```
# Package imports
import numpy as np
import matplotlib.pyplot as plt
from testCases import *
import sklearn
import sklearn.datasets
import sklearn.linear_model
from \ planar\_utils \ import \ plot\_decision\_boundary, \ sigmoid, \ load\_planar\_dataset, \ load\_extra\_datasets
%matplotlib inline
np.random.seed(1) # set a seed so that the results are consistent
X, Y = load_planar_dataset()
# Visualize the data:
\verb|plt.scatter(X[0, :], X[1, :], c=Y, s=40, cmap=plt.cm.Spectral);|\\
       3
       2
       1
       0
      -1
      -2
      -3
### START CODE HERE ### (≈ 3 lines of code)
shape_X = X.shape
shape Y = Y.shape
m = shape_X[1]
                     # training set size
### END CODE HERE ###
print ('The shape of X is: ' + str(shape_X))
print ('The shape of Y is: ' + str(shape_Y))
print ('I have m = %d training examples!' % (m))
     The shape of X is: (2, 400)
     The shape of Y is: (1, 400)
     I have m = 400 training examples!
# Train the logistic regression classifier
clf = sklearn.linear_model.LogisticRegressionCV();
clf.fit(X.T, Y.T);
     /usr/local/lib/python3.8/dist-packages/sklearn/utils/validation.py:993: DataConversionWarning: A column-vector y was passed when a
       y = column_or_1d(y, warn=True)
    4
# Plot the decision boundary for logistic regression
plot_decision_boundary(lambda x: clf.predict(x), X, Y)
plt.title("Logistic Regression")
# Print accuracy
LR_predictions = clf.predict(X.T)
print ('Accuracy of logistic regression: %d ' % float((np.dot(Y,LR_predictions)) + np.dot(1-Y,1-LR_predictions))/float(Y.size)*100) +
       '% ' + "(percentage of correctly labelled datapoints)")
```

```
# GRADED FUNCTION: layer_sizes
def layer_sizes(X, Y):
    Arguments:
    X -- input dataset of shape (input size, number of examples)
    Y -- labels of shape (output size, number of examples)
    Returns:
    n_x -- the size of the input layer
    n_h -- the size of the hidden layer
    n\_y -- the size of the output layer
    ### START CODE HERE ### (≈ 3 lines of code)
    n_x = X.shape[0] # size of input layer
    n_h = 4
    n_y = Y.shape[0] # size of output layer
    ### END CODE HERE ###
    return (n_x, n_h, n_y)
X_assess, Y_assess = layer_sizes_test_case()
(n x, n h, n y) = layer sizes(X assess, Y assess)
print("The size of the input layer is: n_x = " + str(n_x))
print("The size of the hidden layer is: n_h = " + str(n_h))
print("The size of the output layer is: n_y = " + str(n_y))
     The size of the input layer is: n_x = 5
     The size of the hidden layer is: n_h = 4
     The size of the output layer is: n_y = 2
# GRADED FUNCTION: initialize_parameters
def initialize_parameters(n_x, n_h, n_y):
    ....
    Argument:
    n_x -- size of the input layer
    n_h -- size of the hidden layer
    n\_y -- size of the output layer
    Returns:
    params -- python dictionary containing your parameters:
                    W1 -- weight matrix of shape (n_h, n_x)
                    b1 -- bias vector of shape (n_h, 1)
                    W2 -- weight matrix of shape (n_y, n_h)
                    b2 -- bias vector of shape (n_y, 1)
    np.random.seed(2) # we set up a seed so that your output matches ours although the initialization is random.
    ### START CODE HERE ### (\approx 4 lines of code)
    W1 = np.random.randn(n_h, n_x) * 0.01
    b1 = np.zeros(shape=(n_h, 1))
    W2 = np.random.randn(n_y, n_h) * 0.01
    b2 = np.zeros(shape=(n_y, 1))
    ### END CODE HERE ###
    assert (W1.shape == (n_h, n_x))
    assert (b1.shape == (n_h, 1))
    assert (W2.shape == (n_y, n_h))
    assert (b2.shape == (n_y, 1))
    parameters = {"W1": W1,
                   "b1": b1,
                   "W2": W2,
                   "b2": b2}
    return parameters
n_x, n_h, n_y = initialize_parameters_test_case()
parameters = initialize_parameters(n_x, n_h, n_y)
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))
```

```
W1 = [[-0.00416758 - 0.00056267]]
      [-0.02136196 0.01640271]
      [-0.01793436 -0.00841747]
      [ 0.00502881 -0.01245288]]
     b1 = [[0.]]
      [0.]
      [0.]
      [0.]]
     W2 = [[-0.01057952 - 0.00909008 \ 0.00551454 \ 0.02292208]]
     b2 = [[0.]]
