YAGS

Yet Another Graph System

Version 0.0.1

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Acknowledgements

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Chapter 1

Preface

Ejemplo de cita: [12]

1.1 Disclaimer

THIS IS NOT AN OFFICIAL RELEASE YET, this is a version in development. This particular version, 0.0.1, changes from one day to another without warning and even without a change in the version number. Also, the operations and global variables can still change name or even disappear without warning. No commitment is made at the moment concerning compatibility of this version of the software with any future version.

As of this writing (16/Feb/2016) there are only two trustable chapters in this manual: Appendixes 'YAGS Functions by Topic' and 'YAGS Functions Reference'; also the file `cheatsheet-yags.pdf` (within directory: `YAGSDIR/doc/`) may be useful. All other chapters may contain errors, broken links and misleading information (with higher probability).

The first official version will be 0.0.2 and is scheduled to be ready this year (2016), so come back soon.

1.2 Welcome to YAGS

YAGS - *Yet Another Graph System* is a computing system for dealing with graphs, in the sense of Graph Theory (not bar graphs, pie charts nor graphs of functions). Hence our graphs are ordered pairs $G = (V, E)$, where V is a finite set of vertices and E is a finite set of edges which are (ordered or unordered) pairs of vertices.

YAGS was initiated by M.A. Pizaña in May 2003, and soon incorporated the work of R. MacKinney-Romero and R. Villarroel-Flores.

Our motivation here was this and that.

Our Pourposes and Aim.

authors, contacts

1.3 Citing YAGS

If you publish a result and you used YAGS during your research, please cite us as you would normally do with a research paper:

R. MacKinney-Romero, M.A. Pizaña and R. Villarroel-Flores.
YAGS - Yet Another Graph System, Version 0.0.1 (2016)
http://xamanek.izt.uam.mx/yags/

```
@manual{YAGS, author = {R. MacKinney-Romero and M.A. Pizaña and R.
Villarroel-Flores}, title = {YAGS - Yet Another Graph System, Version 0.0.1},
year = {2016}, note = {http://xamanek.izt.uam.mx/yags/}, }
```

1.4 Copyright

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1.6   More Information

More information about YAGS can be found on its official web page:

    'http://xamanek.izt.uam.mx/yags/'

    You can receive notifications about YAGS (i.e. new releases, bug fixes, etc.) by subscribing to its email distribution list:

    'http://xamanek.izt.uam.mx/cgi-bin/mailman/listinfo/yagsnews/'

    If you are a developer, you may contribute to our project on public repository:

    'https://github.com/yags/main/'

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YAGS Functions by Topic

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A.9   Cliques

Functions dealing with cliques.

- `Basement( G, KnG, x )`
  `Basement( G, KnG, V )`
  Returns the basement of vertex x (vertex set V) of the iterated clique graph KnG with respect to G.

- `CliqueGraph( G )`
  `CliqueGraph( G, maxNumCli )`
  Returns the intersection graph of the (maximal) cliques of G; aborts if $maxNumCli$ cliques are found.

- `CliqueNumber( G )`
  Returns the order, $\omega(G)$, of a maximum clique of G.

- Cliques(*G*)
  Cliques(*G*, *maxNumCli*)
  Returns the list of (maximal) cliques of `G`; aborts if `maxNumCli` cliques are found.

- CompletesOfGivenOrder(*G*, *Ord*)
  Returns the list of vertex sets of all complete subgraphs of order `Ord` of `G`.

- IsCliqueGated(*G*)
  Returns 'true' if `G` is a clique gated graph.

- IsCliqueHelly(*G*)
  Returns 'true' if the set of (maximal) cliques `G` satisfy the *Helly* property.

- IsComplete(*G*, *L*)
  Returns 'true' if `L` induces a complete subgraph of `G`.

- IsCompleteGraph(*G*)
  Returns 'true' if graph `G` is a complete graph, 'false' otherwise.

- NumberOfCliques(*G*)
  NumberOfCliques(*G*, *maxNumCli*)
  Returns the number of (maximal) cliques of `G`.

A.10   Morphisms and Isomorphisms

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Appendix B

YAGS Functions Reference

This chapter contains a complete list of all YAGS's functions, with definitions, in alphabetical order.

B.1 Primera seccion

B.1.1 Order

▷ Order(*G*)   (attribute)

Returns the number of vertices, of graph *G*.

```
 ─────────────── Example ───────────────
 gap> Order(Icosahedron);
 12
```

B.1.2 AddEdges

▷ AddEdges(*G, E*)   (operation)

Returns a new graph created from graph *G* by adding the edges in list *E*.

```
 ─────────────── Example ───────────────
 gap> g:=CycleGraph(4);
 Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
 [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
 gap> AddEdges(g,[[1,3]]);
 Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
 [ [ 2, 3, 4 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3 ] ] )
 gap> AddEdges(g,[[1,3],[2,4]]);
 Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
 [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

B.1.3 AddVerticesByAdjacencies

▷ AddVerticesByAdjacencies(*G, NewAdjList*)   (operation)

Returns a new graph created from graph `G` by adding as many new vertices as Length(*NewAdjList*). Each entry in *NewAdjList* is also a list: the list of neighbors of the corresponding new vertex.

```
———————————————— Example ————————————————
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> AddVerticesByAdjacencies(g,[[1,2],[4,5]]);
Graph( Category := SimpleGraphs, Order := 7, Size := 8, Adjacencies :=
[ [ 2, 6 ], [ 1, 3, 6 ], [ 2, 4 ], [ 3, 5, 7 ], [ 4, 7 ], [ 1, 2 ], [ 4, 5 ] ] )
gap> AddVerticesByAdjacencies(g,[[1,2,7],[4,5]]);
Graph( Category := SimpleGraphs, Order := 7, Size := 9, Adjacencies :=
[ [ 2, 6 ], [ 1, 3, 6 ], [ 2, 4 ], [ 3, 5, 7 ], [ 4, 7 ], [ 1, 2, 7 ], [ 4, 5, 6 ] ] )
```

B.1.4 Adjacencies

▷ Adjacencies(*G*)   (operation)

Returns the adjacency lists of graph `G`.

```
———————————————— Example ————————————————
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> Adjacencies(g);
[ [ 2 ], [ 1, 3 ], [ 2 ] ]
```

B.1.5 Adjacency

▷ Adjacency(*G, x*)   (operation)

Returns the adjacency list of vertex `x` in `G`.

```
———————————————— Example ————————————————
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> Adjacency(g,1);
[ 2 ]
gap> Adjacency(g,2);
[ 1, 3 ]
```

B.1.6 AdjMatrix

▷ AdjMatrix(*G*)   (attribute)

Returns the adjacency matrix of graph `G`.

```
———————————————— Example ————————————————
gap> AdjMatrix(CycleGraph(4));
[ [ false, true, false, true ], [ true, false, true, false ],
  [ false, true, false, true ], [ true, false, true, false ] ]
```

B.1.7 AGraph

▷ AGraph (global variable)

A 4-cycle with two pendant vertices on consecutive vertices of the cycle.

```
——————————————————————— Example ———————————————————————
gap> AGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 5 ], [ 2, 4 ], [ 3, 5 ], [ 2, 4, 6 ], [ 5 ] ] )
```

B.1.8 AntennaGraph

▷ AntennaGraph (global variable)

A `HouseGraph` with a pendant vertex (antenna) on the roof.

```
——————————————————————— Example ———————————————————————
gap> AntennaGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 1, 4, 6 ], [ 5 ] ] )
```

B.1.9 AutomorphismGroup

▷ AutomorphismGroup(*G*) (attribute)
▷ AutGroupGraph(*G*) (attribute)

Returns the group of automorphisms of the graph *G*. Both forms are synonyms.

```
——————————————————————— Example ———————————————————————
gap> AutomorphismGroup(Icosahedron);
Group([ (1,3,2,10,9,12,8,7,5,4)(6,11), (1,7,9)(2,4,12)(3,11,10)(5,8,6) ])
gap> AutGroupGraph(Icosahedron);
Group([ (1,3,2,10,9,12,8,7,5,4)(6,11), (1,7,9)(2,4,12)(3,11,10)(5,8,6) ])
```

B.1.10 BackTrack

▷ BackTrack(*L, Opts, Chk, Done, Extra*) (operation)

Generic, user-customizable backtracking algorithm.

A backtraking algorithm explores a decision tree in search for solutions to a combinatorial problem. The combinatorial problem and the search strategy are specified by the parameters: *L* is just a list that `BackTrack` uses to keep track of solutions and partial solutions. It is usually set to the empty list as a starting point. After a solution is found, it is returned *and* stored in *L*. This value of *L* is then used as a starting point to search for the next solution in case `BackTrack` is called again. Partial solutions are also stored in *L* during the execution of `BackTrack`. *Extra* may be any object, list, record, etc. `BackTrack` only uses it to pass this data to the user-defined functions *Opts*, *Chk* and *Done*, therefore offering you a way to share data between your functions. *Opts*:=function(L,extra) must return the list of continuation options (childs) one has after some partial solution (node) *L* has been reached within the decision tree (*Opts* may use the extra data *Extra* as needed). Each of the values in the list returned by *Opts*(L,extra) will be tried as possible continuations of the partial

solution `L`. If `Opts`(L,extra) always returns the same list, you can put that list in place of the parameter `Opts`. `Chk`:=function(L,extra) must evaluate the partial solution `L` possibly using the extra data `Extra` and must return `false` when it knows that `L` can not be extended to a solution of the problem. Otherwise it returns `true`. `Chk` may assume that `L{[1..Length(L)-1]}` already passed the test. `Done`:=function(L,extra) returns `true` if `L` is already a complete solution and `false` otherwise. In many combinatorial problems, any partial solution of certain length `n` is also a solution (and viceversa), so if this is your case, you can put that length in place of the parameter `Done`.

The following example uses `BackTrack` in its simplest form to compute derrangements (permutations of a set, where none of the elements appears in its original position).

```
─────────────────────── Example ───────────────────────
 gap> N:=4;;L:=[];;extra:=[];;opts:=[1..N];;done:=N;;
 gap> chk:=function(L,extra) local i; i:=Length(L);
 >            return not L[i] in L{[1..i-1]} and L[i]<> i; end;;
 gap> BackTrack(L,opts,chk,done,extra);
 [ 2, 1, 4, 3 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 2, 3, 4, 1 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 2, 4, 1, 3 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 3, 1, 4, 2 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 3, 4, 1, 2 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 3, 4, 2, 1 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 4, 1, 2, 3 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 4, 3, 1, 2 ]
 gap> BackTrack(L,opts,chk,done,extra);
 [ 4, 3, 2, 1 ]
 gap> BackTrack(L,opts,chk,done,extra);
 fail
```

B.1.11 BackTrackBag

▷ BackTrackBag(`Opts, Chk, Done, Extra`)   (operation)

Returns the list of all solutions that would be returned one at a time by `Backtrack`.

The following example computes all derrangements of order 4.

```
─────────────────────── Example ───────────────────────
 gap> N:=4;;
 gap> chk:=function(L,extra) local i; i:=Length(L);
 >            return not L[i] in L{[1..i-1]} and L[i]<> i; end;;
 gap> BackTrackBag([1..N],chk,N,[]);
 [ [ 2, 1, 4, 3 ], [ 2, 3, 4, 1 ], [ 2, 4, 1, 3 ], [ 3, 1, 4, 2 ],
   [ 3, 4, 1, 2 ], [ 3, 4, 2, 1 ], [ 4, 1, 2, 3 ], [ 4, 3, 1, 2 ],
   [ 4, 3, 2, 1 ] ]
```

B.1.12 Basement

▷ Basement(*G, KnG, x*) (operation)
▷ Basement(*G, KnG, V*) (operation)

Given a graph *G*, some iterated clique graph *KnG* of *G* and a vertex *x* of *KnG*, the operation returns the *basement* of *x* with respect to *G* [14]. Loosely speaking, the basement of *x* is the set of vertices of *G* that constitutes the iterated clique *x*.

``` Example
gap> g:=Icosahedron;;Cliques(g);
[ [ 1, 2, 3 ], [ 1, 2, 6 ], [ 1, 3, 4 ], [ 1, 4, 5 ], [ 1, 5, 6 ],
  [ 4, 5, 7 ], [ 4, 7, 11 ], [ 5, 7, 8 ], [ 7, 8, 12 ], [ 7, 11, 12 ],
  [ 5, 6, 8 ], [ 6, 8, 9 ], [ 8, 9, 12 ], [ 2, 6, 9 ], [ 2, 9, 10 ],
  [ 9, 10, 12 ], [ 2, 3, 10 ], [ 3, 10, 11 ], [ 10, 11, 12 ], [ 3, 4, 11 ] ]
gap> kg:=CliqueGraph(g);; k2g:=CliqueGraph(kg);;
gap> Basement(g,k2g,1);Basement(g,k2g,2);
[ 1, 2, 3, 4, 5, 6 ]
[ 1, 2, 3, 4, 6, 10 ]
```

In its second form, *V* is a set of vertices of *KnG*, in that case, the basement is simply the union of the basements of the vertices in *V*.

``` Example
gap> Basement(g,k2g,[1,2]);
[ 1, 2, 3, 4, 5, 6, 10 ]
```

B.1.13 BoundaryVertices

▷ BoundaryVertices(*G*) (attribute)

When *G* is a compact surface, it returns the list of vertices in the boundary (of the triangulation) of the surface. That is, the list of vertices of *G* that have links isomorphic to a path. It returns fail if *G* is not a compact surface.

``` Example
gap> BoundaryVertices(WheelGraph(4,2));
[ 6, 7, 8, 9 ]
gap> BoundaryVertices(Octahedron);
[  ]
```

B.1.14 BoxProduct

▷ BoxProduct(*G, H*) (operation)

Returns the box product, $G \square H$, of two graphs *G* and *H* (also known as the cartesian product).

The box product is calculated as follows:

For each pair of vertices $x \in G, y \in H$ we create a vertex (x,y). Given two such vertices (x,y) and (x',y') they are adjacent iff $x = x$ and $y \sim y'$ or $x \sim x'$ and $y = y'$.

``` Example
gap> g:=PathGraph(3);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

```
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
  [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
  gap> gh:=BoxProduct(g,h);
  Graph( Category := SimpleGraphs, Order := 12, Size := 20, Adjacencies :=
  [ [ 2, 4, 5 ], [ 1, 3, 6 ], [ 2, 4, 7 ], [ 1, 3, 8 ], [ 1, 6, 8, 9 ],
    [ 2, 5, 7, 10 ], [ 3, 6, 8, 11 ], [ 4, 5, 7, 12 ], [ 5, 10, 12 ],
    [ 6, 9, 11 ], [ 7, 10, 12 ], [ 8, 9, 11 ] ] )
  gap> VertexNames(gh);
  [ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ],
    [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

B.1.15 BoxTimesProduct

▷ BoxTimesProduct(*G, H*) (operation)

Returns the boxtimes product of two graphs *G* and *H*, *G* ⊠ *H* (also known as the strong product). The boxtimes product is calculated as follows:

For each pair of vertices $x \in G, y \in H$ we create a vertex (x,y). Given two such vertices (x,y) and (x',y') such that $(x,y) \neq (x',y')$ they are adjacent iff $x \simeq x'$ and $y \simeq y'$.

—————————————————— Example ——————————————————
```
  gap> g:=PathGraph(3);h:=CycleGraph(4);
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
  [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
  gap> gh:=BoxTimesProduct(g,h);
  Graph( Category := SimpleGraphs, Order := 12, Size := 36, Adjacencies :=
  [ [ 2, 4, 5, 6, 8 ], [ 1, 3, 5, 6, 7 ], [ 2, 4, 6, 7, 8 ], [ 1, 3, 5, 7, 8 ],
    [ 1, 2, 4, 6, 8, 9, 10, 12 ], [ 1, 2, 3, 5, 7, 9, 10, 11 ],
    [ 2, 3, 4, 6, 8, 10, 11, 12 ], [ 1, 3, 4, 5, 7, 9, 11, 12 ],
    [ 5, 6, 8, 10, 12 ], [ 5, 6, 7, 9, 11 ], [ 6, 7, 8, 10, 12 ],
    [ 5, 7, 8, 9, 11 ] ] )
  gap> VertexNames(gh);
  [ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ],
    [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

B.1.16 BullGraph

▷ BullGraph (global variable)

A triangle with two pendant vertices (horns).
—————————————————— Example ——————————————————
```
  gap> BullGraph;
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
  [ [ 2 ], [ 1, 3, 4 ], [ 2, 4 ], [ 2, 3, 5 ], [ 4 ] ] )
```

B.1.17 CayleyGraph

▷ CayleyGraph(*Grp, Elms*) (operation)
▷ CayleyGraph(*Grp*) (operation)

Returns the graph *G* whose vertices are the elements of the group `Grp` such that *x* is adjacent to *y* iff $x * g = y$ for some *g* in the list `Elms`. if `Elms` is not provided, then the generators of `G` are used instead.

```
──────────────── Example ────────────────
gap> grp:=Group((1,2,3),(1,2));
Group([ (1,2,3), (1,2) ])
gap> CayleyGraph(grp);
Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
[ [ 3, 4, 5 ], [ 3, 5, 6 ], [ 1, 2, 6 ], [ 1, 5, 6 ], [ 1, 2, 4 ],
  [ 2, 3, 4 ] ] )
gap> CayleyGraph(grp,[(1,2),(2,3)]);
Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
[ [ 2, 3 ], [ 1, 5 ], [ 1, 4 ], [ 3, 6 ], [ 2, 6 ], [ 4, 5 ] ] )
```

B.1.18   ChairGraph

▷ ChairGraph   (global variable)

A tree with degree sequence 3,2,1,1,1.

```
──────────────── Example ────────────────
gap> ChairGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3, 4 ], [ 2 ], [ 2, 5 ], [ 4 ] ] )
```

B.1.19   Circulant

▷ Circulant(n, Jumps)   (operation)

Returns the graph G whose vertices are [1..n] such that x is adjacent to y iff x+z=y mod n for some z the list of `Jumps`.

```
──────────────── Example ────────────────
gap> Circulant(6,[1,2]);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 5, 6 ], [ 1, 3, 4, 6 ], [ 1, 2, 4, 5 ], [ 2, 3, 5, 6 ],
  [ 1, 3, 4, 6 ], [ 1, 2, 4, 5 ] ] )
```

B.1.20   ClawGraph

▷ ClawGraph   (global variable)

The graph on 4 vertices, 3 edges, and maximum degree 3.

```
──────────────── Example ────────────────
gap> ClawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1 ] ] )
```

B.1.21 CliqueGraph

▷ CliqueGraph(*G*)   (attribute)
▷ CliqueGraph(*G, maxNumCli*)   (operation)

   Returns the intersection graph of all the (maximal) cliques of G.
   The additional parameter *maxNumCli* aborts the computation when *maxNumCli* cliques are found, even if they are all the cliques of G. If the bound *maxNumCli* is reached, *fail* is returned.

