap> DiscreteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 0, Adjacencies :=
[ [ ], [ ], [ ] ] )
```

43 ► DisjointUnion(G, H)

Ο

Returns the disjoint union of two graphs G and H, $G \stackrel{.}{\cup} H$.

```
gap> g1:=PathGraph(3);g2:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> DisjointUnion(g1,g2);
Graph( Category := SimpleGraphs, Order := 5, Size := 3, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ], [ 5 ], [ 4 ] ] )
```

```
44 ▶ Distance( G, x, y )
```

О

Returns the length of a minimal path connecting x to y in G.

```
gap> Distance(CycleGraph(5),1,3);
2
gap> Distance(CycleGraph(5),1,5);
1
```

```
45 ▶ DistanceGraph( G, Dist )
```

O

Given a graph G and list of distances Dist, DistanceGraph returns the new graph constructed on the vertices of G where two vertices are adjacent iff the distance (in G) between them belongs to the list Dist.

46 ▶ DistanceMatrix(G)

A

Returns the distance matrix D of a graph G: D[x][y] is the distance in G from vertex x to vertex y. The matrix may be asymmetric if the graph is not simple. An infinite entry in the matrix means that there is no path between the vertices. Floyd's algorithm is used to compute the matrix.

```
gap> g:=PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[[2],[1,3],[2,4],[3]])
gap> Display(DistanceMatrix(g));
[[0, 1, 2, 3],
           1, 2],
        Ο,
 1,
 [ 2,
       1, 0, 1],
 [ 3, 2, 1, 0 ] ]
gap> g:=PathGraph(4:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 4, Size := 3, Adjacencies :=
[[2],[3],[4],[]])
gap> Display(DistanceMatrix(g));
                               2,
] ]
           0,
                     1,
                                         3],
 [ infinity,
                     0,
                               1,
                                         2],
 [ infinity,
             infinity,
                               0.
                                         1],
 [ infinity,
              infinity,
                                         0]]
                        infinity,
```

47 ▶ Distances(G, A, B)

О

Given two lists of vertices A, B of a graph G, Distances returns the list of distances for every pair in the cartesian product of A and B. The order of the vertices in lists A and B affects the order of the list of distances returned.

```
gap> g:=CycleGraph(5);;
gap> Distances(g, [1,3], [2,4]);
[ 1, 2, 1, 1 ]
gap> Distances(g, [3,1], [2,4]);
[ 1, 1, 1, 2 ]
```

```
48 ▶ DistanceSet( G, A, B )
```

Ο

Given two subsets of vertices A, B of a graph G, DistanceSet returns the set of distances for every pair in the cartesian product of A and B.

```
gap> g:=CycleGraph(5);;
gap> DistanceSet(g, [1,3], [2,4]);
[ 1, 2 ]
```

49► Dodecahedron V

The 1-skeleton of Plato's Dodecahedron.

```
gap> Dodecahedron;
Graph( Category := SimpleGraphs, Order := 20, Size := 30, Adjacencies :=
[ [ 2, 5, 6 ], [ 1, 3, 7 ], [ 2, 4, 8 ], [ 3, 5, 9 ], [ 1, 4, 10 ],
        [ 1, 11, 15 ], [ 2, 11, 12 ], [ 3, 12, 13 ], [ 4, 13, 14 ], [ 5, 14, 15 ],
        [ 6, 7, 16 ], [ 7, 8, 17 ], [ 8, 9, 18 ], [ 9, 10, 19 ], [ 6, 10, 20 ],
        [ 11, 17, 20 ], [ 12, 16, 18 ], [ 13, 17, 19 ], [ 14, 18, 20 ],
        [ 15, 16, 19 ] ] )
```

$50 \triangleright DominatedVertices(G)$

Α

V

O

Returns the set of dominated vertices of G.

A vertex x is dominated by another vertex y when the closed neighborhood of x is contained in that of y. However, when there are twin vertices (mutually dominated vertices), exactly one of them (in each equivalent class of mutually dominated vertices) does not appear in the returned set.

```
gap> g1:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> DominatedVertices(g1);
[ 1, 3 ]
gap> g2:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> DominatedVertices(g2);
[ 2 ]
```

51 ► DominoGraph

Two squares glued by an edge.

```
gap> DominoGraph;
    Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
        [ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 4, 6 ], [ 1, 5 ] ] )
52▶ Draw( G )
```

Takes a graph G and makes a drawing of it in a separate window. The user can then view and modify the drawing and finally save the vertex coordinates of the drawing into the graph G.

Within the separate window, type h to toggle on/off the help menu. Besides the keyword commands indicated in the help menu, the user may also move vertices (by dragging them), move the whole drawing (by dragging the background) and scale the drawing (by using the mouse wheel).

```
gap> Coordinates(Icosahedron);
fail
gap> Draw(Icosahedron);
gap> Coordinates(Icosahedron);
[ [ 29, -107 ], [ 65, -239 ], [ 240, -62 ], [ 78, 79 ], [ -107, 28 ],
        [ -174, -176 ], [ -65, 239 ], [ -239, 62 ], [ -78, -79 ], [ 107, -28 ],
        [ 174, 176 ], [ -29, 107 ] ]
```

This preliminary version, should work fine on GNU/Linux. For other plataforms, you should probably (at least) set up correctly the variable <code>drawproc</code> which should point to the correct external program binary. Java binaries are provided for GNU/Linux, Mac OS X and Windows.

F

```
gap> drawproc;
"/usr/share/gap/pkg/yags/bin/draw/application.linux64/draw"
```

```
53► DumpObject( Obj )
```

Dumps all information available for object O. This information includes to which categories it belongs as well as its type and hashing information used by GAP.

```
gap> DumpObject( true );
  Object( TypeObj := NewType( NewFamily( "BooleanFamily", [ 11 ], [ 11 ] ),
      [ 11, 34 ] ), Categories := [ "IS_BOOL" ] )

54   EasyExec( dir, progname, instring )
```

54 ► EasyExec(dir, progname, instring)

• EasyExec(progname, instring)

O

Calls external program *prog* located in directory *dir*, feeding it with *instring* as input and returning the output of the external program as a string. *dir* must be a directory object or a list of directory objects. If *dir* is not provided, *prog* must be in the system's binary PATH. 'fail' is returned if the program could not be located.

