

3D Minigolf

An Analysis of Different Approaches handle complex maze-like courses

Project 1-2

Phase 3

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Problem definition

- Extend AI bot for maze-like courses
- Introduce small random error, which the AI bot should deal with
- Hold a competition between the bots

Contents

- Physics Engine
- Terrain Generation
- Search Algorithms
- Experiments
- Conclusion

Physics Engine

Runge-Kutta 4th order:

$$k_{i,1} = h_i \cdot f(t_i, w_i)$$

$$k_{i,2} = h_i \cdot f\left(t_i + \frac{1}{2}h_i, w_i + \frac{1}{2}k_{i,1}\right)$$

$$k_{i,3} = h_i \cdot f\left(t_i + \frac{1}{2}h_i, w_i + \frac{1}{2}k_{i,2}\right)$$

$$k_{i,4} = h_i \cdot f(t_i + h_i, w_i + k_{i,3})$$

$$w_{i+1} = w_i + \frac{1}{6} \cdot (k_{i,1} + 2k_{i,2} + 2k_{i,3} + k_{i,4})$$

t_i = time at step i

w_i = function approximation at t_i

h_i = the timestep, i.e. $t_{i+1} - t_i$

f = the derivative function of the desired function

Runge-Kutta 4th order vs Euler

Euler's Method (1st order):

$$w_{i+1} = w_i + h \cdot f(t_i, w_i)$$

- How do they compare in computational time?
 - 1 iteration (i.e. updating the position of the ball once):
 - Euler's method : 336 885 ns
 - RK4: 1 414 861 ns
- Is this an issue?
 - 1/60th of a second: 16 666 666 ns

Physics engine

Euler vs. Runge-Kutta 4th order: Euler / Runge-Kutta

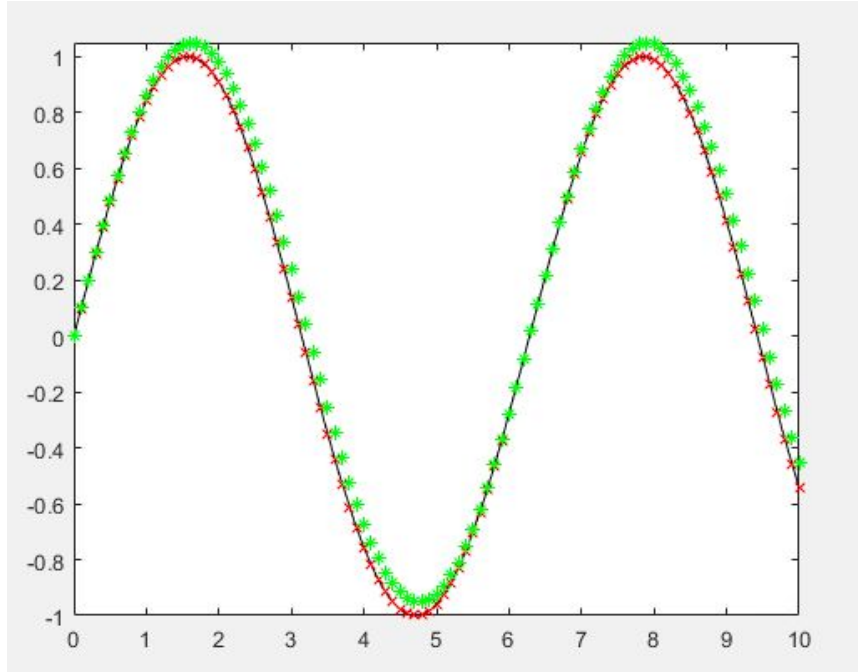


fig 1

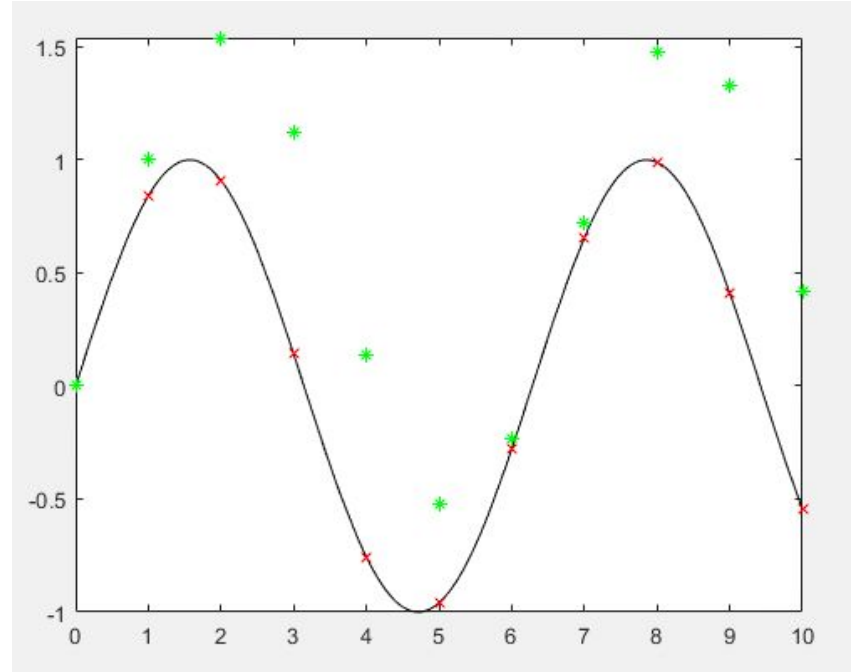
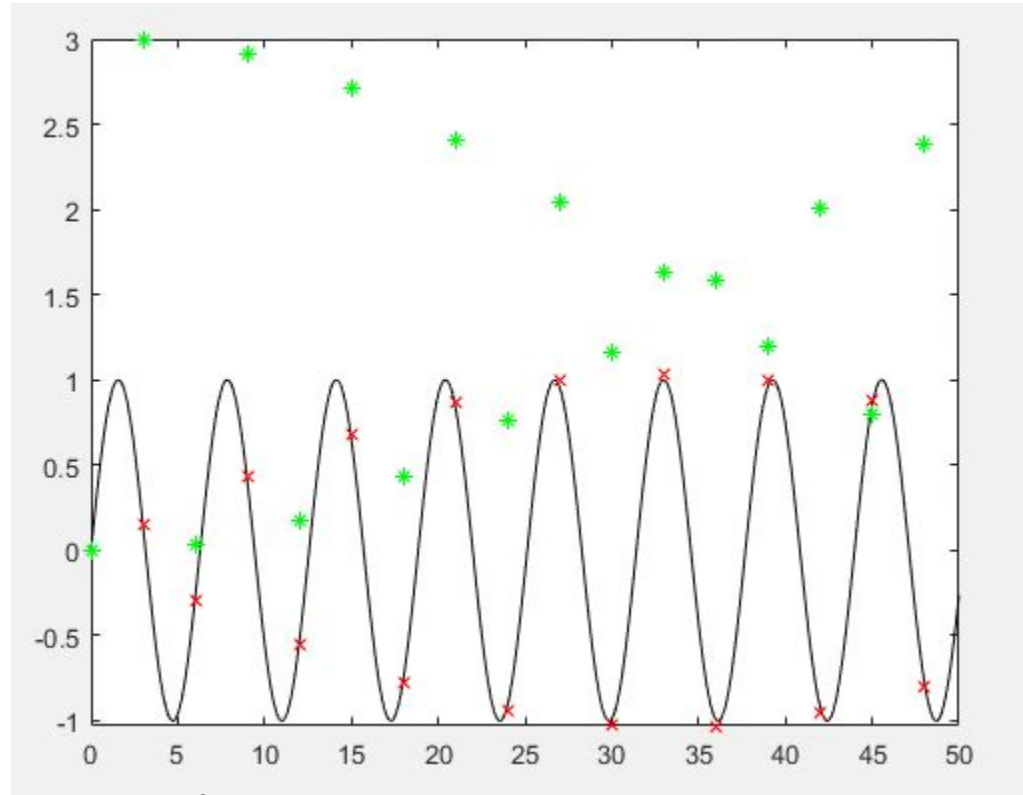