─────────────────── Example ───────────────────
```
gap> CliqueGraph(Octahedron);
Graph( Category := SimpleGraphs, Order := 8, Size := 24, Adjacencies :=
[ [ 2, 3, 4, 5, 6, 7 ], [ 1, 3, 4, 5, 6, 8 ], [ 1, 2, 4, 5, 7, 8 ],
  [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 4, 5, 7, 8 ],
  [ 1, 3, 4, 5, 6, 8 ], [ 2, 3, 4, 5, 6, 7 ] ] )
gap> CliqueGraph(Octahedron,9);
Graph( Category := SimpleGraphs, Order := 8, Size := 24, Adjacencies :=
[ [ 2, 3, 4, 5, 6, 7 ], [ 1, 3, 4, 5, 6, 8 ], [ 1, 2, 4, 5, 7, 8 ],
  [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 4, 5, 7, 8 ],
  [ 1, 3, 4, 5, 6, 8 ], [ 2, 3, 4, 5, 6, 7 ] ] )
gap> CliqueGraph(Octahedron,8);
fail
```

B.1.22 CliqueNumber

▷ CliqueNumber(*G*)   (attribute)

   Returns the order, $\omega(G)$, of a maximum clique of G.

─────────────────── Example ───────────────────
```
gap> g:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size := 14, Adjacencies :=
[ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ], [ 2, 3, 5, 6, 8 ], [ 4, 6 ],
  [ 2, 4, 5, 7, 8 ], [ 6, 8 ], [ 1, 2, 4, 6, 7 ] ] )
gap> CliqueNumber(g);
4
```

B.1.23 Cliques

▷ Cliques(*G*)   (attribute)
▷ Cliques(*G, maxNumCli*)   (operation)

   Returns the set of all (maximal) cliques of a graph G. A clique is a maximal complete subgraph. Here, we use the Bron-Kerbosch algorithm [1].
   In the second form, It stops computing cliques after *maxNumCli* of them have been found.

─────────────────── Example ───────────────────
```
gap> Cliques(Octahedron);
[ [ 1, 3, 5 ], [ 1, 3, 6 ], [ 1, 4, 5 ], [ 1, 4, 6 ], [ 2, 3, 5 ],
  [ 2, 3, 6 ], [ 2, 4, 5 ], [ 2, 4, 6 ] ]
gap> Cliques(Octahedron,4);
[ [ 1, 3, 5 ], [ 1, 3, 6 ], [ 1, 4, 5 ], [ 1, 4, 6 ] ]
```

B.1.24 ClockworkGraph (basic)

▷ ClockworkGraph(*NNFSList*)   (operation)
▷ ClockworkGraph(*NNFSList, rank*)   (operation)
▷ ClockworkGraph(*NNFSList, Perm*)   (operation)
▷ ClockworkGraph(*NNFSList, rank, Perm*)   (operation)

Returns the clockwork graph [10][12] specified by its parameters. A clockwork graph consists of two parts: the crown and the core, both of them are *cyclically segmented*. When not specified, the rank is assumed to be 2 and the *return permutation*, Perm, is assumed to be trivial, let us assume this is our case. Consider the following examples:

```
─────────────────────────── Example ───────────────────────────
gap> ClockworkGraph([[0],[0],[0],[0]]);
Graph( Category := SimpleGraphs, Order := 12, Size := 28, Adjacencies :=
[ [ 2, 3, 4, 10, 12 ], [ 1, 3, 5, 11, 12 ], [ 1, 2, 4, 5 ], [ 1, 3, 5, 6, 7 ],
  [ 2, 3, 4, 6, 8 ], [ 4, 5, 7, 8 ], [ 4, 6, 8, 9, 10 ], [ 5, 6, 7, 9, 11 ],
  [ 7, 8, 10, 11 ], [ 1, 7, 9, 11, 12 ], [ 2, 8, 9, 10, 12 ], [ 1, 2, 10, 11 ] ] )
gap> ClockworkGraph([[1],[1],[1],[1]]);
Graph( Category := SimpleGraphs, Order := 12, Size := 32, Adjacencies :=
[ [ 2, 3, 4, 10, 12 ], [ 1, 3, 5, 11, 12 ], [ 1, 2, 4, 5, 6, 12 ], [ 1, 3, 5, 6, 7 ],
  [ 2, 3, 4, 6, 8 ], [ 3, 4, 5, 7, 8, 9 ], [ 4, 6, 8, 9, 10 ], [ 5, 6, 7, 9, 11 ],
  [ 6, 7, 8, 10, 11, 12 ], [ 1, 7, 9, 11, 12 ], [ 2, 8, 9, 10, 12 ],
  [ 1, 2, 3, 9, 10, 11 ] ] )
```

In both cases, the crown is the subgraph induced by the vertices $\{1,2,4,5,7,8,10,11\}$ and the core is induced by $\{3,6,9,12\}$. Also in both cases the cyclic segmentations (partitions) of the crown and the core are $\{\{1,2\},\{4,5\},\{7,8\},\{10,11\}\}$ and $\{\{3\},\{6\},\{9\},\{12\}\}$ respectively. The number of segmentes s is specified by s:=Length(*NNFSList*) which is 4 in these cases. The crown is isomorphic to BoxProduct(CycleGraph(s),Completegraph(rank)): All the crown segments are complete subgraphs and the vertices of cyclically consecutive segments are joined by a perfect matching. The adjacencies between crown and core vertices are simple to describe: Cyclically intercalate crown and core segments, making each core vertex adjacent to the vertices in the previous and the following crown segments. Hence in our examples vertex 3 is adjacent to vertices 1 and 2 (previous segment), but also 4 and 5 (following segment). Note that since the segmentations and intercalations are *cyclic*, we have that vertex 12 is adjacent to 10 and 11, but also to 1 and 2. Finally the edges between core vertices are as follows: first each core segment is a complete subgraph; the vertices within each core segment are linearly ordered and for vertex number t in segment number s there is a non-negative integer *NNFSList*[s][t] which specifies, the *Number of Neighbors in the Following core Segment* for that vertex (hence the name *NNFSList*) (Since the vertices in core segments are linearly ordered, it is enough to specify the *number* of neighbors in the following segment and the *first* ones of those are selected as the neighbors). Hence in our two examples above, each core segment consists of exaclty one vertex. In the first example each core segment is adjacent to no vertex in the following segment (e.g. 3 is not adjacent to 6) but in the second one, each core segment is adjacent to exactly one vertex in the following segment (e.g. 3 is adjacent to 6).

A more complicated example should be now mostly self-explanatory:

```
─────────────────────────── Example ───────────────────────────
gap> ClockworkGraph([[2],[0,1,3],[0,1,1],[1]]);
Graph( Category := SimpleGraphs, Order := 16, Size := 59, Adjacencies :=
```

```
[ [ 2, 3, 4, 14, 16 ], [ 1, 3, 5, 15, 16 ], [ 1, 2, 4, 5, 6, 7, 16 ],
  [ 1, 3, 5, 6, 7, 8, 9 ], [ 2, 3, 4, 6, 7, 8, 10 ], [ 3, 4, 5, 7, 8, 9, 10 ],
  [ 3, 4, 5, 6, 8, 9, 10, 11 ], [ 4, 5, 6, 7, 9, 10, 11, 12, 13 ],
  [ 4, 6, 7, 8, 10, 11, 12, 13, 14 ], [ 5, 6, 7, 8, 9, 11, 12, 13, 15 ],
  [ 7, 8, 9, 10, 12, 13, 14, 15 ], [ 8, 9, 10, 11, 13, 14, 15, 16 ],
  [ 8, 9, 10, 11, 12, 14, 15, 16 ], [ 1, 9, 11, 12, 13, 15, 16 ],
  [ 2, 10, 11, 12, 13, 14, 16 ], [ 1, 2, 3, 12, 13, 14, 15 ] ] )
```

The crown and core segmentations are $\{\{1,2\},\{4,5\},\{9,10\},\{14,15\}\}$ and $\{\{3\},\{6,7,8\},\{11,12,13\},\{16\}\}$ respectively and the adjacencies specified by the *NNFSList* are: 3 is adjacent to 6 and 7; 6 is adjacent to none (in the following core segment); 7 is adjacent to 11; 8 to 11, 12 and 13; 11 to none; 12 to 16; 13 to 16 and 16 to 3.

When `rank` and/or `Perm` are specified, they have the following effects: `rank` (which must be at least 2) is the number of vertices in each crown segment, and `Perm` (which must belong to SymmetricGroup(`rank`)) specifies the perfect matching joining the vertices in the last crown segment with the vertices in the first crown segment: The k-th vertex in the last crown segment $k \in \{1, 2, \ldots, rank\}$ is made adjacent to the *Perm*(k)-th vertex of the first crown segment.

A number of requisites are put forward in the literature for a graph to be a clockwork graph but this operation does not enforce those conditions, on the contrary, it tries to make sense of the data provided as much as possible. For instance *NNFSList*:=[[2],[2],[2],[2]] would be inconsistent since there are not enough vertices in each core segment to provide for the required 2 neighbors. However, the result is just the same as with *NNFSList*:=[[1],[1],[1],[1]]. The requisites that are mandatory are exactly these: the `rank` must be at least 2, `Perm` must belong to SymmetricGroup(`rank`), *NNFSList* must be a list of lists of non-negative integers, and the number of segments (= Length(*NNFSList*)) must be at least 3. A call to ClockworkGraph which fails to conform to these requisites will produce an error.

Clockwork graphs have been very useful in constructing examples and counter-examples in clique graph theory. In particular, they have been used to construct examples of clique-periodic graphs of all possible periods [3], clique-divergent graphs of linear and polynomial growth rate [8][10], clique-convergent graphs whose period is not invariant under removal of dominated vertices [4], clique-convergent graphs which become clique-divergent by just gluing a 4-cycle to a vertex [5], rank-divergent graphs [13], etc.

B.1.25 ComplementGraph

▷ ComplementGraph(*G*) (attribute)

Returns the new graph H such that $V(H) = V(G)$ and $xy \in E(H) \iff xy \notin E(G)$.

──────────── Example ────────────
```
gap> g:=ClawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1 ] ] )
gap> ComplementGraph(g);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [  ], [ 3, 4 ], [ 2, 4 ], [ 2, 3 ] ] )
```

B.1.26 CompleteBipartiteGraph

▷ CompleteBipartiteGraph(`n, m`) (function)

Returns the complete bipartite whose parts have order `n` and `m` respectively. This is the joint (Zykov sum) of two discrete graphs of order `n` and `m`.

―――――――――――――――――――――――― Example ――――――――――――――――――――――――
```
gap> CompleteBipartiteGraph(2,3);
Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
[ [ 3, 4, 5 ], [ 3, 4, 5 ], [ 1, 2 ], [ 1, 2 ], [ 1, 2 ] ] )
```

B.1.27 CompleteGraph

▷ CompleteGraph(`n`) (function)

Returns the complete graph of order `n`. A complete graph is a graph where all vertices are connected to each other.

―――――――――――――――――――――――― Example ――――――――――――――――――――――――
```
gap> CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

B.1.28 CompletelyParedGraph

▷ CompletelyParedGraph(`G`) (operation)

Returns the completely pared graph of `G`, which is obtained by repeatedly applying `ParedGraph` until no more dominated vertices remain.

―――――――――――――――――――――――― Example ――――――――――――――――――――――――
```
gap> g:=PathGraph(6);
Graph( Category := SimpleGraphs, Order := 6, Size := 5, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4, 6 ], [ 5 ] ] )
gap> CompletelyParedGraph(g);
Graph( Category := SimpleGraphs, Order := 1, Size := 0, Adjacencies :=
[ [ ] ] )
```

B.1.29 CompleteMultipartiteGraph

▷ CompleteMultipartiteGraph(`n1, n2`) (function)

Returns the complete multipartite graph where the orders of the parts are `n1`, `n2`, ... It is also the Zykov sum of discrete graphs of order `n1`, `n2`, ...

―――――――――――――――――――――――― Example ――――――――――――――――――――――――
```
gap> CompleteMultipartiteGraph(2,2,2);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
  [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

B.1.30   CompletesOfGivenOrder

▷ CompletesOfGivenOrder(G, Ord)   (operation)

Returns the list of vertex sets of all complete subgraphs of order Ord of G.

```
———————————————————————————— Example —————————————————————————————
gap> g:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size := 14, Adjacencies :=
[ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ], [ 2, 3, 5, 6, 8 ], [ 4, 6 ],
  [ 2, 4, 5, 7, 8 ], [ 6, 8 ], [ 1, 2, 4, 6, 7 ] ] )
gap> CompletesOfGivenOrder(g,3);
[ [ 1, 2, 8 ], [ 2, 3, 4 ], [ 2, 4, 6 ], [ 2, 4, 8 ], [ 2, 6, 8 ],
  [ 4, 5, 6 ], [ 4, 6, 8 ], [ 6, 7, 8 ] ]
gap> CompletesOfGivenOrder(g,4);
[ [ 2, 4, 6, 8 ] ]
```

B.1.31   Composition

▷ Composition(G, H)   (operation)

Returns the composition $G[H]$ of two graphs G and H.

A composition of graphs is obtained by calculating the GraphSum of G with Order(G) copies of H, $G[H] = GraphSum(G, [H, \ldots, H])$.

```
———————————————————————————— Example —————————————————————————————
gap> g:=CycleGraph(4);;h:=DiscreteGraph(2);;
gap> Composition(g,h);
Graph( Category := SimpleGraphs, Order := 8, Size := 16, Adjacencies :=
[ [ 3, 4, 7, 8 ], [ 3, 4, 7, 8 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
  [ 3, 4, 7, 8 ], [ 3, 4, 7, 8 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ] ] )
```

B.1.32   Cone

▷ Cone(G)   (operation)

Returns the cone of graph G. The cone of G is the graph obtained from G by adding a new vertex which is adjacent to every vertex of G. The new vertex is the first one in the new graph.

```
———————————————————————————— Example —————————————————————————————
gap> Cone(CycleGraph(4));
Graph( Category := SimpleGraphs, Order := 5, Size := 8, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 5 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 2, 4 ] ] )
```

B.1.33   ConnectedComponents

▷ ConnectedComponents(G)   (attribute)

Returns the connected components of G.

B.1.34   ConnectedGraphsOfGivenOrder

▷ ConnectedGraphsOfGivenOrder(*n*)   (operation)

Returns the list of all connected graphs of order *n* (upto isomorphism). This operation uses Brendan McKay's data published here: \URL{https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html}.

These data are included with the YAGS distribution in its `data` directory. Hence this operation simply reads the corresponding file in that directory using `ImportGraph6( Filename )`. Therefore, the integer *n* must be in the range from 1 upto 9. Data for graphs on 10 vertices is also available, but not included with YAGS, it may not be practical to use that data, but if you would like to try, all you have to do is to copy (and to uncompress) the corresponding file into the directory *YAGS-Directory*/data.

```
————————————————————————— Example —————————————————————————
gap> ConnectedGraphsOfGivenOrder(3);
[ Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
    [ [ 3 ], [ 3 ], [ 1, 2 ] ] ), Graph( Category := SimpleGraphs, Order :=
    3, Size := 3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] ) ]
gap> ConnectedGraphsOfGivenOrder(4);
[ Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
    [ [ 4 ], [ 4 ], [ 4 ], [ 1, 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
    [ [ 3, 4 ], [ 4 ], [ 1 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 3, 4 ], [ 4 ], [ 1, 4 ], [ 1, 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 3, 4 ], [ 3, 4 ], [ 1, 2 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
    [ [ 3, 4 ], [ 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
    [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] ) ]
gap> Length(ConnectedGraphsOfGivenOrder(9));
261080
gap> ConnectedGraphsOfGivenOrder(10);
#W Unreadable File: /opt/gap4r7/pkg/yags/data/graph10c.g6
fail
```

B.1.35   Coordinates

▷ Coordinates(*G*)   (operation)

Gets the coordinates of the vertices of *G*, which are used to draw *G* by `Draw( G )`. If the coordinates have not been previously set, `Coordinates` returns *fail*.

```
————————————————————————— Example —————————————————————————
gap> g:=CycleGraph(4);;
gap> Coordinates(g);
fail
gap> SetCoordinates(g,[[-10,-10 ],[-10,20],[20,-10 ], [20,20]]);
gap> Coordinates(g);
[ [ -10, -10 ], [ -10, 20 ], [ 20, -10 ], [ 20, 20 ] ]
```

B.1.36 CopyGraph

▷ CopyGraph(*G*)   (operation)

Returns a fresh copy of graph *G*. Only the order and adjacency information is copied, all other known attributes of *G* are not. Mainly used to transform a graph from one category to another. The new graph will be forced to comply with the `TargetGraphCategory`.

```
――――――――――― Example ―――――――――――
gap> g:=CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> g1:=CopyGraph(g:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 3, 4 ], [ 4 ], [ ] ] )
gap> CopyGraph(g1:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

B.1.37 Cube

▷ Cube   (global variable)

The 1-skeleton of Plato's cube.