```
gap> s:=EasyExec("date","");;
gap> s;
"Sun Nov 9 10:36:16 CST 2014\n"
gap> s:=EasyExec("sort","4\n2\n3\n1");;
gap> s;
"1\n2\n3\n4\n"
```

```
55 \triangleright Eccentricity( G, x )
```

Returns the distance from a vertex x in graph G to its most distant vertex in G.

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> Eccentricity(g,1);
4
gap> Eccentricity(g,3);
2
```

```
56 \triangleright \text{Edges}(G)
```

Returns the list of edges of graph G in the case of SimpleGraphs.

```
gap> g1:=CompleteGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 3, Adjacencies :=
[ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] )
gap> Edges(g1);
[ [ 1, 2 ], [ 1, 3 ], [ 2, 3 ] ]
```

In the case of UndirectedGraphs, it also returns the loops. While in the other categories, Edges actually does not return the edges, but the loops and arrows of G.

```
gap> g2:=CompleteGraph(3:GraphCategory:=UndirectedGraphs);
      Graph( Category := UndirectedGraphs, Order := 3, Size := 6, Adjacencies :=
      [[1, 2, 3], [1, 2, 3], [1, 2, 3]])
      gap> Edges(g2);
      [[1, 1], [1, 2], [1, 3], [2, 2], [2, 3], [3, 3]]
      gap> g3:=CompleteGraph(3:GraphCategory:=Graphs);
      Graph( Category := Graphs, Order := 3, Size := 9, Adjacencies :=
      [[1, 2, 3], [1, 2, 3], [1, 2, 3]])
      gap> Edges(g3);
      [[1, 1], [1, 2], [1, 3], [2, 1], [2, 2], [2, 3], [3, 1],
        [3,2],[3,3]]
                                                                                         F
57 ► FanGraph( N )
    Returns the N-Fan: The join of a vertex and a (N+1)-path.
      gap> FanGraph(4);
      Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
      [[2, 3, 4, 5, 6], [1, 3], [1, 2, 4], [1, 3, 5], [1, 4, 6],
      [1, 5])
58 ► FishGraph
                                                                                         V
    A square and a triangle glued by a vertex.
      gap> FishGraph;
      Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
      [[2, 3, 4, 6], [1, 3], [1, 2], [1, 5], [4, 6], [1, 5]])
                                                                                         V
59 ► GemGraph
    The 3-Fan graph.
      gap> GemGraph;
      Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
      [[2, 3, 4, 5], [1, 3], [1, 2, 4], [1, 3, 5], [1, 4]])
60 ► Graph( Rec )
                                                                                         O
    Returns a new graph created from the record Rec. The record must provide the field Category and either
    the field Adjacencies or the field AdjMatrix
      gap> Graph(rec(Category:=SimpleGraphs,Adjacencies:=[[2],[1]]));
      Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies := [ [ 2 ], [ 1 ] ] )
      gap> Graph(rec(Category:=SimpleGraphs,AdjMatrix:=[[false, true],[true, false]]));
      Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies := [ [ 2 ], [ 1 ] ] )
    Its main purpose is to import graphs from files, which could have been previously exported using PrintTo.
      gap> g:=CycleGraph(4);
      Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
      [[2,4],[1,3],[2,4],[1,3]])
      gap> PrintTo("aux.g","h1:=",g,";");
      gap> Read("aux.g");
      gap> h1;
      Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
      [[2, 4], [1, 3], [2, 4], [1, 3]])
```

```
61 ► GraphByAdjacencies( AdjList )
```

Returns a new graph having AdjList as its list of adjacencies. The order of the created graph is Length(A), and the set of neighbors of vertex x is A[x].

```
gap> GraphByAdjacencies([[2],[1,3],[2]]);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

Note, however, that the graph is forced to comply with the TargetGraphCategory.

```
gap> GraphByAdjacencies([[1,2,3],[],[]]);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2, 3 ], [ 1 ], [ 1 ] ])
```

62 ► GraphByAdjMatrix(*Mat*)

F

F

Returns a new graph created from an adjacency matrix Mat. The matrix Mat must be a square boolean matrix.

```
gap> m:=[ [ false, true, false ], [ true, false, true ], [ false, true, false ] ];;
gap> g:=GraphByAdjMatrix(m);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> AdjMatrix(g);
[ [ false, true, false ], [ true, false, true ], [ false, true, false ] ]
```

Note, however, that the graph is forced to comply with the TargetGraphCategory.

```
gap> m:=[[ true, true], [ false, false ] ];;
gap> g:=GraphByAdjMatrix(m);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> AdjMatrix(g);
[ [ false, true ], [ true, false ] ]
```

63 ► GraphByCompleteCover(Cover)

F

Returns the minimal graph where the elements of *Cover* are (the vertex sets of) complete subgraphs.

```
gap> GraphByCompleteCover([[1,2,3,4],[4,6,7]]);
Graph( Category := SimpleGraphs, Order := 7, Size := 9, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3, 6, 7 ], [ ], [ 4, 7 ],
        [ 4, 6 ] ] )
```

64 ▶ GraphByEdges(L)

F

Returns the minimal graph such that the pairs in L are edges.

```
gap> GraphByEdges([[1,2],[1,3],[1,4],[4,5]]);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1, 5 ], [ 4 ] ] )
```

The vertices of the constructed graph range from 1 to the maximum of the numbers appearing in L.

```
gap> GraphByEdges([[4,3],[4,5]]);
Graph( Category := SimpleGraphs, Order := 5, Size := 2, Adjacencies :=
[ [ ], [ ], [ 4 ], [ 3, 5 ], [ 4 ] ] )
```

Note that GraphByWalks has an even greater functionality.

```
65 ► GraphByRelation( V, Rel )
F GraphByRelation( N, Rel )
F
```

Returns a new graph created from a set of vertices V and a binary relation Rel, where $x \sim y$ iff Rel(x,y)=true. In the second form, N is an integer and V is assumed to be $\{1, 2, ..., N\}$.

```
gap> Rel:=function(x,y) return Intersection(x,y)<>[]; end;;
gap> GraphByRelation([[1,2,3],[3,4,5],[5,6,7]],Rel);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> GraphByRelation(8,function(x,y) return AbsInt(x-y)<=2; end);
Graph( Category := SimpleGraphs, Order := 8, Size := 13, Adjacencies :=
[ [ 2, 3 ], [ 1, 3, 4 ], [ 1, 2, 4, 5 ], [ 2, 3, 5, 6 ], [ 3, 4, 6, 7 ],
        [ 4, 5, 7, 8 ], [ 5, 6, 8 ], [ 6, 7 ] ] )</pre>
```

```
66 ► GraphByWalks( Walk1, Walk2, ...)
```

F

F

Returns the minimal graph such that Walk1, Walk2, etc are Walks.

```
gap> GraphByWalks([1,2,3,4,1],[1,5,6]);
Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
[ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ], [ 1, 6 ], [ 5 ] ])
```

Walks can be *nested*, which greatly improves the versatility of this function.

