

YAGS

Yet Another Graph System

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YAGS - Yet Another Graph System

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For details, see the file GPL in the installation directory of YAGS typically under GAP-DIR/pkg/yags/GPL or see <http://www.gnu.org/licenses/gpl-3.0.html>.

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Chapter 1

Preface

1.1 Disclaimer

THIS IS NOT AN OFFICIAL RELEASE YET, this is a version in development. This particular version, 0.0.1, changes from one day to another without warning and even without a change in the version number. Also, the operations and global variables can still change name or even disappear without warning. No commitment is made at the moment concerning compatibility of this version of the software with any future version.

As of this writing (16/Feb/2016) there are only two trustworthy chapters in this manual: Appendixes ‘[YAGS Functions by Topic](#)’ and ‘[YAGS Functions Reference](#)’; also the file `cheatsheet-yags.pdf` (within directory: `YAGSDIR/doc/`) may be useful. All other chapters may contain errors, broken links and misleading information (with higher probability).

The first official version will be 0.0.2 and is scheduled to be ready this year (2016), so come back soon.

1.2 Welcome to YAGS

YAGS - *Yet Another Graph System* is a **GAP** package for dealing with graphs, in the sense of Graph Theory (not bar graphs, pie charts nor graphs of functions). Our graphs are then, ordered pairs $G = (V, E)$, where V is a finite set of vertices and E is a finite set of edges which are (ordered or unordered) pairs of vertices.

YAGS was initiated by M.A. Pizaña in May 2003, and soon incorporated the work of R. MacKinney-Romero and R. Villarroel-Flores. It sprang from our need of computing graphs and graph parameters within our research on graph theory and clique graphs. Consequently, YAGS is well suited for these purposes.

YAGS is a **GAP** package and hence its code is interpreted and not compiled (although some compilation possibilities exist in **GAP**). Therefore, from the very beginning, it was clear that speed is not our main goal. Instead, we wanted a very functional, full-featured system; a system adequate for rapid prototyping of algorithms; and a quick, easy-to-use, way for testing the rapidly changing working conjectures that are typical of the research process.

Over the years, YAGS grew to its present size of more than 200 methods and more than 8 thousands lines of code. We considered that all this code and effort could (and should) be useful for other people and then we decided to engaged in the task of tying up loose ends and writing this manual.

We would like to mention that we started using GRAPE, and we are grateful with its author, Leonard H. Soicher, for the very useful system that we used for several years. But at some point we needed some Object-Oriented features that were not easy to implement in GRAPE and our own subsystem had to follow its own way. If the reader has a profound need for having groups acting on her/his graphs, then GRAPE may be the best choice. On the other hand, YAGS offers a much wider set of functions (Appendix B); a graph-drawing subsystem (Draw (B.1.55)); many methods for dealing with graph homomorphism (Chapter 5); an Object-Oriented approach that simplifies the task of working with several different graph categories (Chapter 4); and a generic backtracking subsystem useful to solve many combinatorial problems easily (Chapter 6).

1.3 Citing YAGS

If you publish a result and you used YAGS during your research, please cite us as you would normally do with a research paper:

R. MacKinney-Romero, M.A. Pizaña and R. Villarroel-Flores.
YAGS - Yet Another Graph System, Version 0.0.1 (2016)
<http://xamanek.izt.uam.mx/yags/>

```
@manual{YAGS, author = {R. MacKinney-Romero and M.A. Pizaña and R.
Villarroel-Flores}, title = {YAGS - Yet Another Graph System, Version 0.0.1},
year = {2016}, note = {http://xamanek.izt.uam.mx/yags/}, }
```

Also, if you install YAGS we will very happy to know about it, so please contribute to increase world's happiness by sending us a notification to: yags@xamanek.izt.uam.mx.

1.4 Authors

The authors of YAGS in the chronological order of their first contribution are as follows:

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1.5 More Information

More information about YAGS can be found on its official web page: <http://xamanek.izt.uam.mx/yags/>

You can receive notifications about YAGS (i.e. new releases, bug fixes, etc.) by subscribing to its email distribution list: <http://xamanek.izt.uam.mx/cgi-bin/mailman/listinfo/yagsnews/>

If you are a developer, you may contribute to our project on our public repository: <https://github.com/yags/main/>

Comments, support requests, bug reports and installation notifications are welcome at yags@xamanek.izt.uam.mx.

Chapter 2

Getting Started

2.1 What is YAGS?

YAGS - *Yet Another Graph System* is a GAP package for dealing with graphs, in the sense of Graph Theory (not bar graphs, pie charts nor graphs of functions). Hence our graphs are ordered pairs $G = (V, E)$, where V is a finite set of vertices and E is a finite set of edges which are (ordered or unordered) pairs of vertices.

YAGS was designed to be useful for research on graphs theory and clique graphs. It is a very functional, full-featured system; a system adequate for rapid prototyping of algorithms; and it is a quick, easy-to-use way, for testing the rapidly changing working conjectures which are typical of the research process.

YAGS offers an ample set of functions (Appendix B); a graph-drawing subsystem (Draw (B.1.55)); many methods for dealing with graph homomorphism (Chapter 5); an Object-Oriented approach that simplifies the task of working with several different graph categories (Chapter 4); and a generic back-tracking subsystem useful to solve many combinatorial problems easily (Chapter 6).

2.2 Installing YAGS

Concise installation instructions follow:

1. Install GAP following the instructions at <http://www.gap-system.org/>.
2. Obtain YAGS from its repository <https://github.com/yags/main/archive/master.zip>.
3. Unpack YAGS: the contents of the zip file should go under GAP-DIR/pkg/yags/.
4. Test YAGS by running GAP, loading YAGS and executing a few basic commands in a terminal:

Example

```
> gap
--- some GAP info here ---
gap> RequirePackage("yags");
--- some YAGS info here ---
true
gap> CliqueNumber(Icosahedron);NumberOfCliques(Icosahedron);
3
20
gap>
```


5. (Optional) Make us happier by sending us a brief installation notification to yags@xamanek.izt.uam.mx

Did it work? Congratulations! Otherwise, consider the following troubleshooting issues:

- **IS GAP WORKING?**
Make sure it is. Follow carefully GAP's installation and troubleshooting procedures.
- **IS THE INSTALLATION DIRECTORY CORRECT?**
The *GAP's installation directory*, GAP-DIR, is typically something like /opt/gap4r7/ (in MS Windows it may look like C:\gap4r7\). If this is the case, the *YAGS's installation directory*, YAGS-DIR, is /opt/gap4r7/pkg/yags/ (in Windows, it would be C:\gap4r7\pkg\yags\). Then, the full path for YAGS's info file PackageInfo.g should be /opt/gap4r7/pkg/yags/PackageInfo.g (or C:\gap4r7\pkg\yags\PackageInfo.g)
- **ARE YOU USING GRAPE?**
GRAPE and YAGS are incompatible: they can not be loaded at the same time. If you had an initialization file that loads GRAPE automatically, you should disable it in order to use YAGS. Alternatively, the command `gap -r` starts gap disabling any user-specific configuration files.
- **UNAUTHORIZED TO ACCESS GAP'S DIRECTORIES?**
The installation procedure above assumed that you have full access to your computer (i.e. that you are the root of the system or that you are using your PC or Mac). If this is not the case, you can also install YAGS under your user directory. For instance, if your user directory is /home/mike/ then you can create a subdirectory /home/mike/gaplocal/ and hence your YAGS's installation directory will be /home/mike/gaplocal/pkg/yags/. If you do this, you can start GAP using `gap -l "/home/mike/gaplocal"` so that GAP knows where your YAGS is.

Finally, if you are fond of git, then you could clone our repository as usual:

```
git clone http://github.com/yags/main.git GAP-DIR/pkg/yags.
```

2.3 A Gentle Tutorial

This tutorial assumes that you already installed GAP and YAGS; and that you have some basic understanding of GAP: user interface, the read-evaluation loop, arithmetic operations, and lists. It is strongly recommended that you have some *working directory*, WORKING-DIR, different from your GAP's and YAGS's installation directories. For instance, if your home directory is /home/mike/ your working directory could be /home/mike/Yags/. Then you should open a terminal, move to your working directory, start GAP and then, load YAGS:

Example

```
/home/mike> cd Yags
/home/mike/Yags> gap
--- some GAP info here ---
gap> RequirePackage("yags");
--- some YAGS info here ---
true
gap>
```

The exact appearance of your system prompt (`/home/mike>` and `/home/map/Yags/>` in the example) may be different depending on your system, but the commands `'cd YAGS'` and `'gap'` are actually the same in all supported systems (assuming your working directory exists and is named 'Yags'). From there (starting with the command `'RequirePackage("yags");'`) everything happens within **GAP** and hence it is system-independent.

Now we want to define some graph. Say we have the list of edges of the desired graph:

$$\{\{1,2\}, \{2,3\}, \{3,4\}, \{4,1\}, \{1,5\}, \{5,4\}\}$$

We can put those edges in a list and then construct the graph:

Example

```
gap> list:=[[1,2],[2,3],[3,4],[4,1],[1,5],[5,4]];
[ [ 1, 2 ], [ 2, 3 ], [ 3, 4 ], [ 4, 1 ], [ 1, 5 ], [ 5, 4 ] ]
gap> g:=GraphByEdges(list);
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 1, 4 ] ] )
```

Note that lists **GAP** uses brackets (`'['` and `']'`) instead of braces (`'{'` and `'}'`) to represent sets and lists (actually, in **GAP** a set is simply an ordered list). Note also that in **GAP** `'list'` and `'List'` are two different things and you can not use the latter since it is a reserved word of **GAP**. In general, it is better for you to use lowercase names for your variables, to avoid name clashes, since all functions in **GAP** and **YAGS** start with an uppercase letter.

The result in the previous example says that it is a graph, and a *simple graph*. By default all graphs in **YAGS** are simple (no loops, no arrows, no parallel edges, only plain undirected edges), in Chapter 4 we explain how to work with other types of graphs, like digraphs, oriented graphs, and graphs that may have loops (but no parallel edges are supported in **YAGS** at all). In this gentle tutorial all our graphs are simple.

The result also says, that the just constructed graph `g` have 5 vertices and 6 edges. The reported list of adjacencies means that the vertex 1 is adjacent (connected by an edge) to 2, 3 and 4, that the vertex 2 is adjacent to 1 and 3 and so on.

To be sure, we can draw our graph and check if it is the intended graph:

Example

```
gap> Draw(g);
```

A separate window appears with an editable drawing of the graph (but the graph itself is not editable here). On that window, type: `'D'` (toggle dynamics on/off), `'L'` (toggle labels on/off) and `'F'` (fit graph into window) to obtain a nice drawing (the initial one is random). The full list of keyboard commands for the Draw window is displayed when typing `'H'` (toggle help message). Besides these keyboard commands, you can use your mouse in obvious ways to edit the drawing.

To quit, type `'S'`. The drawing is stored within the graph `g` and remembered by **YAGS** in case you want to draw the graph again.

If you are new to **GAP**, it may be worth mentioning that you need not remember or type all the full names of every **YAGS** operation: **GAP** supports command completion. For instance, if you type `Path` and then hit the `<TAB>` key, **GAP** automatically completes the prefix to the unique command that completes it, namely: `PathGraph`. If, on the other hand, the prefix has several possible completions, then **GAP** simply beeps, but a second `<TAB>` makes **GAP** respond with a list of possible completions, so you can then type some additional keys and perhaps type `<TAB>` again, and so on.

Example

```
gap> GraphBy<TAB><TAB>
      GraphByAdjMatrix
      GraphByAdjacencies
      GraphByCompleteCover
      GraphByEdges
      GraphByRelation
      GraphByWalks
gap> GraphBy
```

Also, the <UP> and <DOWN> keys are useful to bring back (and perhaps edit) some commands typed earlier in your GAP session.

As with any command in GAP/YAGS, in case of doubt, you can always access the online help by typing:

Example

```
gap> ?yags:draw
Help: several entries match this topic - type ?2 to get match [2]

[1] yags: Draw
[2] yags: Drawing
gap> ?1
      B.1-55 Draw

      > Draw( G ) ----- operation

      Takes a graph G and makes a drawing of it in a separate window. The
      user can then view and modify the drawing and finally save the
      vertex coordinates of the drawing into the graph G.

      --- many more lines here ---
```

Here, '?' specifies that we want help; 'yags:' specifies on which manual book we want to search (YAGS's book in this case) and 'draw' specifies the topic we would like to be informed about. As it is common, there are more than one place with information on our topic, hence we choose among the options with '?1' in the next command line. It is not necessary to specify the book, but then you could receive many more options, in different books, about some specific topic.

Now that we know that our graph is the one we want, we can ask YAGS a lot of things about it:

Example

```
gap> Order(g); Size(g); Diameter(g); Girth(g);
5
6
2
3
gap> NumberOfCliques(g); CliqueNumber(g);
4
3
gap> Adjacencies(g);Adjacency(g,4);Adjacency(g,3);
[ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ], [ 1, 4 ] ]
[ 1, 3, 5 ]
[ 2, 4 ]
gap> VertexDegrees(g);VertexDegree(g,4);VertexDegree(g,3);
```

```

[ 3, 2, 2, 3, 2 ]
3
2
gap> IsDiamondFree(g);IsCompleteGraph(g);IsLoopless(g);
true
false
true
gap> Cliques(g);CompletesOfGivenOrder(g,3);
[ [ 1, 4, 5 ], [ 1, 2 ], [ 2, 3 ], [ 3, 4 ] ]
[ [ 1, 4, 5 ] ]
gap> CompletesOfGivenOrder(g,2);
[ [ 1, 2 ], [ 1, 4 ], [ 1, 5 ], [ 2, 3 ], [ 3, 4 ], [ 4, 5 ] ]

```

Note that in YAGS a *clique* is always *maximal*. This is just a small sample. There are many more operations, properties and attributes of graphs already programmed and ready to use. They are all listed alphabetically in Appendix B and by topic in Appendix A. There is also a one-page pdf file `YAGS-DIR/doc/cheatsheet-yags.pdf` which contains a very useful synopsis of many of the most common YAGS operations.

What about *modifying* our graphs? Well, all graphs in YAGS are always immutable, which means that, once created, we can never modify a graph. But we can create new graphs which are variations of existing ones:

Example

```

gap> g;
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 1, 4 ] ] )
gap> h:=AddEdges(g,[[1,3],[2,4]]);;
gap> g;
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 1, 4 ] ] )
gap> h;
Graph( Category := SimpleGraphs, Order := 5, Size :=
8, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3, 5 ], [ 1, 4 ] ] )

```

Note that the graph `g` remains the same, but the graph `h` has two additional edges. This is done in this way, because in YAGS everything that is computed about a graph is stored within the graph, so that we never need to compute something twice. This saves time when computing heavy attributes of graphs (like computing cliques and clique graphs), but at the expense of having to make a copy of the graph when we just want a small variation of it.

There are a lot of predefined graphs (the full list can be consulted in Appendix A.4):

Example

```

gap> PathGraph(5);CycleGraph(6);CompleteGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
Graph( Category := SimpleGraphs, Order := 6, Size :=
6, Adjacencies := [ [ 2, 6 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ],
[ 4, 6 ], [ 1, 5 ] ] )
Graph( Category := SimpleGraphs, Order := 5, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 5 ], [ 1, 2, 4, 5 ],

```

```

    [ 1, 2, 3, 5 ], [ 1, 2, 3, 4 ] ] )
gap> CompleteBipartiteGraph(3,3);TreeGraph([2,2,2]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 4, 5, 6 ], [ 4, 5, 6 ], [ 4, 5, 6 ],
    [ 1, 2, 3 ], [ 1, 2, 3 ], [ 1, 2, 3 ] ] )
Graph( Category := SimpleGraphs, Order := 15, Size :=
14, Adjacencies := [ [ 2, 3 ], [ 1, 4, 5 ], [ 1, 6, 7 ],
    [ 2, 8, 9 ], [ 2, 10, 11 ], [ 3, 12, 13 ], [ 3, 14, 15 ], [ 4 ],
    [ 4 ], [ 5 ], [ 5 ], [ 6 ], [ 6 ], [ 7 ], [ 7 ] ] )
gap> Octahedron;ParapluieGraph;
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ],
    [ 1, 2, 5, 6 ], [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
Graph( Category := SimpleGraphs, Order := 7, Size :=
9, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4, 5, 6, 7 ], [ 3, 5 ],
    [ 3, 4, 6 ], [ 3, 5, 7 ], [ 3, 6 ] ] )

```

We have found that GraphByWalks (B.1.73) is one of the most useful and versatile ways of specifying graphs:

Example

```

gap> p5:=PathGraph(5);;c6:=CycleGraph(6);;w4:=WheelGraph(4);;
gap> IsIsomorphicGraph(p5,GraphByWalks([1..5]));
true
gap> IsIsomorphicGraph(c6,GraphByWalks([1,2,3,4,5,6,1]));
true
gap> IsIsomorphicGraph(c6,GraphByWalks([1..6],[6,1]));
true
gap> IsIsomorphicGraph(w4,GraphByWalks([1,[2,3,4,5,2]]));
true
gap> sd:=GraphByWalks([1,[2,3,4,5],6],[5,[6,7,8,1],2]);;
gap> IsIsomorphicGraph(SnubDisphenoid,sd);
true

```

YAGS knows about random graphs, so you can take some random graphs and study their parameters. Furthermore, GraphAttributeStatistics can collect statistics on 100 random graphs at a time returning the collected results of the specified graph parameter on these graphs. The following experiments show, for instance that the values of the minimum degree parameter are much more spread than those of the clique number or those of the diameter.

Example

```

gap> MinDeg:=function(G) return Minimum(VertexDegrees(G)); end;;
gap> g:=RandomGraph(30,1/2);; MinDeg(g); CliqueNumber(g); Diameter(g);
9
6
2
gap> GraphAttributeStatistics(30,1/2,MinDeg);
[ [ 5, 1 ], [ 6, 2 ], [ 7, 6 ], [ 8, 22 ], [ 9, 30 ], [ 10, 30 ],
    [ 11, 5 ], [ 12, 4 ] ]
gap> GraphAttributeStatistics(30,1/2,CliqueNumber);
[ [ 5, 2 ], [ 6, 70 ], [ 7, 24 ], [ 8, 4 ] ]
gap> GraphAttributeStatistics(30,1/2,Diameter);
[ [ 2, 91 ], [ 3, 9 ] ]

```

2.4 Cheatsheet

There is a very useful one-page pdf cheatsheet with YAGS most common functions. It can be consulted in your YAGS installation at `YAGS-DIR/doc/cheatsheet-yags.pdf` or on the web at <http://xamanek.izt.uam.mx/yags/cheatsheet-yags.pdf>. Also, the pdf version of this manual includes it in the next page.

Yags cheatsheet

Graph definitions

Adjacency list

g:=GraphByAdjacencies([[1],[4],[1,2],[1]])

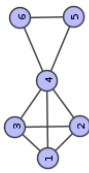


Adjacency matrix

M:=[[false, true, false], [true, false, true], [false, true, false]]
g:=GraphByAdjMatrix(M);

Complete cover

g:=GraphByCompleteCover([[[1,2,3,4],[4,5,6]]]);

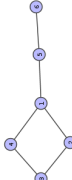


By relation

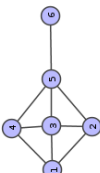
f:=function(x,y) return Intersection(x,y)<>[]; end;;
g:=GraphByRelation([[[1,2,3],[3,4,5],[5,6,7]],f]);

By walks

g:=GraphByWalks([1,2,3,4,1],[1,5,6]);



g:=GraphByWalks([1,[2,3,4],5],[5,6]);



As intersection graph

g:=IntersectionGraph([[[1,2,3],[3,4,5],[5,6,7]]]);

As a copy

h:=CopyGraph(g)

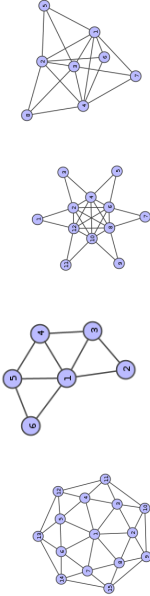
As an induced subgraph

h:=InducedSubgraph(g,[3,4,6]);

Graph families (with parameters)

- g:=DiscreteGraph(n)
- g:=CompleteGraph(n)
- g:=PathGraph(n) n vertices.
- g:=CycleGraph(n)
- g:=CubeGraph(n)
- g:=OctahedralGraph(n)
- g:=JohnsonGraph(n,r) Vertices are subsets of $\{1,2,\dots,n\}$ with r elements, edges between subsets with intersection of $r-1$ elements.

- g:=CompleteBipartiteGraph(n,m)
- g:=CompleteMultiPartiteGraph(n1,n2,[n3,...])
- g:=WheelGraph(n)
- g:=WheelGraph(7,2) Second optional parameter is the radius of the wheel.
- g:=FanGraph(4);
- g:=SunGraph(6);
- g:=SpikyGraph(4);
- Examples: Wheel, Fan, Sun, Spiky:



Named graphs

Platonic

Tetrahedron, Octahedron, Cube, Dodecahedron, Icosahedron.

Other

TrivialGraph, DiamondGraph, ClawGraph, PawGraph, HouseGraph, BullGraph, AntennaGraph, KiteGraph, SnubDisphenoid.

Random graphs

- g:=RandomGraph(n)
- g:=RandomGraph(n,p) Graph with n vertices, each edge with probability p to appear.

Modifying graphs

- h:=RemoveVertices(g,[1,3]);
- h:=AddEdges(g,[1,2]);
- h:=RemoveEdges(g,[1,2],[3,4]);

Parameters

- Order(g)
- Size(g)
- CliqueNumber(g)
- VertexDegree(g,v)

Boolean tests

- IsCompleteGraph(g)
- IsCliqueHelly(g)
- IsDiamondFree(g)

Products

- p:=BoxProduct(g,h)
- p:=TimesProduct(g,h)

- p:=BoxTimesProduct(g,h)
- p:=DisjointUnion(g,h)
- p:=Join(g,h)
- p:=GraphSum(g,1) l is a list of graphs. Suppose that g has n vertices. In the disjoint union of the first n graphs of l (using TrivialGraphs if needed to fill n slots), add all edges between graphs corresponding to adjacent vertices in g.
- p:=Composition(g,h) is the same as GraphSum(g,1), where l is a list of length the order of g, with all components equal to h.

Operators

- h:=CliqueGraph(g)
- h:=CliqueGraph(g,m) Stops when a maximum of m cliques have been found.
- h:=LineGraph(g)
- h:=ComplementGraph(g)
- h:=QuotientGraph(g,p) p is a partition of vertices. The vertices of h are the parts of p, with two vertices adjacent if there are two vertices adjacent in g in the corresponding parts. Singletons in p may be omitted.
- h:=QuotientGraph(g,1) l is a pair of lists of vertices of the same length, with repetitions allowed. In h, each vertex of the first list is identified with the corresponding vertex in the second list.

Lists

- VertexNames(g)
- Cliques(g)
- Cliques(g,m) Stops if a maximum of m cliques have been found.
- AdjMatrix(g)
- Adjacency(g,v)
- Adjacencies(g)
- VertexDegrees(g)
- Edges(g)
- CompletesOfGivenOrder(g,o)

Distances

- Distance(g,x,y)
- DistanceMatrix(g)
- Diameter(g)
- Eccentricity(g,x)
- Radius(g)
- Distances(g,a,b) a, b are lists of vertices. Returns a list.
- DistanceSet(g,a,b) As before, but returns a set.
- DistanceGraph(g,d) The graph with vertex set the vertices of g, two vertices adjacent if their distance is in d.
- PowerGraph(g,n) Same as the distance graph with set of distance $\{1,\dots,n\}$.