```
――――――――――― Example ―――――――――――
gap> Cube;
Graph( Category := SimpleGraphs, Order := 8, Size := 12, Adjacencies :=
[ [ 2, 3, 5 ], [ 1, 4, 6 ], [ 1, 4, 7 ], [ 2, 3, 8 ], [ 1, 6, 7 ],
  [ 2, 5, 8 ], [ 3, 5, 8 ], [ 4, 6, 7 ] ] )
```

B.1.38 CubeGraph

▷ CubeGraph(*n*)   (function)

Returns the hypercube of dimension *n*. This is the box product (cartesian product) of *n* copies of K_2 (an edge).

```
――――――――――― Example ―――――――――――
gap> CubeGraph(3);
Graph( Category := SimpleGraphs, Order := 8, Size := 12, Adjacencies :=
[ [ 2, 3, 5 ], [ 1, 4, 6 ], [ 1, 4, 7 ], [ 2, 3, 8 ], [ 1, 6, 7 ],
  [ 2, 5, 8 ], [ 3, 5, 8 ], [ 4, 6, 7 ] ] )
```

B.1.39 CycleGraph

▷ CycleGraph(*n*)   (function)

Returns the cyclic graph on *n* vertices.

```
――――――――――― Example ―――――――――――
gap> CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
[ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
```

B.1.40 CylinderGraph

▷ CylinderGraph(*b, h*)   (function)

Returns a cylinder of base *b* and height *h*. The order of this graph is *b*(*h*+1) and it is constructed by taking *h*+1 copies of the cyclic graph on *b* vertices, ordering these cycles linearly and then joining consecutive cycles by a zigzagging (2*b*)-cycle. This graph is a triangulation of the cylinder where all internal vertices are of degree 6 and the border vertices are of degree 4.

```
———————————————————————————— Example ————————————————————————————
gap> g:=CylinderGraph(4,1);
Graph( Category := SimpleGraphs, Order := 8, Size := 16, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3, 6, 7 ], [ 2, 4, 7, 8 ], [ 1, 3, 5, 8 ],
  [ 1, 4, 6, 8 ], [ 1, 2, 5, 7 ], [ 2, 3, 6, 8 ], [ 3, 4, 5, 7 ] ] )
gap> g:=CylinderGraph(4,2);
Graph( Category := SimpleGraphs, Order := 12, Size := 28, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3, 6, 7 ], [ 2, 4, 7, 8 ], [ 1, 3, 5, 8 ],
  [ 1, 4, 6, 8, 9, 10 ], [ 1, 2, 5, 7, 10, 11 ], [ 2, 3, 6, 8, 11, 12 ],
  [ 3, 4, 5, 7, 9, 12 ], [ 5, 8, 10, 12 ], [ 5, 6, 9, 11 ], [ 6, 7, 10, 12 ],
  [ 7, 8, 9, 11 ] ] )
```

B.1.41 DartGraph

▷ DartGraph   (global variable)

A diamond with a pendant vertex and maximum degree 4.

```
———————————————————————————— Example ————————————————————————————
gap> DartGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 4, 5 ], [ 2, 4, 5 ], [ 2, 3 ], [ 2, 3 ] ] )
```

B.1.42 DeclareQtfyProperty

▷ DeclareQtfyProperty(*Name, Filter*)   (function)

For internal use.

Declares a YAGS quantifiable property named *Name* for filter *Filter*. This in turns, declares a boolean GAP property *Name* and an integer GAP attribute *QtfyName*.

The user must provide the method *Name*(*Obj, qtfy*). If *qtfy* is false, the method must return a boolean indicating whether the property holds, otherwise, the method must return a non-negative integer quantifying how far is the object from satisfying the property. In the latter case, returning 0 actually means that the object does satisfy the property.

```
———————————————————————————— Example ————————————————————————————
gap> DeclareQtfyProperty("Is2Regular",Graphs);
gap> InstallMethod(Is2Regular,"for graphs",true,[Graphs,IsBool],0,
> function(G,qtfy)
>   local x,count;
>   count:=0;
>   for x in Vertices(G) do
>     if VertexDegree(G,x)<> 2 then
>       if not qtfy then
```

```
>            return false;
>          fi;
>              count:=count+1;
>        fi;
>    od;
>    if not qtfy then return true; fi;
>    return count;
> end);
gap> Is2Regular(CycleGraph(4));
true
gap> QtfyIs2Regular(CycleGraph(4));
0
gap> Is2Regular(DiamondGraph);
false
gap> QtfyIs2Regular(DiamondGraph);
2
```

B.1.43 Diameter

▷ Diameter(G) (attribute)

Returns the maximum among the distances between pairs of vertices of G.
―――――――― Example ――――――――
```
gap> g:=CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
[ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
gap> Diameter(g);
2
```

B.1.44 DiamondGraph

▷ DiamondGraph (global variable)

The graph on 4 vertices and 5 edges.
―――――――― Example ――――――――
```
gap> DiamondGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3 ] ] )
```

B.1.45 DiscreteGraph

▷ DiscreteGraph(n) (function)

Returns the discrete graph of order n. A discrete graph is a graph without edges.
―――――――― Example ――――――――
```
gap> DiscreteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 0, Adjacencies :=
[ [  ], [  ], [  ], [  ] ] )
```

B.1.46   DisjointUnion

▷ DisjointUnion(*G, H*)   (operation)

Returns the disjoint union of two graphs *G* and *H*, *G* ⊍ *H*.

```
───────────────────────────── Example ─────────────────────────────
gap> g:=PathGraph(3);h:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> DisjointUnion(g,h);
Graph( Category := SimpleGraphs, Order := 5, Size := 3, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ], [ 5 ], [ 4 ] ] )
```

B.1.47   Distance

▷ Distance(*G, x, y*)   (operation)

Returns the length of a minimal path connecting *x* to *y* in *G*.

```
───────────────────────────── Example ─────────────────────────────
gap> Distance(CycleGraph(5),1,3);
2
gap> Distance(CycleGraph(5),1,5);
1
```

B.1.48   Distances

▷ Distances(*G, A, B*)   (operation)

Given two lists of vertices *A*, *B* of a graph *G*, Distances returns the list of distances for every pair in the cartesian product of *A* and *B*. The order of the vertices in lists *A* and *B* affects the order of the list of distances returned.

```
───────────────────────────── Example ─────────────────────────────
gap> g:=CycleGraph(5);;
gap> Distances(g, [1,3], [2,4]);
[ 1, 2, 1, 1 ]
gap> Distances(g, [3,1], [2,4]);
[ 1, 1, 1, 2 ]
```

B.1.49   DistanceGraph

▷ DistanceGraph(*G, Dist*)   (operation)

Given a graph *G* and list of distances *Dist*, DistanceGraph returns the new graph constructed on the vertices of *G* where two vertices are adjacent iff the distance (in *G*) between them belongs to the list *Dist*.

```
                              ————— Example —————
  gap> g:=CycleGraph(5);
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
  [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
  gap> DistanceGraph(g,[2]);
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
  [ [ 3, 4 ], [ 4, 5 ], [ 1, 5 ], [ 1, 2 ], [ 2, 3 ] ] )
  gap> DistanceGraph(g,[1,2]);
  Graph( Category := SimpleGraphs, Order := 5, Size := 10, Adjacencies :=
  [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 5 ], [ 1, 2, 4, 5 ], [ 1, 2, 3, 5 ],
    [ 1, 2, 3, 4 ] ] )
```

B.1.50 DistanceMatrix

▷ DistanceMatrix(*G*) (attribute)

Returns the distance matrix D of a graph G: D[x][y] is the distance in G from vertex x to vertex y. The matrix may be asymmetric if the graph is not simple. An infinite entry in the matrix means that there is no path between the vertices. Floyd's algorithm is used to compute the matrix.

```
                              ————— Example —————
  gap> g:=PathGraph(4);
  Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
  [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
  gap> Display(DistanceMatrix(g));
  [ [  0,  1,  2,  3 ],
    [  1,  0,  1,  2 ],
    [  2,  1,  0,  1 ],
    [  3,  2,  1,  0 ] ]
  gap> g:=PathGraph(4:GraphCategory:=OrientedGraphs);
  Graph( Category := OrientedGraphs, Order := 4, Size := 3, Adjacencies :=
  [ [ 2 ], [ 3 ], [ 4 ], [  ] ] )
  gap> Display(DistanceMatrix(g));
  [ [        0,        1,        2,        3 ],
    [ infinity,        0,        1,        2 ],
    [ infinity, infinity,        0,        1 ],
    [ infinity, infinity, infinity,        0 ] ]
```

B.1.51 DistanceSet

▷ DistanceSet(*G, A, B*) (operation)

Given two subsets of vertices *A*, *B* of a graph *G*, DistanceSet returns the set of distances for every pair in the cartesian product of *A* and *B*.

```
                              ————— Example —————
  gap> g:=CycleGraph(5);;
  gap> DistanceSet(g, [1,3], [2,4]);
  [ 1, 2 ]
```

B.1.52 Dodecahedron

▷ Dodecahedron   (global variable)

The 1-skeleton of Plato's Dodecahedron.

```
————————————————— Example —————————————————
gap> Dodecahedron;
Graph( Category := SimpleGraphs, Order := 20, Size := 30, Adjacencies :=
[ [ 2, 5, 6 ], [ 1, 3, 7 ], [ 2, 4, 8 ], [ 3, 5, 9 ], [ 1, 4, 10 ],
  [ 1, 11, 15 ], [ 2, 11, 12 ], [ 3, 12, 13 ], [ 4, 13, 14 ], [ 5, 14, 15 ],
  [ 6, 7, 16 ], [ 7, 8, 17 ], [ 8, 9, 18 ], [ 9, 10, 19 ], [ 6, 10, 20 ],
  [ 11, 17, 20 ], [ 12, 16, 18 ], [ 13, 17, 19 ], [ 14, 18, 20 ],
  [ 15, 16, 19 ] ] )
```

B.1.53 DominatedVertices

▷ DominatedVertices(G)   (attribute)

Returns the set of dominated vertices of G.

A vertex x is dominated by another vertex y when the closed neighborhood of x is contained in that of y. However, when there are twin vertices (mutually dominated vertices), exactly one of them (in each equivalent class of mutually dominated vertices) does not appear in the returned set.

```
————————————————— Example —————————————————
gap> g1:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> DominatedVertices(g1);
[ 1, 3 ]
gap> g2:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> DominatedVertices(g2);
[ 2 ]
```

B.1.54 DominoGraph

▷ DominoGraph   (global variable)

Two squares glued by an edge.

```
————————————————— Example —————————————————
gap> DominoGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 4, 6 ], [ 1, 5 ] ] )
```

B.1.55 Draw

▷ Draw(G)   (operation)

Takes a graph G and makes a drawing of it in a separate window. The user can then view and modify the drawing and finally save the vertex coordinates of the drawing into the graph G.

Within the separate window, type h to toggle on/off the help menu. Besides the keyword commands indicated in the help menu, the user may also move vertices (by dragging them), move the whole drawing (by dragging the background) and scale the drawing (by using the mouse wheel).

```
──────────── Example ────────────
gap> Coordinates(Icosahedron);
fail
gap> Draw(Icosahedron);
gap> Coordinates(Icosahedron);
[ [ 29, -107 ], [ 65, -239 ], [ 240, -62 ], [ 78, 79 ], [ -107, 28 ],
  [ -174, -176 ], [ -65, 239 ], [ -239, 62 ], [ -78, -79 ], [ 107, -28 ],
  [ 174, 176 ], [ -29, 107 ] ]
```

Draw() uses an external java program (included with YAGS) and hence, may not work on some platforms.

Current version has been tested successfully on GNU/Linux, Mac OS X and Windows7. For other platforms (specially 32-bit platforms), you should probably (at least) set up correctly the variables YAGSInfo.Draw.prog and YAGSInfo.Draw.opts. The former is a strings representing the external binary program path and name; the latter is a list of strings representing the required command line options. Java binaries are provided for 32 and 64 bit versions of GNU/Linux (which also works for Mac OS X) and of MS Windows.

```
──────────── Example ────────────
gap> YAGSInfo.Draw.prog; YAGSInfo.Draw.opts;
"/usr/share/gap/pkg/yags/bin/draw/application.linux64/draw"
[  ]
```

B.1.56   DumpObject

▷ DumpObject(*Obj*)   (operation)

Dumps all information available for object *Obj*. This information includes to which categories it belongs as well as its type and hashing information used by GAP.

```
──────────── Example ────────────
gap> DumpObject( true );
Object( TypeObj := NewType( NewFamily( "BooleanFamily", [ 11 ], [ 11 ] ),
[ 11, 34 ] ), Categories := [ "IS_BOOL" ] )
```

B.1.57   EasyExec

▷ EasyExec(*Dir, ProgName, InString*)   (operation)
▷ EasyExec(*ProgName, InString*)   (operation)

Calls external program *ProgName* located in directory *Dir*, feeding it with *InString* as input and returning the output of the external program as a string. *Dir* must be a directory object or a list of diretory objects. If *Dir* is not provided, *ProgName* must be in the system's binary PATH. fail is returned if the program could not be located.

```
──────────── Example ────────────
gap> s:=EasyExec("date","");;
gap> s;
"Sun Nov  9 10:36:16 CST 2014\n"
```

```
gap> s:=EasyExec("sort","4\n2\n3\n1");;
gap> s;
"1\n2\n3\n4\n"
```

Currently, this operation is not working on MS Windows.

B.1.58 Eccentricity

▷ Eccentricity(*G, x*) (function)

Returns the distance from a vertex *x* in graph *G* to its most distant vertex in *G*.
```
———————————————————— Example ————————————————————
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> Eccentricity(g,1);
4
gap> Eccentricity(g,3);
2
```

B.1.59 Edges

▷ Edges(*G*) (operation)

Returns the list of edges of graph *G* in the case of `SimpleGraphs`.
```
———————————————————— Example ————————————————————
gap> g1:=CompleteGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size := 3, Adjacencies :=
[ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] )
gap> Edges(g1);
[ [ 1, 2 ], [ 1, 3 ], [ 2, 3 ] ]
```

In the case of `UndirectedGraphs`, it also returns the loops. While in the other categories, `Edges` actually does not return the edges, but the loops and arrows of *G*.
```
———————————————————— Example ————————————————————
gap> g2:=CompleteGraph(3:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 3, Size := 6, Adjacencies :=
[ [ 1, 2, 3 ], [ 1, 2, 3 ], [ 1, 2, 3 ] ] )
gap> Edges(g2);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 2, 2 ], [ 2, 3 ], [ 3, 3 ] ]
gap> g3:=CompleteGraph(3:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 9, Adjacencies :=
[ [ 1, 2, 3 ], [ 1, 2, 3 ], [ 1, 2, 3 ] ] )
gap> Edges(g3);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ], [ 3, 1 ],
  [ 3, 2 ], [ 3, 3 ] ]
```

B.1.60 EquivalenceRepresentatives

▷ EquivalenceRepresentatives(*L*, *Eqiv*) (operation)

Returns a sublist of *L*, which is a complete list of representatives of *L* under the equivalent relation *Equiv*.

```
───────────────────────── Example ─────────────────────────
gap> L:=[10,2,6,5,9,7,3,1,4,8];
[ 10, 2, 6, 5, 9, 7, 3, 1, 4, 8 ]
gap> EquivalenceRepresentatives(L,function(x,y) return (x mod 4)=(y mod 4); end);
[ 10, 5, 7, 4 ]
gap> L:=Links(SnubDisphenoid);;Length(L);
8
gap> L:=EquivalenceRepresentatives(L,IsIsomorphicGraph);;Length(L);
2
gap> L;
[ Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
    [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ) ]
```

B.1.61 FanGraph

▷ FanGraph(*n*) (function)

Returns the *n*-Fan: The join of a vertex and a (*n+1*)-path.

```
───────────────────────── Example ─────────────────────────
gap> FanGraph(4);
Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
[ [ 2, 3, 4, 5, 6 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4, 6 ],
[ 1, 5 ] ] )
```

B.1.62 FishGraph

▷ FishGraph (global variable)

A square and a triangle glued by a vertex.

```
───────────────────────── Example ─────────────────────────
gap> FishGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 3, 4, 6 ], [ 1, 3 ], [ 1, 2 ], [ 1, 5 ], [ 4, 6 ], [ 1, 5 ] ] )
```

B.1.63 GemGraph

▷ GemGraph (global variable)

The 3-Fan graph.

```
───────────────────────── Example ─────────────────────────
gap> GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ] )
```

B.1.64 Girth

▷ Girth(*G*) (attribute)

Returns the length of the minimum induced cycle in *G*. At this time, this works only when *G* belongs to the graph categories `SimpleGraphs` or `UndirectedGraphs`. If *G* has loops, its girth is 1 by definition.

```
———————————————————————————— Example ————————————————————————————
gap> Girth(Octahedron);
3
gap> Girth(PetersenGraph);
5
gap> Girth(Cube);
4
gap> Girth(PathGraph(5));
infinity
gap> g:=AddEdges(CycleGraph(4),[[3,3]]:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 4, Size := 5, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 3, 4 ], [ 1, 3 ] ] )
gap> Girth(g);
1
```

B.1.65 Graph

▷ Graph(*Rec*) (operation)

Returns a new graph created from the record *Rec*. The record must provide the field `Category` and either the field `Adjacencies` or the field `AdjMatrix`.

```
———————————————————————————— Example ————————————————————————————
gap> Graph(rec(Category:=SimpleGraphs,Adjacencies:=[[2],[1]]));
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> Graph(rec(Category:=SimpleGraphs,AdjMatrix:=[[false, true],[true, false]]));
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies := [ [ 2 ], [ 1 ] ] )
```

Its main purpose is to import graphs from files, which could have been previously exported using `PrintTo`.