```
gap> GraphByWalks([1,[2,3,4],5],[5,6]);
Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 5 ], [ 1, 2, 4, 5 ], [ 1, 3, 5 ], [ 2, 3, 4, 6 ], [ 5 ] ] )
```

The vertices in the constructed graph range from 1 to the maximum of the numbers appearing in walk1, walk2, ... etc.

```
gap> GraphByWalks([4,2],[3,6]);
    Graph( Category := SimpleGraphs, Order := 6, Size := 2, Adjacencies :=
        [ [ ], [ 4 ], [ 6 ], [ 2 ], [ ], [ 3 ] ] )
67 ► GraphCategory( [ G, ... ] )
```

For internal use. Returns the minimal common category to a list of graphs. If the list of graphs is empty, the default category is returned.

The partial order (by inclusion) among graph categories is as follows:

```
SimpleGraphs < UndirectedGraphs < Graphs,
OrientedGraphs < LooplessGraphs < Graphs,
SimpleGraphs < LooplessGraphs < Graphs
```

```
gap> g1:=CompleteGraph(2:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> g2:=CompleteGraph(2:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ ] ] )
gap> g3:=CompleteGraph(2:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 2, Size := 3, Adjacencies :=
[ [ 1, 2 ], [ 1, 2 ] ] )
gap> GraphCategory([g1,g2,g3]);
<Operation "Graphs">
gap> GraphCategory([g1,g2]);
<Operation "LooplessGraphs">
gap> GraphCategory([g1,g3]);
<Operation "UndirectedGraphs">
```

68► Graphs()

Graphs is the most general graph category in YAGS. This category contains all graphs that can be represented in YAGS. A graph in this category may contain loops, arrows and edges (which in YAGS are exactly the same as two opposite arrows between some pair of vertices). This graph category has no parent category.

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

69 ► GraphSum(G, L)

O

Returns the lexicographic sum of a list of graphs L over a graph G.

The lexicographic sum is computed as follows:

Given G, with Order(G) = n and a list of n graphs $L = [G_1, \ldots, G_n]$, We take the disjoint union of G_1, G_2, \ldots, G_n and then we add all the edges between G_i and G_j whenever [i, j] is and edge of G.

If L contains holes, the trivial graph is used in place.

```
gap> t:=TrivialGraph;; g:=CycleGraph(4);;
gap> GraphSum(PathGraph(3),[t,g,t]);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ],
        [ 1, 2, 4, 6 ], [ 2, 3, 4, 5 ] ] )
gap> GraphSum(PathGraph(3),[,g,]);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ],
        [ 1, 2, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

```
70 ► GraphToRaw( filename, G )
```

О

Converts a YAGS graph G into a raw format (number of vertices, coordinates and adjacency matrix) and writes the converted data to the file filename. For use by the external program draw (see Draw(G)).

```
gap> g:=CycleGraph(4);;
gap> GraphToRaw("mygraph.raw",g);
```

Ο

```
Ο
71 ► GraphUpdateFromRaw( filename, G )
    Updates the coordinates of G from a file filename in raw format. Intended for internal use only.
                                                                                            O
72 ▶ GroupGraph( G, Grp, act )
  ► GroupGraph( G, Grp )
                                                                                            O
    Given a graph G, a group Grp and an action act of Grp in some set S which contains Vertices (G),
    GroupGraph returns a new graph with vertex set \{act(v,g):g\in Grp,v\in Vertices(G)\} and edge set
    \{\{act(v,g), act(u,g)\}: g \ inGrp\{u,v\} \in Edges(G)\}.
    If act is omited, the standard GAP action OnPoints is used.
      gap> GroupGraph(GraphByWalks([1,2]),Group([(1,2,3,4,5),(2,5)(3,4)]));
      Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
       [[2,5],[1,3],[2,4],[3,5],[1,4]])
73 ► HouseGraph
                                                                                            V
    A 4-Cycle and a triangle glued by an edge.
      gap> HouseGraph;
      Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
       [[2, 4, 5], [1, 3], [2, 4], [1, 3, 5], [1, 4]])
                                                                                            V
74 ► Icosahedron
    The 1-skeleton of Plato's icosahedron.
      gap> Icosahedron;
      Graph( Category := SimpleGraphs, Order := 12, Size := 30, Adjacencies :=
       [[2, 3, 4, 5, 6], [1, 3, 6, 9, 10], [1, 2, 4, 10, 11],
        [1, 3, 5, 7, 11], [1, 4, 6, 7, 8], [1, 2, 5, 8, 9],
         [4, 5, 8, 11, 12], [5, 6, 7, 9, 12], [2, 6, 8, 10, 12],
         [2, 3, 9, 11, 12], [3, 4, 7, 10, 12], [7, 8, 9, 10, 11]])
75 ▶ in( G, C )
                                                                                            O
    Returns true if graph G belongs to category C and false otherwise.
76 ► InducedSubgraph( G, V )
                                                                                            O
    Returns the subgraph of graph G induced by the vertex set V.
      gap> g:=CycleGraph(6);
      Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
       [[2,6],[1,3],[2,4],[3,5],[4,6],[1,5]])
      gap> InducedSubgraph(g,[3,4,6]);
      Graph( Category := SimpleGraphs, Order := 3, Size := 1, Adjacencies :=
       [[2],[1],[])
    The order of the elements in V does matter.
      gap> InducedSubgraph(g,[6,3,4]);
```

Graph(Category := SimpleGraphs, Order := 3, Size := 1, Adjacencies :=

Returns the list of in-neighbors of x in G.

[[],[3],[2]])

77 ► InNeigh(G, x)

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [ ] ] )
gap> InNeigh(tt,3);
[ 1, 2 ]
gap> OutNeigh(tt,3);
[ 4, 5 ]
```

78 ► IntersectionGraph(L)

F

Returns the intersection graph of the family of sets L. This graph has a vertex for every set in L, and two such vertices are adjacent iff the corresponding sets have non-empty intersection.

```
gap> IntersectionGraph([[1,2,3],[3,4,5],[5,6,7]]);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

```
79 ► IsBoolean( Obj )
```

 \mathbf{F}

Returns true if object O is true or false and false otherwise.

```
gap> IsBoolean( true ); IsBoolean( fail ); IsBoolean ( false );
true
false
true
```

$80 \blacktriangleright$ IsCliqueGated(G)

Ρ

Returns true if G is a clique gated graph [HK96].

```
81 ► IsCliqueHelly( G )
```

Р

Returns true if the set of (maximal) cliques G satisfy the Helly property.