fig 2

Function $f(x) = \sin(x)$ approximated by Euler's method and Runge-Kutta 4th order method with stepsize 0.1 (fig 1) and stepsize 1 (fig 2)

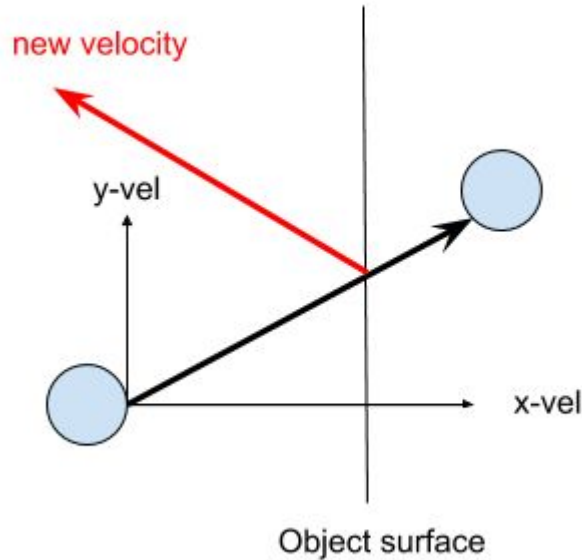
Runge-Kutta 4th order vs Euler

- Euler is faster
- Runge-Kutta is more accurate and reliable
- Runge-Kutta doesn't sacrifice computational time while remaining accurate



Function $f(x) = \sin(x)$ approximated by Euler's method and Runge-Kutta 4th order method with stepsize 3

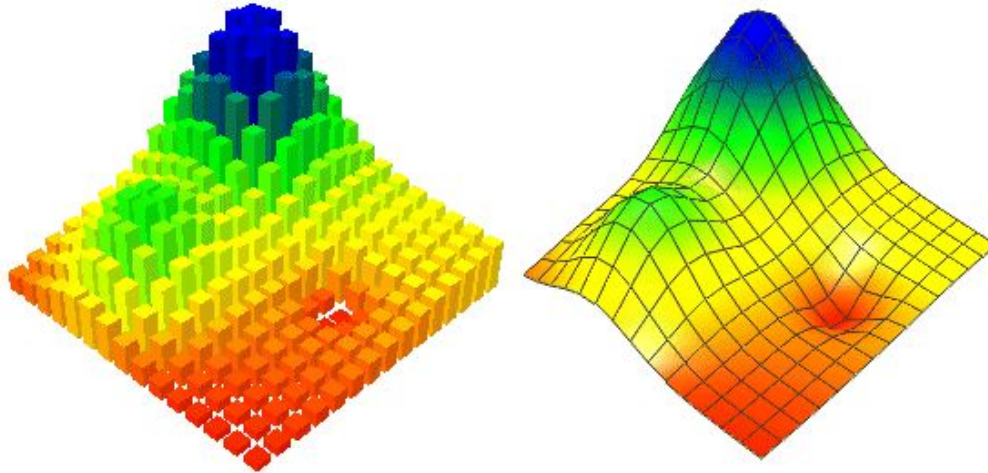
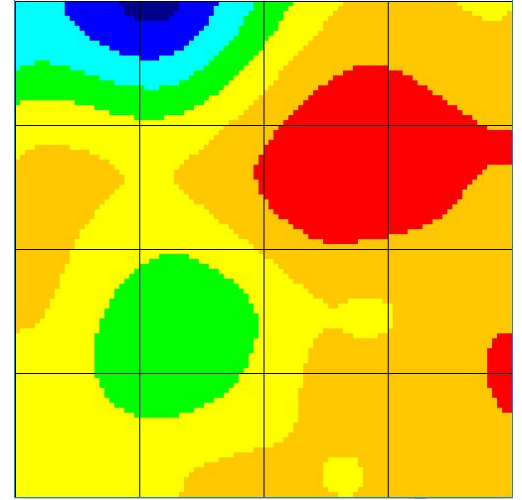
Collision detection



- Check coordinates
- Find intersection of velocity and object surface
- Reflect back accordingly

Terrain Generation

- Set of points
- Bicubic Interpolation
- Regular Grid of Unit Squares
- Polynomials describing surface



