

# your special pdf

## what's modular arithmetic ?



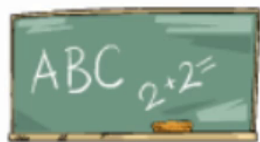
$$14 \% 3 = ?$$

$$14 \% 3 = 2$$

$$x \% y = m$$

find the smallest non negative  
number  $m$  such that  $x-m$   
is multiple of  $y$

## math behind modular arithmetic



$$14 \% 3 = 2$$

$$x \% y = m$$

$$4 * 3 + 2 = 14$$

$$q * y + m = x$$



$$23 \% 6 = ? \quad 5$$

$$2 \% 2 = ? \quad 0$$

$$4 \% 5 = ? \quad 4$$

$$0 \% 2 = ? \quad 0$$

$$1 \% 0 = ? \quad \text{math error}$$

$$12 \% 6 = ? \quad 0$$

↙ cyclic

in the previous example  $\text{num} \% 5$



0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 0 1 2 3 4

you can easily see that if we want  
 $\text{num} \% x$  our mod range from 0 to  $x-1$

↙  $(a+b) \% c = ((a \% c) + (b \% c)) \% c$

↙  $(a*b) \% c = ((a \% c) * (b \% c)) \% c$



$a \% c$  in range 0 to  $c-1$

$b \% c$  in range 0 to  $c-1$

↙  $(a-b) \% c = ((a \% c) - (b \% c) + c) \% c$

↙  $(a/b) \% c = ((a \% c) * (b^{-1} \% c)) \% c$