The Helly property is defined as follows:

A non-empty family \mathcal{F} of non-empty sets satisfies the Helly property if every pairwise intersecting subfamily of \mathcal{F} has a non-empty total intersection.

Here we use the Dragan-Szwarcfiter characterization [Dra89,Szw97] to compute the Helly property.

82 ► IsComplete(G, L)

Ο

Returns true if L induces a complete subgraph of G.

```
gap> IsComplete(DiamondGraph,[1,2,3]);
true
gap> IsComplete(DiamondGraph,[1,2,4]);
false
```

Ρ

```
83 \triangleright IsCompleteGraph(G)
```

Returns true if graph G is a complete graph, false otherwise. In a complete graph every pair of vertices is an edge.

```
84 \blacktriangleright IsDiamondFree( G )
```

Returns true if G is free from induced diamonds, false otherwise.

```
gap> IsDiamondFree(Cube);
true
gap> IsDiamondFree(Octahedron);
false
```

```
85► IsEdge( G , [x, y] )
```

Returns true if [x,y] is an edge of G.

```
gap> IsEdge(PathGraph(3),[1,2]);
true
gap> IsEdge(PathGraph(3),[1,3]);
false
```

```
86 ► IsIsomorphicGraph(G, H)
```

Returns true when G is isomorphic to H and false otherwise.

```
gap> g:=PowerGraph(CycleGraph(6),2);;h:=Octahedron;;
gap> IsIsomorphicGraph(g,h);
true
```

```
87 ► IsLoopless( G )
```

Р

O

Returns true if graph G have no loops, false otherwise. Loops are edges from a vertex to itself.

```
88 ► IsoMorphism( G, H )

► NextIsoMorphism( G, H, f )

O
```

IsoMorphism returns one isomorphism from G to H. NextIsoMorphism returns the next isomorphism from G to H in the lexicographic order, it returns fail if there are no more isomorphisms. If G has n vertices, an isomorphisms $f: G \to H$ is represented as the list $[f(1), f(2), \ldots, f(n)]$.

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> f:=IsoMorphism(g,h);
[ 1, 3, 2, 4 ]
gap> NextIsoMorphism(g,h,f);
[ 1, 4, 2, 3 ]
gap> NextIsoMorphism(g,h,f);
[ 2, 3, 1, 4 ]
gap> NextIsoMorphism(g,h,f);
[ 2, 4, 1, 3 ]
```

```
89 ► IsoMorphisms( G, H )
```

O

Returns the list of all isomorphism from G to H. If G has n vertices, an isomorphisms $f: G \to H$ is represented as the list $[f(1), f(2), \ldots, f(n)]$.

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> IsoMorphisms(g,h);
[ [ 1, 3, 2, 4 ], [ 1, 4, 2, 3 ], [ 2, 3, 1, 4 ], [ 2, 4, 1, 3 ],
      [ 3, 1, 4, 2 ], [ 3, 2, 4, 1 ], [ 4, 1, 3, 2 ], [ 4, 2, 3, 1 ] ]
```

$90 \blacktriangleright$ IsOriented(G)

P A

▶ QtfyIsOriented(G)

Returns true if graph G is an oriented graph, false otherwise. Regardless of the categories that G belongs to, G is oriented if whenever [x,y] is an edge of G, [y,x] is not.

91 ► IsSimple(
$$G$$
)

Ρ

Returns true if graph G is a simple graph, false otherwise. Regardless of the categories that G belongs to, G is simple if and only if G is undirected and loopless.

Returns true if the graph G is simple regardless of its category.

92 ► IsTournament(G)

Р

Returns true if G is a tournament.

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [ ] ] )
gap> IsTournament(tt);
true
```

$93 \triangleright IsTransitiveTournament(G)$

Ρ

Returns true if G is a transitive tournament.

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [ ] ] )
gap> IsTransitiveTournament(tt);
true
```

$94 \triangleright IsUndirected(G)$

Р

Returns true if graph G is an undirected graph, false otherwise. Regardless of the categories that G belongs to, G is undirected if whenever [x,y] is an edge of G, [y,x] is also an egde of G.

95 ► JohnsonGraph(n, r)

F

Returns the Johnson graph J(n,r). A Johnson Graph is a graph constructed as follows. Each vertex represents a subset of the set $\{1,\ldots,n\}$ with cardinality r.

$$V(J(n,r)) = \{X \subset \{1, \dots, n\} | |X| = r\}$$

and there is an edge between two vertices if and only if the cardinality of the intersection of the sets they represent is r-1

$$X \sim X'$$
 iff $|X \cup X'| = r - 1$.

```
gap> JohnsonGraph(4,2);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
        [ 1, 3, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

```
96► Join( G, H )
```

Returns the result of joining graph G and H, G + H (also known as the Zykov sum).

Joining graphs is computed as follows:

First, we obtain the disjoint union of graphs G and H. Second, for each vertex $g \in G$ we add an edge to each vertex $h \in H$.

```
gap> g1:=DiscreteGraph(2);g2:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 2, Size := 0, Adjacencies :=
[ [ ], [ ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> Join(g1,g2);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ],
        [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ] ] )
```

97► KiteGraph V

A diamond with a pending vertex and maximum degree 3.

```
gap> KiteGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 4 ], [ 2, 4, 5 ], [ 2, 3, 5 ], [ 3, 4 ] ] )
```

```
98 \triangleright LineGraph( G )
```

Returns the line graph L(G) of graph G. The line graph is the intersection graph of the edges of G, *i.e.* the vertices of L(G) are the edges of G two of them being adjacent iff they are incident.

```
gap> g:=Tetrahedron;
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> LineGraph(g);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
        [ 1, 3, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

```
99► Link( G, x )
```

Returns the subgraph of G induced by the neighbors of x.

```
gap> Link(SnubDisphenoid,1);
Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
[ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
gap> Link(SnubDisphenoid,3);
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] )
```

```
100 ► Links( G )
```

Returns the list of subgraphs of G induced by the neighbors of each vertex of G.