Terrain Generation

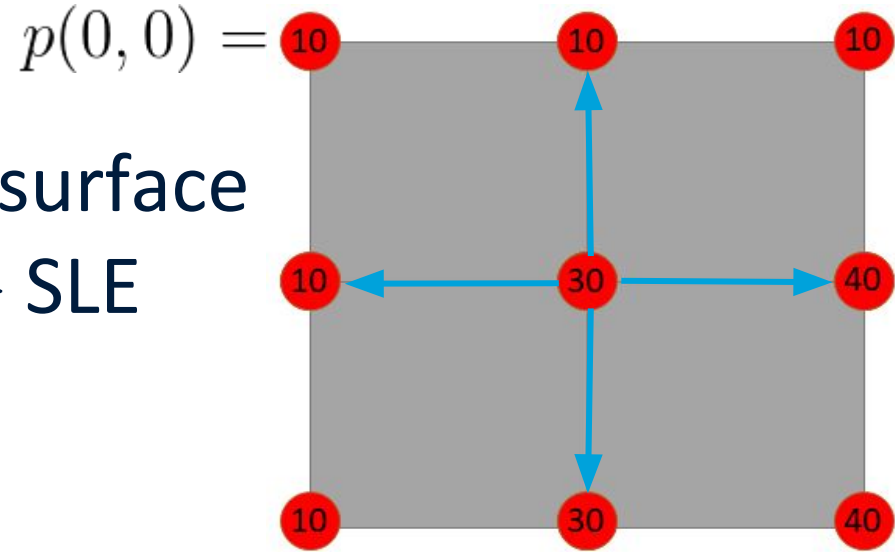
- Polynomials describing surface
- Sets of coefficients $a \rightarrow$ SLE

$$(1) \quad p(x, y) = \sum_{i=0}^3 \sum_{j=0}^3 a_{ij} x^i y^j$$

$$(2) \quad p_x(x, y) = \sum_{i=1}^3 \sum_{j=0}^3 a_{ij} i x^{i-1} y^j$$

$$(3) \quad p_y(x, y) = \sum_{i=0}^3 \sum_{j=1}^3 a_{ij} x^i j y^{j-1}$$

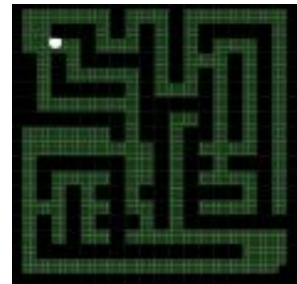
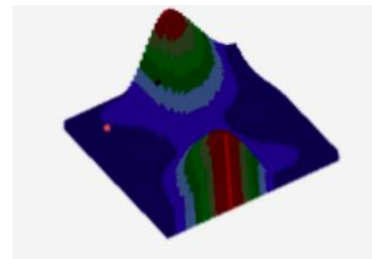
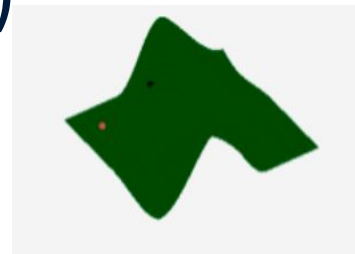
$$(4) \quad p_{xy}(x, y) = \sum_{i=1}^3 \sum_{j=1}^3 a_{ij} i x^{i-1} j y^{j-1}$$

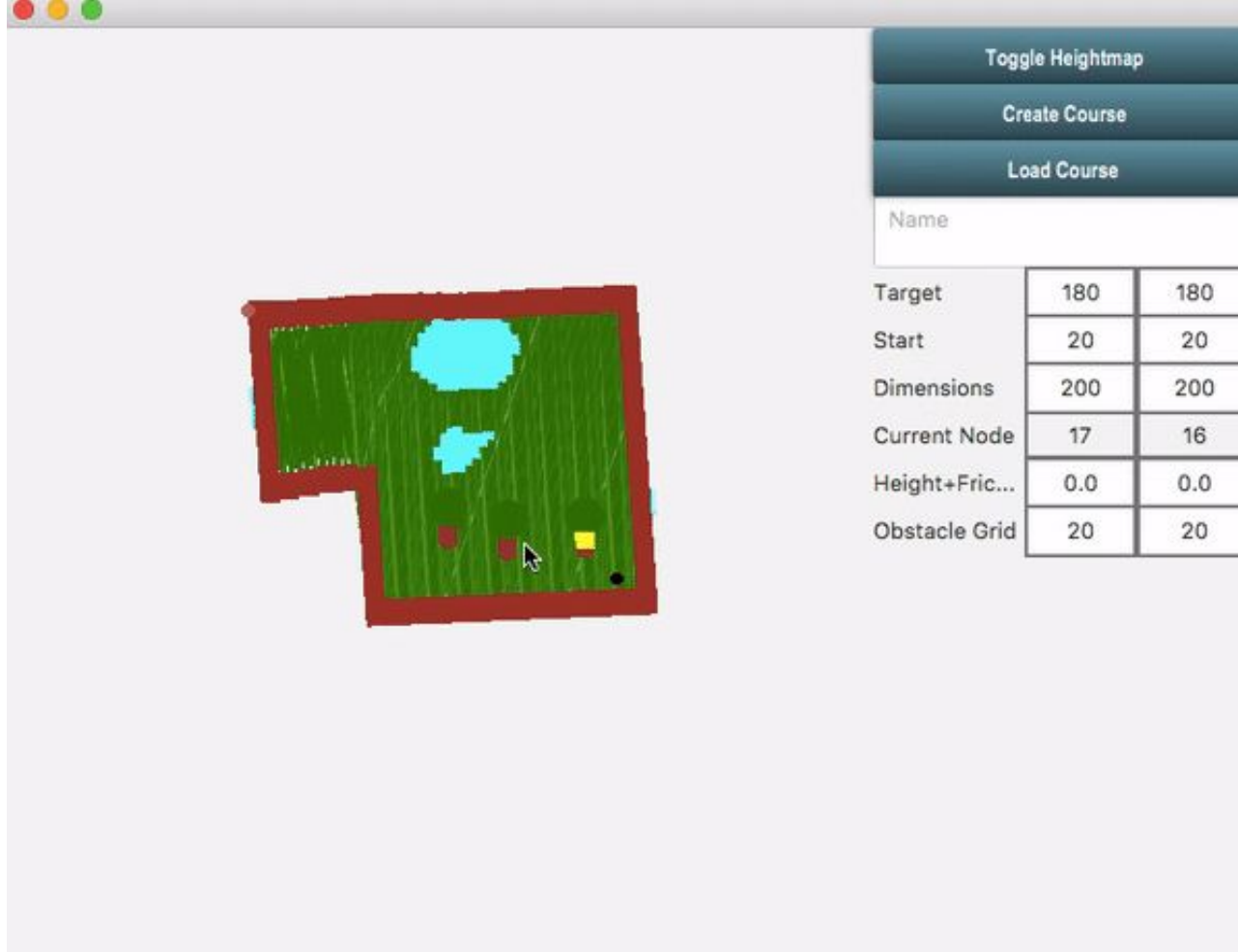


$$p_x(1, 1) = \frac{p(0, 3) - p(0, 1)}{2}$$

Visualisation Techniques

- JavaFX(Triangle Mesh, FXML)
- Features:
 - course creator
 - heightmap
 - minimap
 - level saving, loading





AI Algorithm

1. hilly surface - no obstacles
2. hilly surface - water - obstacles - maze
3. noise factor