Chapter 3

Cliques

3.1 Cliques and Clique Number

3.2 Clique Graphs

3.3 Basements, Stars and Neckties

3.4 Clique Behavior

Chapter 4

Graph Categories

4.1 The Default Graph Category

4.2 The Target Graph Category

4.3 Changing the Target Graph Category Temporarily

4.4 Digraphs, Tournaments, etc.

Chapter 5

Morphisms of Graphs

5.1 A Quick Start

5.2 Main Procedures

5.3 User-Defined Types of Morphisms

5.4 Predefined Types of Morphisms

Chapter 6

Backtracking

6.1 A Simple Example

6.2 How Does it Work?

6.3 Backtracking in Depth

Appendix A

YAGS Functions by Topic

A complete list of all YAGS's functions by topic.

A.1 Most Common Functions

- `AddEdges(G, E)`
Returns a new graph obtained from *G* by adding the list of edges in *E*. (B.1.2)
- `Adjacency(G, x)`
Returns the list of vertices in *G* which are adjacent to vertex *x*. (B.1.5)
- `AutomorphismGroup(G)`
Returns the automorphism group of graph *G*. A synonym is `AutGroupGraph(G)`. (B.1.9)
- `BoxProduct(G, H);`
Returns the BoxProduct (or cartesian product) of graphs *G* and *H*. (B.1.14)
- `BoxTimesProduct(G, H)`
Returns the BoxTimesProduct (or strong product) of graphs *G* and *H*. (B.1.15)
- `Circulant(n, Jumps)`
Returns minimal $(1, 2, \dots, n)$ -invariant graph where vertex 1 is adjacent to vertices in *Jumps*. (B.1.19)
- `CliqueGraph(G)`
`CliqueGraph(G, maxNumCli)`
Returns the intersection graph of the (maximal) cliques of *G*; aborts if *maxNumCli* cliques are found. (B.1.21)
- `Cliques(G)`
`Cliques(G, maxNumCli)`
Returns the list of (maximal) cliques of *G*; aborts if *maxNumCli* cliques are found. (B.1.23)
- `ComplementGraph(G)`
Returns the new graph *H* such that $V(H) = V(G)$ and $xy \in E(H) \iff xy \notin E(G)$. (B.1.25)
- `CompleteGraph(n)`
Returns the graph on *n* vertices having all possible edges present. (B.1.27)

- `CompleteMultipartiteGraph(n1, n2 [, n3 ...])`
Returns the graph with $r \geq 2$ parts of orders $n1, n2, \dots$ such that each vertex is adjacent exactly to all the vertices in the other parts not containing itself. (B.1.29)
- `ConnectedComponents(G)`
Returns the equivalence partition of $V(G)$ corresponding to the equivalence relation **reachable** in G . (B.1.33)
- `CycleGraph(n)`
Returns the cyclic graph on n vertices. (B.1.39)
- `Diameter(G)`
Returns the maximum among the distances between pairs of vertices of G . (B.1.43)
- `DiscreteGraph(n)`
Returns the graph on n vertices with no edges. (B.1.45)
- `DisjointUnion(G, H)`
Returns the disjoint union of two graphs G and H . (B.1.46)
- `Distance(G, x, y)`
Returns the length of a minimal path connecting x to y in G . (B.1.47)
- `Draw(G)`
Draws the graph G on a new window. (B.1.55)
- `Edges(G)`
Returns the list of edges of graph G . (B.1.59)
- `GraphAttributeStatistics(OrderList, ProbList, Attribute)`
Returns statistics for graph attribute *Attribute*. (B.1.66)
- `GraphByAdjacencies(AdjList)`
Returns a new graph having *AdjList* as its list of adjacencies. (B.1.68)
- `GraphByAdjMatrix(Mat)`
Returns a new graph created from an adjacency matrix *Mat*. (B.1.69)
- `GraphByCompleteCover(Cover)`
Returns the graph where the elements of *Cover* are (the vertex sets of) complete subgraphs. (B.1.70)
- `GraphByEdges(L)`
Returns the minimal graph such that the pairs in L are edges. (B.1.71)
- `GraphByRelation(V, Rel)`
`GraphByRelation(n, Rel)`
Returns a new graph G where $xy \in E(G)$ iff $Rel(x, y) = true$. (B.1.72)
- `GraphByWalks(Walk1, Walk2, ...)`
Returns the minimal graph such that *Walk1, Walk2*, etc are Walks. (B.1.73)

- `GraphSum(G, L)`
Returns the lexicographic sum of a list of graphs L over a graph G . (B.1.77)
- `InducedSubgraph(G, V)`
Returns the subgraph of graph G induced by the vertex set V . (B.1.86)
- `InNeigh(G, x)`
Returns the list of in-neighbors of x in G . (B.1.87)
- `IntersectionGraph(L)`
Returns the graph G where $V(G) = L$ and $XY \in E(G) \iff X \cap Y \neq \emptyset$. (B.1.89)
- `IsEdge(G, x, y)`
`IsEdge(G, [x,y])`
Returns true if $[x,y]$ is an edge of G . (B.1.97)
- `IsIsomorphicGraph(G, H)`
Returns true when G is isomorphic to H and false otherwise. (B.1.98)
- `Join(G, H)`
Returns the disjoint union of G and H with all the possible edges between G and H added. (B.1.111)
- `LineGraph(G)`
Returns the intersection graph of the edges of G . (B.1.113)
- `Link(G, x)`
Returns the subgraph induced in G by the neighbors of x . (B.1.114)
- `MaxDegree(G)`
Returns the maximum degree in graph G . (B.1.117)
- `Order(G)`
Returns the number of vertices, of graph G . (B.1.125)
- `PathGraph(n)`
Returns the path graph on n vertices. (B.1.133)
- `QuotientGraph(G, Part)`
`QuotientGraph(G, L1, L2)`
Returns the quotient graph of graph G given a vertex partition $Part$, by identifying any two vertices in the same part. (B.1.141)
- `RandomGraph(n, p)`
`RandomGraph(n)`
Returns a random graph of order n with edge probability p (a rational in $[0, 1]$). (B.1.144)
- `RemoveEdges(G, E)`
Returns a new graph created from graph G by removing the edges in list E . (B.1.148)
- `SetDefaultGraphCategory(Catgy)`
Sets the default graph category to $Catgy$. (B.1.153)

- `Size(G)`
Returns the number of edges of graph *G*. (B.1.155)
- `TimesProduct(G, H)`
Returns the times product (tensor product) $G \times H$ of two graphs *G* and *H*. (B.1.165)
- `TrivialGraph`
The one vertex graph.(B.1.168)
- `VertexDegree(G, x)`
Returns the degree of vertex *x* in Graph *G*. (B.1.173)
- `VertexNames(G)`
Returns the list of names of the vertices of *G*. (B.1.175)
- `WheelGraph(n)`
`WheelGraph(n, r)`
This is the cone of an *n*-cycle; when present, *r* is the radius of the wheel. (B.1.177)

A.2 Drawing

- `Coordinates(G)`
Returns the list of coordinates of the vertices of *G* if they exist; fail otherwise. (B.1.35)
- `Draw(G)`
Draws the graph *G* on a new window. (B.1.55)
- `GraphToRaw(FileName, G)`
Writes the graph *G* in raw format to the file *FileName*. (B.1.78)
- `GraphUpdateFromRaw(FileName, G)`
Updates the coordinates of *G* from a file *FileName* in raw format. (B.1.79)
- `SetCoordinates(G, Coord)`
Sets the coordinates of the vertices of *G*, which are used to draw *G* by `Draw(G)`. (B.1.152)

A.3 Constructing Graphs

- `AddEdges(G, E)`
Returns a new graph obtained from *G* by adding the list of edges in *E*. (B.1.2)
- `AddVerticesByAdjacencies(G, NewAdjList)`
Returns a new graph obtained from *G* by adding some vertices with adjacencies described by *NewAdjList*. (B.1.3)
- `Graph(Rec)`
Returns a new graph created from the information in record *Rec*. (B.1.65)
- `GraphByAdjacencies(AdjList)`
Returns a new graph having *AdjList* as its list of adjacencies. (B.1.68)

- `GraphByAdjMatrix(Mat)`
Returns a new graph created from an adjacency matrix *Mat*. (B.1.69)
- `GraphByCompleteCover(Cover)`
Returns the graph where the elements of *Cover* are (the vertex sets of) complete subgraphs. (B.1.70)
- `GraphByEdges(L)`
Returns the minimal graph such that the pairs in *L* are edges. (B.1.71)
- `GraphByRelation(V, Rel)`
`GraphByRelation(n, Rel)`
Returns a new graph *G* where $xy \in E(G)$ iff $Rel(x,y) = true$. (B.1.72)
- `GraphByWalks(Walk1, Walk2, ...)`
Returns the minimal graph such that *Walk1*, *Walk2*, etc are Walks. (B.1.73)
- `IntersectionGraph(L)`
Returns the graph *G* where $V(G) = L$ and $XY \in E(G) \iff X \cap Y \neq \emptyset$. (B.1.89)
- `RandomGraph(n, p)`
`RandomGraph(n)`
Returns a random graph of order *n* with edge probability *p* (a rational in $[0, 1]$). (B.1.144)
- `RemoveEdges(G, E)`
Returns a new graph created from graph *G* by removing the edges in list *E*. (B.1.148)
- `RemoveVertices(G, V)`
Returns a new graph created from graph *G* by removing the vertices in list *V*. (B.1.149)

A.4 Families of Graphs

- `AGraph`
A 4-cycle with two pendant vertices on consecutive vertices of the cycle. (B.1.7)
- `AntennaGraph`
A `HouseGraph` with a pendant vertex (antenna) on the roof. (B.1.8)
- `BullGraph`
A triangle with two pendant vertices (horns). (B.1.16)
- `ChairGraph`
A tree with degree sequence 3,2,1,1,1. (B.1.18)
- `Circulant(n, Jumps)`
Returns minimal $(1, 2, \dots, n)$ -invariant graph where vertex 1 is adjacent to vertices in *Jumps*. (B.1.19)
- `ClawGraph`
The graph on 4 vertices, 3 edges, and maximum degree 3. (B.1.20)

- `ClockworkGraph(NNFSList)`
`ClockworkGraph(NNFSList, rank)`
`ClockworkGraph(NNFSList, Perm)`
`ClockworkGraph(NNFSList, rank, Perm)`
Returns the clockwork graph specified by its parameters. (B.1.24)
- `CompleteBipartiteGraph(n, m)`
Returns the minimal graph such that all vertices in $\{1..n\}$ are adjacent to all in $\{n+1..n+m\}$. (B.1.26)
- `CompleteGraph(n)`
Returns the graph on n vertices having all possible edges present. (B.1.27)
- `CompleteMultipartiteGraph(n1, n2 [, n3 ...])`
Returns the graph with $r \geq 2$ parts of orders $n1, n2, \dots$ such that each vertex is adjacent exactly to all the vertices in the other parts not containing itself. (B.1.29)
- `Cube`
The 1-skeleton of Plato's cube. (B.1.37)
- `CubeGraph(n)`
Returns the underlying graph of the n -hypercube. (B.1.38)
- `CycleGraph(n)`
Returns the cyclic graph on n vertices. (B.1.39)
- `CylinderGraph(b, h)`
Returns graph on $b(h+1)$ vertices which is a $\{4,6\}$ -regular triangulation of the cylinder. (B.1.40)
- `DartGraph`
A diamond with a pendant vertex and maximum degree 4. (B.1.41)
- `DiamondGraph`
The graph on 4 vertices and 5 edges. (B.1.44)
- `DiscreteGraph(n)`
Returns the graph on n vertices with no edges. (B.1.45)
- `Dodecahedron`
The 1-skeleton of Plato's Dodecahedron. (B.1.52)
- `DominoGraph`
Two squares glued by an edge. (B.1.54)
- `FanGraph(n)`
Returns the n -Fan: The join of a vertex and a $(n+1)$ -path. (B.1.61)
- `FishGraph`
A square and a triangle glued by a vertex. (B.1.62)
- `GemGraph`
The 3-Fan graph. (B.1.63)

- **HouseGraph**
A 4-Cycle and a triangle glued by an edge. (B.1.82)
- **Icosahedron**
The 1-skeleton of Plato's icosahedron. (B.1.83)
- **JohnsonGraph(n, r)**
Returns a new graph G where $V(G)$ is the set of r -subsets of $\{1, 2, \dots, n\}$, two of them being adjacent iff their intersection contains exactly $r-1$ elements. (B.1.110)
- **KiteGraph**
A diamond with a pendant vertex and maximum degree 3. (B.1.112)
- **OctahedralGraph(n)**
Returns the $(2n-2)$ -regular graph on $2n$ vertices. (B.1.123)
- **Octahedron**
The 1-skeleton of Plato's octahedron. (B.1.124)
- **ParachuteGraph**
Returns the suspension of a 4-path with a pendant vertex attached to the south pole. (B.1.130)
- **ParapluieGraph**
A 3-Fan graph with a 3-path attached to the universal vertex. (B.1.131)
- **PathGraph(n)**
Returns the path graph on n vertices. (B.1.133)
- **PawGraph**
A triangle with a pendant vertex. (B.1.134)
- **PetersenGraph**
The 3-regular graph on 10 vertices having girth 5. (B.1.135)
- **RandomCirculant(n)**
RandomCirculant(n, k)
RandomCirculant(n, p)
Returns a circulant on n vertices with its *jumps* selected randomly. (B.1.143)
- **RGraph**
A square with two pendant vertices attached to the same vertex of the square. (B.1.150)
- **SnubDisphenoid**
The 1-skeleton of the 84th Johnson solid. (B.1.156)
- **SpikyGraph(n)**
Returns a complete on n vertices, with an additional complete on n vertices glued to each of its $(n-1)$ -dimensional faces. (B.1.159)
- **SunGraph(n)**
Returns a complete graph on n vertices with a zigzagging corona of $2n$ vertices glued to a n -cycle of the complete graph. (B.1.160)

- `Tetrahedron`
The 1-skeleton of Plato's tetrahedron. (B.1.163)
- `TorusGraph(n , m)`
Returns (the underlying graph of) a triangulation of the torus on $n.m$ vertices. (B.1.166)
- `TreeGraph(arity , depth)`
`TreeGraph(ArityList)`
Returns the tree, the connected cycle-free graph, specified by its parameters. (B.1.167)
- `TrivialGraph`
The one vertex graph. (B.1.168)
- `WheelGraph(n)`
`WheelGraph(n , r)`
This is the cone of an n -cycle; when present r is the radius of the wheel. (B.1.177)

A.5 Small Graphs

- `ConnectedGraphsOfGivenOrder(n)`
Returns the list of all connected graphs of order n (upto isomorphism). (B.1.34)
- `Graph6ToGraph(String)`
Returns the graph represented by *String* which is encoded using Brendan McKay's graph6 format. (B.1.67)
- `GraphsOfGivenOrder(n)`
Returns the list of all graphs of order n (upto isomorphism). (B.1.76)
- `ImportGraph6(Filename)`
Returns the list of graphs represented in *Filename* which are encoded using Brendan McKay's graph6 format. (B.1.84)
- `HararyToMcKay(Spec)`
Returns the McKay's *index* of a Harary's graph specification *Spec*. (B.1.81)
- `McKayToHarary(index)`
Returns the Harary's graph specification of a McKay's *index*. (B.1.81)

A.6 Attributes and Properties

- `Adjacencies(G)`
Returns the list of adjacencies of G : The neighbors of vertex x are listed in position x of that list. (B.1.4)
- `Adjacency(G , x)`
Returns the list of vertices in G which are adjacent to vertex x . (B.1.5)
- `AdjMatrix(G)`
Returns the Adjacency Matrix of G . (B.1.6)

- `AutomorphismGroup(G)`
Returns the automorphism group of graph G . A synonym is `AutGroupGraph(G)`. (B.1.9)
- `BoundaryVertices(G)`
Returns the list of vertices of G that have links isomorphic to a path. But it returns fail if G is not a compact surface. (B.1.13)
- `ConnectedComponents(G)`
Returns the equivalence partition of $V(G)$ corresponding to the equivalence relation *reachable* in G . (B.1.33)
- `Diameter(G)`
Returns the maximum among the distances between pairs of vertices of G . (B.1.43)
- `Distance(G, x, y)`
Returns the length of a minimal path connecting x to y in G . (B.1.47)
- `DistanceMatrix(G)`
Returns an $n \times n$ matrix D , where $D[x][y]$ is the distance between x and y in G . (B.1.50)
- `DistanceSet(G, A, B)`
Returns the set of distances between pairs of vertices in $A \times B$. (B.1.51)
- `Distances(G, A, B)`
Returns the list of distances between pairs of vertices in $A \times B$. (B.1.48)
- `DominatedVertices(G)`
Returns the set of dominated vertices of G . (B.1.53)
- `Eccentricity(G, x)`
Returns the distance from a vertex x in graph G to its most distant vertex in G . (B.1.58)
- `Edges(G)`
Returns the list of edges of graph G . (B.1.59)
- `Girth(G)`
Returns the length of the minimum induced cycle in G . (B.1.64)
- `GraphAttributeStatistics(OrderList, ProbList, Attribute)`
Returns statistics for graph attribute *Attribute*. (B.1.66)
- `InteriorVertices(G)`
Returns the list of vertices of G that have links isomorphic to a cycle. But it returns fail if G is not a compact surface. (B.1.88)
- `IsCompactSurface(G)`
Returns true if every link of G is either an n -cycle, for $n \geq 4$ or an m -path, for $m \geq 2$; it returns false otherwise. (B.1.93)
- `IsDiamondFree(G)`
Returns true if G is free from induced diamonds, false otherwise. (B.1.96)

- `IsEdge(G, x, y)`
(B.1.97)
- `IsEdge(G, [x,y])`
Returns true if $[x,y]$ is an edge of G . (B.1.97)
- `IsLocallyConstant(G)`
Returns true if all the links of G are isomorphic to each other; false otherwise (B.1.99)
- `IsLocallyH(G, H)`
Returns true if all the links of G are isomorphic to H ; false otherwise. (B.1.100)
- `IsLoopless(G)`
Returns true when G is isomorphic to H and false otherwise. (B.1.101)
- `IsOriented(G)`
Returns true if whenever xy is an edge (arrow) of G , yx is not. (B.1.104)
- `IsSimple(G)`
Returns true if G contains no loops and no arrows. (B.1.105)
- `IsSurface(G)`
Returns true if every link of G is an n -cycle, for $n \geq 4$; false otherwise. (B.1.106)
- `IsUndirected(G)`
Returns true if whenever xy is an edge (arrow) of G , yx is also an edge of G . (B.1.109)
- `Link(G, x)`
Returns the subgraph induced in G by the neighbors of x . (B.1.114)
- `Links(G)`
Returns the list of subgraphs of G induced by the neighbors of each vertex of G . (B.1.115)
- `MaxDegree(G)`
Returns the maximum degree in graph G . (B.1.117)
- `MinDegree(G)`
Returns the minimum degree in graph G . (B.1.118)
- `NumberOfConnectedComponents(G)`
Returns the number of connected components of G . (B.1.122)
- `Order(G)`
Returns the number of vertices, of graph G . (B.1.125)
- `Radius(G)`
Returns the minimal eccentricity among the vertices of graph G . (B.1.142)
- `Size(G)`
Returns the number of edges of graph G . (B.1.155)
- `SpanningForest(G)`
Returns a spanning forest of G . (B.1.157)

- `SpanningForestEdges(G)`
Returns the edges of a spanning forest of G . (B.1.158)
- `VertexDegree(G, x)`
Returns the degree of vertex x in Graph G . (B.1.173)
- `VertexDegrees(G)`
Returns the list of degrees of the vertices in graph G . (B.1.174)
- `VertexNames(G)`
Returns the list of names of the vertices of G . (B.1.175)
- `Vertices(G)`
Returns the list $[1..Order(G)]$. (B.1.176)

A.7 Unary Operators

- `ComplementGraph(G)`
Returns the new graph H such that $V(H) = V(G)$ and $xy \in E(H) \iff xy \notin E(G)$. (B.1.25)
- `CompletelyParedGraph(G)`
Returns the graph obtained from G by iteratively removing all dominated vertices. (B.1.28)
- `Cone(G)`
Returns a new graph obtained from G by adding a new vertex which is adjacent to all vertices of G . (B.1.32)
- `CliqueGraph(G)`
`CliqueGraph(G, maxNumCli)`
Returns the intersection graph of the (maximal) cliques of G ; aborts if `maxNumCli` cliques are found. (B.1.21)
- `DistanceGraph(G, Dist)`
Returns a new graph where two vertices are adjacent iff the distance between them belonged to `Dist`. (B.1.49)
- `InducedSubgraph(G, V)`
Returns the subgraph of graph G induced by the vertex set V . (B.1.86)
- `LineGraph(G)`
Returns the intersection graph of the edges of G . (B.1.113)
- `ParedGraph(G)`
Returns the induced subgraph obtained from G by removing its dominated vertices. (B.1.132)
- `PowerGraph(G, exp)`
Returns a new graph where two vertices are neighbors iff their distance in G is less than or equal to `exp`. (B.1.136)

- `QuotientGraph(G, Part)`
`QuotientGraph(G, L1, L2)`
Returns the quotient graph of graph G given a vertex partition $Part$, by identifying any two vertices in the same part. (B.1.141)
- `Suspension(G)`
Returns the graph obtained from G by adding two new vertices which are adjacent to every vertex of G but not to each other. (B.1.161)

A.8 Binary Operators

- `BoxProduct(G, H);`
Returns the BoxProduct (or cartesian product) of graphs G and H . (B.1.14)
- `BoxTimesProduct(G, H)`
Returns the BoxTimesProduct (or strong product) of graphs G and H . (B.1.15)
- `Composition(G, H)`
Returns the composition $G[H]$ of two graphs G and H . (B.1.31)
- `DisjointUnion(G, H)`
Returns the disjoint union of two graphs G and H . (B.1.46)
- `GraphSum(G, L)`
Returns the lexicographic sum of a list of graphs L over a graph G . (B.1.77)
- `Join(G, H)`
Returns the disjoint union of G and H with all the possible edges between G and H added. (B.1.111)
- `TimesProduct(G, H)`
Returns the times product (tensor product) $G \times H$ of two graphs G and H . (B.1.165)

A.9 Cliques

Functions dealing with cliques.