 \mathbf{C}

O

O

O

```
gap> Links(SnubDisphenoid);
      [ Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
          [[2,5],[1,3],[2,4],[3,5],[1,4]]),
        Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
          [[2,5],[1,3],[2,4],[3,5],[1,4]]),
        Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
          [[2,3],[1,4],[1,4],[2,3]]),
        Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
          [[2,3],[1,4],[1,4],[2,3]]),
        Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
          [[2,5],[1,3],[2,4],[3,5],[1,4]]),
        Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
          [[2,5],[1,3],[2,4],[3,5],[1,4]]),
        Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
          [[3, 4], [3, 4], [1, 2], [1, 2]]),
        Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
          [[2,3],[1,4],[1,4],[2,3]])]
101 ► LooplessGraphs()
      gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
```

LooplessGraphs is a graph category in YAGS. A graph in this category may contain arrows and edges but no loops. The parent of this category is Graphs

```
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[[1, 2], [1], [2]])
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=LooplessGraphs);
Graph( Category := LooplessGraphs, Order := 3, Size := 3, Adjacencies :=
[[2],[1],[2]])
```

102 ► MaxDegree(G)

Returns the maximum degree in graph G.

```
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
[[2, 3, 4, 5], [1, 3], [1, 2, 4], [1, 3, 5], [1, 4]])
gap> MaxDegree(g);
```

103 ▶ MinDegree(G)

Returns the minimum degree in graph G.

```
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
[[2, 3, 4, 5], [1, 3], [1, 2, 4], [1, 3, 5], [1, 4]])
gap> MinDegree(g);
```

```
104 ► NextPropertyMorphism( G1, G2, m, c)
```

Returns the next morphisms (in lexicographic order) from G1 to G2 satisfying the list of properties cstarting with (possibly incomplete) morphism m. The morphism found will me returned and stored in m

in order to use it as the next starting point, in case NextPropertyMorphism is called again. The operation returns fail if there are no more morphisms of the specified type.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: CHK_WEAK, CHK_MORPH, CHK_METRIC, CHK_CMPLT, CHK_MONO and CHK_EPI.

If G1 has n vertices and $f: G1 \to G2$ is a morphism, it is represented as $[f(1), f(2), \ldots, f(n)]$.

```
gap> g1:=CycleGraph(4);;g2:=CompleteBipartiteGraph(2,2);;
       gap> m:=[];; c:=[CHK_MORPH,CHK_MONO];;
       gap> NextPropertyMorphism(g1,g2,m,c);
       [1, 3, 2, 4]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [ 1, 4, 2, 3 ]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [2, 3, 1, 4]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [ 2, 4, 1, 3 ]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [3, 1, 4, 2]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [3, 2, 4, 1]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [4, 1, 3, 2]
       gap> NextPropertyMorphism(g1,g2,m,c);
       [4, 2, 3, 1]
       gap> NextPropertyMorphism(g1,g2,m,c);
       fail
105 ► NumberOfCliques( G )
```

Returns the number of (maximal) cliques of G. In the second form, It stops computing cliques after MaxNum-Cli of them have been counted and returns MaxNumCli in case G has MaxNumCli or more cliques.

```
gap> NumberOfCliques(Icosahedron);
20
gap> NumberOfCliques(Icosahedron,15);
15
gap> NumberOfCliques(Icosahedron,50);
20
```

▶ NumberOfCliques(G, MaxNumCli)

This implementation discards the cliques once counted hence, given enough time, it can compute the number of cliques of G even if the set of cliques does not fit in memory.

```
gap> NumberOfCliques(OctahedralGraph(30));
1073741824
```

```
106 \triangleright \text{NumberOfConnectedComponents}(G)
```

Α

Α

O

Returns the number of connected components of G.

```
107 ▶ OctahedralGraph( n )
```

 \mathbf{F}

Return the *n*-dimensional octahedron. This is the complement of *n* copies of K_2 (an edge). It is also the (2n-2)-regular graph on 2n vertices.

```
gap> OctahedralGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

108 ► Octahedron V

The 1-skeleton of Plato's octahedron.

```
gap> Octahedron;
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
      [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

109 ► Order(G)

Returns the number of vertices, of graph G.

```
gap> Order(Icosahedron);
12
```

```
110 ► OrientedGraphs()
```

 \mathbf{C}

OrientedGraphs is a graph category in YAGS. A graph in this category may contain arrows, but no loops or edges. The parent of this category is LooplessGraphs.

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ ], [ 2 ] ] )
```

111 \blacktriangleright OutNeigh(G, x)

Ο

Returns the list of out-neighbors of x in G.

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [ ] ] )
gap> InNeigh(tt,3);
[ 1, 2 ]
gap> OutNeigh(tt,3);
[ 4, 5 ]
```

112 ▶ ParachuteGraph

V

The complement of a ParapluieGraph; The suspension of a 4-path with a pendant vertex attached to the south pole.

```
gap> ParachuteGraph;
Graph( Category := SimpleGraphs, Order := 7, Size := 12, Adjacencies :=
[ [ 2 ], [ 1, 3, 4, 5, 6 ], [ 2, 4, 7 ], [ 2, 3, 5, 7 ], [ 2, 4, 6, 7 ],
        [ 2, 5, 7 ], [ 3, 4, 5, 6 ] ] )
```

$113 \blacktriangleright \texttt{ParapluieGraph}$

V

A 3-Fan graph with a 3-path attached to the universal vertex.

```
gap> ParapluieGraph;
Graph( Category := SimpleGraphs, Order := 7, Size := 9, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4, 5, 6, 7 ], [ 3, 5 ], [ 3, 4, 6 ], [ 3, 5, 7 ],
      [ 3, 6 ] ] )
```

114 \blacktriangleright ParedGraph(G)

Ο

Returns the pared graph of G. This is the induced subgraph obtained from G by removing its dominated vertices. When there are twin vertices (mutually dominated vertices), exactly one of them survives the paring in each equivalent class of mutually dominated vertices.

```
gap> g1:=PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
gap> ParedGraph(g1);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> g2:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> ParedGraph(g2);
Graph( Category := SimpleGraphs, Order := 1, Size := 0, Adjacencies :=
[ [ ] ] )
```

115 ▶ PathGraph(n)

F

Returns the path graph on n vertices.

```
gap> PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
```

116 ► PawGraph

V

The graph on 4 vertices, 4 edges and maximum degree 3: A triangle with a pendant vertex.

```
gap> PawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3, 4 ], [ 2, 4 ], [ 2, 3 ] ] )
```

117 ▶ PetersenGraph

V

The 3-regular graph on 10 vertices having girth 5.

```
gap> PetersenGraph;
Graph( Category := SimpleGraphs, Order := 10, Size := 15, Adjacencies :=
[ [ 2, 5, 6 ], [ 1, 3, 7 ], [ 2, 4, 8 ], [ 3, 5, 9 ], [ 1, 4, 10 ],
      [ 1, 8, 9 ], [ 2, 9, 10 ], [ 3, 6, 10 ], [ 4, 6, 7 ], [ 5, 7, 8 ] ] )
```

```
118 \blacktriangleright PowerGraph( G, exp )
```

Ο

Returns the DistanceGraph of G using [0, 1, ..., exp] as the list of distances. Note that the distance 0 in the list produces loops in the new graph only when the TargetGraphCategory admits loops.