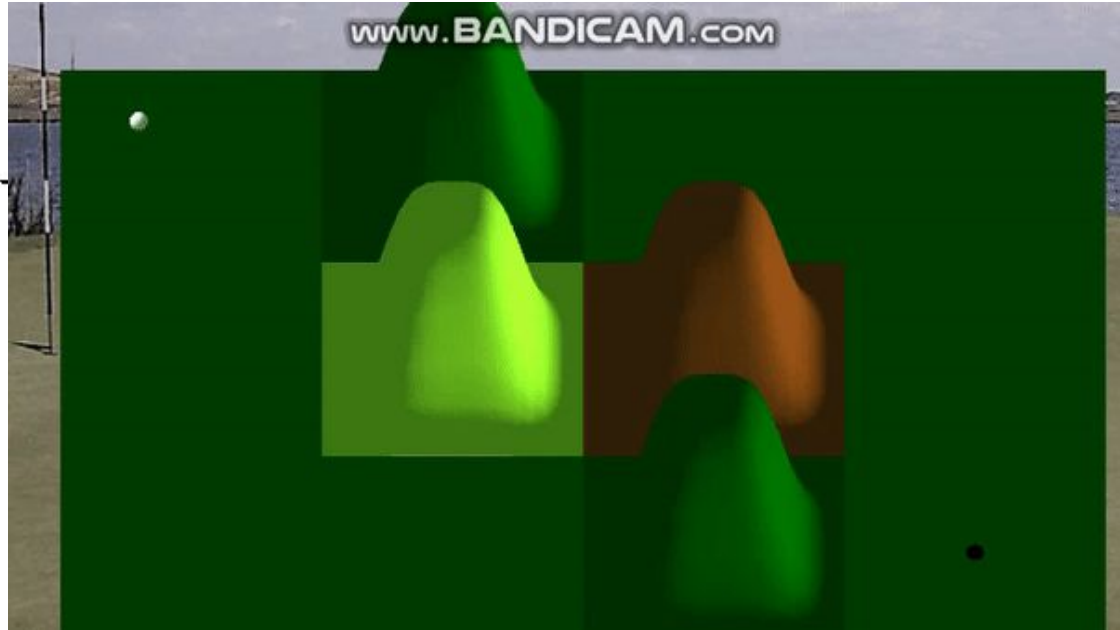
+maximum hit force

+minimize operations(function evaluations) for search

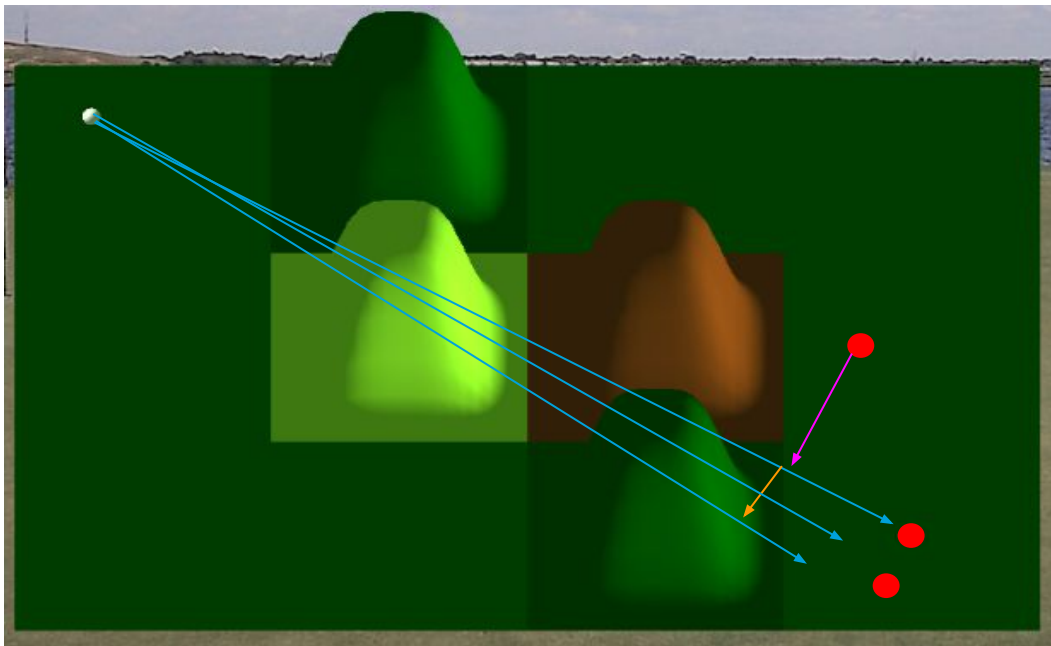
Hole-In-One without obstacles

Continuous optimization problem

$$f(x) : \mathbb{R}^2 \{ |x| < V_{max} \}$$



Local Search/Geometric Heuristic



$V \rightarrow$ compute initial shot

while solution not found:

$S \leftarrow \text{simulate}(V)$

$d \leftarrow \text{deviation}(S)$

if $d < 0$:

$V \leftarrow \text{leftOf}(V, dV)$

if $d > 0$:

$V \leftarrow \text{rightOf}(V, dV)$

if $d = 0$:

$V \leftarrow \text{incForce}(V, dV)$

if $d = \text{last } d$:

decrease stepsize dV

end

$$\text{deviation} \leftarrow \vec{X}_{\text{start-closest}} \times \vec{X}_{\text{start-hole}}$$

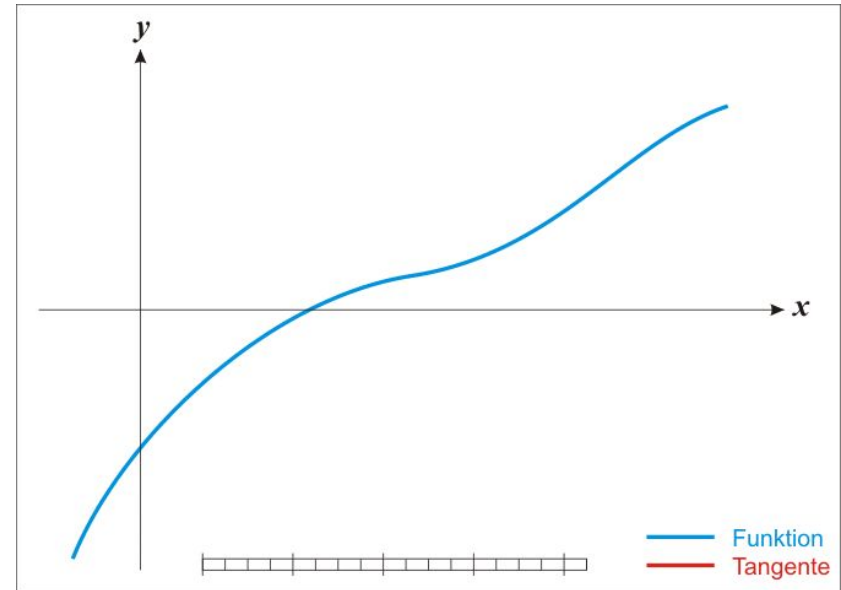
Newton's Method

- euc.dist. = $f(x) = 0 \leftarrow$ find root input vector x
- iterate until root is found
- approximate partial derivatives by *finite differences(centred)*

$$f'(x) = \frac{f(x+h) - f(x-h)}{2h} - \frac{h^2}{6} f'''(\xi)$$

- small step size (0.0001)
- *can* fail:
 - stationary start
 - cycle
 - not continuous close to root