# GRADED FUNCTION: forward_propagation
def forward_propagation(X, parameters):
    Argument:
    X -- input data of size (n_x, m)
    parameters -- python dictionary containing your parameters (output of initialization function)
    A2 -- The sigmoid output of the second activation
    cache -- a dictionary containing "Z1", "A1", "Z2" and "A2"
    \ensuremath{\mathtt{\#}} Retrieve each parameter from the dictionary "parameters"
    ### START CODE HERE ### (≈ 4 lines of code)
    W1 = parameters['W1']
    b1 = parameters['b1']
    W2 = parameters['W2']
    b2 = parameters['b2']
    ### END CODE HERE ###
    # Implement Forward Propagation to calculate A2 (probabilities)
    ### START CODE HERE ### (\approx 4 lines of code)
    Z1 = np.dot(W1, X) + b1
    A1 = np.tanh(Z1)
    Z2 = np.dot(W2, A1) + b2
    A2 = sigmoid(Z2)
    ### END CODE HERE ###
    assert(A2.shape == (1, X.shape[1]))
    cache = {"Z1": Z1,
              "A1": A1,
             "Z2": Z2,
             "A2": A2}
    return A2, cache
X_assess, parameters = forward_propagation_test_case()
A2, cache = forward_propagation(X_assess, parameters)
\ensuremath{\mathtt{\#}} Note: we use the mean here just to make sure that your output matches ours.
print(np.mean(cache['Z1']), np.mean(cache['A1']), np.mean(cache['A2']))
     \hbox{-0.0004997557777419913} \hbox{ -0.000496963353231779} \hbox{ 0.00043818745095914653} \hbox{ 0.500109546852431}
# GRADED FUNCTION: compute cost
def compute_cost(A2, Y, parameters):
    Computes the cross-entropy cost given in equation (13)
    Arguments:
    A2 -- The sigmoid output of the second activation, of shape (1, number of examples)
    Y -- "true" labels vector of shape (1, number of examples)
    parameters -- python dictionary containing your parameters W1, b1, W2 and b2
    Returns:
    cost -- cross-entropy cost given equation (13)
    m = Y.shape[1] # number of example
    # Compute the cross-entropy cost
    ### START CODE HERE ### (\approx 2 lines of code)
    logprobs = np.dot(Y, np.log(A2).T) + np.dot(1 - Y, np.log(1 - A2).T)
    cost = np.float64(-logprobs / m)
    ### END CODE HERE ###
    cost = np.squeeze(cost)
                               # makes sure cost is the dimension we expect.
```

```
# E.g., turns [[17]] into 17
    assert(isinstance(cost, float))
    return cost
A2, Y_assess, parameters = compute_cost_test_case()
print("cost = " + str(compute_cost(A2, Y_assess, parameters)))
     cost = 0.6929198937761264
# GRADED FUNCTION: backward_propagation
def backward_propagation(parameters, cache, X, Y):
    Implement the backward propagation using the instructions above.
    Arguments:
    parameters -- python dictionary containing our parameters
    cache -- a dictionary containing "Z1", "A1", "Z2" and "A2".
    X -- input data of shape (2, number of examples)
    Y -- "true" labels vector of shape (1, number of examples)
    Returns:
    grads -- python dictionary containing your gradients with respect to different parameters
    m = X.shape[1]
    # First, retrieve W1 and W2 from the dictionary "parameters".
    ### START CODE HERE ### (≈ 2 lines of code)
    W1 = parameters['W1']
    W2 = parameters['W2']
    ### END CODE HERE ###
    # Retrieve also A1 and A2 from dictionary "cache".
    ### START CODE HERE ### (\approx 2 lines of code)
    A1 = cache['A1']
    A2 = cache['A2']