- `Basement(G, KnG, x)`
`Basement(G, KnG, V)`
Returns the basement of vertex x (vertex set V) of the iterated clique graph KnG with respect to G . (B.1.12)
- `CliqueGraph(G)`
`CliqueGraph(G, maxNumCli)`
Returns the intersection graph of the (maximal) cliques of G ; aborts if $maxNumCli$ cliques are found. (B.1.21)
- `CliqueNumber(G)`
Returns the order, $\omega(G)$, of a maximum clique of G . (B.1.22)

- `Cliques(G)`
`Cliques(G, maxNumCli)`
Returns the list of (maximal) cliques of G ; aborts if `maxNumCli` cliques are found. (B.1.23)
- `CompletesOfGivenOrder(G, ord)`
Returns the list of vertex sets of all complete subgraphs of order `ord` of G . (B.1.30)
- `IsCliqueGated(G)`
Returns true if G is a clique gated graph. (B.1.91)
- `IsCliqueHelly(G)`
Returns true if the set of (maximal) cliques G satisfy the *Helly* property. (B.1.92)
- `IsComplete(G, L)`
Returns true if L induces a complete subgraph of G . (B.1.94)
- `IsCompleteGraph(G)`
Returns true if graph G is a complete graph, false otherwise. (B.1.95)
- `NumberOfCliques(G)`
`NumberOfCliques(G, maxNumCli)`
Returns the number of (maximal) cliques of G . (B.1.121)

A.10 Morphisms and Isomorphisms

- `IsIsomorphicGraph(G, H)`
Returns true when G is isomorphic to H and false otherwise. (B.1.98)
- `IsoMorphism(G, H)`
Returns one isomorphism from G to H ; fail if there is none. (B.1.102)
- `IsoMorphisms(G, H)`
Returns the list of all isomorphism from G to H . (B.1.103)
- `NextIsoMorphism(G, H, F)`
Returns the next isomorphism (after F) from G to H . (B.1.119)
- `NextPropertyMorphism(G, H, F, PropList)`
Returns the next morphism (after F) from G to H satisfying the list of properties *PropList*. (B.1.120)
- `PropertyMorphism(G, H, PropList)`
Returns the first morphism from G to H satisfying the list of properties *PropList*. (B.1.137)
- `PropertyMorphisms(G, H, PropList)`
Returns all morphisms from G to H satisfying the list of properties *PropList*. (B.1.138)

A.11 Graphs Categories

- `CopyGraph(G)`
Returns a fresh copy of G . Useful to change the category of a graph. (B.1.36)
- `GraphCategory([G, ...])`;
For internal use. Returns the minimal common category to a list of graphs. (B.1.74)
- `Graphs()`
The category of all graphs that can be represented in YAGS. (B.1.75)
- `in(G, Catgy)`
Returns true if graph G belongs to category $Catgy$ and false otherwise. (B.1.85)
- `LooplessGraphs()`
The category of all graph that may contain arrows and edges but no loops. (B.1.116)
- `OrientedGraphs()`
The category of all graphs that may contain arrows but no edges or loops. (B.1.127)
- `SetDefaultGraphCategory(Catgy)`
Sets the default graph category to $Catgy$. (B.1.153)
- `SimpleGraphs()`
The category of all graphs which may contain edges but no arrows or loops. (B.1.154)
- `TargetGraphCategory([G, ...])`;
For internal use. Within YAGS methods, returns the graph category to which the new graph will belong. (B.1.162)
- `UndirectedGraphs()`
The category of all graphs that may contain loops and edges but no arrows. (B.1.171)

A.12 Digraphs

- `InNeigh(G, x)`
Returns the list of in-neighbors of x in G . (B.1.87)
- `IsTournament(G)`
Returns true if G contains no loops or edges but only arrows and it is maximal w.r.t. this property. (B.1.107)
- `IsTransitiveTournament(G)`
Returns true if G is a Tournament and whenever xy and yz are arrows, then xz is an arrow too. (B.1.108)
- `Orientations(G)`
Returns the list of all the oriented graphs that are obtained from G by replacing each edge by one arrow. (B.1.126)

- `OutNeigh(G, x)`
Returns the list of out-neighbors of *x* in *G*. (B.1.128)
- `PaleyTournament(prime)`
Returns the Paley tournament associated with prime number *prime*. (B.1.129)

A.13 Groups and Rings

- `CayleyGraph(Grp)`
`CayleyGraph(Grp, Elms)`
Returns the CayleyGraph of group *Grp*. (B.1.17)
- `Circulant(n, Jumps)`
Returns minimal $(1,2,\dots,n)$ -invariant graph where vertex 1 is adjacent to vertices in *Jumps*. (B.1.19)
- `GroupGraph(G, Grp)`
`GroupGraph(G, Grp, Act)`
Returns the minimal *Grp*-invariant (under the action *Act*) graph containing *G*. (B.1.80)
- `QuadraticRingGraph(Rng)`
Returns a graph *H* whose vertices are the elements of the ring *Rng* and $xy \in E(H) \iff x + z^2 = y$ for some *z* in *Rng*. (B.1.140)
- `RingGraph(Rng, Elms)`
Returns the graph *G* whose vertices are the elements of the ring *Rng* such that *x* is adjacent to *y* iff $x+r=y$ for some *r* in *Elms*. (B.1.151)
- `UnitsRingGraph(Rng)`
Returns the graph *G* whose vertices are the elements of *Rng* such that *x* is adjacent to *y* iff $x+z=y$ for some unit *z* of *Rng*. (B.1.172)

A.14 Backtracking

- `BackTrack(L, Opts, Chk, Done, Extra)`
Returns the next solution (after *L*) to a backtracking combinatorial problem specified by its parameters. (B.1.10)
- `BackTrackBag(Opts, Chk, Done, Extra)`
Returns the list of all solutions to a backtracking combinatorial problem specified by its parameters. (B.1.11)

A.15 Miscellaneous

- `DumpObject(Obj)`
For internal use. Dumps all information available for object *Obj*. (B.1.56)

- `EasyExec(Dir, ProgName, InString)`
`EasyExec(ProgName, InString)`
Calls the external program *ProgName* with input string *InString*; returns the output string. (B.1.57)
- `EquivalenceRepresentatives(L, Equiv)`
Returns a sublist of *L*, which is a complete list of representatives of *L* under the equivalent relation *Equiv*. (B.1.60)
- `IsBoolean(Obj)`
Returns true if object *Obj* is true or false and false otherwise. (B.1.90)
- `QtifyIsSimple(G)`
For internal use. Returns how far is graph *G* from being simple. (B.1.139)
- `RandomlyPermuted(Obj)`
Returns a copy of *Obj* with the order of its elements permuted randomly. (B.1.147)
- `RandomPermutation(n)`
Returns a random permutation of the list $[1, 2, \dots, n]$. (B.1.145)
- `RandomSubset(Set)`
(B.1.146)
- `RandomSubset(Set, k)`
(B.1.146)
- `RandomSubset(Set, p)`
Returns a random subset of the set *Set*. It also works for lists though. (B.1.146)
- `TimeInSeconds()`
Returns the time in seconds since 1970-01-01 00:00:00 UTC as an integer. (B.1.164)
- `UFFind(UFS, x)`
For internal use. Implements the *find* operation on the *union-find structure*. (B.1.169)
- `UFUnite(UFS, x, y)`
For internal use. Implements the *unite* operation on the *union-find structure*. (B.1.170)
- `YAGSExec(ProgName, InString)`
For internal use. Calls external program *ProgName* located in directory `YAGSDir/bin/` feeding it with *InString* as input and returning the output of the external program as a string. (B.1.178)

A.16 Undocumented

- `DeclareQtifyProperty(Name, Filter)`
For internal use. Declare a quantifiable property. (B.1.42)
- `DumpObject(Obj)`
For internal use. Dumps all information available for object *Obj*. (B.1.56)

- `EasyExec(Dir, ProgName, InString)`
`EasyExec(ProgName, InString)`
Calls the external program *ProgName* with input string *InString*; returns the output string. (B.1.57)
- `GraphToRaw(FileName, G)`
Writes the graph *G* in raw format to the file *FileName*. (B.1.78)
- `GraphUpdateFromRaw(FileName, G)`
Updates the coordinates of *G* from a file *FileName* in raw format. (B.1.79)
- `QtfyIsSimple(G)`
For internal use. Returns how far is graph *G* from being simple. (B.1.139)
- `YAGSExec(ProgName, InString)`
For internal use. Calls external program *ProgName* located in directory `YAGSDir/bin/` feeding it with *InString* as input and returning the output of the external program as a string. (B.1.178)

Appendix B

YAGS Functions Reference

This chapter contains a complete list of all YAGS's functions, with definitions, in alphabetical order.

B.1 Full Alphabetic List

B.1.1 Order

▷ `Order(G)` (attribute)

Returns the number of vertices, of graph G .

Example

```
gap> Order(Icosahedron);  
12
```

B.1.2 AddEdges

▷ `AddEdges(G , E)` (operation)

Returns a new graph created from graph G by adding the edges in list E .

Example

```
gap> g:=CycleGraph(4);  
Graph( Category := SimpleGraphs, Order := 4, Size :=  
4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )  
gap> AddEdges(g, [[1,3]]);  
Graph( Category := SimpleGraphs, Order := 4, Size :=  
5, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3 ] ] )  
gap> AddEdges(g, [[1,3],[2,4]]);  
Graph( Category := SimpleGraphs, Order := 4, Size :=  
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],  
[ 1, 2, 3 ] ] )
```

B.1.3 AddVerticesByAdjacencies

▷ `AddVerticesByAdjacencies(G , $NewAdjList$)` (operation)

Returns a new graph created from graph G by adding as many new vertices as `Length(NewAdjList)`. Each entry in `NewAdjList` is also a list: the list of neighbors of the corresponding new vertex.

Example

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> AddVerticesByAdjacencies(g,[[1,2],[4,5]]);
Graph( Category := SimpleGraphs, Order := 7, Size :=
8, Adjacencies := [ [ 2, 6 ], [ 1, 3, 6 ], [ 2, 4 ], [ 3, 5, 7 ],
[ 4, 7 ], [ 1, 2 ], [ 4, 5 ] ] )
gap> AddVerticesByAdjacencies(g,[[1,2,7],[4,5]]);
Graph( Category := SimpleGraphs, Order := 7, Size :=
9, Adjacencies := [ [ 2, 6 ], [ 1, 3, 6 ], [ 2, 4 ], [ 3, 5, 7 ],
[ 4, 7 ], [ 1, 2, 7 ], [ 4, 5, 6 ] ] )
```

B.1.4 Adjacencies

▷ `Adjacencies(G)` (operation)

Returns the adjacency lists of graph G .

Example

```
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> Adjacencies(g);
[ [ 2 ], [ 1, 3 ], [ 2 ] ]
```

B.1.5 Adjacency

▷ `Adjacency(G , x)` (operation)

Returns the adjacency list of vertex x in G .

Example

```
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> Adjacency(g,1);
[ 2 ]
gap> Adjacency(g,2);
[ 1, 3 ]
```

B.1.6 AdjMatrix

▷ `AdjMatrix(G)` (attribute)

Returns the adjacency matrix of graph G .

Example

```
gap> AdjMatrix(CycleGraph(4));
[ [ false, true, false, true ], [ true, false, true, false ],
[ false, true, false, true ], [ true, false, true, false ] ]
```

B.1.7 AGraph

▷ AGraph

(global variable)

A 4-cycle with two pendant vertices on consecutive vertices of the cycle.

Example

```
gap> AGraph;
Graph( Category := SimpleGraphs, Order := 6, Size :=
6, Adjacencies := [ [ 2 ], [ 1, 3, 5 ], [ 2, 4 ], [ 3, 5 ],
[ 2, 4, 6 ], [ 5 ] ] )
```

B.1.8 AntennaGraph

▷ AntennaGraph

(global variable)

A HouseGraph with a pendant vertex (antenna) on the roof.

Example

```
gap> AntennaGraph;
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 1, 4, 6 ], [ 5 ] ] )
```

B.1.9 AutomorphismGroup

▷ AutomorphismGroup(G)

(attribute)

▷ AutGroupGraph(G)

(attribute)

Returns the group of automorphisms of the graph G . Both forms are synonyms.

Example

```
gap> AutomorphismGroup(Icosahedron);
Group([ (1,2,6,9,8,12,7,11,4,3)(5,10), (1,2,6)(3,9,5)(4,10,8)
(7,11,12) ])
gap> AutGroupGraph(Icosahedron);
Group([ (1,2,6,9,8,12,7,11,4,3)(5,10), (1,2,6)(3,9,5)(4,10,8)
(7,11,12) ])
```

B.1.10 BackTrack

▷ BackTrack(L , $Opts$, Chk , $Done$, $Extra$)

(operation)

Generic, user-customizable backtracking algorithm.

A backtracking algorithm explores a decision tree in search for solutions to a combinatorial problem. The combinatorial problem and the search strategy are specified by the parameters: L is just a list that BackTrack uses to keep track of solutions and partial solutions. It is usually set to the empty list as a starting point. After a solution is found, it is returned *and* stored in L . This value of L is then used as a starting point to search for the next solution in case BackTrack is called again. Partial solutions are also stored in L during the execution of BackTrack. $Extra$ may be any object, list, record, etc. BackTrack only uses it to pass this data to the user-defined functions $Opts$, Chk and $Done$, therefore offering you a way to share data between your functions. $Opts := \text{function}(L, extra)$

must return the list of continuation options (childs) one has after some partial solution (node) L has been reached within the decision tree ($Opts$ may use the extra data $Extra$ as needed). Each of the values in the list returned by $Opts(L, extra)$ will be tried as possible continuations of the partial solution L . If $Opts(L, extra)$ always returns the same list, you can put that list in place of the parameter $Opts$. $Chk := function(L, extra)$ must evaluate the partial solution L possibly using the extra data $Extra$ and must return false when it knows that L can not be extended to a solution of the problem. Otherwise it returns true. Chk may assume that $L\{[1..Length(L)-1]\}$ already passed the test. $Done := function(L, extra)$ returns true if L is already a complete solution and false otherwise. In many combinatorial problems, any partial solution of certain length n is also a solution (and viceversa), so if this is your case, you can put that length in place of the parameter $Done$.

The following example uses `BackTrack` in its simplest form to compute derangements (permutations of a set, where none of the elements appears in its original position).

Example

```
gap> N:=4;;L:=[];;extra:=[];;opts:= [1..N];;done:=N;;
gap> chk:=function(L,extra) local i; i:=Length(L);
>      return not L[i] in L{[1..i-1]} and L[i]<> i; end;;
gap> BackTrack(L,opts,chk,done,extra);
[ 2, 1, 4, 3 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 2, 3, 4, 1 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 2, 4, 1, 3 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 3, 1, 4, 2 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 3, 4, 1, 2 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 3, 4, 2, 1 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 4, 1, 2, 3 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 4, 3, 1, 2 ]
gap> BackTrack(L,opts,chk,done,extra);
[ 4, 3, 2, 1 ]
gap> BackTrack(L,opts,chk,done,extra);
fail
```

B.1.11 BackTrackBag

▷ `BackTrackBag($Opts$, Chk , $Done$, $Extra$)`

(operation)

Returns the list of all solutions that would be returned one at a time by `Backtrack`.

The following example computes all derangements of order 4.

Example

```
gap> N:=4;;
gap> chk:=function(L,extra) local i; i:=Length(L);
>      return not L[i] in L{[1..i-1]} and L[i]<> i; end;;
gap> BackTrackBag([1..N],chk,N,[]);
[ [ 2, 1, 4, 3 ], [ 2, 3, 4, 1 ], [ 2, 4, 1, 3 ], [ 3, 1, 4, 2 ],
```



```
[ 3, 4, 1, 2 ], [ 3, 4, 2, 1 ], [ 4, 1, 2, 3 ], [ 4, 3, 1, 2 ],
[ 4, 3, 2, 1 ] ]
```

B.1.12 Basement

- ▷ `Basement(G , KnG , x)` (operation)
 ▷ `Basement(G , KnG , V)` (operation)

Given a graph G , some iterated clique graph KnG of G and a vertex x of KnG , the operation returns the *basement* of x with respect to G [14]. Loosely speaking, the basement of x is the set of vertices of G that constitutes the iterated clique x .

Example

```
gap> g:=Icosahedron;;Cliques(g);
[ [ 1, 2, 3 ], [ 1, 2, 6 ], [ 1, 3, 4 ], [ 1, 4, 5 ], [ 1, 5, 6 ],
  [ 4, 5, 7 ], [ 4, 7, 11 ], [ 5, 7, 8 ], [ 7, 8, 12 ],
  [ 7, 11, 12 ], [ 5, 6, 8 ], [ 6, 8, 9 ], [ 8, 9, 12 ], [ 2, 6, 9 ],
  [ 2, 9, 10 ], [ 9, 10, 12 ], [ 2, 3, 10 ], [ 3, 10, 11 ],
  [ 10, 11, 12 ], [ 3, 4, 11 ] ]
gap> kg:=CliqueGraph(g);; k2g:=CliqueGraph(kg);;
gap> Basement(g,k2g,1);Basement(g,k2g,2);
[ 1, 2, 3, 4, 5, 6 ]
[ 1, 2, 3, 4, 6, 10 ]
```

In its second form, V is a set of vertices of KnG , in that case, the basement is simply the union of the basements of the vertices in V .

Example

```
gap> Basement(g,k2g,[1,2]);
[ 1, 2, 3, 4, 5, 6, 10 ]
```

B.1.13 BoundaryVertices

- ▷ `BoundaryVertices(G)` (attribute)

When G is a compact surface, it returns the list of vertices in the boundary (of the triangulation) of the surface. That is, the list of vertices of G that have links isomorphic to a path. It returns `fail` if G is not a compact surface.

Example

```
gap> BoundaryVertices(WheelGraph(4,2));
[ 6, 7, 8, 9 ]
gap> BoundaryVertices(Octahedron);
[ ]
```

B.1.14 BoxProduct

- ▷ `BoxProduct(G , H)` (operation)

Returns the box product, $G \square H$, of two graphs G and H (also known as the cartesian product).

The box product is calculated as follows:

For each pair of vertices $x \in G, y \in H$ we create a vertex (x, y) . Given two such vertices (x, y) and (x', y') they are adjacent iff $x = x'$ and $y \sim y'$ or $x \sim x'$ and $y = y'$.

Example

```
gap> g:=PathGraph(3);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> gh:=BoxProduct(g,h);
Graph( Category := SimpleGraphs, Order := 12, Size :=
20, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3, 6 ], [ 2, 4, 7 ],
[ 1, 3, 8 ], [ 1, 6, 8, 9 ], [ 2, 5, 7, 10 ], [ 3, 6, 8, 11 ],
[ 4, 5, 7, 12 ], [ 5, 10, 12 ], [ 6, 9, 11 ], [ 7, 10, 12 ],
[ 8, 9, 11 ] ] )
gap> VertexNames(gh);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ],
[ 2, 3 ], [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

B.1.15 BoxTimesProduct

▷ BoxTimesProduct(G, H)

(operation)

Returns the boxtimes product of two graphs G and H , $G \boxtimes H$ (also known as the strong product).

The boxtimes product is calculated as follows:

For each pair of vertices $x \in G, y \in H$ we create a vertex (x, y) . Given two such vertices (x, y) and (x', y') such that $(x, y) \neq (x', y')$ they are adjacent iff $x \simeq x'$ and $y \simeq y'$.

Example

```
gap> g:=PathGraph(3);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> gh:=BoxTimesProduct(g,h);
Graph( Category := SimpleGraphs, Order := 12, Size :=
36, Adjacencies := [ [ 2, 4, 5, 6, 8 ], [ 1, 3, 5, 6, 7 ],
[ 2, 4, 6, 7, 8 ], [ 1, 3, 5, 7, 8 ], [ 1, 2, 4, 6, 8, 9, 10, 12 ],
[ 1, 2, 3, 5, 7, 9, 10, 11 ], [ 2, 3, 4, 6, 8, 10, 11, 12 ],
[ 1, 3, 4, 5, 7, 9, 11, 12 ], [ 5, 6, 8, 10, 12 ],
[ 5, 6, 7, 9, 11 ], [ 6, 7, 8, 10, 12 ], [ 5, 7, 8, 9, 11 ] ] )
gap> VertexNames(gh);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ],
[ 2, 3 ], [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]
```

B.1.16 BullGraph

▷ BullGraph

(global variable)

A triangle with two pendant vertices (horns).

Example

```
gap> BullGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2 ], [ 1, 3, 4 ], [ 2, 4 ], [ 2, 3, 5 ], [ 4 ]
] )
```

B.1.17 CayleyGraph

- ▷ `CayleyGraph(Grp, Elms)` (operation)
 ▷ `CayleyGraph(Grp)` (operation)

Returns the graph G whose vertices are the elements of the group Grp such that x is adjacent to y iff $x * g = y$ for some g in the list $Elms$. if $Elms$ is not provided, then the generators of G are used instead.

Example

```
gap> grp:=Group((1,2,3),(1,2));
Group([ (1,2,3), (1,2) ])
gap> CayleyGraph(grp);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 3, 4, 5 ], [ 3, 5, 6 ], [ 1, 2, 6 ],
[ 1, 5, 6 ], [ 1, 2, 4 ], [ 2, 3, 4 ] ] )
gap> CayleyGraph(grp,[(1,2),(2,3)]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
6, Adjacencies := [ [ 2, 3 ], [ 1, 5 ], [ 1, 4 ], [ 3, 6 ], [ 2, 6 ],
[ 4, 5 ] ] )
```

B.1.18 ChairGraph

- ▷ `ChairGraph` (global variable)

A tree with degree sequence 3,2,1,1,1.

Example

```
gap> ChairGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3, 4 ], [ 2 ], [ 2, 5 ], [ 4 ] ] )
```

B.1.19 Circulant

- ▷ `Circulant(n, Jumps)` (operation)

Returns the graph G whose vertices are $[1..n]$ such that x is adjacent to y iff $x+z=y \bmod n$ for some z the list of *Jumps*.

Example

```
gap> Circulant(6,[1,2]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 2, 3, 5, 6 ], [ 1, 3, 4, 6 ], [ 1, 2, 4, 5 ],
[ 2, 3, 5, 6 ], [ 1, 3, 4, 6 ], [ 1, 2, 4, 5 ] ] )
```

B.1.20 ClawGraph

- ▷ `ClawGraph` (global variable)

The graph on 4 vertices, 3 edges, and maximum degree 3.

Example

```
gap> ClawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1 ] ] )
```

B.1.21 CliqueGraph

- ▷ `CliqueGraph(G)` (attribute)
- ▷ `CliqueGraph(G , $maxNumCli$)` (operation)

Returns the intersection graph of all the (maximal) cliques of G .

The additional parameter $maxNumCli$ aborts the computation when $maxNumCli$ cliques are found, even if they are all the cliques of G . If the bound $maxNumCli$ is reached, *fail* is returned.

Example

```
gap> CliqueGraph(Octahedron);
Graph( Category := SimpleGraphs, Order := 8, Size :=
24, Adjacencies := [ [ 2, 3, 4, 5, 6, 7 ], [ 1, 3, 4, 5, 6, 8 ],
[ 1, 2, 4, 5, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ],
[ 1, 2, 4, 5, 7, 8 ], [ 1, 3, 4, 5, 6, 8 ], [ 2, 3, 4, 5, 6, 7 ] ] )
gap> CliqueGraph(Octahedron,9);
Graph( Category := SimpleGraphs, Order := 8, Size :=
24, Adjacencies := [ [ 2, 3, 4, 5, 6, 7 ], [ 1, 3, 4, 5, 6, 8 ],
[ 1, 2, 4, 5, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ], [ 1, 2, 3, 6, 7, 8 ],
[ 1, 2, 4, 5, 7, 8 ], [ 1, 3, 4, 5, 6, 8 ], [ 2, 3, 4, 5, 6, 7 ] ] )
gap> CliqueGraph(Octahedron,8);
fail
```

B.1.22 CliqueNumber

- ▷ `CliqueNumber(G)` (attribute)

Returns the order, $\omega(G)$, of a maximum clique of G .