```
———————————————————————————— Example ————————————————————————————
gap> g:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> PrintTo("aux.g","h1:=",g,";");
gap> Read("aux.g");
gap> h1;
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
```

B.1.66 GraphAttributeStatistics

▷ GraphAttributeStatistics(*OrderList, ProbList, Attribute*) (function)

Returns statistics for graph attribute `Attribute`. For each of the orders `n` in `OrderList` and for each of the probabilities `p` in `ProbList` this function generates 100 random graphs of order `n` and edge probability `p` and then evaluates the graph attribute `Attribute` on each of them. The function then returns statistical data on these experiments. The form in which the statistical data is reported depend on a number of issues and is best explained by examples.

First let us consider the case where `Attribute` is a Boolean attribute (always returns `true` or `false`) and where `OrderList` and `ProbList` consist of a unique value. In this case, the respective lists may be replaced by the corresponding unique values on invocation:

```
────────── Example ──────────
gap> GraphAttributeStatistics(10,1/2,IsCliqueHelly);
43
```

This tells us that 43 of the 100 examined random graphs resulted to be clique-Helly; The random sample was constructed using graphs of order 10 and edge probability 1/2.

Now we can specify a list of probabilities to be examined:

```
────────── Example ──────────
gap> GraphAttributeStatistics(10,1/10*[1..9],IsCliqueHelly);
[ 100, 100, 95, 77, 36, 22, 41, 72, 97 ]
```

The last example tells us that, for graphs on 10 vertices, the property IsCliqueHelly is least probable to be true for graphs with edge probabilities 5/10 6/10 and 7/10, being 6/10 the probability that reaches the minimum in the random sample. Note that the 36 in the previous example does not match the 43 in the first one, this is to be expected as the statistics are compiled from a random sample of graphs. Also, note that in the previous example, 900 random graphs where generated and examined.

We can also specify a list of orders to consider:

```
────────── Example ──────────
gap> GraphAttributeStatistics([10,12..20],1/10*[1..9],IsCliqueHelly);
[ [ 100, 100, 91, 63, 30, 23, 39, 65, 99 ], [ 100, 98, 81, 35, 4, 2, 20, 63, 98 ]
    , [ 100, 95, 49, 15, 1, 2, 13, 51, 98 ], [ 99, 82, 39, 3, 0, 2, 9, 42, 97 ],
   [ 100, 86, 15, 0, 0, 0, 7, 32, 93 ], [ 100, 69, 5, 0, 0, 0, 3, 24, 90 ] ]
gap> Display(last);
[ [  100,  100,  91,  63,  30,  23,  39,  65,  99 ],
  [  100,   98,  81,  35,   4,   2,  20,  63,  98 ],
  [  100,   95,  49,  15,   1,   2,  13,  51,  98 ],
  [   99,   82,  39,   3,   0,   2,   9,  42,  97 ],
  [  100,   86,  15,   0,   0,   0,   7,  32,  93 ],
  [  100,   69,   5,   0,   0,   0,   3,  24,  90 ] ]
```

Which tell us that the observed bimodal distribution is even more pronounced when the order of the graphs considered grows.

In the case of a non-Boolean attribute `GraphAttributeStatistics()` reports the values that `Attribute` took on the sample as well as the number of times that each of these values where obtained:

```
────────── Example ──────────
gap> GraphAttributeStatistics(10,1/2,Diameter);
[ [ 2, 26 ], [ 3, 60 ], [ 4, 8 ], [ 6, 1 ], [ infinity, 5 ] ]
```

The returned statistics mean that among the 100 generated random graphs on 10 vertices with edge probability 1/2, there were 26 graphs with diameter 2, 60 graphs of diameter 3, 8 of 4, 1 of 6 and 5 graphs which were not connected.

Now it should be evident the format of the returned statistics when we specify a list of probabilities and/or a list of orders to be considered for a non-Boolean Attribute:

```
 ────────────────────────────── Example ──────────────────────────────
 gap> GraphAttributeStatistics(10,1/5*[1..4],Diameter);
 [ [ [ 3, 3 ], [ 4, 5 ], [ 5, 9 ], [ 6, 3 ], [ 7, 2 ], [ infinity, 78 ] ],
   [ [ 2, 8 ], [ 3, 55 ], [ 4, 19 ], [ 5, 3 ], [ infinity, 15 ] ],
   [ [ 2, 73 ], [ 3, 26 ], [ 4, 1 ] ], [ [ 2, 100 ] ] ]
 gap> GraphAttributeStatistics([10,12,14],1/5*[1..4],Diameter);
 [ [ [ [ 4, 8 ], [ 5, 7 ], [ 6, 3 ], [ infinity, 82 ] ],
       [ [ 2, 3 ], [ 3, 64 ], [ 4, 15 ], [ 5, 3 ], [ infinity, 15 ] ],
       [ [ 2, 69 ], [ 3, 30 ], [ infinity, 1 ] ], [ [ 2, 100 ] ] ],
   [ [ [ 3, 1 ], [ 4, 11 ], [ 5, 13 ], [ 6, 7 ], [ 7, 3 ], [ 8, 2 ],
           [ infinity, 63 ] ],
       [ [ 2, 8 ], [ 3, 69 ], [ 4, 18 ], [ 5, 2 ], [ infinity, 3 ] ],
       [ [ 2, 79 ], [ 3, 21 ] ], [ [ 2, 100 ] ] ],
   [ [ [ 3, 1 ], [ 4, 15 ], [ 5, 13 ], [ 6, 5 ], [ 7, 4 ], [ 8, 3 ],
           [ infinity, 59 ] ], [ [ 2, 6 ], [ 3, 82 ], [ 4, 9 ], [ infinity, 3 ] ],
       [ [ 2, 86 ], [ 3, 14 ] ], [ [ 2, 100 ] ] ] ]
```

B.1.67 Graph6ToGraph

▷ Graph6ToGraph(*String*)   (operation)

Returns the graph represented by *String* which is encoded using Brendan McKay's graph6 format. This operation allows us to read data in databases which use this format. Several such databases can be found here: \URL{https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html}.

The graph6 format is described here: \URL{https://cs.anu.edu.au/people/Brendan.McKay/data/formats.txt}.

```
 ────────────────────────────── Example ──────────────────────────────
 gap> Graph6ToGraph("D?{");
 Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
 [ [ 5 ], [ 5 ], [ 5 ], [ 5 ], [ 1, 2, 3, 4 ] ] )
 gap> Graph6ToGraph("FUzvW");
 Graph( Category := SimpleGraphs, Order := 7, Size := 15, Adjacencies :=
 [ [ 3, 4, 5, 6, 7 ], [ 4, 5, 6, 7 ], [ 1, 5, 6, 7 ], [ 1, 2, 6 ],
   [ 1, 2, 3, 7 ], [ 1, 2, 3, 4, 7 ], [ 1, 2, 3, 5, 6 ] ] )
 gap> Graph6ToGraph("HUzv~z}");
 Graph( Category := SimpleGraphs, Order := 9, Size := 29, Adjacencies :=
 [ [ 3, 4, 5, 6, 7, 8, 9 ], [ 4, 5, 6, 7, 8, 9 ], [ 1, 5, 6, 7, 8, 9 ],
   [ 1, 2, 6, 7, 8, 9 ], [ 1, 2, 3, 7, 8, 9 ], [ 1, 2, 3, 4, 7, 8, 9 ],
   [ 1, 2, 3, 4, 5, 6, 9 ], [ 1, 2, 3, 4, 5, 6 ], [ 1, 2, 3, 4, 5, 6, 7 ] ] )
```

See also ImportGraph6(*Filename*).

B.1.68 GraphByAdjacencies

▷ GraphByAdjacencies(*AdjList*)   (function)

Returns a new graph having *AdjList* as its list of adjacencies. The order of the created graph is Length(A), and the set of neighbors of vertex *x* is $A[x]$.

```
 ─────────────── Example ───────────────
 gap> GraphByAdjacencies([[2],[1,3],[2]]);
 Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
 [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

Note, however, that the graph is forced to comply with the `TargetGraphCategory`.

```
 ─────────────── Example ───────────────
 gap> GraphByAdjacencies([[1,2,3],[],[]]);
 Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
 [ [ 2, 3 ], [ 1 ], [ 1 ] ] )
```

B.1.69 GraphByAdjMatrix

▷ GraphByAdjMatrix(*Mat*) (function)

Returns a new graph created from an adjacency matrix *Mat*. The matrix *Mat* must be a square boolean matrix.

```
 ─────────────── Example ───────────────
 gap> m:=[ [ false, true, false ], [ true, false, true ], [ false, true, false ] ];;
 gap> g:=GraphByAdjMatrix(m);
 Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
 [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
 gap> AdjMatrix(g);
 [ [ false, true, false ], [ true, false, true ], [ false, true, false ] ]
```

Note, however, that the graph is forced to comply with the `TargetGraphCategory`.

```
 ─────────────── Example ───────────────
 gap> m:=[ [ true, true], [ false, false ] ];;
 gap> g:=GraphByAdjMatrix(m);
 Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies := [ [ 2 ], [ 1 ] ] )
 gap> AdjMatrix(g);
 [ [ false, true ], [ true, false ] ]
```

B.1.70 GraphByCompleteCover

▷ GraphByCompleteCover(*Cover*) (function)

Returns the minimal graph where the elements of *Cover* are (the vertex sets of) complete subgraphs.

```
 ─────────────── Example ───────────────
 gap> GraphByCompleteCover([[1,2,3,4],[4,6,7]]);
 Graph( Category := SimpleGraphs, Order := 7, Size := 9, Adjacencies :=
 [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3, 6, 7 ], [ ], [ 4, 7 ],
   [ 4, 6 ] ] )
```

B.1.71 GraphByEdges

▷ GraphByEdges(*L*) (function)

Returns the minimal graph such that the pairs in *L* are edges.

```
                          Example
  gap> GraphByEdges([[1,2],[1,3],[1,4],[4,5]]);
  Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
  [ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1, 5 ], [ 4 ] ] )
```

The vertices of the constructed graph range from 1 to the maximum of the numbers appearing in `L`.

```
                          Example
  gap> GraphByEdges([[4,3],[4,5]]);
  Graph( Category := SimpleGraphs, Order := 5, Size := 2, Adjacencies :=
  [ [  ], [  ], [ 4 ], [ 3, 5 ], [ 4 ] ] )
```

Note that `GraphByWalks` has an even greater functionality.

B.1.72 GraphByRelation

▷ GraphByRelation(*V, Rel*)   (function)
▷ GraphByRelation(*n, Rel*)   (function)

Returns a new graph created from a set of vertices `V` and a binary relation `Rel`, where $x \sim y$ iff `Rel(x,y)=true`. In the second form, `n` is an integer and `V` is assumed to be $\{1, 2, \ldots, n\}$.

```
                          Example
  gap> Rel:=function(x,y) return Intersection(x,y)<>[]; end;;
  gap> GraphByRelation([[1,2,3],[3,4,5],[5,6,7]],Rel);
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
  gap> GraphByRelation(8,function(x,y) return AbsInt(x-y)<=2; end);
  Graph( Category := SimpleGraphs, Order := 8, Size := 13, Adjacencies :=
  [ [ 2, 3 ], [ 1, 3, 4 ], [ 1, 2, 4, 5 ], [ 2, 3, 5, 6 ], [ 3, 4, 6, 7 ],
    [ 4, 5, 7, 8 ], [ 5, 6, 8 ], [ 6, 7 ] ] )
```

B.1.73 GraphByWalks

▷ GraphByWalks(*Walk1, Walk2, ...*)   (function)

Returns the minimal graph such that `Walk1`, `Walk2`, etc are Walks.

```
                          Example
  gap> GraphByWalks([1,2,3,4,1],[1,5,6]);
  Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
  [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ], [ 1, 6 ], [ 5 ] ] )
```

Walks can be `nested`, which greatly improves the versatility of this function.

```
                          Example
  gap> GraphByWalks([1,[2,3,4],5],[5,6]);
  Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
  [ [ 2, 3, 4 ], [ 1, 3, 5 ], [ 1, 2, 4, 5 ], [ 1, 3, 5 ], [ 2, 3, 4, 6 ], [ 5 ] ] )
```

The vertices in the constructed graph range from 1 to the maximum of the numbers appearing in `Walk1`, `Walk2`, ... etc.

```
                          Example
  gap> GraphByWalks([4,2],[3,6]);
  Graph( Category := SimpleGraphs, Order := 6, Size := 2, Adjacencies :=
  [ [  ], [ 4 ], [ 6 ], [ 2 ], [  ], [ 3 ] ] )
```
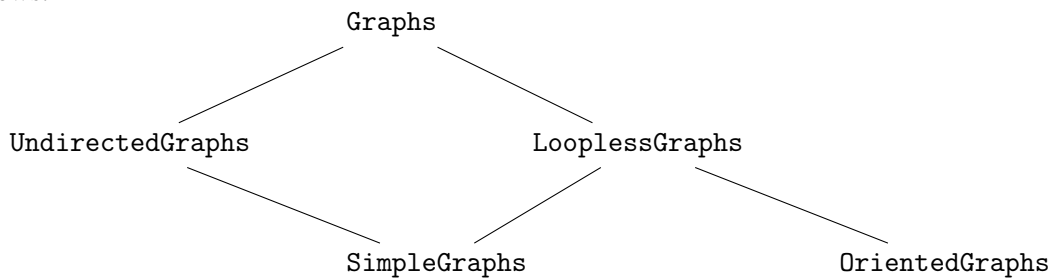
B.1.74 GraphCategory

▷ GraphCategory(*[G, ...]*)   (function)

For internal use. Returns the minimal common category to a list of graphs. If the list of graphs is empty, the default category is returned. The partial order (by inclusion) among graph categories is as follows:

```
                            Graphs

        UndirectedGraphs                 LooplessGraphs

                    SimpleGraphs                    OrientedGraphs
```

```
———————————————————————— Example ————————————————————————
 gap> g1:=CompleteGraph(2:GraphCategory:=SimpleGraphs);
 Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
 [ [ 2 ], [ 1 ] ] )
 gap> g2:=CompleteGraph(2:GraphCategory:=OrientedGraphs);
 Graph( Category := OrientedGraphs, Order := 2, Size := 1, Adjacencies :=
 [ [ 2 ], [ ] ] )
 gap> g3:=CompleteGraph(2:GraphCategory:=UndirectedGraphs);
 Graph( Category := UndirectedGraphs, Order := 2, Size := 3, Adjacencies :=
 [ [ 1, 2 ], [ 1, 2 ] ] )
 gap> GraphCategory([g1,g2,g3]);
 <Operation "Graphs">
 gap> GraphCategory([g1,g2]);
 <Operation "LooplessGraphs">
 gap> GraphCategory([g1,g3]);
 <Operation "UndirectedGraphs">
```

B.1.75 Graphs

▷ Graphs(*G*)   (function)

Graphs is the most general graph category in YAGS. This category contains all graphs that can be represented in YAGS. A graph in this category may contain loops, arrows and edges (which in YAGS are exactly the same as two opposite arrows between some pair of vertices). This graph category has no parent category.

```
———————————————————————— Example ————————————————————————
 gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
 Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
 [ [ 1, 2 ], [ 1 ], [ 2 ] ] )
 gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=SimpleGraphs);
 Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
 [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

B.1.76 GraphsOfGivenOrder

▷ GraphsOfGivenOrder(*n*) (operation)

Returns the list of all graphs of order *n* (upto isomorphism). This operation uses Brendan McKay's data published here: \URL{https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html}.

These data are included with the **YAGS** distribution in its data directory. Hence this operation simply reads the corresponding file in that directory using ImportGraph6(*Filename*). Therefore, the integer *n* must be in the range from 1 upto 9. Data for graphs on 10 vertices is also available, but not included with **YAGS**, it may not be practical to use that data, but if you would like to try, all you have to do is to copy (and to uncompress) the corresponding file into the directory *YAGS-Directory*/data.

```
──────────────────── Example ────────────────────
gap> GraphsOfGivenOrder(2);
[ Graph( Category := SimpleGraphs, Order := 2, Size := 0, Adjacencies :=
    [ [ ], [ ] ] ), Graph( Category := SimpleGraphs, Order := 2, Size :=
    1, Adjacencies := [ [ 2 ], [ 1 ] ] ) ]
gap> GraphsOfGivenOrder(3);
[ Graph( Category := SimpleGraphs, Order := 3, Size := 0, Adjacencies :=
    [ [ ], [ ], [ ] ] ), Graph( Category := SimpleGraphs, Order :=
    3, Size := 1, Adjacencies := [ [ 3 ], [ ], [ 1 ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
    [ [ 3 ], [ 3 ], [ 1, 2 ] ] ), Graph( Category := SimpleGraphs, Order :=
    3, Size := 3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] ) ]
gap> Length(GraphsOfGivenOrder(9));
274668
gap> GraphsOfGivenOrder(10);
#W Unreadable File: /opt/gap4r7/pkg/yags/data/graph10.g6
fail
```

B.1.77 GraphSum

▷ GraphSum(*G, L*) (operation)

Returns the lexicographic sum of a list of graphs *L* over a graph *G*.

The lexicographic sum is computed as follows:

Given *G*, with $Order(G) = n$ and a list of *n* graphs $L = [G_1, \ldots, G_n]$, We take the disjoint union of $G_1, G_2, \ldots, G_n$ and then we add all the edges between G_i and G_j whenever $[i, j]$ is and edge of *G*.

If *L* contains holes, the trivial graph is used in place.

```
──────────────────── Example ────────────────────
gap> t:=TrivialGraph;; g:=CycleGraph(4);;
gap> GraphSum(PathGraph(3),[t,g,t]);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ],
  [ 1, 2, 4, 6 ], [ 2, 3, 4, 5 ] ] )
gap> GraphSum(PathGraph(3),[,g,]);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ],
  [ 1, 2, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

B.1.78 GraphToRaw

▷ GraphToRaw(*FileName, G*) (operation)

Converts a YAGS graph `G` into a raw format (number of vertices, coordinates and adjacency matrix) and writes the converted data to the file `FileName`. For use by the external program `draw` (see `Draw(G)`).

```
―――――――――――――― Example ――――――――――――――
  gap> g:=CycleGraph(4);;
  gap> GraphToRaw("mygraph.raw",g);
```

B.1.79 GraphUpdateFromRaw

▷ GraphUpdateFromRaw(*FileName, G*) (operation)

Updates the coordinates of `G` from a file `FileName` in raw format. Intended for internal use only.