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$



Particle Swarm Optimization

- **population-based - global**
- **improve candidate solution**
- **exploitative behaviour**

Each particle i has :

position $\vec{x}_{i,t}$ velocity $\vec{v}_{i,t}$ fitness $f(\vec{x}_{i,t})$ personal best $\vec{p}_{i,t}$

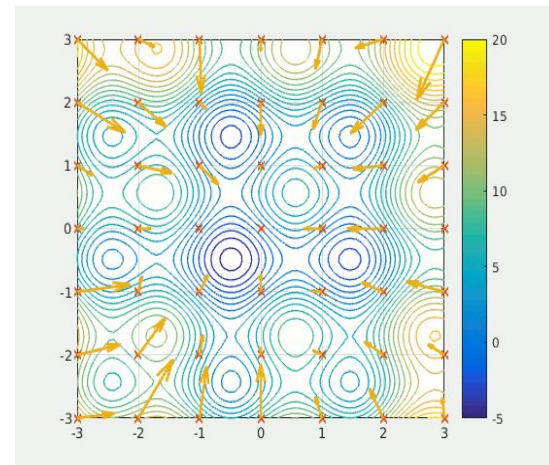
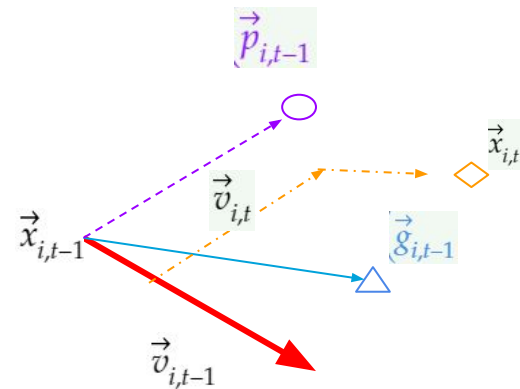
global best : $\vec{g}_{i,t}$

iteration step :

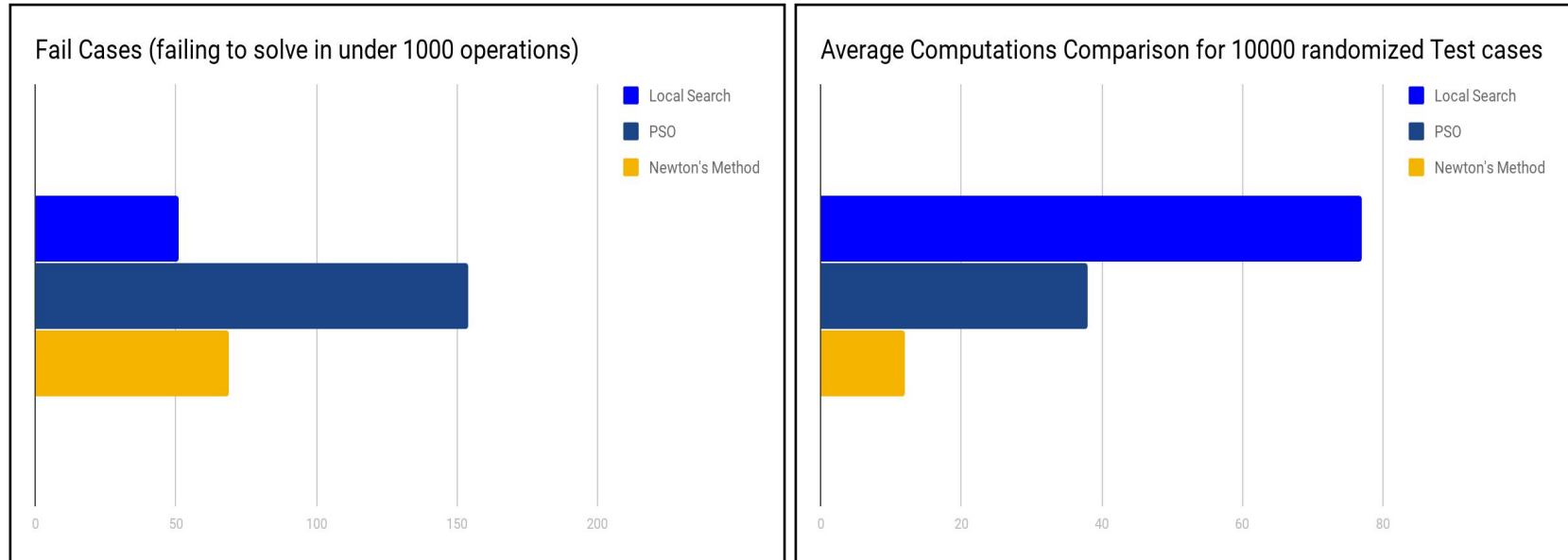
inertia term + *cognitive component* + *social component*

$$\vec{v}_{i,t} = \omega \cdot \vec{v}_{i,t-1} + c_1 \cdot \vec{r}_1 \times (\vec{p}_{i,t-1} - \vec{x}_{i,t-1}) + c_2 \cdot \vec{r}_2 \times (\vec{g}_{i,t-1} - \vec{x}_{i,t-1}); \vec{x}_{i,t} = \vec{x}_{i,t-1} + \vec{v}_{i,t};$$

constant parameters : c_1, c_2 ; damped parameter : ω ; random parameters $U\{0,1\} \vec{r}_1 \vec{r}_2$;