Example

```
gap> g:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size :=
14, Adjacencies := [ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ],
[ 2, 3, 5, 6, 8 ], [ 4, 6 ], [ 2, 4, 5, 7, 8 ], [ 6, 8 ],
[ 1, 2, 4, 6, 7 ] ] )
gap> CliqueNumber(g);
4
```

B.1.23 Cliques

- ▷ `Cliques(G)` (attribute)
- ▷ `Cliques(G , $maxNumCli$)` (operation)

Returns the set of all (maximal) cliques of a graph G . A clique is a maximal complete subgraph. Here, we use the Bron-Kerbosch algorithm [1].

In the second form, It stops computing cliques after $maxNumCli$ of them have been found.

Example

```
gap> Cliques(Octahedron);
[ [ 1, 3, 5 ], [ 1, 3, 6 ], [ 1, 4, 5 ], [ 1, 4, 6 ], [ 2, 3, 5 ],
[ 2, 3, 6 ], [ 2, 4, 5 ], [ 2, 4, 6 ] ]
gap> Cliques(Octahedron,4);
[ [ 1, 3, 5 ], [ 1, 3, 6 ], [ 1, 4, 5 ], [ 1, 4, 6 ] ]
```

B.1.24 ClockworkGraph (basic)

- ▷ `ClockworkGraph(NNFSList)` (operation)
- ▷ `ClockworkGraph(NNFSList, rank)` (operation)
- ▷ `ClockworkGraph(NNFSList, Perm)` (operation)
- ▷ `ClockworkGraph(NNFSList, rank, Perm)` (operation)

Returns the clockwork graph [10][12] specified by its parameters. A clockwork graph consists of two parts: the crown and the core, both of them are *cyclically segmented*. When not specified, the *rank* is assumed to be 2 and the *return permutation*, *Perm*, is assumed to be trivial, let us assume this is our case. Consider the following examples:

Example

```
gap> ClockworkGraph([[0],[0],[0],[0]]);
Graph( Category := SimpleGraphs, Order := 12, Size :=
28, Adjacencies := [ [ 2, 3, 4, 10, 12 ], [ 1, 3, 5, 11, 12 ],
[ 1, 2, 4, 5 ], [ 1, 3, 5, 6, 7 ], [ 2, 3, 4, 6, 8 ],
[ 4, 5, 7, 8 ], [ 4, 6, 8, 9, 10 ], [ 5, 6, 7, 9, 11 ],
[ 7, 8, 10, 11 ], [ 1, 7, 9, 11, 12 ], [ 2, 8, 9, 10, 12 ],
[ 1, 2, 10, 11 ] ] )
gap> ClockworkGraph([[1],[1],[1],[1]]);
Graph( Category := SimpleGraphs, Order := 12, Size :=
32, Adjacencies := [ [ 2, 3, 4, 10, 12 ], [ 1, 3, 5, 11, 12 ],
[ 1, 2, 4, 5, 6, 12 ], [ 1, 3, 5, 6, 7 ], [ 2, 3, 4, 6, 8 ],
[ 3, 4, 5, 7, 8, 9 ], [ 4, 6, 8, 9, 10 ], [ 5, 6, 7, 9, 11 ],
[ 6, 7, 8, 10, 11, 12 ], [ 1, 7, 9, 11, 12 ], [ 2, 8, 9, 10, 12 ],
[ 1, 2, 3, 9, 10, 11 ] ] )
```

In both cases, the crown is the subgraph induced by the vertices $\{1, 2, 4, 5, 7, 8, 10, 11\}$ and the core is induced by $\{3, 6, 9, 12\}$. Also in both cases the cyclic segmentations (partitions) of the crown and the core are $\{\{1, 2\}, \{4, 5\}, \{7, 8\}, \{10, 11\}\}$ and $\{\{3\}, \{6\}, \{9\}, \{12\}\}$ respectively. The number of segments s is specified by $s := \text{Length}(\text{NNFSList})$ which is 4 in these cases. The crown is isomorphic to $\text{BoxProduct}(\text{CycleGraph}(s), \text{CompleteGraph}(\text{rank}))$: All the crown segments are complete subgraphs and the vertices of cyclically consecutive segments are joined by a perfect matching. The adjacencies between crown and core vertices are simple to describe: Cyclically intercalate crown and core segments, making each core vertex adjacent to the vertices in the previous and the following crown segments. Hence in our examples vertex 3 is adjacent to vertices 1 and 2 (previous segment), but also 4 and 5 (following segment). Note that since the segmentations and intercalations are *cyclic*, we have that vertex 12 is adjacent to 10 and 11, but also to 1 and 2. Finally the edges between core vertices are as follows: first each core segment is a complete subgraph; the vertices within each core segment are linearly ordered and for vertex number t in segment number s there is a non-negative integer $\text{NNFSList}[s][t]$ which specifies, the *Number of Neighbors in the Following core Segment* for that vertex (hence the name *NNFSList*) (Since the vertices in core segments are linearly ordered, it is enough to specify the *number* of neighbors in the following segment and the *first* ones of those are selected as the neighbors). Hence in our two examples above, each core segment consists of exactly one vertex. In the first example each core segment is adjacent to no vertex in the following segment (e.g. 3 is not adjacent to 6) but in the second one, each core segment is adjacent to exactly one vertex in the following segment (e.g. 3 is adjacent to 6).

A more complicated example should be now mostly self-explanatory:

Example

```
gap> ClockworkGraph([2],[0,1,3],[0,1,1],[1]);
Graph( Category := SimpleGraphs, Order := 16, Size :=
59, Adjacencies := [ [ 2, 3, 4, 14, 16 ], [ 1, 3, 5, 15, 16 ],
[ 1, 2, 4, 5, 6, 7, 16 ], [ 1, 3, 5, 6, 7, 8, 9 ],
[ 2, 3, 4, 6, 7, 8, 10 ], [ 3, 4, 5, 7, 8, 9, 10 ],
[ 3, 4, 5, 6, 8, 9, 10, 11 ], [ 4, 5, 6, 7, 9, 10, 11, 12, 13 ],
[ 4, 6, 7, 8, 10, 11, 12, 13, 14 ],
[ 5, 6, 7, 8, 9, 11, 12, 13, 15 ], [ 7, 8, 9, 10, 12, 13, 14, 15 ],
[ 8, 9, 10, 11, 13, 14, 15, 16 ], [ 8, 9, 10, 11, 12, 14, 15, 16 ],
[ 1, 9, 11, 12, 13, 15, 16 ], [ 2, 10, 11, 12, 13, 14, 16 ],
[ 1, 2, 3, 12, 13, 14, 15 ] ] )
```

The crown and core segmentations are $\{\{1,2\},\{4,5\},\{9,10\},\{14,15\}\}$ and $\{\{3\},\{6,7,8\},\{11,12,13\},\{16\}\}$ respectively and the adjacencies specified by the *NNFSList* are: 3 is adjacent to 6 and 7; 6 is adjacent to none (in the following core segment); 7 is adjacent to 11; 8 to 11, 12 and 13; 11 to none; 12 to 16; 13 to 16 and 16 to 3.

When *rank* and/or *Perm* are specified, they have the following effects: *rank* (which must be at least 2) is the number of vertices in each crown segment, and *Perm* (which must belong to *SymmetricGroup(rank)*) specifies the perfect matching joining the vertices in the last crown segment with the vertices in the first crown segment: The *k*-th vertex in the last crown segment $k \in \{1, 2, \dots, rank\}$ is made adjacent to the *Perm(k)*-th vertex of the first crown segment.

A number of requisites are put forward in the literature for a graph to be a clockwork graph but this operation does not enforce those conditions, on the contrary, it tries to make sense of the data provided as much as possible. For instance *NNFSList* := [[2],[2],[2],[2]] would be inconsistent since there are not enough vertices in each core segment to provide for the required 2 neighbors. However, the result is just the same as with *NNFSList* := [[1],[1],[1],[1]]. The requisites that are mandatory are exactly these: the *rank* must be at least 2, *Perm* must belong to *SymmetricGroup(rank)*, *NNFSList* must be a list of lists of non-negative integers, and the number of segments (= Length(*NNFSList*)) must be at least 3. A call to *ClockworkGraph* which fails to conform to these requisites will produce an error.

Clockwork graphs have been very useful in constructing examples and counter-examples in clique graph theory. In particular, they have been used to construct examples of clique-periodic graphs of all possible periods [3], clique-divergent graphs of linear and polynomial growth rate [8][10], clique-convergent graphs whose period is not invariant under removal of dominated vertices [4], clique-convergent graphs which become clique-divergent by just gluing a 4-cycle to a vertex [5], rank-divergent graphs [13], etc.

B.1.25 ComplementGraph

▷ ComplementGraph(*G*)

(attribute)

Returns the new graph *H* such that $V(H) = V(G)$ and $xy \in E(H) \iff xy \notin E(G)$.

Example

```
gap> g:=ClawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1 ] ] )
gap> ComplementGraph(g);
```

```
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ ], [ 3, 4 ], [ 2, 4 ], [ 2, 3 ] ] )
```

B.1.26 CompleteBipartiteGraph

▷ CompleteBipartiteGraph(n , m) (function)

Returns the complete bipartite whose parts have order n and m respectively. This is the joint (Zykov sum) of two discrete graphs of order n and m .

Example

```
gap> CompleteBipartiteGraph(2,3);
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 3, 4, 5 ], [ 3, 4, 5 ], [ 1, 2 ], [ 1, 2 ],
[ 1, 2 ] ] )
```

B.1.27 CompleteGraph

▷ CompleteGraph(n) (function)

Returns the complete graph of order n . A complete graph is a graph where all vertices are connected to each other.

Example

```
gap> CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3 ] ] )
```

B.1.28 CompletelyParedGraph

▷ CompletelyParedGraph(G) (operation)

Returns the completely pared graph of G , which is obtained by repeatedly applying ParedGraph until no more dominated vertices remain.

Example

```
gap> g:=PathGraph(6);
Graph( Category := SimpleGraphs, Order := 6, Size :=
5, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4, 6 ],
[ 5 ] ] )
gap> CompletelyParedGraph(g);
Graph( Category := SimpleGraphs, Order := 1, Size :=
0, Adjacencies := [ [ ] ] )
```

B.1.29 CompleteMultipartiteGraph

▷ CompleteMultipartiteGraph($n1$, $n2$) (function)

Returns the complete multipartite graph where the orders of the parts are $n1$, $n2$, ... It is also the Zykov sum of discrete graphs of order $n1$, $n2$, ...

Example

```
gap> CompleteMultipartiteGraph(2,2,2);
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ], [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

B.1.30 CompletesOfGivenOrder

▷ CompletesOfGivenOrder(G , ord)

(operation)

Returns the list of vertex sets of all complete subgraphs of order ord of G .

Example

```
gap> g:=SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size :=
14, Adjacencies := [ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ],
[ 2, 3, 5, 6, 8 ], [ 4, 6 ], [ 2, 4, 5, 7, 8 ], [ 6, 8 ],
[ 1, 2, 4, 6, 7 ] ] )
gap> CompletesOfGivenOrder(g,3);
[ [ 1, 2, 8 ], [ 2, 3, 4 ], [ 2, 4, 6 ], [ 2, 4, 8 ], [ 2, 6, 8 ],
[ 4, 5, 6 ], [ 4, 6, 8 ], [ 6, 7, 8 ] ]
gap> CompletesOfGivenOrder(g,4);
[ [ 2, 4, 6, 8 ] ]
```

B.1.31 Composition

▷ Composition(G , H)

(operation)

Returns the composition $G[H]$ of two graphs G and H .

A composition of graphs is obtained by calculating the GraphSum of G with $Order(G)$ copies of H , $G[H] = \text{GraphSum}(G, [H, \dots, H])$.

Example

```
gap> g:=CycleGraph(4);;h:=DiscreteGraph(2);;
gap> Composition(g,h);
Graph( Category := SimpleGraphs, Order := 8, Size :=
16, Adjacencies := [ [ 3, 4, 7, 8 ], [ 3, 4, 7, 8 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ], [ 3, 4, 7, 8 ], [ 3, 4, 7, 8 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ] ] )
```

B.1.32 Cone

▷ Cone(G)

(operation)

Returns the cone of graph G . The cone of G is the graph obtained from G by adding a new vertex which is adjacent to every vertex of G . The new vertex is the first one in the new graph.

Example

```
gap> Cone(CycleGraph(4));
Graph( Category := SimpleGraphs, Order := 5, Size :=
8, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 5 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 2, 4 ] ] )
```


B.1.33 ConnectedComponents

▷ `ConnectedComponents(G)` (attribute)

Returns the connected components of *G*.

B.1.34 ConnectedGraphsOfGivenOrder

▷ `ConnectedGraphsOfGivenOrder(n)` (operation)

Returns the list of all connected graphs of order *n* (upto isomorphism). This operation uses Brendan McKay's data published here: <https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html>.

These data are included with the YAGS distribution in its data directory. Hence this operation simply reads the corresponding file in that directory using `ImportGraph6(Filename)`. Therefore, the integer *n* must be in the range from 1 upto 9. Data for graphs on 10 vertices is also available, but not included with YAGS, it may not be practical to use that data, but if you would like to try, all you have to do is to copy (and to uncompress) the corresponding file into the directory `YAGS-DIR/data`.

Example

```
gap> ConnectedGraphsOfGivenOrder(3);
[ Graph( Category := SimpleGraphs, Order := 3, Size :=
  2, Adjacencies := [ [ 3 ], [ 3 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size :=
  3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] ) ]
gap> ConnectedGraphsOfGivenOrder(4);
[ Graph( Category := SimpleGraphs, Order := 4, Size :=
  3, Adjacencies := [ [ 4 ], [ 4 ], [ 4 ], [ 1, 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size :=
  3, Adjacencies := [ [ 3, 4 ], [ 4 ], [ 1 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size :=
  4, Adjacencies := [ [ 3, 4 ], [ 4 ], [ 1, 4 ], [ 1, 2, 3 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size :=
  4, Adjacencies := [ [ 3, 4 ], [ 3, 4 ], [ 1, 2 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 4, Size :=
  5, Adjacencies := [ [ 3, 4 ], [ 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ]
  ] ), Graph( Category := SimpleGraphs, Order := 4, Size :=
  6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
  [ 1, 2, 3 ] ] ) ]
gap> Length(ConnectedGraphsOfGivenOrder(9));
261080
gap> ConnectedGraphsOfGivenOrder(10);
#W Unreadable File: /opt/gap4r7/pkg/yags/data/graph10c.g6
fail
```

B.1.35 Coordinates

▷ `Coordinates(G)` (operation)

Gets the coordinates of the vertices of *G*, which are used to draw *G* by `Draw(G)`. If the coordinates have not been previously set, `Coordinates` returns *fail*.

Example

```
gap> g:=CycleGraph(4);
gap> Coordinates(g);
fail
gap> SetCoordinates(g,[[ -10,-10 ],[-10,20],[20,-10 ], [20,20]]);
gap> Coordinates(g);
[ [ -10, -10 ], [ -10, 20 ], [ 20, -10 ], [ 20, 20 ] ]
```

B.1.36 CopyGraph

▷ CopyGraph(G)

(operation)

Returns a fresh copy of graph G . Only the order and adjacency information is copied, all other known attributes of G are not. Mainly used to transform a graph from one category to another. The new graph will be forced to comply with the TargetGraphCategory.

Example

```
gap> g:=CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3 ] ] )
gap> g1:=CopyGraph(g:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 3, 4 ], [ 4 ], [ ] ] )
gap> CopyGraph(g1:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3 ] ] )
```

B.1.37 Cube

▷ Cube

(global variable)

The 1-skeleton of Plato's cube.

Example

```
gap> Cube;
Graph( Category := SimpleGraphs, Order := 8, Size :=
12, Adjacencies := [ [ 2, 3, 5 ], [ 1, 4, 6 ], [ 1, 4, 7 ],
[ 2, 3, 8 ], [ 1, 6, 7 ], [ 2, 5, 8 ], [ 3, 5, 8 ], [ 4, 6, 7 ] ] )
```

B.1.38 CubeGraph

▷ CubeGraph(n)

(function)

Returns the hypercube of dimension n . This is the box product (cartesian product) of n copies of K_2 (an edge).

Example

```
gap> CubeGraph(3);
Graph( Category := SimpleGraphs, Order := 8, Size :=
12, Adjacencies := [ [ 2, 3, 5 ], [ 1, 4, 6 ], [ 1, 4, 7 ],
[ 2, 3, 8 ], [ 1, 6, 7 ], [ 2, 5, 8 ], [ 3, 5, 8 ], [ 4, 6, 7 ] ] )
```

B.1.39 CycleGraph

▷ CycleGraph(*n*) (function)

Returns the cyclic graph on *n* vertices.

Example

```
gap> CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ]
] )
```

B.1.40 CylinderGraph

▷ CylinderGraph(*b*, *h*) (function)

Returns a cylinder of base *b* and height *h*. The order of this graph is $b(h+1)$ and it is constructed by taking $h+1$ copies of the cyclic graph on *b* vertices, ordering these cycles linearly and then joining consecutive cycles by a zigzagging $(2b)$ -cycle. This graph is a triangulation of the cylinder where all internal vertices are of degree 6 and the border vertices are of degree 4.

Example

```
gap> g:=CylinderGraph(4,1);
Graph( Category := SimpleGraphs, Order := 8, Size :=
16, Adjacencies := [ [ 2, 4, 5, 6 ], [ 1, 3, 6, 7 ], [ 2, 4, 7, 8 ],
[ 1, 3, 5, 8 ], [ 1, 4, 6, 8 ], [ 1, 2, 5, 7 ], [ 2, 3, 6, 8 ],
[ 3, 4, 5, 7 ] ] )
gap> g:=CylinderGraph(4,2);
Graph( Category := SimpleGraphs, Order := 12, Size :=
28, Adjacencies := [ [ 2, 4, 5, 6 ], [ 1, 3, 6, 7 ], [ 2, 4, 7, 8 ],
[ 1, 3, 5, 8 ], [ 1, 4, 6, 8, 9, 10 ], [ 1, 2, 5, 7, 10, 11 ],
[ 2, 3, 6, 8, 11, 12 ], [ 3, 4, 5, 7, 9, 12 ], [ 5, 8, 10, 12 ],
[ 5, 6, 9, 11 ], [ 6, 7, 10, 12 ], [ 7, 8, 9, 11 ] ] )
```

B.1.41 DartGraph

▷ DartGraph (global variable)

A diamond with a pendant vertex and maximum degree 4.

Example

```
gap> DartGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 2 ], [ 1, 3, 4, 5 ], [ 2, 4, 5 ], [ 2, 3 ],
[ 2, 3 ] ] )
```

B.1.42 DeclareQtifyProperty

▷ DeclareQtifyProperty(*Name*, *Filter*) (function)

For internal use.

Declares a YAGS quantifiable property named *Name* for filter *Filter*. This in turns, declares a boolean GAP property *Name* and an integer GAP attribute *QtifyName*.

The user must provide the method *Name(Obj, qtfy)*. If *qtfy* is false, the method must return a boolean indicating whether the property holds, otherwise, the method must return a non-negative integer quantifying how far is the object from satisfying the property. In the latter case, returning 0 actually means that the object does satisfy the property.

Example

```
gap> DeclareQtifyProperty("Is2Regular",Graphs);
gap> InstallMethod(Is2Regular,"for graphs",true,[Graphs,IsBool],0,
> function(G,qtfy)
>   local x,count;
>   count:=0;
>   for x in Vertices(G) do
>     if VertexDegree(G,x)<> 2 then
>       if not qtfy then
>         return false;
>       fi;
>       count:=count+1;
>     fi;
>   od;
>   if not qtfy then return true; fi;
>   return count;
> end);
gap> Is2Regular(CycleGraph(4));
true
gap> QtfyIs2Regular(CycleGraph(4));
0
gap> Is2Regular(DiamondGraph);
false
gap> QtfyIs2Regular(DiamondGraph);
2
```

B.1.43 Diameter

▷ Diameter(*G*)

(attribute)

Returns the maximum among the distances between pairs of vertices of *G*.

Example

```
gap> g:=CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ]
] )
gap> Diameter(g);
2
```

B.1.44 DiamondGraph

▷ DiamondGraph

(global variable)

The graph on 4 vertices and 5 edges.

Example

```
gap> DiamondGraph;
Graph( Category := SimpleGraphs, Order := 4, Size :=
5, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3 ], [ 1, 2, 4 ], [ 1, 3 ] ] )
```

B.1.45 DiscreteGraph

▷ DiscreteGraph(n) (function)

Returns the discrete graph of order n . A discrete graph is a graph without edges.

Example

```
gap> DiscreteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
0, Adjacencies := [ [ ], [ ], [ ], [ ] ] )
```

B.1.46 DisjointUnion

▷ DisjointUnion(G, H) (operation)

Returns the disjoint union of two graphs G and H , $G \dot{\cup} H$.

Example

```
gap> g:=PathGraph(3);h:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> DisjointUnion(g,h);
Graph( Category := SimpleGraphs, Order := 5, Size :=
3, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ], [ 5 ], [ 4 ] ] )
```

B.1.47 Distance

▷ Distance(G, x, y) (operation)

Returns the length of a minimal path connecting x to y in G .

Example

```
gap> Distance(CycleGraph(5),1,3);
2
gap> Distance(CycleGraph(5),1,5);
1
```

B.1.48 Distances

▷ Distances(G, A, B) (operation)

Given two lists of vertices A, B of a graph G , Distances returns the list of distances for every pair in the cartesian product of A and B . The order of the vertices in lists A and B affects the order of the list of distances returned.

Example

```
gap> g:=CycleGraph(5);
gap> Distances(g, [1,3], [2,4]);
[ 1, 2, 1, 1 ]
gap> Distances(g, [3,1], [2,4]);
[ 1, 1, 1, 2 ]
```

B.1.49 DistanceGraph▷ DistanceGraph(G , $Dist$)

(operation)

Given a graph G and list of distances $Dist$, DistanceGraph returns the new graph constructed on the vertices of G where two vertices are adjacent iff the distance (in G) between them belongs to the list $Dist$.

Example

```
gap> g:=CycleGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ]
] )
gap> DistanceGraph(g,[2]);
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 3, 4 ], [ 4, 5 ], [ 1, 5 ], [ 1, 2 ], [ 2, 3 ]
] )
gap> DistanceGraph(g,[1,2]);
Graph( Category := SimpleGraphs, Order := 5, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 5 ], [ 1, 2, 4, 5 ],
[ 1, 2, 3, 5 ], [ 1, 2, 3, 4 ] ] )
```

B.1.50 DistanceMatrix▷ DistanceMatrix(G)

(attribute)

Returns the distance matrix D of a graph G : $D[x][y]$ is the distance in G from vertex x to vertex y . The matrix may be asymmetric if the graph is not simple. An infinite entry in the matrix means that there is no path between the vertices. Floyd's algorithm is used to compute the matrix.

Example

```
gap> g:=PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
gap> Display(DistanceMatrix(g));
[ [ 0, 1, 2, 3 ],
[ 1, 0, 1, 2 ],
[ 2, 1, 0, 1 ],
[ 3, 2, 1, 0 ] ]
gap> g:=PathGraph(4:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2 ], [ 3 ], [ 4 ], [ ] ] )
gap> Display(DistanceMatrix(g));
[ [ 0, 1, 2, 3 ],
[ infinity, 0, 1, 2 ],
```

[infinity,	infinity,	0,	1],
[infinity,	infinity,	infinity,	0]]

B.1.51 DistanceSet

▷ DistanceSet(G , A , B)

(operation)

Given two subsets of vertices A , B of a graph G , DistanceSet returns the set of distances for every pair in the cartesian product of A and B .

Example