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> PowerGraph(g,1);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> PowerGraph(g,1:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 5, Size := 13, Adjacencies :=
[ [ 1, 2 ], [ 1, 2, 3 ], [ 2, 3, 4 ], [ 3, 4, 5 ], [ 4, 5 ] ] )
```

```
119 \triangleright PropertyMorphism( G1, G2, c)
```

O

Returns the first morphisms (in lexicographic order) from G1 to G2 satisfying the list of properties c A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: CHK_WEAK, CHK_MORPH, CHK_METRIC, CHK_CMPLT, CHK_MONO and CHK_EPI.

If G1 has n vertices and $f: G1 \to G2$ is a morphism, it is represented as $[f(1), f(2), \ldots, f(n)]$.

```
gap> g1:=CycleGraph(4);;g2:=CompleteBipartiteGraph(2,2);;
gap> c:=[CHK_MORPH];;
gap> PropertyMorphism(g1,g2,c);
[ 1, 3, 1, 3 ]
```

```
120 ▶ PropertyMorphisms( G1, G2, c)
```

Ο

Returns all morphisms from G1 to G2 satisfying the list of properties c

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: CHK_WEAK, CHK_MORPH, CHK_METRIC, CHK_CMPLT, CHK_MONO and CHK_EPI.

If G1 has n vertices and $f: G1 \to G2$ is a morphism, it is represented as $[f(1), f(2), \ldots, f(n)]$.

```
gap> g1:=CycleGraph(4);;g2:=CompleteBipartiteGraph(2,2);;
gap> c:=[CHK_WEAK,CHK_MONO];;
gap> PropertyMorphisms(g1,g2,c);
[[1, 3, 2, 4], [1, 4, 2, 3], [2, 3, 1, 4], [2, 4, 1, 3],
      [3, 1, 4, 2], [3, 2, 4, 1], [4, 1, 3, 2], [4, 2, 3, 1]]
```

121 ▶ QtfyIsSimple(G)

Α

For internal use. Returns how far is graph G from being simple.

```
122 ► QuotientGraph( G, Part )

OutlientGraph( G, L1, L2 )

OutlientGraph( G, L1, L2 )
```

Returns the quotient graph of graph G given a vertex partition Part, by identifying any two vertices in the same part. The vertices of the quotient graph are the parts in the partition Part two of them being adjacent iff any vertex in one part is adjacent to any vertex in the other part. Singletons may be omitted in Part.

```
gap> g:=PathGraph(8);;
gap> QuotientGraph(g,[[1,5,8],[2],[3],[4],[6],[7]]);
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ], [ 1, 6 ], [ 1, 5 ] ] )
gap> QuotientGraph(g,[[1,5,8]]);
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ], [ 1, 6 ], [ 1, 5 ] ] )
```

In its second form, QuotientGraph identifies each vertex in list L1, with the corresponding vertex in list L2. L1 and L2 must have the same length, but any or both of them may have repetitions.

```
gap> g:=PathGraph(8);;
       gap> QuotientGraph(g,[[1,7],[4,8]]);
       Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
       [[2, 4, 6], [1, 3], [2, 4], [1, 3, 5], [4, 6], [1, 5]])
       gap> QuotientGraph(g,[1,4],[7,8]);
       Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
       [[2,4,6],[1,3],[2,4],[1,3,5],[4,6],[1,5]])
123 ▶ Radius(G)
                                                                                        Α
    Returns the minimal eccentricity among the vertices of graph G.
       gap> Radius(PathGraph(5));
                                                                                        F
124 ► RandomGraph( n, p )
  ► RandomGraph( n )
                                                                                        \mathbf{F}
    Returns a random graph of order n taking the rational p \in [0,1] as the edge probability.
       gap> RandomGraph(5,1/3);
       Graph( Category := SimpleGraphs, Order := 5, Size := 2, Adjacencies :=
       [[5],[5],[],[],[1,2]])
       gap> RandomGraph(5,2/3);
       Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
       [[4,5],[3,4,5],[2,4],[1,2,3],[1,2]])
       gap> RandomGraph(5,1/2);
       Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
       [[2,5],[1,3,5],[2],[],[1,2]])
    If p is ommitted, the edge probability is taken to be 1/2.
       gap> RandomGraph(5);
       Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
       [[2,3],[1],[1,4,5],[3,5],[3,4]])
       gap> RandomGraph(5);
       Graph( Category := SimpleGraphs, Order := 5, Size := 3, Adjacencies :=
       [[2,5],[1,4],[],[2],[1]])
125 ► RandomlyPermuted( Obj )
                                                                                        O
    Returns a copy of Obj with the order of its elements permuted randomly. Currently, the operation is
    implemented for lists and graphs.
       gap> RandomlyPermuted([1..9]);
       [ 9, 7, 5, 3, 1, 4, 8, 6, 2 ]
       gap> g:=PathGraph(4);
       Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
       [[2],[1,3],[2,4],[3]])
       gap> RandomlyPermuted(g);
       Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
       [[4],[3,4],[2],[1,2]])
126 ► RandomPermutation( N )
                                                                                        O
    Returns a random permutation of the list [1..N]
```

0

```
gap> RandomPermutation(12);
       (1,8,10)(2,7,9,12)(3,5,11)(4,6)
127 ► RemoveEdges( G, E )
                                                                                          Ο
    Returns a new graph created from graph G by removing the edges in list E.
       gap> g:=CompleteGraph(4);
       Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
       [[2, 3, 4], [1, 3, 4], [1, 2, 4], [1, 2, 3]])
       gap> RemoveEdges(g,[[1,2]]);
       Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
       [[3,4],[3,4],[1,2,4],[1,2,3]])
       gap> RemoveEdges(g,[[1,2],[3,4]]);
       Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
       [[3, 4], [3, 4], [1, 2], [1, 2]])
128 ► RemoveVertices(G, V)
                                                                                          O
    Returns a new graph created from graph G by removing the vertices in list V.
       gap> g:=PathGraph(5);
       Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
       [[2],[1,3],[2,4],[3,5],[4]])
       gap> RemoveVertices(g,[3]);
       Graph( Category := SimpleGraphs, Order := 4, Size := 2, Adjacencies :=
       [[2],[1],[4],[3]])
       gap> RemoveVertices(g,[1,3]);
       Graph( Category := SimpleGraphs, Order := 3, Size := 1, Adjacencies :=
       [[],[3],[2]])
                                                                                          V
129 ► RGraph
    A square with two pendant vertices attached to the same vertex of the square.
       gap> RGraph;
       Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
       [[2],[1,3,5,6],[2,4],[3,5],[2,4],[2]])
130 ► RingGraph( Rng, elms)
                                                                                          O
    Returns the graph G whose vertices are the elements of the ring Rng such that x is adjacent to y iff x+r=y
    for some r in elms.
       gap> r:=FiniteField(8);Elements(r);
       GF(2^3)
       [0*Z(2), Z(2)^0, Z(2^3), Z(2^3)^2, Z(2^3)^3, Z(2^3)^4, Z(2^3)^5, Z(2^3)^6]
       gap> RingGraph(r, [Z(2^3), Z(2^3)^4]);
       Graph( Category := SimpleGraphs, Order := 8, Size := 8, Adjacencies :=
```

Sets the coordinates of the vertices of G, which are used to draw G by Draw(G).

[5,7]])

131 ▶ SetCoordinates (G, Coord)

[[3, 6], [5, 7], [1, 4], [3, 6], [2, 8], [1, 4], [2, 8],