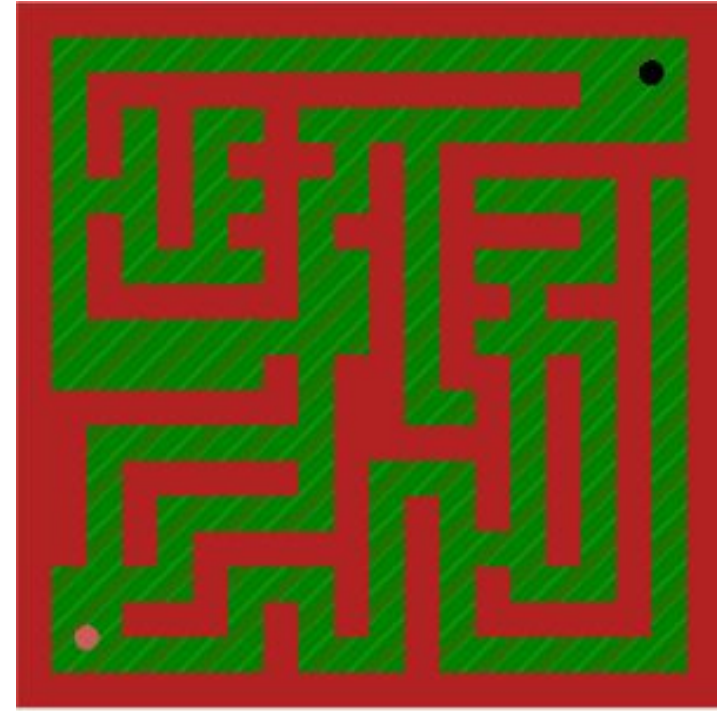


Comparison - Testing - No Obstacles



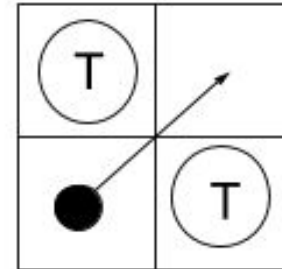
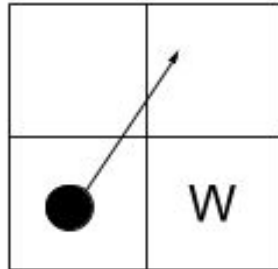
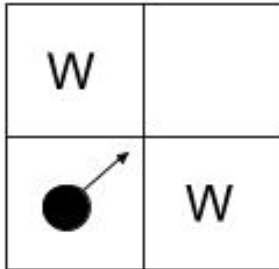
Hole-In-One with obstacles

- Mazes, objects and water
- Discontinuous function



Pathfinding - A*

- Find shortest path through maze
- Obstacle grid
- Water
- g-value: amount of visited nodes
- h-value: minimal amount of nodes to reach goal
- f-value ($g + h$) used for Priority queue



Competition

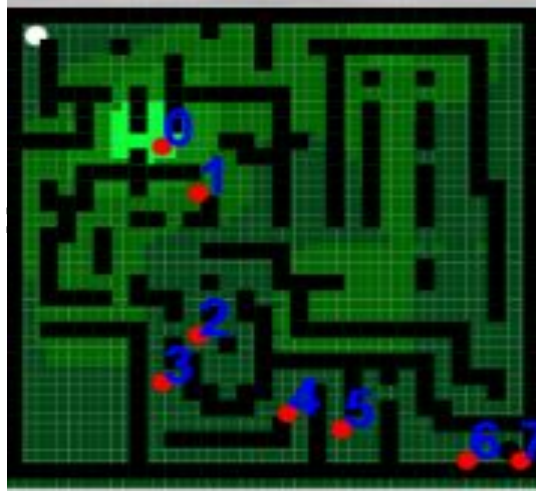
- Group splits into two teams
- Bots compete on several courses
- Results measured in number of iterations(function evaluations)

Algorithm A

Newton's Method + Pathfinding

```
path <- findPathA*  
reducePath  
initialGuess = 0  
for each node in path:  
    for small amount of iterations:  
        initialGuess <- Newtons(node, initialGuess)  
shot <- Newtons(target, initialGuess)
```

local guided search



[critical points]

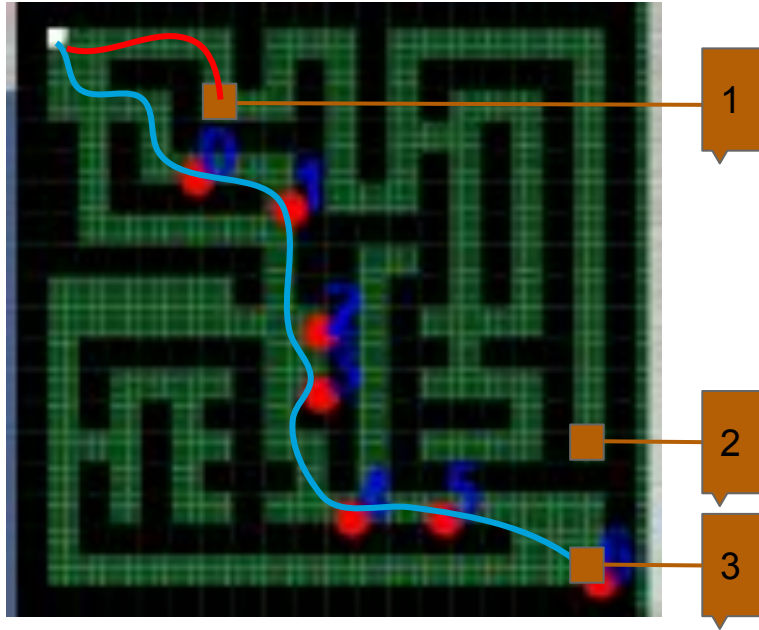


[50% of points]

Algorithm B: PSO & Newton

- Difficulty in local search
- Euclidean in maze \rightarrow suboptimal?
- Path distance
- Below given threshold - zoom in
- Newton - Euclidean vs Path

Algorithm B: Path Distance



$$(\text{size}(p) - 1) - \text{index}(n_{b,p}) + \frac{d(\text{pos}(b), \text{next}(n_{h,p}))}{d_{max}}$$