```
gap> g:=CycleGraph(5);
gap> DistanceSet(g, [1,3], [2,4]);
[ 1, 2 ]
```

B.1.52 Dodecahedron

▷ Dodecahedron

(global variable)

The 1-skeleton of Plato's Dodecahedron.

Example

```
gap> Dodecahedron;
Graph( Category := SimpleGraphs, Order := 20, Size :=
30, Adjacencies := [ [ 2, 5, 6 ], [ 1, 3, 7 ], [ 2, 4, 8 ],
[ 3, 5, 9 ], [ 1, 4, 10 ], [ 1, 11, 15 ], [ 2, 11, 12 ],
[ 3, 12, 13 ], [ 4, 13, 14 ], [ 5, 14, 15 ], [ 6, 7, 16 ],
[ 7, 8, 17 ], [ 8, 9, 18 ], [ 9, 10, 19 ], [ 6, 10, 20 ],
[ 11, 17, 20 ], [ 12, 16, 18 ], [ 13, 17, 19 ], [ 14, 18, 20 ],
[ 15, 16, 19 ] ] )
```

B.1.53 DominatedVertices

▷ DominatedVertices(G)

(attribute)

Returns the set of dominated vertices of G .

A vertex x is dominated by another vertex y when the closed neighborhood of x is contained in that of y . However, when there are twin vertices (mutually dominated vertices), exactly one of them (in each equivalent class of mutually dominated vertices) does not appear in the returned set.

Example

```
gap> g1:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> DominatedVertices(g1);
[ 1, 3 ]
gap> g2:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> DominatedVertices(g2);
[ 2 ]
```

B.1.54 DominoGraph

▷ DominoGraph

(global variable)

Two squares glued by an edge.

Example

```
gap> DominoGraph;
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 4, 6 ], [ 1, 5 ] ] )
```

B.1.55 Draw

▷ Draw(*G*)

(operation)

Takes a graph *G* and makes a drawing of it in a separate window. The user can then view and modify the drawing and finally save the vertex coordinates of the drawing into the graph *G*.

Within the separate window, type *h* to toggle on/off the help menu. Besides the keyboard commands indicated in the help menu, the user may also move vertices (by dragging them), move the whole drawing (by dragging the background) and scale the drawing (by using the mouse wheel).

Example

```
gap> Coordinates(Icosahedron);
fail
gap> Draw(Icosahedron);
gap> Coordinates(Icosahedron);
[ [ 29, -107 ], [ 65, -239 ], [ 240, -62 ], [ 78, 79 ], [ -107, 28 ],
[ -174, -176 ], [ -65, 239 ], [ -239, 62 ], [ -78, -79 ], [ 107, -28 ],
[ 174, 176 ], [ -29, 107 ] ]
```

Draw() uses an external java program (included with YAGS) and hence, may not work on some platforms.

Current version has been tested successfully on GNU/Linux, Mac OS X and Windows7. For other platforms (specially 32-bit platforms), you should probably (at least) set up correctly the variables YAGSInfo.Draw.prog and YAGSInfo.Draw.opts. The former is a string representing the external binary program path and name; the latter is a list of strings representing the required command line options. Java binaries are provided for 32 and 64 bit versions of GNU/Linux (which also works for Mac OS X) and of MS Windows.

Example

```
gap> YAGSInfo.Draw.prog; YAGSInfo.Draw.opts;
"/opt/gap4r7/pkg/yags/bin/draw/application.linux64/draw"
[ ]
```

B.1.56 DumpObject

▷ DumpObject(*Obj*)

(operation)

Dumps all information available for object *Obj*. This information includes to which categories it belongs as well as its type and hashing information used by GAP.

Example

```
gap> DumpObject( true );
Object( TypeObj := NewType( NewFamily( "BooleanFamily", [ 11 ], [ 11 ] ),
[ 11, 34 ] ), Categories := [ "IS_BOOL" ] )
```

B.1.57 EasyExec

- ▷ EasyExec(*Dir*, *ProgName*, *InString*) (operation)
 ▷ EasyExec(*ProgName*, *InString*) (operation)

Calls external program *ProgName* located in directory *Dir*, feeding it with *InString* as input and returning the output of the external program as a string. *Dir* must be a directory object or a list of directory objects. If *Dir* is not provided, *ProgName* must be in the system's binary PATH. fail is returned if the program could not be located.

Example

```
gap> s:=EasyExec("date","");;
gap> s;
"Sun Nov 9 10:36:16 CST 2014\n"
gap> s:=EasyExec("sort","4\n2\n3\n1");;
gap> s;
"1\n2\n3\n4\n"
```

Currently, this operation is not working on MS Windows.

B.1.58 Eccentricity

- ▷ Eccentricity(*G*, *x*) (function)

Returns the distance from a vertex *x* in graph *G* to its most distant vertex in *G*.

Example

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> Eccentricity(g,1);
4
gap> Eccentricity(g,3);
2
```

B.1.59 Edges

- ▷ Edges(*G*) (operation)

Returns the list of edges of graph *G* in the case of SimpleGraphs.

Example

```
gap> g1:=CompleteGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size :=
3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] )
gap> Edges(g1);
[ [ 1, 2 ], [ 1, 3 ], [ 2, 3 ] ]
```

In the case of `UndirectedGraphs`, it also returns the loops. While in the other categories, `Edges` actually does not return the edges, but the loops and arrows of G .

Example

```
gap> g2:=CompleteGraph(3:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 3, Size :=
6, Adjacencies := [ [ 1, 2, 3 ], [ 1, 2, 3 ], [ 1, 2, 3 ] ] )
gap> Edges(g2);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 2, 2 ], [ 2, 3 ], [ 3, 3 ] ]
gap> g3:=CompleteGraph(3:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 9, Adjacencies :=
[ [ 1, 2, 3 ], [ 1, 2, 3 ], [ 1, 2, 3 ] ] )
gap> Edges(g3);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 2, 1 ], [ 2, 2 ], [ 2, 3 ],
[ 3, 1 ], [ 3, 2 ], [ 3, 3 ] ]
```

B.1.60 EquivalenceRepresentatives

▷ `EquivalenceRepresentatives(L, Equiv)` (operation)

Returns a sublist of L , which is a complete list of representatives of L under the equivalent relation *Equiv*.

Example

```
gap> L:=[10,2,6,5,9,7,3,1,4,8];
[ 10, 2, 6, 5, 9, 7, 3, 1, 4, 8 ]
gap> EquivalenceRepresentatives(L,function(x,y) return (x mod 4)=(y mod 4); end);
[ 10, 5, 7, 4 ]
gap> L:=Links(SnubDisphenoid);Length(L);
8
gap> L:=EquivalenceRepresentatives(L,IsIsomorphicGraph);Length(L);
2
gap> L;
[ Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ],
[ 1, 4 ] ] ), Graph( Category := SimpleGraphs, Order :=
4, Size := 4, Adjacencies := [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ],
[ 2, 3 ] ] ) ]
```

B.1.61 FanGraph

▷ `FanGraph(n)` (function)

Returns the n -Fan: The join of a vertex and a $(n+1)$ -path.

Example

```
gap> FanGraph(4);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 2, 3, 4, 5, 6 ], [ 1, 3 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 4, 6 ], [ 1, 5 ] ] )
```

B.1.62 FishGraph

▷ FishGraph

(global variable)

A square and a triangle glued by a vertex.

Example

```
gap> FishGraph;
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 3, 4, 6 ], [ 1, 3 ], [ 1, 2 ], [ 1, 5 ],
[ 4, 6 ], [ 1, 5 ] ] )
```

B.1.63 GemGraph

▷ GemGraph

(global variable)

The 3-Fan graph.

Example

```
gap> GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
7, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 4 ] ] )
```

B.1.64 Girth

▷ Girth(G)

(attribute)

Returns the length of the minimum induced cycle in G . At this time, this works only when G belongs to the graph categories SimpleGraphs or UndirectedGraphs. If G has loops, its girth is 1 by definition.

Example

```
gap> Girth(Octahedron);
3
gap> Girth(PetersenGraph);
5
gap> Girth(Cube);
4
gap> Girth(PathGraph(5));
infinity
gap> g:=AddEdges(CycleGraph(4),[[3,3]]:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 4, Size :=
5, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 3, 4 ], [ 1, 3 ] ] )
gap> Girth(g);
1
```

B.1.65 Graph

▷ Graph(Rec)

(operation)

Returns a new graph created from the record Rec . The record must provide the field *Category* and either the field *Adjacencies* or the field *AdjMatrix*.

Example

```
gap> Graph(rec(Category:=SimpleGraphs,Adjacencies:=[[2],[1]]));
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> Graph(rec(Category:=SimpleGraphs,AdjMatrix:[[false, true],[true, false]]));
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
```

Its main purpose is to import graphs from files, which could have been previously exported using `PrintTo`.

Example

```
gap> g:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> PrintTo("aux.g", "h1:=", g, ";");
gap> Read("aux.g");
gap> h1;
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
```

B.1.66 GraphAttributeStatistics

▷ `GraphAttributeStatistics(OrderList, ProbList, Attribute)`

(function)

Returns statistics for graph attribute *Attribute*. For each of the orders n in *OrderList* and for each of the probabilities p in *ProbList* this function generates 100 random graphs of order n and edge probability p and then evaluates the graph attribute *Attribute* on each of them. The function then returns statistical data on these experiments. The form in which the statistical data is reported depend on a number of issues and is best explained by examples.

First let us consider the case where *Attribute* is a Boolean attribute (always returns `true` or `false`) and where *OrderList* and *ProbList* consist of a unique value. In this case, the respective lists may be replaced by the corresponding unique values on invocation:

Example

```
gap> GraphAttributeStatistics(10,1/2,IsCliqueHelly);
32
```

This tells us that 43 of the 100 examined random graphs resulted to be clique-Helly; The random sample was constructed using graphs of order 10 and edge probability $1/2$.

Now we can specify a list of probabilities to be examined:

Example

```
gap> GraphAttributeStatistics(10,1/10*[1..9],IsCliqueHelly);
[ 100, 100, 94, 63, 34, 16, 30, 76, 95 ]
```

The last example tells us that, for graphs on 10 vertices, the property `IsCliqueHelly` is least probable to be true for graphs with edge probabilities $5/10$ $6/10$ and $7/10$, being $6/10$ the probability that reaches the minimum in the random sample. Note that the 36 in the previous example does not match the 43 in the first one, this is to be expected as the statistics are compiled from a random sample of graphs. Also, note that in the previous example, 900 random graphs were generated and examined.

We can also specify a list of orders to consider:

Example

```
gap> GraphAttributeStatistics([10,12..20],1/10*[1..9],IsCliqueHelly);
[ [ 100, 100, 92, 62, 37, 16, 36, 70, 97 ],
  [ 100, 99, 83, 34, 8, 1, 19, 68, 97 ],
  [ 100, 96, 54, 4, 2, 0, 6, 54, 98 ],
  [ 100, 89, 26, 2, 0, 0, 9, 42, 96 ],
  [ 100, 70, 13, 1, 0, 0, 6, 24, 94 ],
  [ 99, 70, 5, 0, 0, 0, 4, 22, 92 ] ]
gap> Display(last);
[ [ 100, 100, 92, 62, 37, 16, 36, 70, 97 ],
  [ 100, 99, 83, 34, 8, 1, 19, 68, 97 ],
  [ 100, 96, 54, 4, 2, 0, 6, 54, 98 ],
  [ 100, 89, 26, 2, 0, 0, 9, 42, 96 ],
  [ 100, 70, 13, 1, 0, 0, 6, 24, 94 ],
  [ 99, 70, 5, 0, 0, 0, 4, 22, 92 ] ]
```

Which tell us that the observed bimodal distribution is even more pronounced when the order of the graphs considered grows.

In the case of a non-Boolean attribute `GraphAttributeStatistics()` reports the values that *Attribute* took on the sample as well as the number of times that each of these values were obtained:

Example

```
gap> GraphAttributeStatistics(10,1/2,Diameter);
[ [ 2, 34 ], [ 3, 59 ], [ 4, 5 ], [ 5, 1 ], [ infinity, 1 ] ]
```

The returned statistics mean that among the 100 generated random graphs on 10 vertices with edge probability 1/2, there were 26 graphs with diameter 2, 60 graphs of diameter 3, 8 of 4, 1 of 6 and 5 graphs which were not connected.

Now it should be evident the format of the returned statistics when we specify a list of probabilities and/or a list of orders to be considered for a non-Boolean Attribute:

Example

```
gap> GraphAttributeStatistics(10,1/5*[1..4],Diameter);
[ [ [ 3, 1 ], [ 4, 7 ], [ 5, 8 ], [ 6, 6 ], [ infinity, 78 ] ],
  [ [ 2, 6 ], [ 3, 55 ], [ 4, 21 ], [ 5, 1 ], [ 6, 1 ],
    [ infinity, 16 ] ], [ [ 2, 74 ], [ 3, 25 ], [ 4, 1 ] ],
  [ [ 2, 100 ] ] ]
gap> GraphAttributeStatistics([10,12,14],1/5*[1..4],Diameter);
[ [ [ [ 3, 2 ], [ 4, 8 ], [ 5, 11 ], [ 6, 5 ], [ 7, 1 ],
      [ infinity, 73 ] ],
  [ [ 2, 6 ], [ 3, 56 ], [ 4, 23 ], [ 5, 7 ], [ infinity, 8 ] ],
  [ [ 2, 72 ], [ 3, 27 ], [ infinity, 1 ] ],
  [ [ 2, 99 ], [ 3, 1 ] ] ],
  [
    [ [ 3, 4 ], [ 4, 13 ], [ 5, 10 ], [ 6, 6 ], [ 7, 3 ],
      [ infinity, 64 ] ],
    [ [ 2, 7 ], [ 3, 69 ], [ 4, 17 ], [ infinity, 7 ] ],
    [ [ 2, 76 ], [ 3, 24 ] ], [ [ 2, 100 ] ] ],
  [ [ [ 4, 12 ], [ 5, 16 ], [ 6, 7 ], [ 7, 3 ], [ infinity, 62 ] ],
    [ [ 2, 8 ], [ 3, 86 ], [ 4, 4 ], [ infinity, 2 ] ],
    [ [ 2, 86 ], [ 3, 14 ] ], [ [ 2, 100 ] ] ] ]
```

B.1.67 Graph6ToGraph

▷ `Graph6ToGraph(String)`

(operation)

Returns the graph represented by *String* which is encoded using Brendan McKay's graph6 format. This operation allows us to read data in databases which use this format. Several such databases can be found here: <https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html>.

The graph6 format is described here:

<https://cs.anu.edu.au/people/Brendan.McKay/data/formats.txt>.

Example

```
gap> Graph6ToGraph("D?{");
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 5 ], [ 5 ], [ 5 ], [ 5 ], [ 1, 2, 3, 4 ] ] )
gap> Graph6ToGraph("FUzvW");
Graph( Category := SimpleGraphs, Order := 7, Size :=
15, Adjacencies := [ [ 3, 4, 5, 6, 7 ], [ 4, 5, 6, 7 ],
[ 1, 5, 6, 7 ], [ 1, 2, 6 ], [ 1, 2, 3, 7 ], [ 1, 2, 3, 4, 7 ],
[ 1, 2, 3, 5, 6 ] ] )
gap> Graph6ToGraph("HUzv~z");
Graph( Category := SimpleGraphs, Order := 9, Size :=
29, Adjacencies := [ [ 3, 4, 5, 6, 7, 8, 9 ], [ 4, 5, 6, 7, 8, 9 ],
[ 1, 5, 6, 7, 8, 9 ], [ 1, 2, 6, 7, 8, 9 ], [ 1, 2, 3, 7, 8, 9 ],
[ 1, 2, 3, 4, 7, 8, 9 ], [ 1, 2, 3, 4, 5, 6, 9 ],
[ 1, 2, 3, 4, 5, 6 ], [ 1, 2, 3, 4, 5, 6, 7 ] ] )
```

See also `ImportGraph6(Filename)`.

B.1.68 GraphByAdjacencies

▷ `GraphByAdjacencies(AdjList)`

(function)

Returns a new graph having *AdjList* as its list of adjacencies. The order of the created graph is `Length(A)`, and the set of neighbors of vertex x is $A[x]$.

Example

```
gap> GraphByAdjacencies([[2],[1,3],[2]]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

Note, however, that the graph is forced to comply with the `TargetGraphCategory`.

Example

```
gap> GraphByAdjacencies([[1,2,3],[],[ ]]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2, 3 ], [ 1 ], [ 1 ] ] )
```

B.1.69 GraphByAdjMatrix

▷ `GraphByAdjMatrix(Mat)`

(function)

Returns a new graph created from an adjacency matrix *Mat*. The matrix *Mat* must be a square boolean matrix.

Example

```
gap> m:= [ [ false, true, false ], [ true, false, true ], [ false, true, false ] ];;
gap> g:=GraphByAdjMatrix(m);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> AdjMatrix(g);
[ [ false, true, false ], [ true, false, true ],
[ false, true, false ] ]
```

Note, however, that the graph is forced to comply with the TargetGraphCategory.

Example

```
gap> m:= [ [ true, true ], [ false, false ] ];;
gap> g:=GraphByAdjMatrix(m);
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> AdjMatrix(g);
[ [ false, true ], [ true, false ] ]
```

B.1.70 GraphByCompleteCover

▷ GraphByCompleteCover(*Cover*)

(function)

Returns the minimal graph where the elements of *Cover* are (the vertex sets of) complete sub-graphs.

Example

```
gap> GraphByCompleteCover([[1,2,3,4],[4,6,7]]);
Graph( Category := SimpleGraphs, Order := 7, Size :=
9, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3, 6, 7 ], [ ], [ 4, 7 ], [ 4, 6 ] ] )
```

B.1.71 GraphByEdges

▷ GraphByEdges(*L*)

(function)

Returns the minimal graph such that the pairs in *L* are edges.

Example

```
gap> GraphByEdges([[1,2],[1,3],[1,4],[4,5]]);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2, 3, 4 ], [ 1 ], [ 1 ], [ 1, 5 ], [ 4 ] ] )
```

The vertices of the constructed graph range from 1 to the maximum of the numbers appearing in *L*.

Example

```
gap> GraphByEdges([[4,3],[4,5]]);
Graph( Category := SimpleGraphs, Order := 5, Size :=
2, Adjacencies := [ [ ], [ ], [ 4 ], [ 3, 5 ], [ 4 ] ] )
```

Note that GraphByWalks has an even greater functionality.

B.1.72 GraphByRelation

- ▷ `GraphByRelation(V, Rel)` (function)
 ▷ `GraphByRelation(n, Rel)` (function)

Returns a new graph created from a set of vertices *V* and a binary relation *Rel*, where $x \sim y$ iff *Rel*(*x*,*y*)=true. In the second form, *n* is an integer and *V* is assumed to be $\{1, 2, \dots, n\}$.

Example

```
gap> Rel:=function(x,y) return Intersection(x,y)<>[]; end;;
gap> GraphByRelation([[1,2,3],[3,4,5],[5,6,7]],Rel);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> GraphByRelation(8,function(x,y) return AbsInt(x-y)<=2; end);
Graph( Category := SimpleGraphs, Order := 8, Size :=
13, Adjacencies := [ [ 2, 3 ], [ 1, 3, 4 ], [ 1, 2, 4, 5 ],
[ 2, 3, 5, 6 ], [ 3, 4, 6, 7 ], [ 4, 5, 7, 8 ], [ 5, 6, 8 ],
[ 6, 7 ] ] )
```

B.1.73 GraphByWalks

- ▷ `GraphByWalks(Walk1, Walk2, ...)` (function)

Returns the minimal graph such that *Walk1*, *Walk2*, etc are Walks.

Example

```
gap> GraphByWalks([1,2,3,4,1],[1,5,6]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
6, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ],
[ 1, 6 ], [ 5 ] ] )
```

Walks can be *nested*, which greatly improves the versatility of this function.

Example

```
gap> GraphByWalks([1,[2,3,4],5],[5,6]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 5 ], [ 1, 2, 4, 5 ],
[ 1, 3, 5 ], [ 2, 3, 4, 6 ], [ 5 ] ] )
```

The vertices in the constructed graph range from 1 to the maximum of the numbers appearing in *Walk1*, *Walk2*, ... etc.

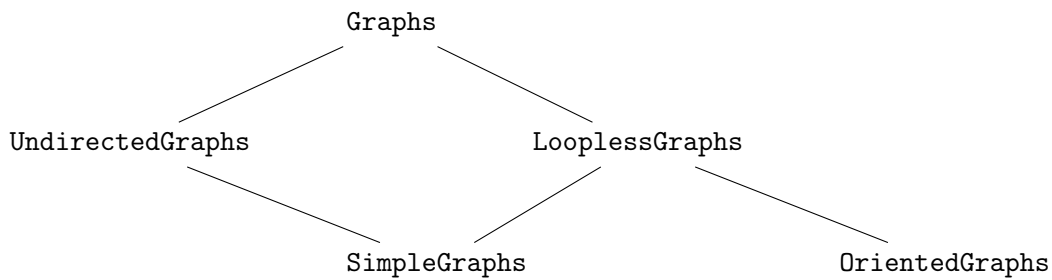
Example

```
gap> GraphByWalks([4,2],[3,6]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
2, Adjacencies := [ [ ], [ 4 ], [ 6 ], [ 2 ], [ ], [ 3 ] ] )
```

B.1.74 GraphCategory

- ▷ `GraphCategory([G, ...])` (function)

For internal use. Returns the minimal common category to a list of graphs. If the list of graphs is empty, the default category is returned. The partial order (by inclusion) among graph categories is as follows:



Example

```

gap> g1:=CompleteGraph(2:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> g2:=CompleteGraph(2:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ ] ] )
gap> g3:=CompleteGraph(2:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 2, Size :=
3, Adjacencies := [ [ 1, 2 ], [ 1, 2 ] ] )
gap> GraphCategory([g1,g2,g3]);
<Category "Graphs">
gap> GraphCategory([g1,g2]);
<Category "LooplessGraphs">
gap> GraphCategory([g1,g3]);
<Category "UndirectedGraphs">

```

B.1.75 Graphs

▷ Graphs(G)

(function)

Graphs is the most general graph category in YAGS. This category contains all graphs that can be represented in YAGS. A graph in this category may contain loops, arrows and edges (which in YAGS are exactly the same as two opposite arrows between some pair of vertices). This graph category has no parent category.

Example

```

gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )

```

B.1.76 GraphsOfGivenOrder

▷ GraphsOfGivenOrder(n)

(operation)

Returns the list of all graphs of order n (upto isomorphism). This operation uses Brendan McKay's data published here: <https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html>.

These data are included with the YAGS distribution in its data directory. Hence this operation simply reads the corresponding file in that directory using `ImportGraph6(Filename)`. Therefore,

the integer n must be in the range from 1 upto 9. Data for graphs on 10 vertices is also available, but not included with YAGS, it may not be practical to use that data, but if you would like to try, all you have to do is to copy (and to uncompress) the corresponding file into the directory *YAGS-DIR/data*.

Example

```
gap> GraphsOfGivenOrder(2);
[ Graph( Category := SimpleGraphs, Order := 2, Size :=
  0, Adjacencies := [ [ ], [ ] ] ),
  Graph( Category := SimpleGraphs, Order := 2, Size :=
  1, Adjacencies := [ [ 2 ], [ 1 ] ] ) ]
gap> GraphsOfGivenOrder(3);
[ Graph( Category := SimpleGraphs, Order := 3, Size :=
  0, Adjacencies := [ [ ], [ ], [ ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size :=
  1, Adjacencies := [ [ 3 ], [ ], [ 1 ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size :=
  2, Adjacencies := [ [ 3 ], [ 3 ], [ 1, 2 ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size :=
  3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] ) ]
gap> Length(GraphsOfGivenOrder(9));
274668
gap> GraphsOfGivenOrder(10);
#W Unreadable File: /opt/gap4r7/pkg/yags/data/graph10.g6
fail
```

B.1.77 GraphSum

▷ GraphSum(G , L)

(operation)

Returns the lexicographic sum of a list of graphs L over a graph G .

The lexicographic sum is computed as follows:

Given G , with $Order(G) = n$ and a list of n graphs $L = [G_1, \dots, G_n]$, We take the disjoint union of G_1, G_2, \dots, G_n and then we add all the edges between G_i and G_j whenever $[i, j]$ is an edge of G .

If L contains holes, the trivial graph is used in place.

Example

```
gap> t:=TrivialGraph;; g:=CycleGraph(4);
gap> GraphSum(PathGraph(3),[t,g,t]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
  12, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ],
    [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ], [ 2, 3, 4, 5 ] ] )
gap> GraphSum(PathGraph(3),[g]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
  12, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ],
    [ 1, 3, 5, 6 ], [ 1, 2, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

B.1.78 GraphToRaw

▷ GraphToRaw($FileName$, G)

(operation)

Converts a YAGS graph G into a raw format (number of vertices, coordinates and adjacency matrix) and writes the converted data to the file $FileName$. For use by the external program draw (see Draw(G)).