```
gap> g:=CycleGraph(4);;
gap> SetCoordinates(g,[[-10,-10],[-10,20],[20,-10], [20,20]]);
gap> Coordinates(g);
[ [ -10, -10 ], [ -10, 20 ], [ 20, -10 ], [ 20, 20 ] ]
```

132 ► SetDefaultGraphCategory(Catqy)

F

Sets the default graph category to *Categy*. The default graph category is used when constructing new graphs when no other graph category is indicated. New graphs are always forced to comply with the TargetGraph-Category, so loops may be removed, and arrows may replaced by edges or viceversa, depending on the category that the new graph belongs to.

The available graph categories are: SimpleGraphs, OrientedGraphs, UndirectedGraphs, LooplessGraphs, and Graphs.

```
gap> SetDefaultGraphCategory(Graphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[[1,2],[1],[2]])
gap> SetDefaultGraphCategory(LooplessGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := LooplessGraphs, Order := 3, Size := 3, Adjacencies :=
[[2],[1],[2]])
gap> SetDefaultGraphCategory(UndirectedGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := UndirectedGraphs, Order := 3, Size := 3, Adjacencies :=
[[1,2],[1,3],[2]])
gap> SetDefaultGraphCategory(SimpleGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[[2],[1,3],[2]])
gap> SetDefaultGraphCategory(OrientedGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := OrientedGraphs, Order := 3, Size := 2, Adjacencies :=
[[2],[],[2]])
```

133 ► SimpleGraphs()

С

SimpleGraphs is a graph category in YAGS. A graph in this category may contain edges, but no loops or arrows. The category has two parents: LooplessGraphs and UndirectedGraphs.

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

134 ► Size(G)

Α

Returns the number of edges of graph G.

```
gap> Size(Icosahedron);
30
```

135 ► SnubDisphenoid

V

The 1-skeleton of the 84th Johnson solid.

```
gap> SnubDisphenoid;
Graph( Category := SimpleGraphs, Order := 8, Size := 18, Adjacencies := [ [ 2, 3, 4, 5, 8 ], [ 1, 3, 6, 7, 8 ], [ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ], [ 1, 4, 6, 7, 8 ], [ 2, 3, 4, 5, 7 ], [ 2, 5, 6, 8 ], [ 1, 2, 5, 7 ] ] )
```

136 ► SpanningForest(G)

O

Returns a spanning forest of G.

```
137 ► SpanningForestEdges(G)
```

Ο

Returns the edges of a spanning forest of G.

```
138 ► SpikyGraph( N )
```

F

The spiky graph is constructed as follows: Take complete graph on N vertices, K_N , and then, for each the N subsets of $Vertices(K_n)$ of order N-1, add an additional vertex which is adjacent precisely to this subset of $Vertices(K_n)$.

```
gap> SpikyGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ], [ 1, 2 ], [ 1, 3 ],
        [ 2, 3 ] ] )
```

139 ► SunGraph(N)

F

Returns the N-Sun: A complete graph on N vertices, K_N , with a corona made with a zigzagging 2N-cycle glued to a N-cycle of the K_N .

$140 \triangleright Suspension(G)$

O

Returns the suspension of graph G. The suspension of G is the graph obtained from G by adding two new vertices which are adjacent to every vertex of G but not to each other. The new vertices are the first ones in the new graph.

```
gap> Suspension(CycleGraph(4));
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ],
        [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ] ] )
```

```
141 ► TargetGraphCategory( [ G, ... ] )
```

F

For internal use. Returns the graph category indicated in the *options stack* if any, otherwise if the list of graphs provided is not empty, returns the minimal common graph category for the graphs in the list, else returns the default graph category.

The partial order (by inclusion) among graph categories is as follows:

```
SimpleGraphs < UndirectedGraphs < Graphs,
OrientedGraphs < LooplessGraphs < Graphs
SimpleGraphs < LooplessGraphs < Graphs
```

This function is internally called by all graph constructing operations in YAGS to decide the graph category that the newly constructed graph is going to belong. New graphs are always forced to comply with the TargetGraphCategory, so loops may be removed, and arrows may replaced by edges or viceversa, depending on the category that the new graph belongs to.

The *options stack* is a mechanism provided by GAP to pass implicit parameters and is used by Target-GraphCategory so that the user may indicate the graph category she/he wants for the new graph.

```
gap> SetDefaultGraphCategory(SimpleGraphs);
gap> g1:=CompleteGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> g2:=CompleteGraph(2:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ ] ] )
gap> DisjointUnion(g1,g2);
Graph( Category := LooplessGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2 ], [ 1 ], [ 4 ], [ ] ] )
gap> DisjointUnion(g1,g2:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 4, Size := 2, Adjacencies :=
[ [ 2 ], [ 1 ], [ 4 ], [ 3 ] ] )
```

In the previous examples, TargetGraphCategory was called internally exactly once for each new graph constructed with the following parameters:

```
gap> TargetGraphCategory();
<Operation "SimpleGraphs">
gap> TargetGraphCategory(:GraphCategory:=OrientedGraphs);
<Operation "OrientedGraphs">
gap> TargetGraphCategory([g1,g2]);
<Operation "LooplessGraphs">
gap> TargetGraphCategory([g1,g2]:GraphCategory:=UndirectedGraphs);
<Operation "UndirectedGraphs">
```

142 ► Tetrahedron V

The 1-skeleton of Plato's tetrahedron.