B.1.80 GroupGraph

▷ GroupGraph(*G, Grp, Act*) (operation)
▷ GroupGraph(*G, Grp*) (operation)

Given a graph `G`, a group `Grp` and an action `Act` of `Grp` in some set S which contains Vertices(`G`), GroupGraph returns a new graph with vertex set $\{act(v,g) : g \in Grp, v \in Vertices(G)\}$ and edge set $\{\{act(v,g), act(u,g)\} : g \; inGrp\{u,v\} \in Edges(G)\}$.

If `Act` is omited, the standard GAP action `OnPoints` is used.

```
―――――――――――――― Example ――――――――――――――
  gap> GroupGraph(GraphByWalks([1,2]),Group([(1,2,3,4,5),(2,5)(3,4)]));
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
  [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
```

B.1.81 HararyToMcKay

▷ HararyToMcKay(*Spec*) (operation)
▷ McKayToHarary(*index*) (operation)

Returns the McKay's `index` of a Harary's graph specification `Spec` and viceversa. Frank Harary published in his book [7], a list af all 208 simple graphs of order upto 6 (upto isomorphism). Each of them had a label (which we call `Harary's graph specification`) of the form [`n`, `m`, `s`] where `n` is the number of vertices, `m` is the number of edges, and `s` is a consecutive integer which uniquely identifies the graph from the others with the same `n` and `m`. On the other hand, Brendan McKay published data sets containing a list of all graphs of order upto 10 (also upto isomorphism), here:

\URL{https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html}

Each graph in these data sets appears in some specific position (which we call *McKay's index*).

We found it convenient to have an automated way to convert from Harary's graph specifications to McKay's indexes and viceversa.

```
                              ___ Example ___
 gap> HararyToMcKay([1,0,1]);
 1
 gap> HararyToMcKay([1,0,2]);
 fail
 gap> HararyToMcKay([5,5,2]);
 31
 gap> HararyToMcKay([5,5,3]);
 34
 gap> HararyToMcKay([5,5,5]);
 30
 gap> HararyToMcKay([5,5,6]);
 45
 gap> HararyToMcKay([5,5,7]);
 fail
 gap> HararyToMcKay([6,15,1]);
 208
 gap> HararyToMcKay([6,15,2]);
 fail
 gap> List([1..208],McKayToHarary);
 [ [ 1, 0, 1 ], [ 2, 0, 1 ], [ 2, 1, 1 ], [ 3, 0, 1 ], [ 3, 1, 1 ],
   [ 3, 2, 1 ], [ 3, 3, 1 ], [ 4, 0, 1 ], [ 4, 1, 1 ], [ 4, 2, 1 ],
   [ 4, 3, 3 ], [ 4, 2, 2 ], [ 4, 3, 1 ], [ 4, 3, 2 ], [ 4, 4, 1 ],

                 --- many more lines here ---

   [ 6, 10, 10 ], [ 6, 10, 7 ], [ 6, 11, 3 ], [ 6, 12, 1 ], [ 6, 13, 1 ],
   [ 6, 11, 7 ], [ 6, 11, 9 ], [ 6, 11, 8 ], [ 6, 12, 4 ], [ 6, 12, 5 ],
   [ 6, 13, 2 ], [ 6, 14, 1 ], [ 6, 15, 1 ] ]
```

B.1.82 HouseGraph

▷ HouseGraph (global variable)

A 4-Cycle and a triangle glued by an edge.

```
                              ___ Example ___
 gap> HouseGraph;
 Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
 [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ] )
```

B.1.83 Icosahedron

▷ Icosahedron (global variable)

The 1-skeleton of Plato's icosahedron.

```
                              ___ Example ___
 gap> Icosahedron;
 Graph( Category := SimpleGraphs, Order := 12, Size := 30, Adjacencies :=
 [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6, 9, 10 ], [ 1, 2, 4, 10, 11 ],
   [ 1, 3, 5, 7, 11 ], [ 1, 4, 6, 7, 8 ], [ 1, 2, 5, 8, 9 ],
```

```
    [ 4, 5, 8, 11, 12 ], [ 5, 6, 7, 9, 12 ], [ 2, 6, 8, 10, 12 ],
    [ 2, 3, 9, 11, 12 ], [ 3, 4, 7, 10, 12 ], [ 7, 8, 9, 10, 11 ] ] )
```

B.1.84   ImportGraph6

▷ ImportGraph6(*Filename*)   (operation)

Returns the list of graphs represented in `Filename` which are encoded using Brendan McKay's graph6 format. This operation allows us to read data in databases which use this format. Several such databases can be found here: \URL{https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html}.

The graph6 format is described here: \URL{https://cs.anu.edu.au/people/Brendan.McKay/data/formats.txt}.

The following example assumes that you have a file named graph3.g6 in your working directory which encodes graphs in graph6 format; the contents of this file is assumed to be as indicated after the first command in the example.

——————————————— Example ———————————————
```
gap> Exec("cat graph3.g6");
B?
BO
BW
Bw
gap> ImportGraph6("graph3.g6");
[ Graph( Category := SimpleGraphs, Order := 3, Size := 0, Adjacencies :=
    [ [ ], [ ], [ ] ] ), Graph( Category := SimpleGraphs, Order :=
    3, Size := 1, Adjacencies := [ [ 3 ], [ ], [ 1 ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
    [ [ 3 ], [ 3 ], [ 1, 2 ] ] ), Graph( Category := SimpleGraphs, Order :=
    3, Size := 3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] ) ]
```

B.1.85   in

▷ in(*G, Catgy*)   (operation)

Returns `true` if graph `G` belongs to category `Catgy` and `false` otherwise.
——————————————— Example ———————————————
```
  ##FIXME **** poner ejemplo.
```

B.1.86   InducedSubgraph

▷ InducedSubgraph(*G, V*)   (operation)

Returns the subgraph of graph `G` induced by the vertex set `V`.
——————————————— Example ———————————————
```
gap> g:=CycleGraph(6);
Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
[ [ 2, 6 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4, 6 ], [ 1, 5 ] ] )
gap> InducedSubgraph(g,[3,4,6]);
Graph( Category := SimpleGraphs, Order := 3, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ], [ ] ] )
```

The order of the elements in `V` does matter.

```
——————— Example ———————
gap> InducedSubgraph(g,[6,3,4]);
Graph( Category := SimpleGraphs, Order := 3, Size := 1, Adjacencies :=
[ [  ], [ 3 ], [ 2 ] ] )
```

B.1.87   InNeigh

▷ InNeigh(*G, x*)   (operation)

Returns the list of in-neighbors of *x* in *G*.

```
——————— Example ———————
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [  ] ] )
gap> InNeigh(tt,3);
[ 1, 2 ]
gap> OutNeigh(tt,3);
[ 4, 5 ]
```

B.1.88   InteriorVertices

▷ InteriorVertices(*G*)   (attribute)

When `G` is a compact surface, it returns the list of vertices in the interior (of the triangulation) of the surface. That is, the list of vertices of `G` that have links isomorphic to a cycle. It returns `fail` if `G` is not a compact surface.

```
——————— Example ———————
gap> InteriorVertices(WheelGraph(4,2));
[ 1, 2, 3, 4, 5 ]
gap> InteriorVertices(Octahedron);
[ 1, 2, 3, 4, 5, 6 ]
```

B.1.89   IntersectionGraph

▷ IntersectionGraph(*L*)   (function)

Returns the intersection graph of the family of sets `L`. This graph has a vertex for every set in `L`, and two such vertices are adjacent iff the corresponding sets have non-empty intersection.

```
——————— Example ———————
gap> IntersectionGraph([[1,2,3],[3,4,5],[5,6,7]]);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

B.1.90   IsBoolean

▷ IsBoolean(*Obj*)   (function)

Returns `true` if object `Obj` is `true` or `false` and `false` otherwise.

```
————————————————— Example —————————————————
  gap> IsBoolean( true ); IsBoolean( fail ); IsBoolean ( false );
  true
  false
  true
```

B.1.91 IsCliqueGated

▷ IsCliqueGated(*G*)   (property)

Returns true if *G* is a clique gated graph [6].

B.1.92 IsCliqueHelly

▷ IsCliqueHelly(*G*)   (property)

Returns true if the set of (maximal) cliques *G* satisfy the *Helly* property.

The Helly property is defined as follows:

A non-empty family *F* of non-empty sets satisfies the Helly property if every pairwise intersecting subfamily of *F* has a non-empty total intersection.

Here we use the Dragan-Szwarcfiter characterization [2][15] to compute the Helly property.

```
————————————————— Example —————————————————
  gap> g:=SunGraph(3);
  Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
  [ [ 2, 6 ], [ 1, 3, 4, 6 ], [ 2, 4 ], [ 2, 3, 5, 6 ], [ 4, 6 ],
    [ 1, 2, 4, 5 ] ] )
  gap> IsCliqueHelly(g);
  false
```

B.1.93 IsCompactSurface

▷ IsCompactSurface(*G*)   (property)

Returns true if every link of *G* is either an *n*-cycle, for $n \geq 4$ or an *m*-path, for $m \geq 2$. (not necessarily the same *n*/*m* for all vertices); it returns false otherwise.

This notion correspond to Whitney triangulations of compact surfaces [11] in which the (maximal) cliques of the graph are exactly the triangles of the triangulation.

```
————————————————— Example —————————————————
  gap> IsCompactSurface(Icosahedron);
  true
  gap> IsCompactSurface(RemoveVertices(Icosahedron,[1]));
  true
  gap> IsCompactSurface(WheelGraph(4,2));
  true
  gap> IsCompactSurface(Tetrahedron);
  false
  gap> IsCompactSurface(CompleteGraph(2));
  false
  gap> IsCompactSurface(CompleteGraph(3));
```

```
    true
gap> IsCompactSurface(CompleteGraph(4));
    false
```

Topologically, the difference between a surface and a compact surface is that the points of a surface always have a open neighborhood homeomorphic to an open disk, whereas a compact surface may also contain points with open neighborhoods homeomorphic to a closed half-plane.

B.1.94 IsComplete

▷ IsComplete(`G, L`)   (operation)

Returns `true` if `L` induces a complete subgraph of `G`.

```
─────────────── Example ───────────────
gap> IsComplete(DiamondGraph,[1,2,3]);
true
gap> IsComplete(DiamondGraph,[1,2,4]);
false
```

B.1.95 IsCompleteGraph

▷ IsCompleteGraph(`G`)   (property)

Returns `true` if graph `G` is a complete graph, `false` otherwise. In a complete graph every pair of vertices is an edge.

B.1.96 IsDiamondFree

▷ IsDiamondFree(`G`)   (property)

Returns `true` if `G` is free from induced diamonds, `false` otherwise.

```
─────────────── Example ───────────────
gap> IsDiamondFree(Cube);
true
gap> IsDiamondFree(Octahedron);
false
```

B.1.97 IsEdge

▷ IsEdge(`G, x, y`)   (operation)
▷ IsEdge(`G[, x, y>]`)   (operation)

Returns `true` if [`x,y`] is an edge of `G`.

```
─────────────── Example ───────────────
gap> IsEdge(PathGraph(3),1,2);
true
gap> IsEdge(PathGraph(3),[1,2]);
true
gap> IsEdge(PathGraph(3),1,3);
```

```
false
gap> IsEdge(PathGraph(3),[1,3]);
false
```

The first form, IsEdge(*G*, *x*, *y*), is a bit faster and hence more suitable for use in algoritms which make extensive use of this operation. On the other hand, the first form does no error checking at all, and hence, it may produce an error where the second form returns false (for instance when *x* is not a vertex of *G*). The second form is therefore a bit slower, but more robust.

—————— Example ——————
```
gap> IsEdge(PathGraph(3),[7,3]);
false
gap> IsEdge(PathGraph(3),7,3);
Error, List Element: <list>[7] must have an assigned value in
  return AdjMatrix( G )[x][y]; called from
  <function "unknown">( <arguments> )
 called from read-eval loop at line 4 of *stdin*
you can <return;> after assigning a value
brk>
```

B.1.98   IsIsomorphicGraph

▷ IsIsomorphicGraph(*G*, *H*)   (operation)

Returns true when *G* is isomorphic to *H* and false otherwise.

—————— Example ——————
```
gap> g:=PowerGraph(CycleGraph(6),2);;h:=Octahedron;;
gap> IsIsomorphicGraph(g,h);
true
```

B.1.99   IsLocallyConstant

▷ IsLocallyConstant(*G*)   (property)

Returns true if all the links of *G* are isomorphic to each other; false otherwise.

—————— Example ——————
```
gap> IsLocallyConstant(PathGraph(2));
true
gap> IsLocallyConstant(PathGraph(3));
false
gap> IsLocallyConstant(CompleteGraph(3));
true
gap> IsLocallyConstant(CycleGraph(4));
true
gap> IsLocallyConstant(Icosahedron);
true
gap> IsLocallyConstant(TorusGraph(5,4));
true
gap> IsLocallyConstant(WheelGraph(4,2));
false
gap> IsLocallyConstant(SnubDisphenoid);
false
```

B.1.100 IsLocallyH

▷ IsLocallyH(*G, H*) (operation)

Returns `true` if all the links of *G* are isomorphic to *H*; `false` otherwise.

```
——————————— Example ———————————
gap> IsLocallyH(Octahedron,CycleGraph(4));
true
gap> IsLocallyH(Octahedron,CycleGraph(5));
false
gap> IsLocallyH(Icosahedron,CycleGraph(5));
true
gap> IsLocallyH(TorusGraph(4,4),CycleGraph(6));
true
```

B.1.101 IsLoopless

▷ IsLoopless(*G*) (property)

Returns `true` if graph *G* have no loops, `false` otherwise. Loops are edges from a vertex to itself.

B.1.102 IsoMorphism

▷ IsoMorphism(*G, H*) (operation)

Returns one isomorphism from *G* to *H* or `fail` if none exists. If *G* has *n* vertices, an isomorphisms $f : G \to H$ is represented as the list `F=[f(1), f(2), ..., f(n)]`.

```
——————————— Example ———————————
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> f:=IsoMorphism(g,h);
[ 1, 3, 2, 4 ]
```

See `NextIsoMorphism( G, H, F )`.

B.1.103 IsoMorphisms

▷ IsoMorphisms(*G, H*) (operation)

Returns the list of all isomorphism from *G* to *H*. If *G* has *n* vertices, an isomorphisms $f : G \to H$ is represented as the list `F=[f(1), f(2), ..., f(n)]`.

```
——————————— Example ———————————
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> IsoMorphisms(g,h);
[ [ 1, 3, 2, 4 ], [ 1, 4, 2, 3 ], [ 2, 3, 1, 4 ], [ 2, 4, 1, 3 ],
  [ 3, 1, 4, 2 ], [ 3, 2, 4, 1 ], [ 4, 1, 3, 2 ], [ 4, 2, 3, 1 ] ]
```

B.1.104 IsOriented

▷ IsOriented(*G*) (property)

Returns `true` if graph *G* is an oriented graph, `false` otherwise. Regardless of the categories that *G* belongs to, *G* is oriented if whenever [x,y] is an edge of *G*, [y,x] is not.

B.1.105 IsSimple

▷ IsSimple(*G*) (property)

Returns `true` if graph *G* is a simple graph, `false` otherwise. Regardless of the categories that *G* belongs to, *G* is simple if and only if *G* is undirected and loopless.

Returns `true` if the graph *G* is simple regardless of its category.

B.1.106 IsSurface

▷ IsSurface(*G*) (property)

Returns `true` if every link of *G* is an *n*-cycle, for $n \geq 4$ (not necessarily the same *n* for all vertices); `false` otherwise.

This notion correspond to Whitney triangulations of (closed) surfaces [11] in which the (maximal) cliques of the graph are exactly the triangles of the triangulation.

```
                          ─── Example ───
  gap> IsSurface(SnubDisphenoid);
  true
  gap> IsSurface(Icosahedron);
  true
  gap> IsSurface(RemoveVertices(Icosahedron,[1]));
  false
  gap> IsSurface(TorusGraph(4,5));
  true
  gap> IsSurface(WheelGraph(4,2));
  false
  gap> IsSurface(Tetrahedron);
  false
```

Topologically, the difference between a (closed) surface and a compact surface is that the points of a surface always have a open neighborhood homeomorphic to an open disk, whereas a compact surface may also contain points with open neighborhoods homeomorphic to a closed half-plane.

B.1.107 IsTournament

▷ IsTournament(*G*) (property)

Returns `true` if *G* is a tournament.