Example

```
gap> g:=CycleGraph(4);
gap> GraphToRaw("mygraph.raw",g);
```

B.1.79 GraphUpdateFromRaw

▷ `GraphUpdateFromRaw(FileName, G)` (operation)

Updates the coordinates of G from a file *FileName* in raw format. Intended for internal use only.

B.1.80 GroupGraph

▷ `GroupGraph(G, Grp, Act)` (operation)

▷ `GroupGraph(G, Grp)` (operation)

Given a graph G , a group Grp and an action Act of Grp on some set S which contains $Vertices(G)$, `GroupGraph` returns a new graph with vertex set $\{Act(v, g) : g \in Grp, v \in Vertices(G)\}$ and edge set $\{\{Act(v, g), Act(u, g)\} : g \in Grp, \{u, v\} \in Edges(G)\}$.

If Act is omitted, the standard GAP action `OnPoints` is used.

Example

```
gap> GroupGraph(GraphByWalks([1,2]),Group([(1,2,3,4,5),(2,5)(3,4)]));
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ]
] )
```

B.1.81 HararyToMcKay

▷ `HararyToMcKay(Spec)` (operation)

▷ `McKayToHarary(index)` (operation)

Returns the McKay's *index* of a Harary's graph specification *Spec* and viceversa. Frank Harary published in his book [7], a list of all 208 simple graphs of order upto 6 (upto isomorphism). Each of them had a label (which we call *Harary's graph specification*) of the form $[n, m, s]$ where n is the number of vertices, m is the number of edges, and s is a consecutive integer which uniquely identifies the graph from the others with the same n and m . On the other hand, Brendan McKay published data sets containing a list of all graphs of order upto 10 (also upto isomorphism), here:

<https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html>

Each graph in these data sets appears in some specific position (which we call *McKay's index*). We found it convenient to have an automated way to convert from Harary's graph specifications to McKay's indexes and viceversa.

Example

```
gap> HararyToMcKay([1,0,1]);
1
gap> HararyToMcKay([1,0,2]);
fail
gap> HararyToMcKay([5,5,2]);
31
```

```
gap> HararyToMcKay([5,5,3]);
34
gap> HararyToMcKay([5,5,5]);
30
gap> HararyToMcKay([5,5,6]);
45
gap> HararyToMcKay([5,5,7]);
fail
gap> HararyToMcKay([6,15,1]);
208
gap> HararyToMcKay([6,15,2]);
fail
```

Example

```
gap> List([1..208],McKayToHarary);
[ [ 1, 0, 1 ], [ 2, 0, 1 ], [ 2, 1, 1 ], [ 3, 0, 1 ], [ 3, 1, 1 ],
  [ 3, 2, 1 ], [ 3, 3, 1 ], [ 4, 0, 1 ], [ 4, 1, 1 ], [ 4, 2, 1 ],
  [ 4, 3, 3 ], [ 4, 2, 2 ], [ 4, 3, 1 ], [ 4, 3, 2 ], [ 4, 4, 1 ],

    --- many more lines here ---

  [ 6, 10, 10 ], [ 6, 10, 7 ], [ 6, 11, 3 ], [ 6, 12, 1 ], [ 6, 13, 1 ],
  [ 6, 11, 7 ], [ 6, 11, 9 ], [ 6, 11, 8 ], [ 6, 12, 4 ], [ 6, 12, 5 ],
  [ 6, 13, 2 ], [ 6, 14, 1 ], [ 6, 15, 1 ] ]
```

B.1.82 HouseGraph

▷ HouseGraph

(global variable)

A 4-Cycle and a triangle glued by an edge.

Example

```
gap> HouseGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 2, 4, 5 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 1, 4 ] ] )
```

B.1.83 Icosahedron

▷ Icosahedron

(global variable)

The 1-skeleton of Plato's icosahedron.

Example

```
gap> Icosahedron;
Graph( Category := SimpleGraphs, Order := 12, Size :=
30, Adjacencies := [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6, 9, 10 ],
[ 1, 2, 4, 10, 11 ], [ 1, 3, 5, 7, 11 ], [ 1, 4, 6, 7, 8 ],
[ 1, 2, 5, 8, 9 ], [ 4, 5, 8, 11, 12 ], [ 5, 6, 7, 9, 12 ],
[ 2, 6, 8, 10, 12 ], [ 2, 3, 9, 11, 12 ], [ 3, 4, 7, 10, 12 ],
[ 7, 8, 9, 10, 11 ] ] )
```

B.1.84 ImportGraph6

▷ `ImportGraph6(Filename)` (operation)

Returns the list of graphs represented in *Filename* which are encoded using Brendan McKay's graph6 format. This operation allows us to read data in databases which use this format. Several such databases can be found here: <https://cs.anu.edu.au/people/Brendan.McKay/data/graphs.html>.

The graph6 format is described here:

<https://cs.anu.edu.au/people/Brendan.McKay/data/formats.txt>.

The following example assumes that you have a file named `graph3.g6` in your working directory which encodes graphs in graph6 format; the contents of this file is assumed to be as indicated after the first command in the example. It is also assumed that your Operative System is a Unix-like system.

Example

```
gap> Exec("cat graph3.g6");
B?
B0
BW
Bw
gap> ImportGraph6("graph3.g6");
[ Graph( Category := SimpleGraphs, Order := 3, Size := 0, Adjacencies :=
  [ [ ], [ ], [ ] ] ), Graph( Category := SimpleGraphs, Order :=
  3, Size := 1, Adjacencies := [ [ 3 ], [ ], [ 1 ] ] ),
  Graph( Category := SimpleGraphs, Order := 3, Size := 2, Adjacencies :=
  [ [ 3 ], [ 3 ], [ 1, 2 ] ] ), Graph( Category := SimpleGraphs, Order :=
  3, Size := 3, Adjacencies := [ [ 2, 3 ], [ 1, 3 ], [ 1, 2 ] ] ) ]
```

B.1.85 in

▷ `in(G, Catgy)` (operation)

Returns true if graph *G* belongs to category *Catgy* and false otherwise.

Example

```
gap> g:=WheelGraph(4);
Graph( Category := SimpleGraphs, Order := 5, Size :=
  8, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 5 ], [ 1, 2, 4 ],
  [ 1, 3, 5 ], [ 1, 2, 4 ] ] )
gap> g in SimpleGraphs;
true
gap> g in Graphs;
true
gap> g in OrientedGraphs;
false
```

B.1.86 InducedSubgraph

▷ `InducedSubgraph(G, V)` (operation)

Returns the subgraph of graph *G* induced by the vertex set *V*.

Example

```
gap> g:=CycleGraph(6);
Graph( Category := SimpleGraphs, Order := 6, Size :=
6, Adjacencies := [ [ 2, 6 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4, 6 ],
[ 1, 5 ] ] )
gap> InducedSubgraph(g,[3,4,6]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ], [ ] ] )
```

The order of the elements in V does matter.

Example

```
gap> InducedSubgraph(g,[6,3,4]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
1, Adjacencies := [ [ ], [ 3 ], [ 2 ] ] )
```

B.1.87 InNeigh

▷ InNeigh(G , x) (operation)

Returns the list of in-neighbors of x in G .

Example

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ],
[ ] ] )
gap> InNeigh(tt,3);
[ 1, 2 ]
gap> OutNeigh(tt,3);
[ 4, 5 ]
```

B.1.88 InteriorVertices

▷ InteriorVertices(G) (attribute)

When G is a compact surface, it returns the list of vertices in the interior (of the triangulation) of the surface. That is, the list of vertices of G that have links isomorphic to a cycle. It returns `fail` if G is not a compact surface.

Example

```
gap> InteriorVertices(WheelGraph(4,2));
[ 1, 2, 3, 4, 5 ]
gap> InteriorVertices(Octahedron);
[ 1, 2, 3, 4, 5, 6 ]
```

B.1.89 IntersectionGraph

▷ IntersectionGraph(L) (function)

Returns the intersection graph of the family of sets L . This graph has a vertex for every set in L , and two such vertices are adjacent iff the corresponding sets have non-empty intersection.

Example

```
gap> IntersectionGraph([[1,2,3],[3,4,5],[5,6,7]]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
```

B.1.90 IsBoolean

▷ IsBoolean(*Obj*) (function)

Returns true if object *Obj* is true or false and false otherwise.

Example

```
gap> IsBoolean( true ); IsBoolean( fail ); IsBoolean ( false );
true
false
true
```

B.1.91 IsCliqueGated

▷ IsCliqueGated(*G*) (property)

Returns true if *G* is a clique gated graph [6].

B.1.92 IsCliqueHelly

▷ IsCliqueHelly(*G*) (property)

Returns true if the set of (maximal) cliques *G* satisfy the *Helly* property.

The Helly property is defined as follows:

A non-empty family *F* of non-empty sets satisfies the Helly property if every pairwise intersecting subfamily of *F* has a non-empty total intersection.

Here we use the Dragan-Szwarcfiter characterization [2][15] to compute the Helly property.

Example

```
gap> g:=SunGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 2, 6 ], [ 1, 3, 4, 6 ], [ 2, 4 ],
[ 2, 3, 5, 6 ], [ 4, 6 ], [ 1, 2, 4, 5 ] ] )
gap> IsCliqueHelly(g);
false
```

B.1.93 IsCompactSurface

▷ IsCompactSurface(*G*) (property)

Returns true if every link of *G* is either an *n*-cycle, for $n \geq 4$ or an *m*-path, for $m \geq 2$. (not necessarily the same *n/m* for all vertices); it returns false otherwise.

This notion correspond to Whitney triangulations of compact surfaces [11] in which the (maximal) cliques of the graph are exactly the triangles of the triangulation.

Example

```
gap> IsCompactSurface(Icosahedron);
true
gap> IsCompactSurface(RemoveVertices(Icosahedron,[1]));
true
gap> IsCompactSurface(WheelGraph(4,2));
true
gap> IsCompactSurface(Tetrahedron);
false
gap> IsCompactSurface(CompleteGraph(2));
false
gap> IsCompactSurface(CompleteGraph(3));
true
gap> IsCompactSurface(CompleteGraph(4));
false
```

Topologically, the difference between a surface and a compact surface is that the points of a surface always have a open neighborhood homeomorphic to an open disk, whereas a compact surface may also contain points with open neighborhoods homeomorphic to a closed half-plane.

B.1.94 IsComplete

▷ `IsComplete(G , L)` (operation)

Returns true if L induces a complete subgraph of G .

Example

```
gap> IsComplete(DiamondGraph,[1,2,3]);
true
gap> IsComplete(DiamondGraph,[1,2,4]);
false
```

B.1.95 IsCompleteGraph

▷ `IsCompleteGraph(G)` (property)

Returns true if graph G is a complete graph, false otherwise. In a complete graph every pair of vertices is an edge.

B.1.96 IsDiamondFree

▷ `IsDiamondFree(G)` (property)

Returns true if G is free from induced diamonds, false otherwise.

Example

```
gap> IsDiamondFree(Cube);
true
gap> IsDiamondFree(Octahedron);
false
```


B.1.97 IsEdge

- ▷ `IsEdge(G , x , y)` (operation)
- ▷ `IsEdge(G [, x , y >])` (operation)

Returns true if $[x,y]$ is an edge of G .

Example

```
gap> IsEdge(PathGraph(3),1,2);
true
gap> IsEdge(PathGraph(3),[1,2]);
true
gap> IsEdge(PathGraph(3),1,3);
false
gap> IsEdge(PathGraph(3),[1,3]);
false
```

The first form, `IsEdge(G , x , y)`, is a bit faster and hence more suitable for use in algorithms which make extensive use of this operation. On the other hand, the first form does no error checking at all, and hence, it may produce an error where the second form returns false (for instance when x is not a vertex of G). The second form is therefore a bit slower, but more robust.

Example

```
gap> IsEdge(PathGraph(3),[7,3]);
false
gap> IsEdge(PathGraph(3),7,3);
Error, List Element: <list>[7] must have an assigned value
```

B.1.98 IsIsomorphicGraph

- ▷ `IsIsomorphicGraph(G , H)` (operation)

Returns true when G is isomorphic to H and false otherwise.

Example

```
gap> g:=PowerGraph(CycleGraph(6),2);;h:=Octahedron;;
gap> IsIsomorphicGraph(g,h);
true
```

B.1.99 IsLocallyConstant

- ▷ `IsLocallyConstant(G)` (property)

Returns true if all the links of G are isomorphic to each other; false otherwise.

Example

```
gap> IsLocallyConstant(PathGraph(2));
true
gap> IsLocallyConstant(PathGraph(3));
false
gap> IsLocallyConstant(CompleteGraph(3));
true
gap> IsLocallyConstant(CycleGraph(4));
true
```

```
gap> IsLocallyConstant(Icosahedron);
true
gap> IsLocallyConstant(TorusGraph(5,4));
true
gap> IsLocallyConstant(WheelGraph(4,2));
false
gap> IsLocallyConstant(SnubDisphenoid);
false
```

B.1.100 IsLocallyH

▷ IsLocallyH(G, H) (operation)

Returns true if all the links of G are isomorphic to H ; false otherwise.

Example

```
gap> IsLocallyH(Octahedron,CycleGraph(4));
true
gap> IsLocallyH(Octahedron,CycleGraph(5));
false
gap> IsLocallyH(Icosahedron,CycleGraph(5));
true
gap> IsLocallyH(TorusGraph(4,4),CycleGraph(6));
true
```

B.1.101 IsLoopless

▷ IsLoopless(G) (property)

Returns true if graph G have no loops, false otherwise. Loops are edges from a vertex to itself.

B.1.102 IsoMorphism

▷ IsoMorphism(G, H) (operation)

Returns one isomorphism from G to H or fail if none exists. If G has n vertices, an isomorphism $f: G \rightarrow H$ is represented as the list $F=[f(1), f(2), \dots, f(n)]$.

Example

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> f:=IsoMorphism(g,h);
[ 1, 3, 2, 4 ]
```

See NextIsoMorphism(G, H, F).

B.1.103 IsoMorphisms

▷ IsoMorphisms(G, H) (operation)

Returns the list of all isomorphism from G to H . If G has n vertices, an isomorphism $f: G \rightarrow H$ is represented as the list $F=[f(1), f(2), \dots, f(n)]$.

Example

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> IsoMorphisms(g,h);
[ [ 1, 3, 2, 4 ], [ 1, 4, 2, 3 ], [ 2, 3, 1, 4 ], [ 2, 4, 1, 3 ],
  [ 3, 1, 4, 2 ], [ 3, 2, 4, 1 ], [ 4, 1, 3, 2 ], [ 4, 2, 3, 1 ] ]
```

B.1.104 IsOriented

▷ IsOriented(G) (property)

Returns true if graph G is an oriented graph, false otherwise. Regardless of the categories that G belongs to, G is oriented if whenever $[x,y]$ is an edge of G , $[y,x]$ is not.

B.1.105 IsSimple

▷ IsSimple(G) (property)

Returns true if graph G is a simple graph, false otherwise. Regardless of the categories that G belongs to, G is simple if and only if G is undirected and loopless.

Returns true if the graph G is simple regardless of its category.

B.1.106 IsSurface

▷ IsSurface(G) (property)

Returns true if every link of G is an n -cycle, for $n \geq 4$ (not necessarily the same n for all vertices); false otherwise.

This notion correspond to Whitney triangulations of (closed) surfaces [11] in which the (maximal) cliques of the graph are exactly the triangles of the triangulation.

Example

```
gap> IsSurface(SnubDisphenoid);
true
gap> IsSurface(Icosahedron);
true
gap> IsSurface(RemoveVertices(Icosahedron,[1]));
false
gap> IsSurface(TorusGraph(4,5));
true
gap> IsSurface(WheelGraph(4,2));
false
gap> IsSurface(Tetrahedron);
false
```

Topologically, the difference between a (closed) surface and a compact surface is that the points of a surface always have a open neighborhood homeomorphic to an open disk, whereas a compact surface may also contain points with open neighborhoods homeomorphic to a closed half-plane.

B.1.107 IsTournament▷ IsTournament(G)

(property)

Returns true if G is a tournament.

Example

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ],
[ ] ] )
gap> IsTournament(tt);
true
```

B.1.108 IsTransitiveTournament▷ IsTransitiveTournament(G)

(property)

Returns true if G is a transitive tournament.

Example

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ],
[ ] ] )
gap> IsTransitiveTournament(tt);
true
```

B.1.109 IsUndirected▷ IsUndirected(G)

(property)

Returns true if graph G is an undirected graph, false otherwise. Regardless of the categories that G belongs to, G is undirected if whenever $[x, y]$ is an edge of G , $[y, x]$ is also an edge of G .

B.1.110 JohnsonGraph▷ JohnsonGraph(n, r)

(function)

Returns the Johnson graph $J(n, r)$. The Johnson Graph is the graph whose vertices are r -subset of the set $\{1, 2, \dots, n\}$, two of them being adjacent iff they intersect in exactly $r-1$ elements.

Example

```
gap> g:=JohnsonGraph(4,2);
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ], [ 1, 3, 4, 6 ], [ 2, 3, 4, 5 ] ] )
gap> VertexNames(g);
[ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 2, 4 ], [ 3, 4 ] ]
```

B.1.111 Join

▷ `Join(G , H)` (operation)

Returns the join graph $G + H$ of G and H (also known as the Zykov sum); it is the graph obtained from the disjoint union of G and H by adding every possible edge from every vertex in G to every vertex in H .

Example

```
gap> g:=DiscreteGraph(2);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 2, Size :=
0, Adjacencies := [ [ ], [ ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> Join(g,h);
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 4, 6 ],
[ 1, 2, 3, 5 ], [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ] ] )
```

B.1.112 KiteGraph

▷ `KiteGraph` (global variable)

A diamond with a pendant vertex and maximum degree 3.

Example

```
gap> KiteGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 2 ], [ 1, 3, 4 ], [ 2, 4, 5 ], [ 2, 3, 5 ],
[ 3, 4 ] ] )
```

B.1.113 LineGraph

▷ `LineGraph(G)` (operation)

Returns the line graph $L(G)$ of graph G . The line graph is the intersection graph of the edges of G , i. e. the vertices of $L(G)$ are the edges of G two of them being adjacent iff they are incident.

Example

```
gap> g:=Tetrahedron;
Graph( Category := SimpleGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3 ] ] )
gap> LineGraph(g);
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ], [ 1, 3, 4, 6 ], [ 2, 3, 4, 5 ] ] )
```

B.1.114 Link

▷ `Link(G , x)` (operation)

Returns the subgraph of G induced by the neighbors of x .

Example

```
gap> Link(SnubDisphenoid,1);
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 1, 4 ]
] )
gap> Link(SnubDisphenoid,3);
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] )
```

B.1.115 Links▷ Links(G)

(attribute)

Returns the list of subgraphs of G induced by the neighbors of each vertex of G .

Example

```
gap> Links(SnubDisphenoid);
[ Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ],
[ 1, 4 ] ] ), Graph( Category := SimpleGraphs, Order :=
5, Size := 5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ],
[ 3, 5 ], [ 1, 4 ] ] ),
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ),
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ),
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ],
[ 1, 4 ] ] ), Graph( Category := SimpleGraphs, Order :=
5, Size := 5, Adjacencies := [ [ 2, 5 ], [ 1, 3 ], [ 2, 4 ],
[ 3, 5 ], [ 1, 4 ] ] ),
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 3, 4 ], [ 3, 4 ], [ 1, 2 ], [ 1, 2 ] ] ),
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2, 3 ], [ 1, 4 ], [ 1, 4 ], [ 2, 3 ] ] ) ]
```

B.1.116 LooplessGraphs▷ LooplessGraphs(G)

(function)

LooplessGraphs is a graph category in YAGS. A graph in this category may contain arrows and edges but no loops. The parent of this category is Graphs.

Example

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=LooplessGraphs);
Graph( Category := LooplessGraphs, Order := 3, Size :=
3, Adjacencies := [ [ 2 ], [ 1 ], [ 2 ] ] )
```

B.1.117 MaxDegree

▷ `MaxDegree(G)` (operation)

Returns the maximum degree in graph G .

Example

```
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
7, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 4 ] ] )
gap> MaxDegree(g);
4
```

B.1.118 MinDegree

▷ `MinDegree(G)` (operation)

Returns the minimum degree in graph G .

Example

```
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
7, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 4 ] ] )
gap> MinDegree(g);
2
```

B.1.119 NextIsoMorphism

▷ `NextIsoMorphism(G , H , F)` (operation)

Returns the next isomorphism (after F) from G to H in the lexicographic order; returns fail if there are no more isomorphisms. If G has n vertices, an isomorphism $f : G \rightarrow H$ is represented as the list $F = [f(1), f(2), \dots, f(n)]$.