    ### END CODE HERE ###
    # Backward propagation: calculate dW1, db1, dW2, db2.
    ### START CODE HERE ### (pprox 6 lines of code, corresponding to 6 equations on slide above)
    dZ2 = A2 - Y
    dW2 = np.dot(dZ2, A1.T) / m
    db2 = np.sum(dZ2, axis=1, keepdims=True) / m
    dZ1 = np.dot(W2.T, dZ2) * (1 - np.power(A1, 2))
    dW1 = np.dot(dZ1, X.T) / m
    db1 = np.sum(dZ1, axis=1, keepdims=True) / m
    ### END CODE HERE ###
    grads = {"dW1": dW1,
             "db1": db1,
             "dW2": dW2,
             "db2": db2}
    return grads
parameters, cache, X_assess, Y_assess = backward_propagation_test_case()
grads = backward_propagation(parameters, cache, X_assess, Y_assess)
print ("dW1 = "+ str(grads["dW1"]))
print ("db1 = "+ str(grads["db1"]))
print ("dW2 = "+ str(grads["dW2"]))
print ("db2 = "+ str(grads["db2"]))
     dW1 = [[ 0.01018708 - 0.00708701]
      [ 0.00873447 -0.0060768 ]
      [-0.00530847 0.00369379]
      [-0.02206365 0.01535126]]
     db1 = [[-0.00069728]
      [-0.00060606]
      [ 0.000364 ]
      [ 0.00151207]]
     dW2 = [[ 0.00363613   0.03153604   0.01162914   -0.01318316]]
     db2 = [[0.06589489]]
# GRADED FUNCTION: update_parameters
def update_parameters(parameters, grads, learning_rate = 1.2):
```

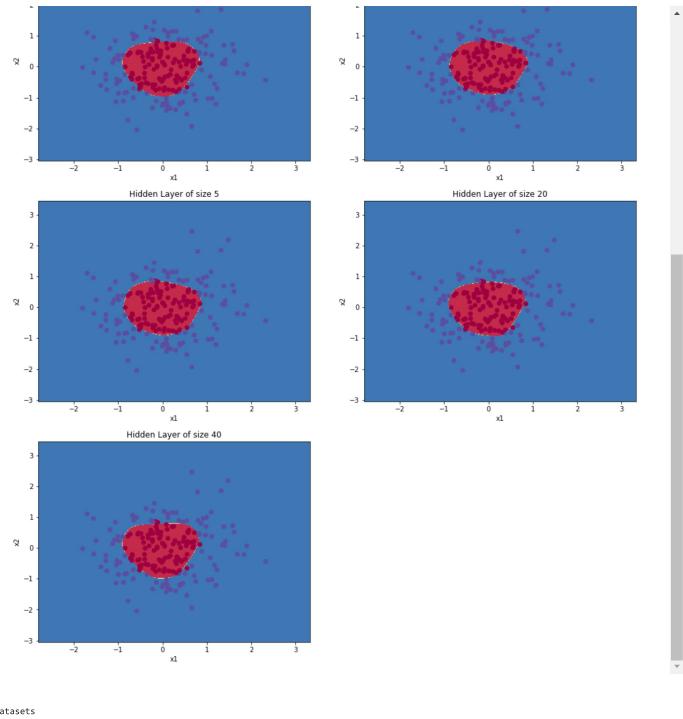
```
Updates parameters using the gradient descent update rule given above
    Arguments:
    parameters -- python dictionary containing your parameters
    grads -- python dictionary containing your gradients
    Returns:
    parameters -- python dictionary containing your updated parameters
    # Retrieve each parameter from the dictionary "parameters"
    ### START CODE HERE ### (≈ 4 lines of code)
    W1 = parameters['W1']
    b1 = parameters['b1']
    W2 = parameters['W2']
    b2 = parameters['b2']
    ### END CODE HERE ###
    # Retrieve each gradient from the dictionary "grads"
    ### START CODE HERE ### (≈ 4 lines of code)
    dW1 = grads['dW1']
    db1 = grads['db1']
    dW2 = grads['dW2']
    db2 = grads['db2']
    ## END CODE HERE ###
    # Update rule for each parameter
    ### START CODE HERE ### (≈ 4 lines of code)
    W1 = W1 - learning_rate * dW1
    b1 = b1 - learning_rate * db1
    W2 = W2 - learning_rate * dW2
    b2 = b2 - learning_rate * db2
    ### END CODE HERE ###
    parameters = {"W1": W1,
                  "b1": b1,
                  "W2": W2,
                  "b2": b2}
    return parameters
parameters, grads = update_parameters_test_case()
parameters = update_parameters(parameters, grads)
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))
     W1 = [[-0.00643025 \quad 0.01936718]]
      [-0.02410458 0.03978052]
      [-0.01653973 -0.02096177]
      [ 0.01046864 -0.05990141]]
     b1 = [[-1.02420756e-06]
     [ 1.27373948e-05]
      [ 8.32996807e-07]
      [-3.20136836e-06]]
     W2 = [[-0.01041081 - 0.04463285 0.01758031 0.04747113]]
     b2 = [[0.00010457]]
# GRADED FUNCTION: nn_model
def nn_model(X, Y, n_h, num_iterations = 10000, print_cost=False):
    Arguments:
    X -- dataset of shape (2, number of examples)
    Y -- labels of shape (1, number of examples)
    n h -- size of the hidden layer
    num_iterations -- Number of iterations in gradient descent loop
    print_cost -- if True, print the cost every 1000 iterations
    parameters -- parameters learnt by the model. They can then be used to predict.