```
                          ─── Example ───
  gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
  Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
  [ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [ ] ] )
```

```
gap> IsTournament(tt);
true
```

B.1.108 IsTransitiveTournament

▷ IsTransitiveTournament(*G*)   (property)

Returns `true` if *G* is a transitive tournament.
```
———————————————————— Example ————————————————————
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [ ] ] )
gap> IsTransitiveTournament(tt);
true
```

B.1.109 IsUndirected

▷ IsUndirected(*G*)   (property)

Returns `true` if graph *G* is an undirected graph, `false` otherwise. Regardless of the categories that *G* belongs to, *G* is undirected if whenever [x,y] is an edge of *G*, [y,x] is also an egde of *G*.

B.1.110 JohnsonGraph

▷ JohnsonGraph(*n*, *r*)   (function)

Returns the Johnson graph $J(n,r)$. The Johnson Graph is the graph whose vertices are r-subset of the set $\{1,2,\ldots,n\}$, two of them being adjacent iff they intersect in exactly r-1 elements.
```
———————————————————— Example ————————————————————
gap> g:=JohnsonGraph(4,2);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
  [ 1, 3, 4, 6 ], [ 2, 3, 4, 5 ] ] )
gap> VertexNames(g);
[ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 2, 4 ], [ 3, 4 ] ]
```

B.1.111 Join

▷ Join(*G*, *H*)   (operation)

Returns the join graph *G* + *H* of *G* and *H* (also known as the Zykov sum); it is the graph obtained from the disjoint union of *G* and *H* by adding every possible edge from every vertex in *G* to every vertex in *H*.
```
———————————————————— Example ————————————————————
gap> g:=DiscreteGraph(2);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 2, Size := 0, Adjacencies :=
[ [ ], [ ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
```

```
gap> Join(g,h);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ],
  [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ] ] )
```

B.1.112   KiteGraph

▷ KiteGraph   (global variable)

A diamond with a pendant vertex and maximum degree 3.
```
———————————————————————— Example ————————————————————————
gap> KiteGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 4 ], [ 2, 4, 5 ], [ 2, 3, 5 ], [ 3, 4 ] ] )
```

B.1.113   LineGraph

▷ LineGraph(*G*)   (operation)

Returns the line graph $L(G)$ of graph `G`. The line graph is the intersection graph of the edges of
`G`, `i.e.` the vertices of $L(G)$ are the edges of `G` two of them being adjacent iff they are incident.
```
———————————————————————— Example ————————————————————————
gap> g:=Tetrahedron;
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> LineGraph(g);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
  [ 1, 3, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

B.1.114   Link

▷ Link(*G*, *x*)   (operation)

Returns the subgraph of `G` induced by the neighbors of `x`.
```
———————————————————————— Example ————————————————————————
gap> Link(SnubDisphenoid,1);
Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
[ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] )
gap> Link(SnubDisphenoid,3);
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] )
```

B.1.115   Links

▷ Links(*G*)   (attribute)

Returns the list of subgraphs of `G` induced by the neighbors of each vertex of `G`.

```
────────────────── Example ──────────────────
gap> Links(SnubDisphenoid);
[ Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
    [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] ),
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
    [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
    [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] ),
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
    [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 3, 4 ], [ 3, 4 ], [ 1, 2 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
    [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ) ]
```

B.1.116 LooplessGraphs

▷ LooplessGraphs(*G*)   (function)

LooplessGraphs is a graph category in YAGS. A graph in this category may contain arrows and edges but no loops. The parent of this category is Graphs.

```
────────────────── Example ──────────────────
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=LooplessGraphs);
Graph( Category := LooplessGraphs, Order := 3, Size := 3, Adjacencies :=
[ [ 2 ], [ 1 ], [ 2 ] ] )
```

B.1.117 MaxDegree

▷ MaxDegree(*G*)   (operation)

Returns the maximum degree in graph *G*.

```
────────────────── Example ──────────────────
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ] )
gap> MaxDegree(g);
4
```

B.1.118 MinDegree

▷ MinDegree(*G*)   (operation)

Returns the minimum degree in graph *G*.

```
                            —— Example ——
  gap> g:=GemGraph;
  Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
  [ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ] )
  gap> MinDegree(g);
  2
```

B.1.119 NextIsoMorphism

▷ NextIsoMorphism(`G, H, F`)   (operation)

Returns the next isomorphism (after `F`) from `G` to `H` in the lexicographic order; returns `fail` if there are no more isomorphisms. If `G` has `n` vertices, an isomorphisms $f : G \to H$ is represented as the list `F=[f(1), f(2), ..., f(n)]`.

```
                            —— Example ——
  gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
  gap> f:=IsoMorphism(g,h);
  [ 1, 3, 2, 4 ]
  gap> NextIsoMorphism(g,h,f);
  [ 1, 4, 2, 3 ]
  gap> NextIsoMorphism(g,h,f);
  [ 2, 3, 1, 4 ]
  gap> NextIsoMorphism(g,h,f);
  [ 2, 4, 1, 3 ]
```

B.1.120 NextPropertyMorphism

▷ NextPropertyMorphism(`G, H, F, PropList`)   (operation)

Returns the next morphism (in lexicographic order) from `G` to `H` satisfying the list of properties `PropList` starting with (possibly incomplete) morphism `F`. The morphism found will me returned *and* stored in `F` in order to use it as the next starting point, in case `NextPropertyMorphism` is called again. The operation returns `fail` if there are no more morphisms of the specified type.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: `CHK_WEAK`, `CHK_MORPH`, `CHK_METRIC`, `CHK_CMPLT`, `CHK_MONO` and `CHK_EPI`.

If `G` has `n` vertices and $f : G \to H$ is a morphism, it is represented as `F=[f(1), f(2), ..., f(n)]`.

```
                            —— Example ——
  gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
  gap> f:=[];; PropList:=[CHK_MORPH,CHK_MONO];;
  gap> NextPropertyMorphism(g,h,f,PropList);
  [ 1, 3, 2, 4 ]
  gap> NextPropertyMorphism(g,h,f,PropList);
  [ 1, 4, 2, 3 ]
  gap> NextPropertyMorphism(g,h,f,PropList);
  [ 2, 3, 1, 4 ]
  gap> NextPropertyMorphism(g,h,f,PropList);
  [ 2, 4, 1, 3 ]
  gap> NextPropertyMorphism(g,h,f,PropList);
```

```
[ 3, 1, 4, 2 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 3, 2, 4, 1 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 4, 1, 3, 2 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 4, 2, 3, 1 ]
gap> NextPropertyMorphism(g,h,f,PropList);
fail
```

B.1.121 NumberOfCliques

▷ NumberOfCliques(*G*) (attribute)
▷ NumberOfCliques(*G, maxNumCli*) (operation)

Returns the number of (maximal) cliques of `G`. In the second form, It stops computing cliques after `maxNumCli` of them have been counted and returns `maxNumCli` in case `G` has `maxNumCli` or more cliques.

———————————————— Example ————————————————
```
gap> NumberOfCliques(Icosahedron);
20
gap> NumberOfCliques(Icosahedron,15);
15
gap> NumberOfCliques(Icosahedron,50);
20
```

This implementation discards the cliques once counted hence, given enough time, it can compute the number of cliques of `G` even if the set of cliques does not fit in memory.

———————————————— Example ————————————————
```
gap> NumberOfCliques(OctahedralGraph(30));
1073741824
```

B.1.122 NumberOfConnectedComponents

▷ NumberOfConnectedComponents(*G*) (attribute)

Returns the number of connected components of `G`.

B.1.123 OctahedralGraph

▷ OctahedralGraph(*n*) (function)

Return the `n`-dimensional octahedron. This is the complement of `n` copies of K_2 (an edge). It is also the `(2n-2)`-regular graph on $2n$ vertices.

———————————————— Example ————————————————
```
gap> OctahedralGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

B.1.124 Octahedron

▷ Octahedron (global variable)

The 1-skeleton of Plato's octahedron.

———————————————— Example ————————————————
```
gap> Octahedron;
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ], [ 1, 2, 5, 6 ],
  [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

B.1.125 Order

▷ Order(*G*) (attribute)

Returns the number of vertices, of graph *G*.

———————————————— Example ————————————————
```
gap> Order(Icosahedron);
12
```

B.1.126 Orientations

▷ Orientations(*G*) (operation)

Returns the list of all the oriented graphs that are obtained from *G* by replacing (in every possible way) each edge [x,y] of *G* by one arrow: either [x,y] or [y,x]. In each of these orientations Loops are removed and existing arrows of *G* are left untouched.

Note that this operation will use time and memory which is exponential on the number of edges of *G*.

———————————————— Example ————————————————
```
gap> g:=GraphByWalks([1,1,2,3,1,3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 6, Adjacencies :=
[ [ 1, 2, 3 ], [ 3 ], [ 1, 2 ] ] )
gap> Orientations(g);
[ Graph( rec( Category := OrientedGraphs, Order := 3, Size :=
    3, Adjacencies := [ [ 2 ], [ ], [ 1, 2 ] ] ) ),
  Graph( rec( Category := OrientedGraphs, Order := 3, Size :=
    3, Adjacencies := [ [ 2 ], [ 3 ], [ 1 ] ] ) ),
  Graph( rec( Category := OrientedGraphs, Order := 3, Size :=
    3, Adjacencies := [ [ 2, 3 ], [ ], [ 2 ] ] ) ),
  Graph( rec( Category := OrientedGraphs, Order := 3, Size :=
    3, Adjacencies := [ [ 2, 3 ], [ 3 ], [ ] ] ) ) ]
gap> Length(Orientations(Octahedron));
4096
```

Note that Orientations(*G*) returns a list of graphs, each of them in the category OrientedGraphs regardless of the TargetGraphCategory.

B.1.127 OrientedGraphs

▷ OrientedGraphs(*G*)   (function)

OrientedGraphs is a graph category in YAGS. A graph in this category may contain arrows, but no loops or edges. The parent of this category is LooplessGraphs.

```
———————————————————————— Example ————————————————————————
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 3, Size := 2, Adjacencies :=
[ [ 2 ], [  ], [ 2 ] ] )
```

B.1.128 OutNeigh

▷ OutNeigh(*G, x*)   (operation)

Returns the list of out-neighbors of *x* in *G*.

```
———————————————————————— Example ————————————————————————
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size := 10, Adjacencies :=
[ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ], [  ] ] )
gap> InNeigh(tt,3);
[ 1, 2 ]
gap> OutNeigh(tt,3);
[ 4, 5 ]
```

B.1.129 PaleyTournament

▷ PaleyTournament(*prime*)   (operation)

Returns the Paley tournament associated with prime number *prime*. *prime* must be congruent to 3 mod 4. The Paley tournament is the oriented circulant whose *jumps* are all the squares of the ring $\mathbb{Z}_p$.

```
———————————————————————— Example ————————————————————————
gap> Filtered([1..30],x -> 0=((x-3) mod 4) and IsPrime(x));
[ 3, 7, 11, 19, 23 ]
gap> PaleyTournament(3);PaleyTournament(7);PaleyTournament(11);
Graph( Category := OrientedGraphs, Order := 3, Size := 3, Adjacencies :=
[ [ 2 ], [ 3 ], [ 1 ] ] )
Graph( Category := OrientedGraphs, Order := 7, Size := 21, Adjacencies :=
[ [ 2, 3, 5 ], [ 3, 4, 6 ], [ 4, 5, 7 ], [ 1, 5, 6 ], [ 2, 6, 7 ],
  [ 1, 3, 7 ], [ 1, 2, 4 ] ] )
Graph( Category := OrientedGraphs, Order := 11, Size := 55, Adjacencies :=
[ [ 2, 4, 5, 6, 10 ], [ 3, 5, 6, 7, 11 ], [ 1, 4, 6, 7, 8 ],
  [ 2, 5, 7, 8, 9 ], [ 3, 6, 8, 9, 10 ], [ 4, 7, 9, 10, 11 ],
  [ 1, 5, 8, 10, 11 ], [ 1, 2, 6, 9, 11 ], [ 1, 2, 3, 7, 10 ],
  [ 2, 3, 4, 8, 11 ], [ 1, 3, 4, 5, 9 ] ] )
gap> PaleyTournament(5);
fail
```

Note that `PaleyTournament( ` *prime* ` )` returns a graph in the category `OrientedGraphs` regardless of the `TargetGraphCategory`.

B.1.130 ParachuteGraph

▷ ParachuteGraph (global variable)

The complement of a `ParapluieGraph`; The suspension of a 4-path with a pendant vertex attached to the south pole.

```
 ─────────────────────────── Example ───────────────────────────
 gap> ParachuteGraph;
 Graph( Category := SimpleGraphs, Order := 7, Size := 12, Adjacencies :=
 [ [ 2 ], [ 1, 3, 4, 5, 6 ], [ 2, 4, 7 ], [ 2, 3, 5, 7 ], [ 2, 4, 6, 7 ],
   [ 2, 5, 7 ], [ 3, 4, 5, 6 ] ] )
```

B.1.131 ParapluieGraph

▷ ParapluieGraph (global variable)

A 3-Fan graph with a 3-path attached to the universal vertex.

```
 ─────────────────────────── Example ───────────────────────────
 gap> ParapluieGraph;
 Graph( Category := SimpleGraphs, Order := 7, Size := 9, Adjacencies :=
 [ [ 2 ], [ 1, 3 ], [ 2, 4, 5, 6, 7 ], [ 3, 5 ], [ 3, 4, 6 ], [ 3, 5, 7 ],
   [ 3, 6 ] ] )
```

B.1.132 ParedGraph

▷ ParedGraph(*G*) (operation)

Returns the pared graph of *G*. This is the induced subgraph obtained from *G* by removing its dominated vertices. When there are twin vertices (mutually dominated vertices), exactly one of them survives the paring in each equivalent class of mutually dominated vertices.

```
 ─────────────────────────── Example ───────────────────────────
 gap> g1:=PathGraph(4);
 Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
 [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
 gap> ParedGraph(g1);
 Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
 [ [ 2 ], [ 1 ] ] )
 gap> g2:=PathGraph(2);
 Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
 [ [ 2 ], [ 1 ] ] )
 gap> ParedGraph(g2);
 Graph( Category := SimpleGraphs, Order := 1, Size := 0, Adjacencies :=
 [ [ ] ] )
```

B.1.133 PathGraph

▷ PathGraph(*n*) (function)

Returns the path graph on *n* vertices.

———— Example ————
```
gap> PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
```

B.1.134 PawGraph

▷ PawGraph (global variable)

The graph on 4 vertices, 4 edges and maximum degree 3: A triangle with a pendant vertex.

———— Example ————
```
gap> PawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3, 4 ], [ 2, 4 ], [ 2, 3 ] ] )
```

B.1.135 PetersenGraph

▷ PetersenGraph (global variable)

The 3-regular graph on 10 vertices having girth 5.

———— Example ————
```
gap> PetersenGraph;
Graph( Category := SimpleGraphs, Order := 10, Size := 15, Adjacencies :=
[ [ 2, 5, 6 ], [ 1, 3, 7 ], [ 2, 4, 8 ], [ 3, 5, 9 ], [ 1, 4, 10 ],
  [ 1, 8, 9 ], [ 2, 9, 10 ], [ 3, 6, 10 ], [ 4, 6, 7 ], [ 5, 7, 8 ] ] )
```

B.1.136 PowerGraph

▷ PowerGraph(*G, exp*) (operation)

Returns the DistanceGraph of *G* using [0, 1, ..., *exp*] as the list of distances. Note that the distance 0 in the list produces loops in the new graph only when the TargetGraphCategory admits loops.

———— Example ————
```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> PowerGraph(g,1);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> PowerGraph(g,1:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 5, Size := 13, Adjacencies :=
[ [ 1, 2 ], [ 1, 2, 3 ], [ 2, 3, 4 ], [ 3, 4, 5 ], [ 4, 5 ] ] )
```

B.1.137 PropertyMorphism

▷ PropertyMorphism(*G, H, PropList*) (operation)

Returns the first morphism (in lexicographic order) from `G` to `H` satisfying the list of properties `PropList`.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: `CHK_WEAK`, `CHK_MORPH`, `CHK_METRIC`, `CHK_CMPLT`, `CHK_MONO` and `CHK_EPI`.

If `G` has `n` vertices and $f : G \to H$ is a morphism, it is represented as `F=[f(1), f(2), ..., f(n)]`.

```
────────────── Example ──────────────
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> PropList:=[CHK_MORPH];;
gap> PropertyMorphism(g,h,PropList);
[ 1, 3, 1, 3 ]
```

B.1.138 PropertyMorphisms

▷ PropertyMorphisms(*G, H, PropList*) (operation)

Returns all morphisms from `G` to `H` satisfying the list of properties `PropList`.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: `CHK_WEAK`, `CHK_MORPH`, `CHK_METRIC`, `CHK_CMPLT`, `CHK_MONO` and `CHK_EPI`.

If `G` has `n` vertices and $f : G \to H$ is a morphism, it is represented as `F=[f(1), f(2), ..., f(n)]`.

```
────────────── Example ──────────────
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> PropList:=[CHK_WEAK,CHK_MONO];;
gap> PropertyMorphisms(g,h,PropList);
[ [ 1, 3, 2, 4 ], [ 1, 4, 2, 3 ], [ 2, 3, 1, 4 ], [ 2, 4, 1, 3 ],
  [ 3, 1, 4, 2 ], [ 3, 2, 4, 1 ], [ 4, 1, 3, 2 ], [ 4, 2, 3, 1 ] ]
```

B.1.139 QtfyIsSimple

▷ QtfyIsSimple(*G*) (attribute)

For internal use. Returns how far is graph `G` from being simple.