Example

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> f:=IsoMorphism(g,h);
[ 1, 3, 2, 4 ]
gap> NextIsoMorphism(g,h,f);
[ 1, 4, 2, 3 ]
gap> NextIsoMorphism(g,h,f);
[ 2, 3, 1, 4 ]
gap> NextIsoMorphism(g,h,f);
[ 2, 4, 1, 3 ]
```

B.1.120 NextPropertyMorphism

▷ `NextPropertyMorphism(G , H , F , $PropList$)` (operation)

Returns the next morphism (in lexicographic order) from G to H satisfying the list of properties $PropList$ starting with (possibly incomplete) morphism F . The morphism found will be returned

and stored in F in order to use it as the next starting point, in case `NextPropertyMorphism` is called again. The operation returns `fail` if there are no more morphisms of the specified type.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: `CHK_WEAK`, `CHK_MORPH`, `CHK_METRIC`, `CHK_CMPLT`, `CHK_MONO` and `CHK_EPI`.

If G has n vertices and $f : G \rightarrow H$ is a morphism, it is represented as $F=[f(1), f(2), \dots, f(n)]$.

Example

```
gap> g:=CycleGraph(4);h:=CompleteBipartiteGraph(2,2);
gap> f:=[];; PropList:=[CHK_MORPH,CHK_MONO];;
gap> NextPropertyMorphism(g,h,f,PropList);
[ 1, 3, 2, 4 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 1, 4, 2, 3 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 2, 3, 1, 4 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 2, 4, 1, 3 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 3, 1, 4, 2 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 3, 2, 4, 1 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 4, 1, 3, 2 ]
gap> NextPropertyMorphism(g,h,f,PropList);
[ 4, 2, 3, 1 ]
gap> NextPropertyMorphism(g,h,f,PropList);
fail
```

B.1.121 NumberOfCliques

- ▷ `NumberOfCliques(G)` (attribute)
- ▷ `NumberOfCliques(G , $maxNumCli$)` (operation)

Returns the number of (maximal) cliques of G . In the second form, It stops computing cliques after $maxNumCli$ of them have been counted and returns $maxNumCli$ in case G has $maxNumCli$ or more cliques.

Example

```
gap> NumberOfCliques(Icosahedron);
20
gap> NumberOfCliques(Icosahedron,15);
15
gap> NumberOfCliques(Icosahedron,50);
20
```

This implementation discards the cliques once counted hence, given enough time, it can compute the number of cliques of G even if the set of cliques does not fit in memory. This test may take several minutes to complete:

Example

```
gap> NumberOfCliques(OctahedralGraph(30));
1073741824
```


B.1.122 NumberOfConnectedComponents

▷ `NumberOfConnectedComponents(G)` (attribute)

Returns the number of connected components of G .

B.1.123 OctahedralGraph

▷ `OctahedralGraph(n)` (function)

Return the n -dimensional octahedron. This is the complement of n copies of K_2 (an edge). It is also the $(2n-2)$ -regular graph on $2n$ vertices.

Example

```
gap> OctahedralGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ], [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

B.1.124 Octahedron

▷ `Octahedron` (global variable)

The 1-skeleton of Plato's octahedron.

Example

```
gap> Octahedron;
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2, 5, 6 ], [ 1, 2, 3, 4 ], [ 1, 2, 3, 4 ] ] )
```

B.1.125 Order

▷ `Order(G)` (attribute)

Returns the number of vertices, of graph G .

Example

```
gap> Order(Icosahedron);
12
```

B.1.126 Orientations

▷ `Orientations(G)` (operation)

Returns the list of all the oriented graphs that are obtained from G by replacing (in every possible way) each edge $[x, y]$ of G by one arrow: either $[x, y]$ or $[y, x]$. In each of these orientations Loops are removed and existing arrows of G are left untouched.

Note that this operation will use time and memory which is exponential on the number of edges of G .

Example

```
gap> g:=GraphByWalks([1,1,2,3,1,3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 6, Adjacencies :=
[ [ 1, 2, 3 ], [ 3 ], [ 1, 2 ] ] )
gap> Orientations(g);
[ Graph( Category := OrientedGraphs, Order := 3, Size :=
  3, Adjacencies := [ [ 2 ], [ ], [ 1, 2 ] ] ),
  Graph( Category := OrientedGraphs, Order := 3, Size :=
  3, Adjacencies := [ [ 2 ], [ 3 ], [ 1 ] ] ),
  Graph( Category := OrientedGraphs, Order := 3, Size :=
  3, Adjacencies := [ [ 2, 3 ], [ ], [ 2 ] ] ),
  Graph( Category := OrientedGraphs, Order := 3, Size :=
  3, Adjacencies := [ [ 2, 3 ], [ 3 ], [ ] ] ) ]
gap> Length(Orientations(Octahedron));
4096
```

Note that `Orientations(G)` returns a list of graphs, each of them in the category `OrientedGraphs` regardless of the `TargetGraphCategory`.

B.1.127 OrientedGraphs

▷ `OrientedGraphs(G)`

(function)

`OrientedGraphs` is a graph category in YAGS. A graph in this category may contain arrows, but no loops or edges. The parent of this category is `LooplessGraphs`.

Example

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ ], [ 2 ] ] )
```

B.1.128 OutNeigh

▷ `OutNeigh(G, x)`

(operation)

Returns the list of out-neighbors of x in G .

Example

```
gap> tt:=CompleteGraph(5:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 5, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5 ], [ 3, 4, 5 ], [ 4, 5 ], [ 5 ],
[ ] ] )
gap> InNeigh(tt,3);
[ 1, 2 ]
gap> OutNeigh(tt,3);
[ 4, 5 ]
```

B.1.129 PaleyTournament

▷ PaleyTournament(*prime*)

(operation)

Returns the Paley tournament associated with prime number *prime*. *prime* must be congruent to 3 mod 4. The Paley tournament is the oriented circulant whose *jumps* are all the squares of the ring \mathbb{Z}_p .

Example

```
gap> Filtered([1..30], x -> 0=((x-3) mod 4) and IsPrime(x));
[ 3, 7, 11, 19, 23 ]
gap> PaleyTournament(3);PaleyTournament(7);PaleyTournament(11);
Graph( Category := OrientedGraphs, Order := 3, Size :=
3, Adjacencies := [ [ 2 ], [ 3 ], [ 1 ] ] )
Graph( Category := OrientedGraphs, Order := 7, Size :=
21, Adjacencies := [ [ 2, 3, 5 ], [ 3, 4, 6 ], [ 4, 5, 7 ],
[ 1, 5, 6 ], [ 2, 6, 7 ], [ 1, 3, 7 ], [ 1, 2, 4 ] ] )
Graph( Category := OrientedGraphs, Order := 11, Size :=
55, Adjacencies := [ [ 2, 4, 5, 6, 10 ], [ 3, 5, 6, 7, 11 ],
[ 1, 4, 6, 7, 8 ], [ 2, 5, 7, 8, 9 ], [ 3, 6, 8, 9, 10 ],
[ 4, 7, 9, 10, 11 ], [ 1, 5, 8, 10, 11 ], [ 1, 2, 6, 9, 11 ],
[ 1, 2, 3, 7, 10 ], [ 2, 3, 4, 8, 11 ], [ 1, 3, 4, 5, 9 ] ] )
gap> PaleyTournament(5);
fail
```

Note that PaleyTournament(*prime*) returns a graph in the category OrientedGraphs regardless of the TargetGraphCategory.

B.1.130 ParachuteGraph

▷ ParachuteGraph

(global variable)

The complement of a ParapluieGraph; The suspension of a 4-path with a pendant vertex attached to the south pole.

Example

```
gap> ParachuteGraph;
Graph( Category := SimpleGraphs, Order := 7, Size :=
12, Adjacencies := [ [ 2 ], [ 1, 3, 4, 5, 6 ], [ 2, 4, 7 ],
[ 2, 3, 5, 7 ], [ 2, 4, 6, 7 ], [ 2, 5, 7 ], [ 3, 4, 5, 6 ] ] )
```

B.1.131 ParapluieGraph

▷ ParapluieGraph

(global variable)

A 3-Fan graph with a 3-path attached to the universal vertex.

Example

```
gap> ParapluieGraph;
Graph( Category := SimpleGraphs, Order := 7, Size :=
9, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4, 5, 6, 7 ], [ 3, 5 ],
[ 3, 4, 6 ], [ 3, 5, 7 ], [ 3, 6 ] ] )
```

B.1.132 ParedGraph

▷ ParedGraph(G) (operation)

Returns the pared graph of G . This is the induced subgraph obtained from G by removing its dominated vertices. When there are twin vertices (mutually dominated vertices), exactly one of them survives the paring in each equivalent class of mutually dominated vertices.

Example

```
gap> g1:=PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
gap> ParedGraph(g1);
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> g2:=PathGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> ParedGraph(g2);
Graph( Category := SimpleGraphs, Order := 1, Size :=
0, Adjacencies := [ [ ] ] )
```

B.1.133 PathGraph

▷ PathGraph(n) (function)

Returns the path graph on n vertices.

Example

```
gap> PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
```

B.1.134 PawGraph

▷ PawGraph (global variable)

The graph on 4 vertices, 4 edges and maximum degree 3: A triangle with a pendant vertex.

Example

```
gap> PawGraph;
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3, 4 ], [ 2, 4 ], [ 2, 3 ] ] )
```

B.1.135 PetersenGraph

▷ PetersenGraph (global variable)

The 3-regular graph on 10 vertices having girth 5.

Example

```
gap> PetersenGraph;
Graph( Category := SimpleGraphs, Order := 10, Size :=
15, Adjacencies := [ [ 2, 5, 6 ], [ 1, 3, 7 ], [ 2, 4, 8 ],
```

```
[ 3, 5, 9 ], [ 1, 4, 10 ], [ 1, 8, 9 ], [ 2, 9, 10 ], [ 3, 6, 10 ],
[ 4, 6, 7 ], [ 5, 7, 8 ] ] )
```

B.1.136 PowerGraph

▷ `PowerGraph(G, exp)`

(operation)

Returns the `DistanceGraph` of G using $[0, 1, \dots, \text{exp}]$ as the list of distances. Note that the distance 0 in the list produces loops in the new graph only when the `TargetGraphCategory` admits loops.

Example

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> PowerGraph(g,1);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> PowerGraph(g,1:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 5, Size := 13, Adjacencies :=
[ [ 1, 2 ], [ 1, 2, 3 ], [ 2, 3, 4 ], [ 3, 4, 5 ], [ 4, 5 ] ] )
```

B.1.137 PropertyMorphism

▷ `PropertyMorphism(G, H, PropList)`

(operation)

Returns the first morphism (in lexicographic order) from G to H satisfying the list of properties *PropList*.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: `CHK_WEAK`, `CHK_MORPH`, `CHK_METRIC`, `CHK_CMPLT`, `CHK_MONO` and `CHK_EPI`.

If G has n vertices and $f : G \rightarrow H$ is a morphism, it is represented as $F = [f(1), f(2), \dots, f(n)]$.

Example

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> PropList:=[CHK_MORPH];;
gap> PropertyMorphism(g,h,PropList);
[ 1, 3, 1, 3 ]
```

B.1.138 PropertyMorphisms

▷ `PropertyMorphisms(G, H, PropList)`

(operation)

Returns all morphisms from G to H satisfying the list of properties *PropList*.

A number of preprogrammed properties are provided by YAGS, and the user may create additional ones. The properties provided are: `CHK_WEAK`, `CHK_MORPH`, `CHK_METRIC`, `CHK_CMPLT`, `CHK_MONO` and `CHK_EPI`.

If G has n vertices and $f : G \rightarrow H$ is a morphism, it is represented as $F = [f(1), f(2), \dots, f(n)]$.

Example

```
gap> g:=CycleGraph(4);;h:=CompleteBipartiteGraph(2,2);;
gap> PropList:=[CHK_WEAK,CHK_MONO];;
gap> PropertyMorphisms(g,h,PropList);
[ [ 1, 3, 2, 4 ], [ 1, 4, 2, 3 ], [ 2, 3, 1, 4 ], [ 2, 4, 1, 3 ],
  [ 3, 1, 4, 2 ], [ 3, 2, 4, 1 ], [ 4, 1, 3, 2 ], [ 4, 2, 3, 1 ] ]
```

B.1.139 QtfyIsSimple

▷ QtfyIsSimple(G) (attribute)

For internal use. Returns how far is graph G from being simple.

B.1.140 QuadraticRingGraph

▷ QuadraticRingGraph(Rng) (operation)

Returns the graph G whose vertices are the elements of Rng such that x is adjacent to y iff $x + z^2 = y$ for some z in Rng .

Example

```
gap> QuadraticRingGraph(ZmodnZ(8));
Graph( Category := SimpleGraphs, Order := 8, Size :=
12, Adjacencies := [ [ 2, 5, 8 ], [ 1, 3, 6 ], [ 2, 4, 7 ],
  [ 3, 5, 8 ], [ 1, 4, 6 ], [ 2, 5, 7 ], [ 3, 6, 8 ], [ 1, 4, 7 ] ] )
```

B.1.141 QuotientGraph

▷ QuotientGraph(G , $Part$) (operation)

▷ QuotientGraph(G , $L1$, $L2$) (operation)

Returns the quotient graph of graph G given a vertex partition $Part$, by identifying any two vertices in the same part. The vertices of the quotient graph are the parts in the partition $Part$ two of them being adjacent iff any vertex in one part is adjacent to any vertex in the other part. Singletons may be omitted in $Part$.

Example

```
gap> g:=PathGraph(8);;
gap> QuotientGraph(g,[[1,5,8],[2],[3],[4],[6],[7]]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 4, 5, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ],
  [ 1, 6 ], [ 1, 5 ] ] )
gap> QuotientGraph(g,[[1,5,8]]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 4, 5, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ],
  [ 1, 6 ], [ 1, 5 ] ] )
```

In its second form, QuotientGraph identifies each vertex in list $L1$, with the corresponding vertex in list $L2$. $L1$ and $L2$ must have the same length, but any or both of them may have repetitions.

Example

```
gap> g:=PathGraph(8);;
gap> QuotientGraph(g,[[1,7],[4,8]]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 4, 6 ], [ 1, 5 ] ] )
gap> QuotientGraph(g,[1,4],[7,8]);
Graph( Category := SimpleGraphs, Order := 6, Size :=
7, Adjacencies := [ [ 2, 4, 6 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3, 5 ],
[ 4, 6 ], [ 1, 5 ] ] )
```

B.1.142 Radius▷ Radius(G)

(attribute)

Returns the minimal eccentricity among the vertices of graph G .

Example

```
gap> Radius(PathGraph(5));
2
```

B.1.143 RandomCirculant▷ RandomCirculant(n)

(operation)

▷ RandomCirculant(n , k)

(operation)

▷ RandomCirculant(n , p)

(operation)

Returns a circulant on n vertices with its *jumps* selected randomly. In its third form, each possible jump has probability p of being selected. In its second form, when k is a positive integer, exactly k jumps are selected (provided there are at least k possible jumps to select from). The first form is equivalent to specifying $p=1/2$.

Example

```
gap> RandomCirculant(11,2);
Graph( Category := SimpleGraphs, Order := 11, Size :=
22, Adjacencies := [ [ 5, 6, 7, 8 ], [ 6, 7, 8, 9 ], [ 7, 8, 9, 10 ],
[ 8, 9, 10, 11 ], [ 1, 9, 10, 11 ], [ 1, 2, 10, 11 ],
[ 1, 2, 3, 11 ], [ 1, 2, 3, 4 ], [ 2, 3, 4, 5 ], [ 3, 4, 5, 6 ],
[ 4, 5, 6, 7 ] ] )
gap> RandomCirculant(11,2);
Graph( Category := SimpleGraphs, Order := 11, Size :=
22, Adjacencies := [ [ 3, 5, 8, 10 ], [ 4, 6, 9, 11 ],
[ 1, 5, 7, 10 ], [ 2, 6, 8, 11 ], [ 1, 3, 7, 9 ], [ 2, 4, 8, 10 ],
[ 3, 5, 9, 11 ], [ 1, 4, 6, 10 ], [ 2, 5, 7, 11 ], [ 1, 3, 6, 8 ],
[ 2, 4, 7, 9 ] ] )
gap> RandomCirculant(11,1/2);
Graph( Category := SimpleGraphs, Order := 11, Size :=
22, Adjacencies := [ [ 2, 3, 10, 11 ], [ 1, 3, 4, 11 ],
[ 1, 2, 4, 5 ], [ 2, 3, 5, 6 ], [ 3, 4, 6, 7 ], [ 4, 5, 7, 8 ],
[ 5, 6, 8, 9 ], [ 6, 7, 9, 10 ], [ 7, 8, 10, 11 ], [ 1, 8, 9, 11 ],
[ 1, 2, 9, 10 ] ] )
gap> RandomCirculant(11,1/2);
```

```

Graph( Category := SimpleGraphs, Order := 11, Size :=
55, Adjacencies := [ [ 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 ],
  [ 1, 3, 4, 5, 6, 7, 8, 9, 10, 11 ],
  [ 1, 2, 4, 5, 6, 7, 8, 9, 10, 11 ],
  [ 1, 2, 3, 5, 6, 7, 8, 9, 10, 11 ],
  [ 1, 2, 3, 4, 6, 7, 8, 9, 10, 11 ],
  [ 1, 2, 3, 4, 5, 7, 8, 9, 10, 11 ],
  [ 1, 2, 3, 4, 5, 6, 8, 9, 10, 11 ],
  [ 1, 2, 3, 4, 5, 6, 7, 9, 10, 11 ],
  [ 1, 2, 3, 4, 5, 6, 7, 8, 10, 11 ],
  [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 11 ],
  [ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 ] ] )
gap> RandomCirculant(11,1/2);
Graph( Category := SimpleGraphs, Order := 11, Size :=
11, Adjacencies := [ [ 5, 8 ], [ 6, 9 ], [ 7, 10 ], [ 8, 11 ],
  [ 1, 9 ], [ 2, 10 ], [ 3, 11 ], [ 1, 4 ], [ 2, 5 ], [ 3, 6 ],
  [ 4, 7 ] ] )

```

B.1.144 RandomGraph

- ▷ RandomGraph(n , p) (function)
- ▷ RandomGraph(n) (function)

Returns a random graph of order n taking the rational $p \in [0, 1]$ as the edge probability.

Example

```

gap> RandomGraph(5,1/3);
Graph( Category := SimpleGraphs, Order := 5, Size :=
2, Adjacencies := [ [ 5 ], [ 5 ], [ ], [ ], [ 1, 2 ] ] )
gap> RandomGraph(5,2/3);
Graph( Category := SimpleGraphs, Order := 5, Size :=
6, Adjacencies := [ [ 4, 5 ], [ 3, 4, 5 ], [ 2, 4 ], [ 1, 2, 3 ],
  [ 1, 2 ] ] )
gap> RandomGraph(5,1/2);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2, 5 ], [ 1, 3, 5 ], [ 2 ], [ ], [ 1, 2 ] ] )

```

If p is omitted, the edge probability is taken to be $1/2$.

Example

```

gap> RandomGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
5, Adjacencies := [ [ 2, 3 ], [ 1 ], [ 1, 4, 5 ], [ 3, 5 ], [ 3, 4 ]
  ] )
gap> RandomGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
3, Adjacencies := [ [ 2, 5 ], [ 1, 4 ], [ ], [ 2 ], [ 1 ] ] )

```

B.1.145 RandomPermutation

- ▷ RandomPermutation(n) (operation)

Returns a random permutation of the list $[1, 2, \dots, n]$.

Example

```
gap> RandomPermutation(12);
(1,12,8,10,2,9,6,5)(3,7,11)
```

B.1.146 RandomSubset

- ▷ RandomSubset(*Set*) (operation)
- ▷ RandomSubset(*Set*, *k*) (operation)
- ▷ RandomSubset(*Set*, *p*) (operation)

Returns a random subset of the set *Set*. When the positive integer *k* is provided, the returned subset has *k* elements (or fail if *Set* does not have at least *k* elements). When the probability *p* is provided, each element of *Set* has probability *p* of being selected for inclusion in the returned subset. When *k* and *p* are both missing, it is equivalent to specifying $p=1/2$. In the ambiguous case when the second parameter is 1, it is interpreted as the value of *k*.

Example

```
gap> RandomSubset([1..10],5);
[ 10, 7, 5, 3, 1 ]
gap> RandomSubset([1..10],5);
[ 4, 10, 9, 6, 1 ]
gap> RandomSubset([1..10],5);
[ 5, 2, 6, 7, 9 ]
gap> RandomSubset([1..10],5);
[ 10, 7, 3, 8, 9 ]
gap> RandomSubset([1..10],1/2);
[ 1, 3, 5, 8, 9 ]
gap> RandomSubset([1..10],1/2);
[ 3, 4, 8, 10 ]
gap> RandomSubset([1..10],1/2);
[ 1, 4, 7, 10 ]
gap> RandomSubset([1..10],1/2);
[ 1, 2, 5, 7, 9 ]
```

Even if this operation is intended to be applied to sets, it does not impose this condition on its operand, and can be applied to lists as well.

Example

```
gap> RandomSubset([1,3,2,2,3,2,1]);
[ 1, 3 ]
gap> RandomSubset([1,3,2,2,3,2,1]);
[ 3, 2, 2, 3, 1 ]
```

B.1.147 RandomlyPermuted

- ▷ RandomlyPermuted(*Obj*) (operation)

Returns a copy of *Obj* with the order of its elements permuted randomly. Currently, the operation is implemented for lists and graphs.

Example

```
gap> RandomlyPermuted([1..9]);
[ 9, 7, 5, 3, 1, 4, 8, 6, 2 ]
```

```
gap> g:=PathGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3 ] ] )
gap> RandomlyPermuted(g);
Graph( Category := SimpleGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 3 ], [ 3, 4 ], [ 1, 2 ], [ 2 ] ] )
```

B.1.148 RemoveEdges

▷ RemoveEdges(G , E) (operation)

Returns a new graph created from graph G by removing the edges in list E .

Example

```
gap> g:=CompleteGraph(4);
Graph( Category := SimpleGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3 ] ] )
gap> RemoveEdges(g,[[1,2]]);
Graph( Category := SimpleGraphs, Order := 4, Size :=
5, Adjacencies := [ [ 3, 4 ], [ 3, 4 ], [ 1, 2, 4 ], [ 1, 2, 3 ] ] )
gap> RemoveEdges(g,[[1,2],[3,4]]);
Graph( Category := SimpleGraphs, Order := 4, Size :=
4, Adjacencies := [ [ 3, 4 ], [ 3, 4 ], [ 1, 2 ], [ 1, 2 ] ] )
```

B.1.149 RemoveVertices

▷ RemoveVertices(G , V) (operation)

Returns a new graph created from graph G by removing the vertices in list V .

Example

```
gap> g:=PathGraph(5);
Graph( Category := SimpleGraphs, Order := 5, Size :=
4, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2, 4 ], [ 3, 5 ], [ 4 ] ] )
gap> RemoveVertices(g,[3]);
Graph( Category := SimpleGraphs, Order := 4, Size :=
2, Adjacencies := [ [ 2 ], [ 1 ], [ 4 ], [ 3 ] ] )
gap> RemoveVertices(g,[1,3]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
1, Adjacencies := [ [ ], [ 3 ], [ 2 ] ] )
```

B.1.150 RGraph

▷ RGraph (global variable)

A square with two pendant vertices attached to the same vertex of the square.

Example

```
gap> RGraph;
Graph( Category := SimpleGraphs, Order := 6, Size :=
6, Adjacencies := [ [ 2 ], [ 1, 3, 5, 6 ], [ 2, 4 ], [ 3, 5 ],
[ 2, 4 ], [ 2 ] ] )
```

B.1.151 RingGraph

▷ `RingGraph(Rng, Elms)`

(operation)

Returns the graph G whose vertices are the elements of the ring Rng such that x is adjacent to y iff $x+r=y$ for some r in $Elms$.

Example

```
gap> r:=FiniteField(8);Elements(r);
GF(2^3)
[ 0*Z(2), Z(2)^0, Z(2^3), Z(2^3)^2, Z(2^3)^3, Z(2^3)^4, Z(2^3)^5,
  Z(2^3)^6 ]
gap> RingGraph(r,[Z(2^3),Z(2^3)^4]);
Graph( Category := SimpleGraphs, Order := 8, Size :=
8, Adjacencies := [ [ 3, 6 ], [ 5, 7 ], [ 1, 4 ], [ 3, 6 ], [ 2, 8 ],
[ 1, 4 ], [ 2, 8 ], [ 5, 7 ] ] )
```

B.1.152 SetCoordinates

▷ `SetCoordinates(G, Coord)`

(operation)

Sets the coordinates of the vertices of G , which are used to draw G by `Draw(G)`.

Example