where $p = \text{path}$

$b = \text{ball}$

$n_{b,p} = \text{node of } b \text{ in } p$

$d(x, y) = \text{Euclidean distance between } x \text{ and } y$

$d_{max} = \text{maximum } d(x, y) \text{ possible in environment}$

$\text{next}(a) = \text{the node after } a \text{ in } p$

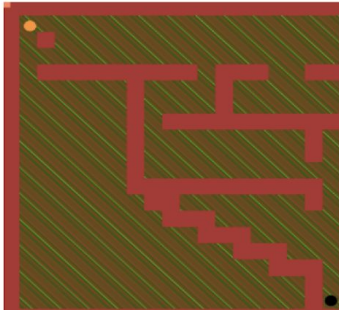
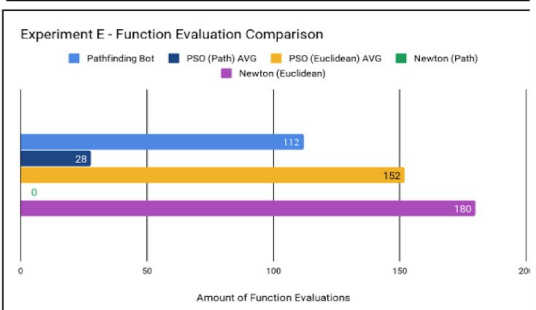
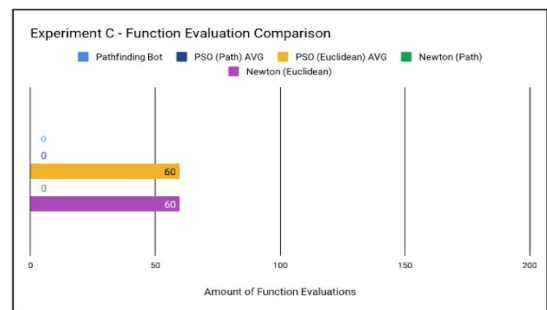
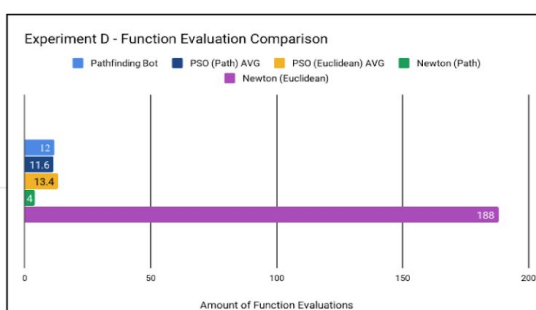
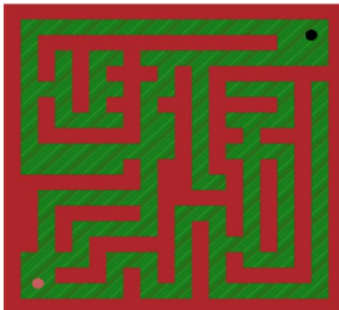
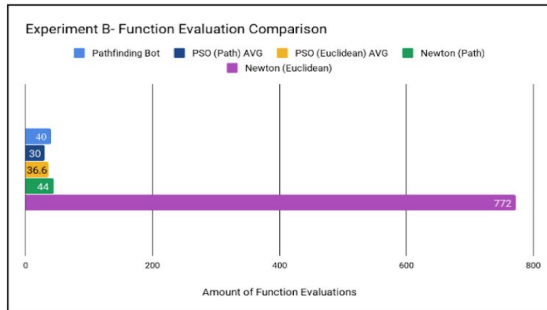
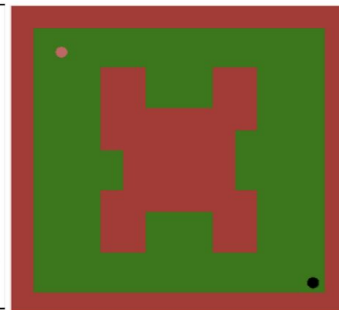
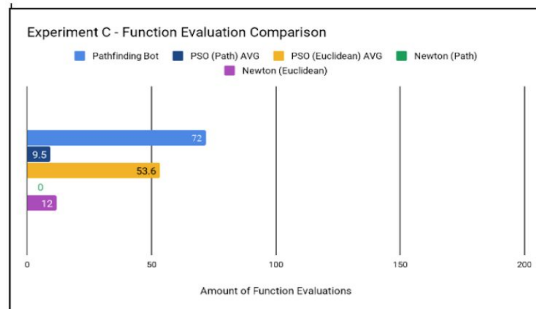
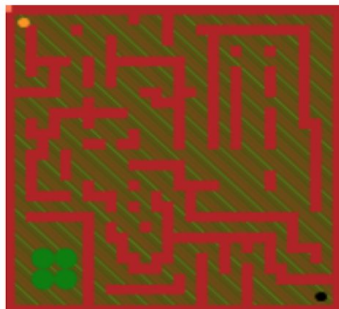
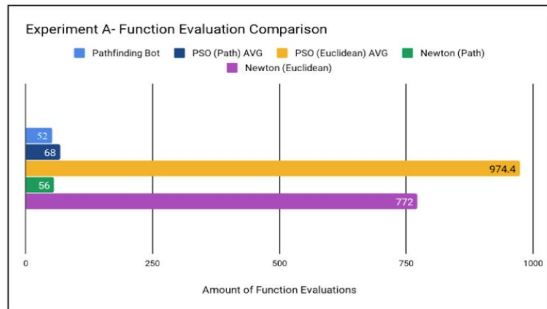
$h = \text{hole}$

Noise

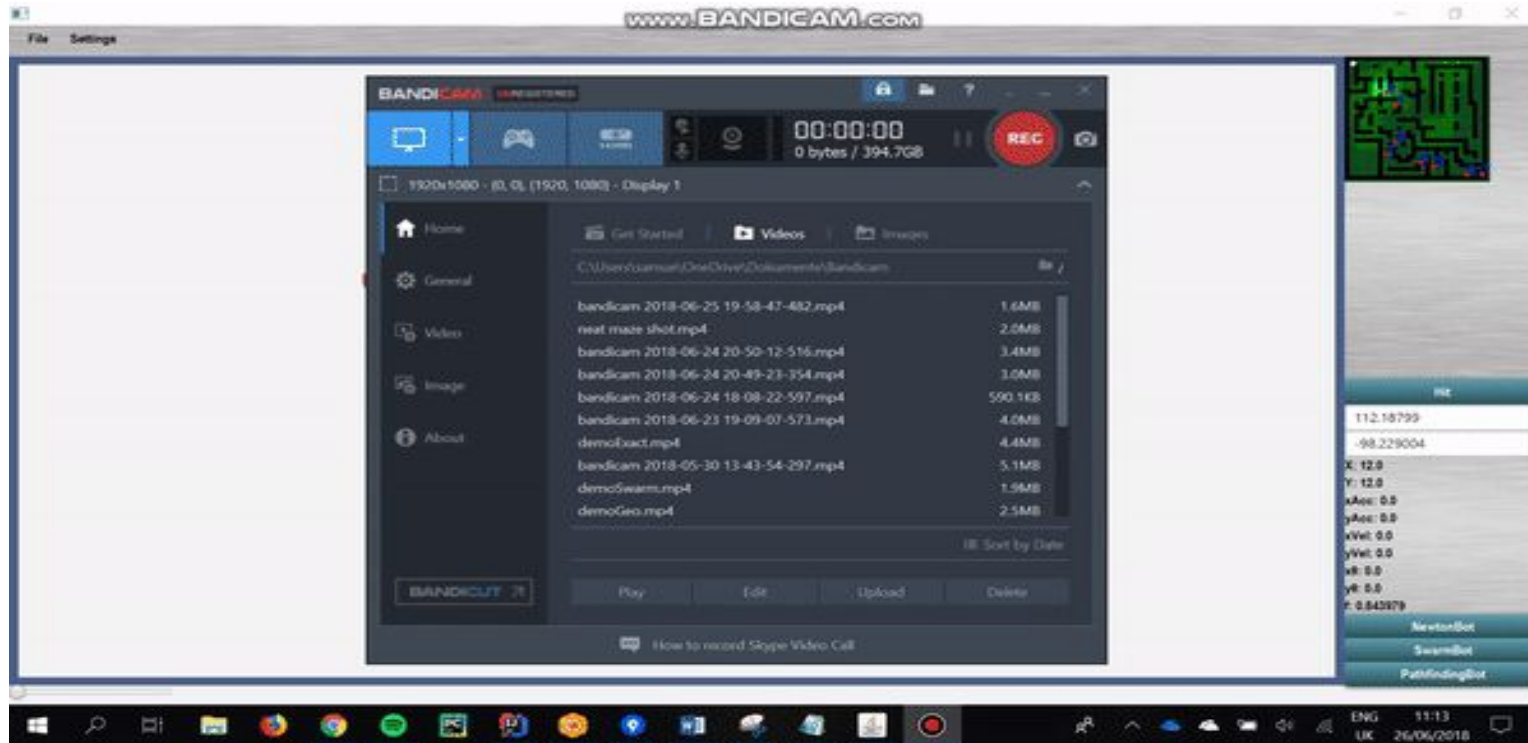
- Small position + velocity change
- More walls → more unwanted collisions
- More water → more failcases
- Player Bot
- “Safe Areas”