B.1.140 QuadraticRingGraph

▷ QuadraticRingGraph(*Rng*) (operation)

Returns the graph G whose vertices are the elements of `Rng` such that x is adjacent to y iff $x + z^2 = y$ for some z in `Rng`.

```
────────────── Example ──────────────
gap> QuadraticRingGraph(ZmodnZ(8));
Graph( Category := SimpleGraphs, Order := 8, Size := 12, Adjacencies :=
```

```
 [ [ 2, 5, 8 ], [ 1, 3, 6 ], [ 2, 4, 7 ], [ 3, 5, 8 ], [ 1, 4, 6 ],
   [ 2, 5, 7 ], [ 3, 6, 8 ], [ 1, 4, 7 ] ] )
```

B.1.141   QuotientGraph

▷ QuotientGraph(*G, Part*)   (operation)
▷ QuotientGraph(*G, L1, L2*)   (operation)

Returns the quotient graph of graph `G` given a vertex partition `Part`, by identifying any two vertices in the same part. The vertices of the quotient graph are the parts in the partition `Part` two of them being adjacent iff any vertex in one part is adjacent to any vertex in the other part. Singletons may be omited in `Part`.

```
––––––––––––––––––––––– Example –––––––––––––––––––––––
gap> g:=PathGraph(8);;
gap> QuotientGraph(g,[[1,5,8],[2],[3],[4],[6],[7]]);
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ], [ 1, 6 ], [ 1, 5 ] ] )
gap> QuotientGraph(g,[[1,5,8]]);
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 5, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ], [ 1, 6 ], [ 1, 5 ] ] )
```

In its second form, `QuotientGraph` identifies each vertex in list `L1`, with the corresponding vertex in list `L2`. `L1` and `L2` must have the same length, but any or both of them may have repetitions.

```
––––––––––––––––––––––– Example –––––––––––––––––––––––
gap> g:=PathGraph(8);;
gap> QuotientGraph(g,[[1,7],[4,8]]);
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 4, 6 ], [ 1, 5 ] ] )
gap> QuotientGraph(g,[1,4],[7,8]);
Graph( Category := SimpleGraphs, Order := 6, Size := 7, Adjacencies :=
[ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 4, 6 ], [ 1, 5 ] ] )
```

B.1.142   Radius

▷ Radius(*G*)   (attribute)

Returns the minimal eccentricity among the vertices of graph `G`.

```
––––––––––––––––––––––– Example –––––––––––––––––––––––
gap> Radius(PathGraph(5));
2
```

B.1.143   RandomCirculant

▷ RandomCirculant(*n*)   (operation)
▷ RandomCirculant(*n, k*)   (operation)
▷ RandomCirculant(*n, p*)   (operation)

Returns a circulant on `n` vertices with its *jumps* selected randomly. In its third form, each possible jump has probability `p` of being selected. In its second form, when `k` is a positive integer, exactly `k`

jumps are selected (provided there are at least `k` possible jumps to select from). The first form is equivalent to specifying *p*=1/2.

```
                                   ——— Example ———
  gap> RandomCirculant(11,2);
  Graph( Category := SimpleGraphs, Order := 11, Size := 22, Adjacencies :=
  [ [ 4, 6, 7, 9 ], [ 5, 7, 8, 10 ], [ 6, 8, 9, 11 ], [ 1, 7, 9, 10 ], [ 2, 8, 10, 11 ],
    [ 1, 3, 9, 11 ], [ 1, 2, 4, 10 ], [ 2, 3, 5, 11 ], [ 1, 3, 4, 6 ], [ 2, 4, 5, 7 ],
    [ 3, 5, 6, 8 ] ] )
  gap> RandomCirculant(11,2);
  Graph( Category := SimpleGraphs, Order := 11, Size := 22, Adjacencies :=
  [ [ 2, 4, 9, 11 ], [ 1, 3, 5, 10 ], [ 2, 4, 6, 11 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ],
    [ 3, 5, 7, 9 ], [ 4, 6, 8, 10 ], [ 5, 7, 9, 11 ], [ 1, 6, 8, 10 ], [ 2, 7, 9, 11 ],
    [ 1, 3, 8, 10 ] ] )
  gap> RandomCirculant(11,1/2);
  Graph( Category := SimpleGraphs, Order := 11, Size := 11, Adjacencies :=
  [ [ 2, 11 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4, 6 ], [ 5, 7 ], [ 6, 8 ], [ 7, 9 ],
    [ 8, 10 ], [ 9, 11 ], [ 1, 10 ] ] )
  gap> RandomCirculant(11,1/2);
  Graph( Category := SimpleGraphs, Order := 11, Size := 44, Adjacencies :=
  [ [ 2, 3, 4, 5, 8, 9, 10, 11 ], [ 1, 3, 4, 5, 6, 9, 10, 11 ],
    [ 1, 2, 4, 5, 6, 7, 10, 11 ], [ 1, 2, 3, 5, 6, 7, 8, 11 ], [ 1, 2, 3, 4, 6, 7, 8, 9 ],
    [ 2, 3, 4, 5, 7, 8, 9, 10 ], [ 3, 4, 5, 6, 8, 9, 10, 11 ], [ 1, 4, 5, 6, 7, 9, 10, 11 ],
    [ 1, 2, 5, 6, 7, 8, 10, 11 ], [ 1, 2, 3, 6, 7, 8, 9, 11 ], [ 1, 2, 3, 4, 7, 8, 9, 10 ]
  ] )
  gap> RandomCirculant(11,1/2);
  Graph( Category := SimpleGraphs, Order := 11, Size := 33, Adjacencies :=
  [ [ 3, 4, 6, 7, 9, 10 ], [ 4, 5, 7, 8, 10, 11 ], [ 1, 5, 6, 8, 9, 11 ],
    [ 1, 2, 6, 7, 9, 10 ], [ 2, 3, 7, 8, 10, 11 ], [ 1, 3, 4, 8, 9, 11 ],
    [ 1, 2, 4, 5, 9, 10 ], [ 2, 3, 5, 6, 10, 11 ], [ 1, 3, 4, 6, 7, 11 ],
    [ 1, 2, 4, 5, 7, 8 ], [ 2, 3, 5, 6, 8, 9 ] ] )
```

B.1.144   RandomGraph

▷ RandomGraph(*n*, *p*)   (function)
▷ RandomGraph(*n*)   (function)

Returns a random graph of order *n* taking the rational $p \in [0,1]$ as the edge probability.

```
                                   ——— Example ———
  gap> RandomGraph(5,1/3);
  Graph( Category := SimpleGraphs, Order := 5, Size := 2, Adjacencies :=
  [ [ 5 ], [ 5 ], [ ], [ ], [ 1, 2 ] ] )
  gap> RandomGraph(5,2/3);
  Graph( Category := SimpleGraphs, Order := 5, Size := 6, Adjacencies :=
  [ [ 4, 5 ], [ 3, 4, 5 ], [ 2, 4 ], [ 1, 2, 3 ], [ 1, 2 ] ] )
  gap> RandomGraph(5,1/2);
  Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
  [ [ 2, 5 ], [ 1, 3, 5 ], [ 2 ], [ ], [ 1, 2 ] ] )
```

If *p* is ommited, the edge probability is taken to be 1/2.

```
                                   ——— Example ———
  gap> RandomGraph(5);
  Graph( Category := SimpleGraphs, Order := 5, Size := 5, Adjacencies :=
```

```
  [ [ 2, 3 ], [ 1 ], [ 1, 4, 5 ], [ 3, 5 ], [ 3, 4 ] ] )
gap> RandomGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 3, Adjacencies :=
[ [ 2, 5 ], [ 1, 4 ], [  ], [ 2 ], [ 1 ] ] )
```

B.1.145 RandomPermutation

▷ RandomPermutation(*n*) (operation)

Returns a random permutation of the list [1, 2, ... *n*].
```
——————————————— Example ———————————————
gap> RandomPermutation(12);
(1,8,10)(2,7,9,12)(3,5,11)(4,6)
```

B.1.146 RandomSubset

▷ RandomSubset(*Set*) (operation)
▷ RandomSubset(*Set, k*) (operation)
▷ RandomSubset(*Set, p*) (operation)

Returns a random subset of the set *Set*. When the positive integer *k* is provided, the returned subset has *k* elements (or fail if *Set* does not have at least *k* elements). When the probability *p* is provided, each element of *Set* has probability *p* of being selected for inclusion in the returned subset. When *k* and *p* are both missing, it is equivalent to specifying *p*=1/2. In the ambiguous case when the second parameter is 1, it is interpreted as the value of *k*.
```
——————————————— Example ———————————————
gap> RandomSubset([1..10],5);
[ 7, 3, 10, 6, 4 ]
gap> RandomSubset([1..10],5);
[ 3, 7, 6, 9, 10 ]
gap> RandomSubset([1..10],5);
[ 3, 9, 7, 2, 6 ]
gap> RandomSubset([1..10],5);
[ 1, 2, 4, 3, 9 ]
gap> RandomSubset([1..10],1/2);
[ 1, 3, 7, 10 ]
gap> RandomSubset([1..10],1/2);
[ 1, 2, 5, 6, 7, 8, 10 ]
gap> RandomSubset([1..10],1/2);
[ 4, 5, 8, 10 ]
gap> RandomSubset([1..10],1/2);
[ 1, 4, 10 ]
```

Even if this operation is intended to be applied to sets, it does not impose this condition on its operand, and can be applied to lists as well.
```
——————————————— Example ———————————————
gap> RandomSubset([1,3,2,2,3,2,1]);
[ 1, 3, 2, 2, 2 ]
gap> RandomSubset([1,3,2,2,3,2,1]);
[ 2, 2 ]
```

B.1.147 RandomlyPermuted

▷ RandomlyPermuted(*Obj*) (operation)

Returns a copy of *Obj* with the order of its elements permuted randomly. Currently, the operation is implemented for lists and graphs.

```
————————————————— Example —————————————————
gap> RandomlyPermuted([1..9]);
[ 9, 7, 5, 3, 1, 4, 8, 6, 2 ]
gap> g:=PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
gap> RandomlyPermuted(g);
Graph( Category := SimpleGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 4 ], [ 3, 4 ], [ 2 ], [ 1, 2 ] ] )
```

B.1.148 RemoveEdges

▷ RemoveEdges(*G, E*) (operation)

Returns a new graph created from graph *G* by removing the edges in list *E*.

```
————————————————— Example —————————————————
gap> g:=CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> RemoveEdges(g,[[1,2]]);
Graph( Category := SimpleGraphs, Order := 4, Size := 5, Adjacencies :=
[ [ 3, 4 ], [ 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> RemoveEdges(g,[[1,2],[3,4]]);
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
[ [ 3, 4 ], [ 3, 4 ], [ 1, 2 ], [ 1, 2 ] ] )
```

B.1.149 RemoveVertices

▷ RemoveVertices(*G, V*) (operation)

Returns a new graph created from graph *G* by removing the vertices in list *V*.

```
————————————————— Example —————————————————
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size := 4, Adjacencies :=
[ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> RemoveVertices(g,[3]);
Graph( Category := SimpleGraphs, Order := 4, Size := 2, Adjacencies :=
[ [ 2 ], [ 1 ], [ 4 ], [ 3 ] ] )
gap> RemoveVertices(g,[1,3]);
Graph( Category := SimpleGraphs, Order := 3, Size := 1, Adjacencies :=
[ [ ], [ 3 ], [ 2 ] ] )
```

B.1.150 RGraph

▷ RGraph (global variable)

A square with two pendant vertices attached to the same vertex of the square.

```
———————————————— Example ————————————————
gap> RGraph;
Graph( Category := SimpleGraphs, Order := 6, Size := 6, Adjacencies :=
[ [ 2 ], [ 1, 3, 5, 6 ], [ 2, 4 ], [ 3, 5 ], [ 2, 4 ], [ 2 ] ] )
```

B.1.151 RingGraph

▷ RingGraph(*Rng, Elms*) (operation)

Returns the graph G whose vertices are the elements of the ring *Rng* such that x is adjacent to y iff x+r=y for some r in *Elms*.

```
———————————————— Example ————————————————
gap> r:=FiniteField(8);Elements(r);
GF(2^3)
[ 0*Z(2), Z(2)^0, Z(2^3), Z(2^3)^2, Z(2^3)^3, Z(2^3)^4, Z(2^3)^5, Z(2^3)^6 ]
gap> RingGraph(r,[Z(2^3),Z(2^3)^4]);
Graph( Category := SimpleGraphs, Order := 8, Size := 8, Adjacencies :=
[ [ 3, 6 ], [ 5, 7 ], [ 1, 4 ], [ 3, 6 ], [ 2, 8 ], [ 1, 4 ], [ 2, 8 ],
   [ 5, 7 ] ] )
```

B.1.152 SetCoordinates

▷ SetCoordinates(*G, Coord*) (operation)

Sets the coordinates of the vertices of *G*, which are used to draw *G* by Draw(*G*).

```
———————————————— Example ————————————————
gap> g:=CycleGraph(4);;
gap> SetCoordinates(g,[[-10,-10 ],[-10,20],[20,-10 ], [20,20]]);
gap> Coordinates(g);
[ [ -10, -10 ], [ -10, 20 ], [ 20, -10 ], [ 20, 20 ] ]
```

B.1.153 SetDefaultGraphCategory

▷ SetDefaultGraphCategory(*Catgy*) (function)

Sets the default graph category to *Catgy*. The default graph category is used when constructing new graphs when no other graph category is indicated. New graphs are always forced to comply with the TargetGraphCategory, so loops may be removed, and arrows may replaced by edges or viceversa, depending on the category that the new graph belongs to.

The available graph categories are: SimpleGraphs, OrientedGraphs, UndirectedGraphs, LooplessGraphs, and Graphs.

```
———————————————— Example ————————————————
gap> SetDefaultGraphCategory(Graphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
```

```
  Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
  [ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(LooplessGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
  Graph( Category := LooplessGraphs, Order := 3, Size := 3, Adjacencies :=
  [ [ 2 ], [ 1 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(UndirectedGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
  Graph( Category := UndirectedGraphs, Order := 3, Size := 3, Adjacencies :=
  [ [ 1, 2 ], [ 1, 3 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(SimpleGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(OrientedGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
  Graph( Category := OrientedGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 2 ], [ ], [ 2 ] ] )
```

B.1.154 SimpleGraphs

▷ SimpleGraphs(*G*)   (function)

SimpleGraphs is a graph category in YAGS. A graph in this category may contain edges, but no loops or arrows. The category has two parents: LooplessGraphs and UndirectedGraphs.

```
───────────── Example ─────────────
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
  Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
  [ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=SimpleGraphs);
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

B.1.155 Size

▷ Size(*G*)   (attribute)

Returns the number of edges of graph *G*.

```
───────────── Example ─────────────
gap> Size(Icosahedron);
30
```

B.1.156 SnubDisphenoid

▷ SnubDisphenoid   (global variable)

The 1-skeleton of the 84th Johnson solid.

```
───────────── Example ─────────────
gap> SnubDisphenoid;
  Graph( Category := SimpleGraphs, Order := 8, Size := 18, Adjacencies :=
```

```
  [ [ 2, 3, 4, 5, 8 ], [ 1, 3, 6, 7, 8 ], [ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ],
    [ 1, 4, 6, 7, 8 ], [ 2, 3, 4, 5, 7 ], [ 2, 5, 6, 8 ], [ 1, 2, 5, 7 ] ] )
```

B.1.157   SpanningForest

▷ SpanningForest(*G*)   (operation)

   Returns a spanning forest of *G*.

B.1.158   SpanningForestEdges

▷ SpanningForestEdges(*G*)   (operation)

   Returns the edges of a spanning forest of *G*.

B.1.159   SpikyGraph

▷ SpikyGraph(*n*)   (function)

   The spiky graph is constructed as follows: Take complete graph on *n* vertices, K_N, and then, for each the *n* subsets of *Vertices*(K_n) of order *n*-1, add an additional vertex which is adjacent precisely to this subset of *Vertices*(K_n).

```
 ─────────────────────────── Example ───────────────────────────
  gap> SpikyGraph(3);
  Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
  [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ], [ 1, 2 ], [ 1, 3 ],
    [ 2, 3 ] ] )
```

B.1.160   SunGraph

▷ SunGraph(*n*)   (function)

   Returns the *n*-Sun: A complete graph on *n* vertices, K_N, with a corona made with a zigzagging 2*n*-cycle glued to a *n*-cycle of the K_N.

```
 ─────────────────────────── Example ───────────────────────────
  gap> SunGraph(3);
  Graph( Category := SimpleGraphs, Order := 6, Size := 9, Adjacencies :=
  [ [ 2, 6 ], [ 1, 3, 4, 6 ], [ 2, 4 ], [ 2, 3, 5, 6 ], [ 4, 6 ],
    [ 1, 2, 4, 5 ] ] )
  gap> SunGraph(4);
  Graph( Category := SimpleGraphs, Order := 8, Size := 14, Adjacencies :=
  [ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ], [ 2, 3, 5, 6, 8 ], [ 4, 6 ],
    [ 2, 4, 5, 7, 8 ], [ 6, 8 ], [ 1, 2, 4, 6, 7 ] ] )
```

B.1.161   Suspension

▷ Suspension(*G*)   (operation)

Returns the suspension of graph `G`. The suspension of `G` is the graph obtained from `G` by adding two new vertices which are adjacent to every vertex of `G` but not to each other. The new vertices are the first ones in the new graph.

```
────────────────────────── Example ──────────────────────────
gap> Suspension(CycleGraph(4));
Graph( Category := SimpleGraphs, Order := 6, Size := 12, Adjacencies :=
[ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ],
  [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ] ] )
```

B.1.162   TargetGraphCategory

▷ TargetGraphCategory([G, ...])   (function)

For internal use. Returns the graph category indicated in the `options stack` if any, otherwise if the list of graphs provided is not empty, returns the minimal common graph category for the graphs in the list, else returns the default graph category. The partial order (by inclusion) among graph categories is as follows:

```
                        Graphs
                       /      \
                      /        \
        UndirectedGraphs        LooplessGraphs
                      \        /      \
                       \      /        \
                     SimpleGraphs       OrientedGraphs
```
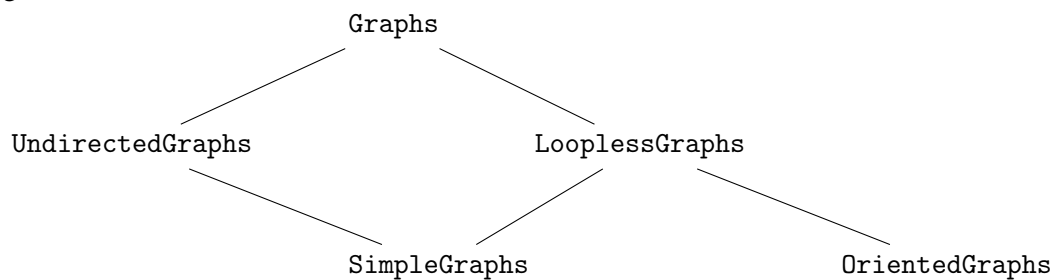
This function is internally called by all graph constructing operations in YAGS to decide the graph category that the newly constructed graph is going to belong. New graphs are always forced to comply with the `TargetGraphCategory`, so loops may be removed, and arrows may replaced by edges or viceversa, depending on the category that the new graph belongs to.

The `options stack` is a mechanism provided by GAP to pass implicit parameters and is used by `TargetGraphCategory` so that the user may indicate the graph category she/he wants for the new graph.