```
gap> g:=CycleGraph(4);;
gap> Coordinates(g);
fail
gap> SetCoordinates(g,[[ -10,-10 ],[ -10,20 ],[ 20,-10 ], [ 20,20 ]]);
gap> Coordinates(g);
[ [ -10, -10 ], [ -10, 20 ], [ 20, -10 ], [ 20, 20 ] ]
```

B.1.153 SetDefaultGraphCategory

▷ `SetDefaultGraphCategory(Catgy)`

(function)

Sets the default graph category to $Catgy$. The default graph category is used when constructing new graphs when no other graph category is indicated. New graphs are always forced to comply with the `TargetGraphCategory`, so loops may be removed, and arrows may be replaced by edges or viceversa, depending on the category that the new graph belongs to.

The available graph categories are: `SimpleGraphs`, `OrientedGraphs`, `UndirectedGraphs`, `LooplessGraphs`, and `Graphs`.

Example

```
gap> SetDefaultGraphCategory(Graphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(LooplessGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := LooplessGraphs, Order := 3, Size :=
3, Adjacencies := [ [ 2 ], [ 1 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(UndirectedGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
```

```

Graph( Category := UndirectedGraphs, Order := 3, Size :=
3, Adjacencies := [ [ 1, 2 ], [ 1, 3 ], [ 2 ] ] )
gap> SetDefaultGraphCategory(OrientedGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := OrientedGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ ], [ 2 ] ] )
gap> SetDefaultGraphCategory(SimpleGraphs);
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )

```

B.1.154 SimpleGraphs

▷ SimpleGraphs(G) (function)

SimpleGraphs is a graph category in YAGS. A graph in this category may contain edges, but no loops or arrows. The category has two parents: LooplessGraphs and UndirectedGraphs.

Example

```

gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=SimpleGraphs);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )

```

B.1.155 Size

▷ Size(G) (attribute)

Returns the number of edges of graph G .

Example

```

gap> Size(Icosahedron);
30

```

B.1.156 SnubDisphenoid

▷ SnubDisphenoid (global variable)

The 1-skeleton of the 84th Johnson solid.

Example

```

gap> SnubDisphenoid;
Graph( Category := SimpleGraphs, Order := 8, Size :=
18, Adjacencies := [ [ 2, 3, 4, 5, 8 ], [ 1, 3, 6, 7, 8 ],
[ 1, 2, 4, 6 ], [ 1, 3, 5, 6 ], [ 1, 4, 6, 7, 8 ],
[ 2, 3, 4, 5, 7 ], [ 2, 5, 6, 8 ], [ 1, 2, 5, 7 ] ] )

```

B.1.157 SpanningForest

▷ `SpanningForest(G)` (operation)

Returns a spanning forest of G .

B.1.158 SpanningForestEdges

▷ `SpanningForestEdges(G)` (operation)

Returns the edges of a spanning forest of G .

B.1.159 SpikyGraph

▷ `SpikyGraph(n)` (function)

The spiky graph is constructed as follows: Take complete graph on n vertices, K_N , and then, for each the n subsets of $Vertices(K_n)$ of order $n-1$, add an additional vertex which is adjacent precisely to this subset of $Vertices(K_n)$.

Example

```
gap> SpikyGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3, 4, 6 ], [ 1, 2, 5, 6 ],
[ 1, 2 ], [ 1, 3 ], [ 2, 3 ] ] )
```

B.1.160 SunGraph

▷ `SunGraph(n)` (function)

Returns the n -Sun: A complete graph on n vertices, K_N , with a corona made with a zigzagging $2n$ -cycle glued to a n -cycle of the K_N .

Example

```
gap> SunGraph(3);
Graph( Category := SimpleGraphs, Order := 6, Size :=
9, Adjacencies := [ [ 2, 6 ], [ 1, 3, 4, 6 ], [ 2, 4 ],
[ 2, 3, 5, 6 ], [ 4, 6 ], [ 1, 2, 4, 5 ] ] )
gap> SunGraph(4);
Graph( Category := SimpleGraphs, Order := 8, Size :=
14, Adjacencies := [ [ 2, 8 ], [ 1, 3, 4, 6, 8 ], [ 2, 4 ],
[ 2, 3, 5, 6, 8 ], [ 4, 6 ], [ 2, 4, 5, 7, 8 ], [ 6, 8 ],
[ 1, 2, 4, 6, 7 ] ] )
```

B.1.161 Suspension

▷ `Suspension(G)` (operation)

Returns the suspension of graph G . The suspension of G is the graph obtained from G by adding two new vertices which are adjacent to every vertex of G but not to each other. The new vertices are the first ones in the new graph.

Example

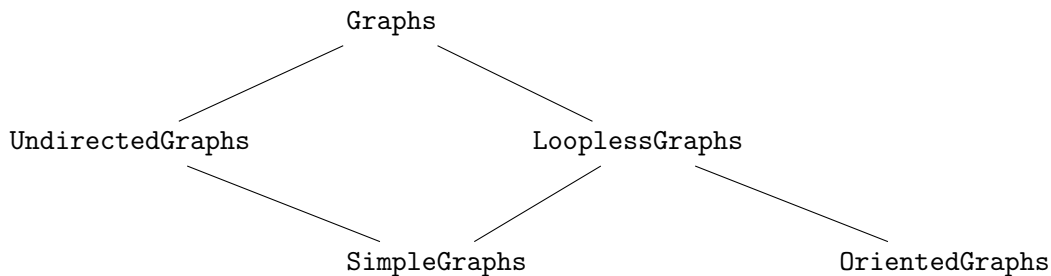
```
gap> Suspension(CycleGraph(4));
Graph( Category := SimpleGraphs, Order := 6, Size :=
12, Adjacencies := [ [ 3, 4, 5, 6 ], [ 3, 4, 5, 6 ], [ 1, 2, 4, 6 ],
[ 1, 2, 3, 5 ], [ 1, 2, 4, 6 ], [ 1, 2, 3, 5 ] ] )
```

B.1.162 TargetGraphCategory

▷ TargetGraphCategory([G, ...])

(function)

For internal use. Returns the graph category indicated in the *options stack* if any, otherwise if the list of graphs provided is not empty, returns the minimal common graph category for the graphs in the list, else returns the default graph category. The partial order (by inclusion) among graph categories is as follows:



This function is internally called by all graph constructing operations in YAGS to decide the graph category that the newly constructed graph is going to belong. New graphs are always forced to comply with the TargetGraphCategory, so loops may be removed, and arrows may be replaced by edges or viceversa, depending on the category that the new graph belongs to.

The *options stack* is a mechanism provided by GAP to pass implicit parameters and is used by TargetGraphCategory so that the user may indicate the graph category she/he wants for the new graph.

Example

```
gap> SetDefaultGraphCategory(SimpleGraphs);
gap> g1:=CompleteGraph(2);
Graph( Category := SimpleGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ 1 ] ] )
gap> g2:=CompleteGraph(2:GraphCategory:=OrientedGraphs);
Graph( Category := OrientedGraphs, Order := 2, Size :=
1, Adjacencies := [ [ 2 ], [ ] ] )
gap> DisjointUnion(g1,g2);
Graph( Category := LooplessGraphs, Order := 4, Size :=
3, Adjacencies := [ [ 2 ], [ 1 ], [ 4 ], [ ] ] )
gap> DisjointUnion(g1,g2:GraphCategory:=UndirectedGraphs);
Graph( Category := UndirectedGraphs, Order := 4, Size :=
2, Adjacencies := [ [ 2 ], [ 1 ], [ 4 ], [ 3 ] ] )
```

In the previous examples, TargetGraphCategory was called internally exactly once for each new graph constructed with the following parameters:

Example

```
gap> TargetGraphCategory();
<Category "SimpleGraphs">
```

```
gap> TargetGraphCategory(:GraphCategory:=OrientedGraphs);
<Category "OrientedGraphs">
gap> TargetGraphCategory([g1,g2]);
<Category "LooplessGraphs">
gap> TargetGraphCategory([g1,g2]:GraphCategory:=UndirectedGraphs);
<Category "UndirectedGraphs">
```

B.1.163 Tetrahedron

▷ Tetrahedron

(global variable)

The 1-skeleton of Plato's tetrahedron.

Example

```
gap> Tetrahedron;
Graph( Category := SimpleGraphs, Order := 4, Size :=
6, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4 ], [ 1, 2, 4 ],
[ 1, 2, 3 ] ] )
```

B.1.164 TimeInSeconds

▷ TimeInSeconds()

(operation)

Returns the time in seconds since 1970-01-01 00:00:00 UTC as an integer. This is useful to measure execution time. It can also be used to impose time constraints on the execution of algorithms. Note however that the time reported is the *wall time*, not necessarily the time spent in the process you intend to measure.

Example

```
gap> TimeInSeconds();
1415551598
gap> K:=CliqueGraph;;NumCli:=NumberOfCliques;;I:=Icosahedron;;
gap> t1:=TimeInSeconds();NumCli(K(K(K(K(I)))));TimeInSeconds()-t1;
1415551608
44644
103
```

Currently, this operation is not working on MS Windows.

B.1.165 TimesProduct

▷ TimesProduct(G , H)

(operation)

Returns the times product of two graphs G and H , $G \times H$ (also known as the tensor product).

The times product is computed as follows:

For each pair of vertices $x \in G, y \in H$ we create a vertex (x, y) . Given two such vertices (x, y) and (x', y') they are adjacent iff $x \sim x'$ and $y \sim y'$.

Example

```
gap> g:=PathGraph(3);h:=CycleGraph(4);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
Graph( Category := SimpleGraphs, Order := 4, Size :=
```

```

4, Adjacencies := [ [ 2, 4 ], [ 1, 3 ], [ 2, 4 ], [ 1, 3 ] ] )
gap> gh:=TimesProduct(g,h);
Graph( Category := SimpleGraphs, Order := 12, Size :=
16, Adjacencies := [ [ 6, 8 ], [ 5, 7 ], [ 6, 8 ], [ 5, 7 ],
[ 2, 4, 10, 12 ], [ 1, 3, 9, 11 ], [ 2, 4, 10, 12 ],
[ 1, 3, 9, 11 ], [ 6, 8 ], [ 5, 7 ], [ 6, 8 ], [ 5, 7 ] ] )
gap> VertexNames(gh);
[ [ 1, 1 ], [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 1 ], [ 2, 2 ],
[ 2, 3 ], [ 2, 4 ], [ 3, 1 ], [ 3, 2 ], [ 3, 3 ], [ 3, 4 ] ]

```

B.1.166 TorusGraph

▷ TorusGraph(n, m)

(function)

Returns (the underlying graph of) a triangulation of the torus on $n.m$ vertices. This graph is constructed using $\{1, 2, \dots, n\} \times \{1, 2, \dots, m\}$ as the vertex set; two of them being adjacent if their difference belongs to $\{(1, 0), (0, 1), (1, 1)\}$ module $\mathbb{Z}_n \times \mathbb{Z}_m$. Hence, in the category of simple graphs, TorusGraph is a 6-regular graph when $n, m \geq 3$.

Example

```

TorusGraph(4,4);
Graph( Category := SimpleGraphs, Order := 16, Size := 48, Adjacencies :=
[ [ 2, 4, 5, 6, 13, 16 ], [ 1, 3, 6, 7, 13, 14 ], [ 2, 4, 7, 8, 14, 15 ],
[ 1, 3, 5, 8, 15, 16 ], [ 1, 4, 6, 8, 9, 10 ], [ 1, 2, 5, 7, 10, 11 ],
[ 2, 3, 6, 8, 11, 12 ], [ 3, 4, 5, 7, 9, 12 ], [ 5, 8, 10, 12, 13, 14 ],
[ 5, 6, 9, 11, 14, 15 ], [ 6, 7, 10, 12, 15, 16 ], [ 7, 8, 9, 11, 13, 16 ],
[ 1, 2, 9, 12, 14, 16 ], [ 2, 3, 9, 10, 13, 15 ], [ 3, 4, 10, 11, 14, 16 ],
[ 1, 4, 11, 12, 13, 15 ] ] )

```

When $n, m \geq 4$, TorusGraph(n, m) is actually a Whitney triangulation: Every triangle of the graph is a face of the triangulation. The clique behavior of these graphs were extensively studied in [9]. However, this operation constructs the described graph for all $n, m \geq 1$.

Example

```

gap> TorusGraph(2,4);
Graph( Category := SimpleGraphs, Order := 8, Size :=
20, Adjacencies := [ [ 2, 4, 5, 6, 8 ], [ 1, 3, 5, 6, 7 ],
[ 2, 4, 6, 7, 8 ], [ 1, 3, 5, 7, 8 ], [ 1, 2, 4, 6, 8 ],
[ 1, 2, 3, 5, 7 ], [ 2, 3, 4, 6, 8 ], [ 1, 3, 4, 5, 7 ] ] )
gap> TorusGraph(2,3);
Graph( Category := SimpleGraphs, Order := 6, Size :=
15, Adjacencies := [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 4, 5, 6 ],
[ 1, 2, 4, 5, 6 ], [ 1, 2, 3, 5, 6 ], [ 1, 2, 3, 4, 6 ],
[ 1, 2, 3, 4, 5 ] ] )

```

Note that in these cases, TorusGraph(n, m) is not 6-regular nor a Whitney triangulation.

B.1.167 TreeGraph

▷ TreeGraph($arity, depth$)

(operation)

▷ TreeGraph($ArityList$)

(operation)

Returns a tree, a connected cycle-free graph. In its second form, the vertices at height k (the root vertex has height 1 here) have `ArityList[k]` children. In its first form, all vertices, but the leaves, have `arity` children and the height of the leaves is `depth+1`.

Example

```
gap> TreeGraph(2,3);
Graph( Category := SimpleGraphs, Order := 15, Size :=
14, Adjacencies := [ [ 2, 3 ], [ 1, 4, 5 ], [ 1, 6, 7 ], [ 2, 8, 9 ],
[ 2, 10, 11 ], [ 3, 12, 13 ], [ 3, 14, 15 ], [ 4 ], [ 4 ], [ 5 ],
[ 5 ], [ 6 ], [ 6 ], [ 7 ], [ 7 ] ] )
gap> TreeGraph([3,2,2]);
Graph( Category := SimpleGraphs, Order := 22, Size :=
21, Adjacencies := [ [ 2, 3, 4 ], [ 1, 5, 6 ], [ 1, 7, 8 ],
[ 1, 9, 10 ], [ 2, 11, 12 ], [ 2, 13, 14 ], [ 3, 15, 16 ],
[ 3, 17, 18 ], [ 4, 19, 20 ], [ 4, 21, 22 ], [ 5 ], [ 5 ], [ 6 ],
[ 6 ], [ 7 ], [ 7 ], [ 8 ], [ 8 ], [ 9 ], [ 9 ], [ 10 ], [ 10 ] ] )
```

B.1.168 TrivialGraph

▷ TrivialGraph (global variable)

The one vertex graph.

Example

```
gap> TrivialGraph;
Graph( Category := SimpleGraphs, Order := 1, Size :=
0, Adjacencies := [ [ ] ] )
```

B.1.169 UFFind

▷ UFFind(*UFS*, *x*) (function)

For internal use. Implements the *find* operation on the *union-find structure*.

B.1.170 UFUnite

▷ UFUnite(*UFS*, *x*, *y*) (function)

For internal use. Implements the *unite* operation on the *union-find structure*.

B.1.171 UndirectedGraphs

▷ UndirectedGraphs(*G*) (function)

UndirectedGraphs is a graph category in YAGS. A graph in this category may contain edges and loops, but no arrows. The parent of this category is Graphs.

Example

```
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=Graphs);
Graph( Category := Graphs, Order := 3, Size := 4, Adjacencies :=
[ [ 1, 2 ], [ 1 ], [ 2 ] ] )
gap> GraphByWalks([1,1],[1,2],[2,1],[3,2]:GraphCategory:=UndirectedGraphs);
```

```
Graph( Category := UndirectedGraphs, Order := 3, Size :=
3, Adjacencies := [ [ 1, 2 ], [ 1, 3 ], [ 2 ] ] )
```

B.1.172 UnitsRingGraph

▷ UnitsRingGraph(*Rng*)

(operation)

Returns the graph G whose vertices are the elements of Rng such that x is adjacent to y iff $x+z=y$ for some unit z of Rng .

Example

```
gap> UnitsRingGraph(ZmodnZ(8));
Graph( Category := SimpleGraphs, Order := 8, Size :=
16, Adjacencies := [ [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ],
[ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ], [ 1, 3, 5, 7 ], [ 2, 4, 6, 8 ],
[ 1, 3, 5, 7 ] ] )
```

B.1.173 VertexDegree

▷ VertexDegree(G , x)

(operation)

Returns the degree of vertex x in Graph G .

Example

```
gap> g:=PathGraph(3);
Graph( Category := SimpleGraphs, Order := 3, Size :=
2, Adjacencies := [ [ 2 ], [ 1, 3 ], [ 2 ] ] )
gap> VertexDegree(g,1);
1
gap> VertexDegree(g,2);
2
```

B.1.174 VertexDegrees

▷ VertexDegrees(G)

(operation)

Returns the list of degrees of the vertices in graph G .

Example

```
gap> g:=GemGraph;
Graph( Category := SimpleGraphs, Order := 5, Size :=
7, Adjacencies := [ [ 2, 3, 4, 5 ], [ 1, 3 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 4 ] ] )
gap> VertexDegrees(g);
[ 4, 2, 3, 3, 2 ]
```

B.1.175 VertexNames

▷ VertexNames(G)

(attribute)

Return the list of names of the vertices of G . The vertices of a graph in YAGS are always $\{1, 2, \dots, \text{Order}(G)\}$, but depending on how the graph was constructed, its vertices may have also

some *names*, that help us identify the origin of the vertices. YAGS will always try to store meaningful names for the vertices. For example, in the case of the LineGraph, the vertex names of the new graph are the edges of the old graph.

Example

```
gap> g:=LineGraph(DiamondGraph);
Graph( Category := SimpleGraphs, Order := 5, Size :=
8, Adjacencies := [ [ 2, 3, 4 ], [ 1, 3, 4, 5 ], [ 1, 2, 5 ],
[ 1, 2, 5 ], [ 2, 3, 4 ] ] )
gap> VertexNames(g);
[ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 3, 4 ] ]
gap> Edges(DiamondGraph);
[ [ 1, 2 ], [ 1, 3 ], [ 1, 4 ], [ 2, 3 ], [ 3, 4 ] ]
```

B.1.176 Vertices

▷ Vertices(*G*)

(operation)

Returns the list [1..Order(*G*)].

Example

```
gap> Vertices(Icosahedron);
[ 1 .. 12 ]
```

B.1.177 WheelGraph

▷ WheelGraph(*n*)

(operation)

▷ WheelGraph(*n*, *r*)

(operation)

In its first form WheelGraph returns the wheel graph on $n+1$ vertices. This is the cone of a cycle: a central vertex adjacent to all the vertices of an n -cycle.

Example

```
gap> WheelGraph(5);
Graph( Category := SimpleGraphs, Order := 6, Size :=
10, Adjacencies := [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6 ], [ 1, 2, 4 ],
[ 1, 3, 5 ], [ 1, 4, 6 ], [ 1, 2, 5 ] ] )
```

In its second form, WheelGraph returns the wheel graph, but adding $r-1$ layers, each layer is a new n -cycle joined to the previous layer by a zigzagging $2n$ -cycle. This graph is a triangulation of the disk.

Example

```
gap> WheelGraph(5,2);
Graph( Category := SimpleGraphs, Order := 11, Size :=
25, Adjacencies := [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6, 7, 8 ],
[ 1, 2, 4, 8, 9 ], [ 1, 3, 5, 9, 10 ], [ 1, 4, 6, 10, 11 ],
[ 1, 2, 5, 7, 11 ], [ 2, 6, 8, 11 ], [ 2, 3, 7, 9 ],
[ 3, 4, 8, 10 ], [ 4, 5, 9, 11 ], [ 5, 6, 7, 10 ] ] )
gap> WheelGraph(5,3);
Graph( Category := SimpleGraphs, Order := 16, Size :=
40, Adjacencies := [ [ 2, 3, 4, 5, 6 ], [ 1, 3, 6, 7, 8 ],
[ 1, 2, 4, 8, 9 ], [ 1, 3, 5, 9, 10 ], [ 1, 4, 6, 10, 11 ],
[ 1, 2, 5, 7, 11 ], [ 2, 6, 8, 11, 12, 13 ], [ 2, 3, 7, 9, 13, 14 ],
```

```
[ 3, 4, 8, 10, 14, 15 ], [ 4, 5, 9, 11, 15, 16 ],
[ 5, 6, 7, 10, 12, 16 ], [ 7, 11, 13, 16 ], [ 7, 8, 12, 14 ],
[ 8, 9, 13, 15 ], [ 9, 10, 14, 16 ], [ 10, 11, 12, 15 ] ] )
```

B.1.178 YAGSExec

▷ YAGSExec(*ProgName*, *InString*)

(operation)

For internal use. Calls external program *ProgName* located in directory *YAGS-DIR/bin/* feeding it with *InString* as input and returning the output of the external program as a string. fail is returned if the program could not be located.

Example

```
gap> YAGSExec("time","");
"1415551127\n"
gap> YAGSExec("nauty","l=0$=1dacn=5 g1,2,3. xbzq");
"(4,5)\n(2,3)\n[2,3,4,5,1]\n[\n"cb0c\n","\n484f264\n","\nb0e19f1\n"]\n"
```

Currently, this operation is not working on MS Windows nor in Mac OS X.

B.1.179 YAGSInfo

▷ YAGSInfo

(global variable)

A global record where much YAGS-related information is stored. This is intended for internal use, and much of this information is undocumented, but some of the data stored here could possibly be useful for advanced users.

However, storing user information in this record and/or changing the values of the stored information is discouraged and may produce unpredictable results and an unstable system.

Example

```
gap> YAGSInfo;
rec( Arch := 1, AuxInfo := "/dev/null",
  DataDirectory := "/opt/gap4r7/pkg/yags/data",
  Directory := "/opt/gap4r7/pkg/yags",
  Draw :=
    rec( opts := [ ],
      prog := "/opt/gap4r7/pkg/yags/bin/draw/application.linux64/draw" ),
  Version := "0.0.1",
  graph6 := rec( BinListToNum := function( L ) ... end,
    BinListToNumList := function( L ) ... end,
    HararyList := [ [ 1, 0, 1 ], [ 2, 0, 1 ], [ 2, 1, 1 ],
      [ 3, 0, 1 ], [ 3, 1, 1 ], [ 3, 2, 1 ], [ 3, 3, 1 ],
      [ 4, 0, 1 ], [ 4, 1, 1 ], [ 4, 2, 1 ], [ 4, 3, 3 ],
      [ 4, 2, 2 ], [ 4, 3, 1 ], [ 4, 3, 2 ], [ 4, 4, 1 ],

      --- many more lines here ---

      [ 6, 13, 1 ], [ 6, 11, 7 ], [ 6, 11, 9 ], [ 6, 11, 8 ],
      [ 6, 12, 4 ], [ 6, 12, 5 ], [ 6, 13, 2 ], [ 6, 14, 1 ],
      [ 6, 15, 1 ] ], McKayN := function( n ) ... end,
    McKayR := function( L ) ... end,
```

```
NumListToString := function( L ) ... end,  
NumToBinList := function( n ) ... end,  
PadLeftnSplitList6 := function( L ) ... end,  
PadRightnSplitList6 := function( L ) ... end,  
StringToBinList := function( Str ) ... end ) )
```

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