Experiment Overview

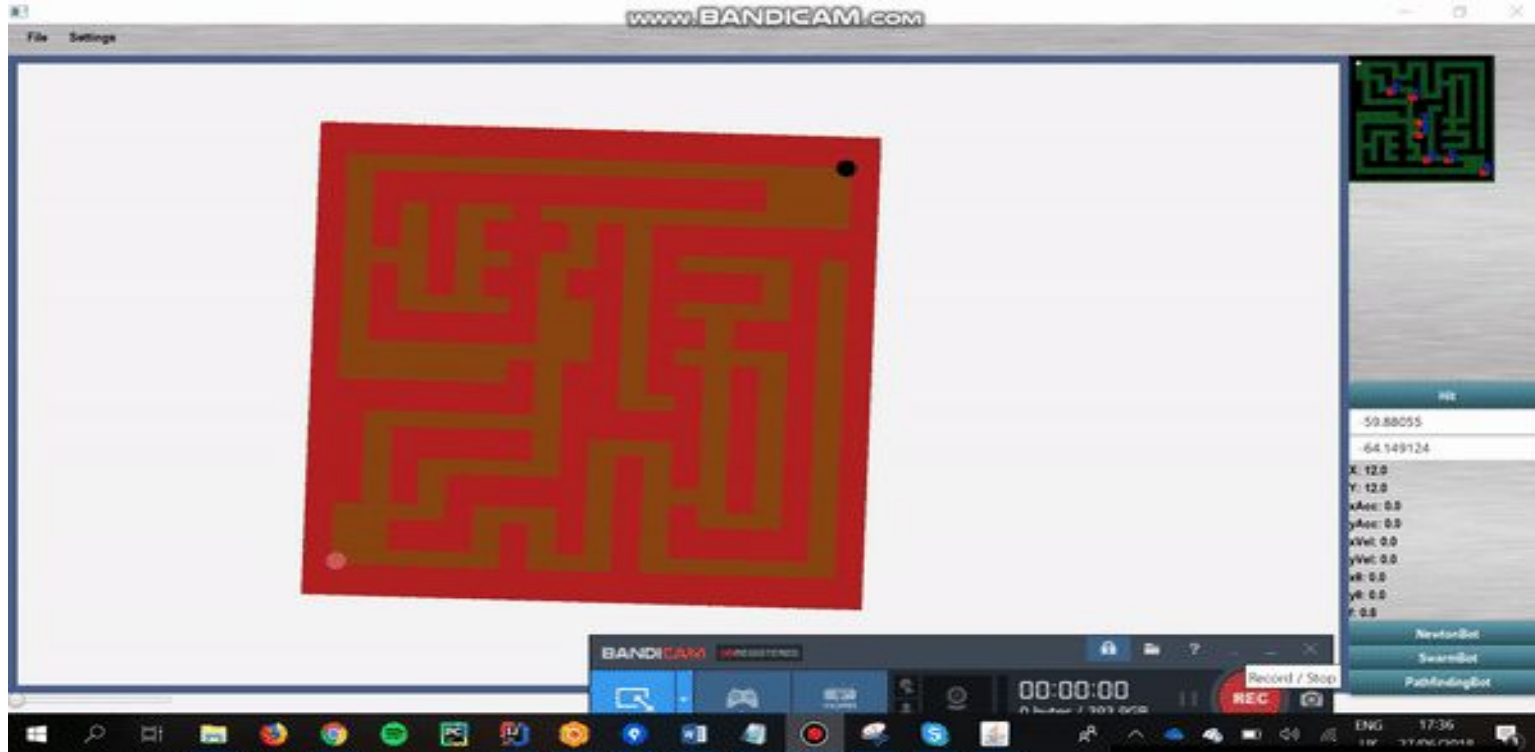
■ Pathfinding Bot ■ PSO (Path) AVG ■ PSO (Euclidean) AVG ■ Newton (Path) ■ Newton (Euclidean)



Experiment A - Algorithm A



Experiment B - Algorithm A



Conclusion

Research Question 1

In which course design does the performance of each algorithm stand out?

What are the course layouts for which the bot cannot find a solution?



Research Question 1

- simple mazes: the PSO outperforms the Pathfinding Bot
- complex mazes: both perform equally well
- water blocks the way → problems converging

Research Question 2

How do the algorithms handle a random noise factor? Up to which amount of noise do the algorithms still find a solution?

- the larger the mazes, the more difficult
- reason: more walls → more collisions;
deviation increases after each deflection
- 0.1% noise is manageable for small mazes

Research Question 3

How much does the pathfinding algorithm A^ actually improve the performance of the Bots in a maze environment?*

- complicated maze: very beneficial to use A^*
- BUT: few obstacles: better to make no assumptions about path

Future Improvement

- Water detection
- More robust to non-continuity(water)
alternative to Newton' Method
- Physics → take ball's momentum into account