    np.random.seed(3)
    n_x = layer_sizes(X, Y)[0]
    n_y = layer_sizes(X, Y)[2]
    # Initialize parameters, then retrieve W1, b1, W2, b2. Inputs: "n_x, n_h, n_y". Outputs = "W1, b1, W2, b2, parameters".
    ### START CODE HERE ### (≈ 5 lines of code)
    parameters = initialize_parameters(n_x, n_h, n_y)
```

W1 = parameters['W1']
b1 = parameters['b1']

```
b2 = parameters['b2']
    ### END CODE HERE ###
    # Loop (gradient descent)
    for i in range(0, num_iterations):
        ### START CODE HERE ### (≈ 4 lines of code)
        # Forward propagation. Inputs: "X, parameters". Outputs: "A2, cache".
        A2, cache = forward_propagation(X, parameters)
        # Cost function. Inputs: "A2, Y, parameters". Outputs: "cost".
        cost = compute_cost(A2, Y, parameters)
        # Backpropagation. Inputs: "parameters, cache, X, Y". Outputs: "grads".
        grads = backward_propagation(parameters, cache, X, Y)
        # Gradient descent parameter update. Inputs: "parameters, grads". Outputs: "parameters".
        parameters = update_parameters(parameters, grads)
        ### END CODE HERE ###
        # Print the cost every 1000 iterations
        if print cost and i % 1000 == 0:
            print ("Cost after iteration %i: %f" %(i, cost))
    return parameters
X_assess, Y_assess = nn_model_test_case()
parameters = nn_model(X_assess, Y_assess, 4, num_iterations=10000, print_cost=False)
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))
     <ipython-input-14-ccd59e612351>:20: RuntimeWarning: divide by zero encountered in log
       logprobs = np.dot(Y, np.log(A2).T) + np.dot(1 - Y, np.log(1 - A2).T)
     /content/planar_utils.py:34: RuntimeWarning: overflow encountered in exp
      s = 1/(1+np.exp(-x))
     W1 = [[-4.18497132 5.33206757]]
     [-7.53803917 1.20755745]
      [-4.19300026 5.32616513]
      [ 7.53798166 -1.20759037]]
     b1 = [[2.32932729]]
      [ 3.81001689]
      [ 2.33008569]
      [-3.81011712]]
     W2 = [[-6033.82357224 -6008.14296509 -6033.08780459 6008.07954278]]
     b2 = [[-52.67922744]]
# GRADED FUNCTION: predict
def predict(parameters, X):
    Using the learned parameters, predicts a class for each example in \boldsymbol{X}
    Arguments:
    parameters -- python dictionary containing your parameters
    X -- input data of size (n_x, m)
    predictions -- vector of predictions of our model (red: 0 / blue: 1)
    # Computes probabilities using forward propagation, and classifies to 0/1 using 0.5 as the threshold.
    ### START CODE HERE ### (\approx 2 lines of code)
    A2, cache = forward_propagation(X, parameters)
    predictions = (A2 > .5)
    ### END CODE HERE ###
    return predictions
parameters, X_assess = predict_test_case()
predictions = predict(parameters, X_assess)
print("predictions mean = " + str(np.mean(predictions)))
```

W2 = parameters['W2']

```
# Build a model with a n_h-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 5, num_iterations = 10000, print_cost=True)
# Plot the decision boundary
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(4))
     Cost after iteration 0: 0.693252
     Cost after iteration 1000: 0.283771
     Cost after iteration 2000: 0.270689
     Cost after iteration 3000: 0.263510
     Cost after iteration 4000: 0.258455
     Cost after iteration 5000: 0.250679
     Cost after iteration 6000: 0.224348
     Cost after iteration 7000: 0.219895
     Cost after iteration 8000: 0.180043
     Cost after iteration 9000: 0.175090
     Text(0.5, 1.0, 'Decision Boundary for hidden layer size 4')
                Decision Boundary for hidden layer size 4
         4
         2
     Ŋ
        0
        -2
# Print accuracy
predictions = predict(parameters, X)
print ('Accuracy: \%d' \% float((np.dot(Y,predictions.T)) + np.dot(1-Y,1-predictions.T))/float(Y.size)*100) + '\%')
     Accuracy: 91%
# This may take about 2 minutes to run
plt.figure(figsize=(16, 32))
hidden layer sizes = [1, 2, 3, 4, 5, 20, 40]
for i, n_h in enumerate(hidden_layer_sizes):
    plt.subplot(5, 2, i+1)
    plt.title('Hidden Layer of size %d' % n_h)
    parameters = nn\_model(X, Y, n\_h, num\_iterations = 5000)
    plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
    predictions = predict(parameters, X)
    accuracy = float((np.dot(Y,predictions.T) + np.dot(1-Y,1-predictions.T))/float(Y.size)*100)
    print ("Accuracy for {} hidden units: {} %".format(n_h, accuracy))
```



Y = Y%2

Visualize the data

 $plt.scatter(X[0, :], \ X[1, :], \ c=Y, \ s=40, \ cmap=plt.cm.Spectral);$