```
────────────────────────── Example ──────────────────────────
gap> SetDefaultGraphCategory(SimpleGraphs);
gap> g1:=CompleteGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [ 1 ] ] )
gap> g2:=CompleteGraph(2:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 2, Size := 1, Adjacencies :=
[ [ 2 ], [  ] ] )
gap> DisjointUnion(g1,g2);
Graph( Category := LooplessGraphs, Order := 4, Size := 3, Adjacencies :=
[ [ 2 ], [ 1 ], [ 4 ], [  ] ] )
gap> DisjointUnion(g1,g2:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 4, Size := 2, Adjacencies :=
[ [ 2 ], [ 1 ], [ 4 ], [ 3 ] ] )
```

In the previous examples, `TargetGraphCategory` was called internally exactly once for each new graph constructed with the following parameters:

```
——————————————— Example ———————————————
gap> TargetGraphCategory();
<Operation "SimpleGraphs">
gap> TargetGraphCategory(:GraphCategory:=OrientedGraphs);
<Operation "OrientedGraphs">
gap> TargetGraphCategory([g1,g2]);
<Operation "LooplessGraphs">
gap> TargetGraphCategory([g1,g2]:GraphCategory:=UndirectedGraphs);
<Operation "UndirectedGraphs">
```

B.1.163 Tetrahedron

▷ Tetrahedron   (global variable)

The 1-skeleton of Plato's tetrahedron.
```
——————————————— Example ———————————————
gap> Tetrahedron;
Graph( Category := SimpleGraphs, Order := 4, Size := 6, Adjacencies :=
[ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
```

B.1.164 TimeInSeconds

▷ TimeInSeconds()   (operation)

Returns the time in seconds since 1970-01-01 00:00:00 UTC as an integer. This is useful to measure execution time. It can also be used to impose time constraints on the execution of algorithms. Note however that the time reported is the *wall time*, not necessarily the time spent in the process you intend to measure.
```
——————————————— Example ———————————————
gap> TimeInSeconds();
1415551598
gap> K:=CliqueGraph;;
gap>  t1:=TimeInSeconds();NumberOfCliques(K(K(K(K(Icosahedron)))));TimeInSeconds()-t1;
1415551608
44644
103
```

Currently, this operation is not working on MS Windows.

B.1.165 TimesProduct

▷ TimesProduct(*G*, *H*)   (operation)

Returns the times product of two graphs *G* and *H*, $G \times H$ (also known as the tensor product).
The times product is computed as follows:
For each pair of vertices $x \in G, y \in H$ we create a vertex (x, y). Given two such vertices (x, y) and (x', y') they are adjacent iff $x \sim x'$ and $y \sim y'$.
```
——————————————— Example ———————————————
gap> g:=PathGraph(3);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
```

```
   [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size := 4, Adjacencies :=
   [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> gh:=TimesProduct(g,h);
Graph( Category := SimpleGraphs, Order := 12, Size := 16, Adjacencies :=
   [ [ 6, 8 ], [ 5, 7 ], [ 6, 8 ], [ 5, 7 ], [ 2, 4, 10, 12 ], [ 1, 3, 9, 11 ],
     [ 2, 4, 10, 12 ], [ 1, 3, 9, 11 ], [ 6, 8 ], [ 5, 7 ], [ 6, 8 ], [ 5, 7 ] ] )
gap> VertexNames(gh);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ],
   [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

B.1.166 TorusGraph

▷ TorusGraph(`n`, `m`)   (function)

Returns (the underlying graph of) a triangulation of the torus on $n.m$ vertices. This graph is constructed using $\{1,2,\ldots,n\} \times \{1,2,\ldots,m\}$ as the vertex set; two of them being adjacent if their difference belongs to $\{(1,0),(0,1),(1,1)\}$ module $\mathbb{Z}_n \times \mathbb{Z}_m$. Hence, in the category of simple graphs, TorusGraph is a 6-regular graph when $n,m \geq 3$.

```
──────────── Example ────────────
TorusGraph(4,4);
Graph( Category := SimpleGraphs, Order := 16, Size := 48, Adjacencies :=
[ [ 2, 4, 5, 6, 13, 16 ], [ 1, 3, 6, 7, 13, 14 ], [ 2, 4, 7, 8, 14, 15 ],
   [ 1, 3, 5, 8, 15, 16 ], [ 1, 4, 6, 8, 9, 10 ], [ 1, 2, 5, 7, 10, 11 ],
   [ 2, 3, 6, 8, 11, 12 ], [ 3, 4, 5, 7, 9, 12 ], [ 5, 8, 10, 12, 13, 14 ],
   [ 5, 6, 9, 11, 14, 15 ], [ 6, 7, 10, 12, 15, 16 ], [ 7, 8, 9, 11, 13, 16 ],
   [ 1, 2, 9, 12, 14, 16 ], [ 2, 3, 9, 10, 13, 15 ], [ 3, 4, 10, 11, 14, 16 ],
   [ 1, 4, 11, 12, 13, 15 ] ] )
```

When $n,m \geq 4$, TorusGraph(`n`, `m`) is actually a Whitney triangulation: Every triangle of the graph is a face of the triagulation. The clique behavior of these graphs were extensively studied in [9]. However, this operation constructs the described graph for all $n,m \geq 1$.

```
──────────── Example ────────────
gap> TorusGraph(2,4);
Graph( Category := SimpleGraphs, Order := 8, Size := 20, Adjacencies :=
[ [ 2, 4, 5, 6, 8 ], [ 1, 3, 5, 6, 7 ], [ 2, 4, 6, 7, 8 ], [ 1, 3, 5, 7, 8 ],
   [ 1, 2, 4, 6, 8 ], [ 1, 2, 3, 5, 7 ], [ 2, 3, 4, 6, 8 ], [ 1, 3, 4, 5, 7 ] ] )
gap> TorusGraph(2,3);
Graph( Category := SimpleGraphs, Order := 6, Size := 15, Adjacencies :=
[ [ 2, 3, 4, 5, 6 ], [ 1, 3, 4, 5, 6 ], [ 1, 2, 4, 5, 6 ], [ 1, 2, 3, 5, 6 ],
   [ 1, 2, 3, 4, 6 ], [ 1, 2, 3, 4, 5 ] ] )
```

Note that in these cases, TorusGraph(`n`, `m`) is not 6-regular nor a Whitney triangulation.

B.1.167 TreeGraph

▷ TreeGraph(`arity, depth`)   (operation)
▷ TreeGraph(`ArityList`)   (operation)

Returns a tree, a connected cycle-free graph. In its second form, the vertices at height `k` (the root vertex has height 1 here) have `ArityList[k]` children. In its first form, all vertices, but the leaves, have `arity` children and the height of the leaves is `depth`+1.

```
——————————————————————— Example ———————————————————————
 gap> TreeGraph(2,3);
 Graph( Category := SimpleGraphs, Order := 15, Size := 14, Adjacencies :=
 [ [ 2, 3 ], [ 1, 4, 5 ], [ 1, 6, 7 ], [ 2, 8, 9 ], [ 2, 10, 11 ], [ 3, 12, 13 ],
   [ 3, 14, 15 ], [ 4 ], [ 4 ], [ 5 ], [ 5 ], [ 6 ], [ 6 ], [ 7 ], [ 7 ] ] )
 gap> TreeGraph([3,2,2]);
 Graph( Category := SimpleGraphs, Order := 22, Size := 21, Adjacencies :=
 [ [ 2, 3, 4 ], [ 1, 5, 6 ], [ 1, 7, 8 ], [ 1, 9, 10 ], [ 2, 11, 12 ], [ 2, 13, 14 ],
   [ 3, 15, 16 ], [ 3, 17, 18 ], [ 4, 19, 20 ], [ 4, 21, 22 ], [ 5 ], [ 5 ], [ 6 ], [ 6 ],
   [ 7 ], [ 7 ], [ 8 ], [ 8 ], [ 9 ], [ 9 ], [ 10 ], [ 10 ] ] )
```

B.1.168   TrivialGraph

▷ TrivialGraph   (global variable)

The one vertex graph.

```
——————————————————————— Example ———————————————————————
 gap> TrivialGraph;
 Graph( Category := SimpleGraphs, Order := 1, Size := 0, Adjacencies :=
 [ [ ] ] )
```

B.1.169   UFFind

▷ UFFind(*UFS*, *x*)   (function)

For internal use. Implements the `find` operation on the `union-find structure`.

B.1.170   UFUnite

▷ UFUnite(*UFS*, *x*, *y*)   (function)

For internal use. Implements the `unite` operation on the `union-find structure`.

B.1.171   UndirectedGraphs

▷ UndirectedGraphs(*G*)   (function)

UndirectedGraphs is a graph category in **YAGS**. A graph in this category may contain edges and loops, but no arrows. The parent of this category is `Graphs`.

```
——————————————————————— Example ———————————————————————
 gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
 Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
 [ [ 1, 2 ], [ 1 ], [ 2 ] ] )
 gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=UndirectedGraphs);
 Graph( Category := UndirectedGraphs, Order := 3, Size := 3, Adjacencies :=
 [ [ 1, 2 ], [ 1, 3 ], [ 2 ] ] )
```

B.1.172 UnitsRingGraph

▷ UnitsRingGraph(*Rng*) (operation)

Returns the graph G whose vertices are the elements of *Rng* such that x is adjacent to y iff x+z=y for some unit z of *Rng*.

```
——————————————————— Example ———————————————————
 gap> UnitsRingGraph(ZmodnZ(8));
 Graph( Category := SimpleGraphs, Order := 8, Size := 16, Adjacencies :=
 [ [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ],
   [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ] ] )
```

B.1.173 VertexDegree

▷ VertexDegree(*G, x*) (operation)

Returns the degree of vertex *x* in Graph *G*.

```
——————————————————— Example ———————————————————
 gap> g:=PathGraph(3);
 Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
 [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
 gap> VertexDegree(g,1);
 1
 gap> VertexDegree(g,2);
 2
```

B.1.174 VertexDegrees

▷ VertexDegrees(*G*) (operation)

Returns the list of degrees of the vertices in graph *G*.

```
——————————————————— Example ———————————————————
 gap> g:=GemGraph;
 Graph( Category := SimpleGraphs, Order := 5, Size := 7, Adjacencies :=
 [ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ] )
 gap> VertexDegrees(g);
 [ 4, 2, 3, 3, 2 ]
```

B.1.175 VertexNames

▷ VertexNames(*G*) (attribute)

Return the list of names of the vertices of *G*. The vertices of a graph in YAGS are always $\{1, 2, \ldots, Order(G)\}$, but depending on how the graph was constructed, its vertices may have also some *names*, that help us identify the origin of the vertices. YAGS will always try to store meaninful names for the vertices. For example, in the case of the LineGraph, the vertex names of the new graph are the edges of the old graph.

```
                              ——————— Example ———————
 gap> g:=LineGraph(DiamondGraph);
 Graph( Category := SimpleGraphs, Order := 5, Size := 8, Adjacencies :=
 [ [ 2, 3, 4 ], [ 1, 3, 4, 5 ], [ 1, 2, 5 ], [ 1, 2, 5 ], [ 2, 3, 4 ] ] )
 gap> VertexNames(g);
 [ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 3, 4 ] ]
 gap> Edges(DiamondGraph);
 [ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 3, 4 ] ]
```

B.1.176   Vertices

▷ Vertices(G)   (operation)

Returns the list [1..Order(G)].

```
                              ——————— Example ———————
 gap> Vertices(Icosahedron);
 [ 1 .. 12 ]
```

B.1.177   WheelGraph

▷ WheelGraph(n)   (operation)
▷ WheelGraph(n, r)   (operation)

In its first form WheelGraph returns the wheel graph on $n+1$ vertices. This is the cone of a cycle: a central vertex adjacent to all the vertices of an n-cycle.

```
                              ——————— Example ———————
 WheelGraph(5);
 gap> Graph( Category := SimpleGraphs, Order := 6, Size := 10, Adjacencies :=
 [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6 ], [ 1, 2, 4 ], [ 1, 3, 5 ], [ 1, 4, 6 ],
   [ 1, 2, 5 ] ] )
```

In its second form, WheelGraph returns returns the wheel graph, but adding r-1 layers, each layer is a new n-cycle joined to the previous layer by a zigzagging $2n$-cycle. This graph is a triangulation of the disk.

```
                              ——————— Example ———————
 gap> WheelGraph(5,2);
 Graph( Category := SimpleGraphs, Order := 11, Size := 25, Adjacencies :=
 [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6, 7, 8 ], [ 1, 2, 4, 8, 9 ], [ 1, 3, 5, 9, 10 ],
   [ 1, 4, 6, 10, 11 ], [ 1, 2, 5, 7, 11 ], [ 2, 6, 8, 11 ], [ 2, 3, 7, 9 ],
   [ 3, 4, 8, 10 ], [ 4, 5, 9, 11 ], [ 5, 6, 7, 10 ] ] )
 gap> WheelGraph(5,3);
 Graph( Category := SimpleGraphs, Order := 16, Size := 40, Adjacencies :=
 [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6, 7, 8 ], [ 1, 2, 4, 8, 9 ], [ 1, 3, 5, 9, 10 ],
   [ 1, 4, 6, 10, 11 ], [ 1, 2, 5, 7, 11 ], [ 2, 6, 8, 11, 12, 13 ],
   [ 2, 3, 7, 9, 13, 14 ], [ 3, 4, 8, 10, 14, 15 ], [ 4, 5, 9, 11, 15, 16 ],
   [ 5, 6, 7, 10, 12, 16 ], [ 7, 11, 13, 16 ], [ 7, 8, 12, 14 ],
   [ 8, 9, 13, 15 ], [ 9, 10, 14, 16 ], [ 10, 11, 12, 15 ] ] )
```

B.1.178 YAGSExec

▷ YAGSExec(*ProgName, InString*)   (operation)

For internal use. Calls external program *ProgName* located in directory *YAGSDir*/bin/ feeding it
with *InString* as input and returning the output of the external program as a string. `fail` is returned
if the program could not be located.

────────────── Example ──────────────
```
gap> YAGSExec("time","");
"1415551127\n"
gap> YAGSExec("nauty","l=0$=1dacn=5 g1,2,3. xbzq");
"(4,5)\n(2,3)\n[2,3,4,5,1]\n[\"cb0c\",\"484f264\",\"b0e19f1\"]\n"
```

Currently, this operation is not working on MS Windows.

B.1.179 YAGSInfo

▷ YAGSInfo   (global variable)

A global record where much **YAGS**-related information is stored. This is intended for internal
use, and much of this information is undocumented, but some of the data stored here could possibly
be useful for advanced users.

However, storing user information in this record and/or changing the values of the stored informa-
tion is discouraged and may produce unpredictable results and an unstable system.

────────────── Example ──────────────
```
gap> YAGSInfo;
rec( AuxInfo := "/dev/null", DataDirectory := "/opt/gap4r7/pkg/yags/data",
  Directory := "/opt/gap4r7/pkg/yags", Internal := rec(  ), Version := "0.0.1",
  graph6 := rec( BinListToNum := function( L ) ... end,
      BinListToNumList := function( L ) ... end, McKayN := function( n ) ... end,
      McKayR := function( L ) ... end, NumListToString := function( L ) ... end,
      NumToBinList := function( n ) ... end, PadLeftnSplitList6 := function( L ) ... end,
      PadRightnSplitList6 := function( L ) ... end,
      StringToBinList := function( Str ) ... end ) )
```

References

[1] C. Bron and J. Kerbosch. *Finding all cliques of an undirected graph–algorithm 457*. Communications of the ACM **16** (1973) 575–577. 22

[2] F.F. Dragan. *Centers of graphs and the Helly property (in Russian)*. PhD thesis, Moldava State University, Chisinău, Moldava, 1989. 48

[3] F. Escalante. *Über iterierte Clique-Graphen*. Abh. Math. Sem. Univ. Hamburg **39** (1973) 59–68. 24

[4] M.E. Frías-Armenta, V. Neumann-Lara and M.A. Pizaña. *Dismantlings and iterated clique graphs*. Discrete Math. **282** (2004) 263–265. 24

[5] M. Frías-Armenta, F. Larrión, V. Neumann-Lara and M. Pizaña. *Edge contraction and edge removal on iterated clique graphs*. Discrete Applied Mathematics **161** (2013) 1427 – 1439. 24

[6] J. Hagauer and S. Klavzar. *Clique-gated graphs*. Discrete Mathematics **161** (1996) 143–149. 48

[7] F. Harary. *Graph theory*. Addison-Wesley Publishing Co., Reading, Mass.-Menlo Park, Calif.-London, 1969. 44

[8] F. Larrión and V. Neumann-Lara. *A family of clique divergent graphs with linear growth*. Graphs Combin. **13** (1997) 263–266. 24

[9] F. Larrión and V. Neumann-Lara. *Clique divergent graphs with unbounded sequence of diameters*. Discrete Math. **197/198** (1999) 491–501. 72

[10] F. Larrión and V. Neumann-Lara. *On clique-divergent graphs with linear growth*. Discrete Math. **245** (2002) 139–153. 23, 24

[11] F. Larrión, V. Neumann-Lara and M.A. Pizaña. *Whitney triangulations, local girth and iterated clique graphs*. Discrete Math. **258** (2002) 123–135. 48, 52

[12] F. Larrión, V. Neumann-Lara and M.A. Pizaña. *Clique divergent clockwork graphs and partial orders*. Discrete Appl. Math. **141** (2004) 195–207. 5, 23

[13] F. Larrión, V. Neumann-Lara and M.A. Pizaña. *Graph relations, clique divergence and surface triangulations*. J. Graph Theory **51** (2006) 110–122. 24

[14] M.A. Pizaña. *Distances and diameters on iterated clique graphs*. Discrete Appl. Math. **141** (2004) 255–161. 19

[15] J.L. Szwarcfiter. *Recognizing clique-Helly graphs*. Ars Combin. **45** (1997) 29–32. 48

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