```
gap> Tetrahedron;
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

```
143 ► TimeInSeconds()

Peturns the time in seconds since 1970 01 01 00:00:00 UTC as an integer. This is useful to measure execution
```

Returns the time in seconds since 1970-01-01 00:00:00 UTC as an integer. This is useful to measure execution time. It can also be used to impose time constraints on the execution of algorithms. Note however that the time reported is the 'wall time', not necessarily the time spent in the process you intend to measure.

```
gap> TimeInSeconds();
1415551598
gap> K:=CliqueGraph;;
gap> t1:=TimeInSeconds();NumberOfCliques(K(K(K(K(Icosahedron)))));TimeInSeconds()-t1;
1415551608
44644
103
```

144 ► TimesProduct(G, H)

O

Returns the times product of two graphs G and H, $G \times H$ (also known as the tensor product).

The times product is computed as follows:

For each pair of vertices $g \in G, h \in H$ we create a vertex (g, h). Given two such vertices (g, h) and (g', h') they are adjacent iff $g \sim g'$ and $h \sim h'$.

```
gap> g1:=PathGraph(3);g2:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> g1g2:=TimesProduct(g1,g2);
Graph( Category := SimpleGraphs, Order := 12, Size := 16, Adjacencies :=
[ [ 6, 8 ], [ 5, 7 ], [ 6, 8 ], [ 5, 7 ], [ 2, 4, 10, 12 ], [ 1, 3, 9, 11 ],
        [ 2, 4, 10, 12 ], [ 1, 3, 9, 11 ], [ 6, 8 ], [ 5, 7 ], [ 6, 8 ], [ 5, 7 ] ] )
gap> VertexNames(g1g2);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ],
        [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

145 ► TrivialGraph

V

The one vertex graph.

```
gap> TrivialGraph;
Graph( Category := SimpleGraphs, Order := 1, Size := 0, Adjacencies :=
[ [ ] ] )
```

```
146 ► UFFind( UFS, x )
```

F

For internal use. Implements the find operation on the union-find structure.

```
147 \blacktriangleright UFUnite( UFS, x, y )
```

 \mathbf{F}

For internal use. Implements the *unite* operation on the *union-find structure*.

```
148 ► UndirectedGraphs()
```

 \mathbf{C}

UndirectedGraphs is a graph category in YAGS. A graph in this category may contain edges and loops, but no arrows. The parent of this category is Graphs

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 3, Size := 3, Adjacencies :=
[ [ 1, 2 ], [ 1, 3 ], [ 2 ] ] )
```

O

O

```
149 ► UnitsRingGraph( Rng )
```

Returns the graph G whose vertices are the elements of Rng such that x is adjacent to y iff x+z=y for some unit z of Rng

```
gap> UnitsRingGraph(ZmodnZ(8));
Graph( Category := SimpleGraphs, Order := 8, Size := 16, Adjacencies :=
[ [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ],
       [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ] ] )
```

```
150 ► VertexDegree( G, x )
```

Returns the degree of vertex x in Graph G.

```
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> VertexDegree(g,1);
1
gap> VertexDegree(g,2);
2
```

151 ► VertexDegrees(G)

O

Returns the list of degrees of the vertices in graph G.

```
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ] )
gap> VertexDegrees(g);
[ 4, 2, 3, 3, 2 ]
```

152 ▶ VertexNames(G)

Α

Return the list of names of the vertices of G. The vertices of a graph in YAGS are always $\{1, 2, \ldots, Order(G)\}$, but depending on how the graph was constructed, its vertices may have also some names, that help us identify the origin of the vertices. YAGS will always try to store meaninful names for the vertices. For example, in the case of the LineGraph, the vertex names of the new graph are the edges of the old graph.

```
gap> g:=LineGraph(DiamondGraph);
Graph( Category := SimpleGraphs, Order := 5, Size := 8, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4, 5 ], [ 1, 2, 5 ], [ 1, 2, 5 ], [ 2, 3, 4 ] ] )
gap> VertexNames(g);
[ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 3, 4 ] ]
gap> Edges(DiamondGraph);
[ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 3, 4 ] ]
```

153 ▶ Vertices(G)

Ο

Returns the list [1..Order(G)].

```
gap> Vertices(Icosahedron);
[ 1 .. 12 ]
```

```
O
154 ► WheelGraph( N )

ightharpoonup WheelGraph( N, Radius )
                                                                                                                       O
```

In its first form WheelGraph returns the wheel graph on N+1 vertices. This is the cone of a cycle: a central vertex adjacent to all the vertices of an N-cycle

```
WheelGraph(5);
gap> Graph( Category := SimpleGraphs, Order := 6, Size := 10, Adjacencies :=
[[2, 3, 4, 5, 6], [1, 3, 6], [1, 2, 4], [1, 3, 5], [1, 4, 6],
 [1, 2, 5]
```

In its second form, WheelGraph returns returns the wheel graph, but adding Radius-1 layers, each layer is a new N-cycle joined to the previous layer by a zigzagging 2N-cycle. This graph is a triangulation of the disk.

```
gap> WheelGraph(5,2);
Graph( Category := SimpleGraphs, Order := 11, Size := 25, Adjacencies :=
[[2, 3, 4, 5, 6], [1, 3, 6, 7, 8], [1, 2, 4, 8, 9], [1, 3, 5, 9, 10],
  [1, 4, 6, 10, 11], [1, 2, 5, 7, 11], [2, 6, 8, 11], [2, 3, 7, 9],
  [3, 4, 8, 10], [4, 5, 9, 11], [5, 6, 7, 10]])
gap> WheelGraph(5,3);
Graph( Category := SimpleGraphs, Order := 16, Size := 40, Adjacencies :=
[[2, 3, 4, 5, 6], [1, 3, 6, 7, 8], [1, 2, 4, 8, 9], [1, 3, 5, 9, 10],
  [1, 4, 6, 10, 11], [1, 2, 5, 7, 11], [2, 6, 8, 11, 12, 13],
  [2, 3, 7, 9, 13, 14], [3, 4, 8, 10, 14, 15], [4, 5, 9, 11, 15, 16],
  [5, 6, 7, 10, 12, 16], [7, 11, 13, 16], [7, 8, 12, 14],
  [8, 9, 13, 15], [9, 10, 14, 16], [10, 11, 12, 15]])
```

```
155 ► YagsExec( progname, instring )
```

O

For internal use. Calls external program prog located in directory 'yags-dir/bin/' feeding it with instring as input and returning the output of the external program as a string. 'fail' is returned if the program could not be located.

```
gap> YagsExec("time","");
"1415551127\n"
gap> YagsExec("nauty","l=0$=1dacn=5 g1,2,3. xbzq");
(4,5)\n(2,3)\n[2,3,4,5,1]\n[\cb0c\],\484f264\],\b0e19f1\]\n
```

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