

## Cinemática Inversa

$$t_x = -3 = l_1 c_1 + l_2 c_{12} + l_3 c_{123}$$

$$t_y = 2 = l_1 s_1 + l_2 s_{12} + l_3 s_{123}$$

$$t_z = 0$$

$$t_x - l_3 a_x = t_x' = l_1 c_1 + l_2 c_{12}$$

$$t_y - l_3 a_y = t_y' = l_1 s_1 + l_2 s_{12}$$

$$\Rightarrow \begin{cases} t_x'^2 = l_1^2 c_1^2 + l_2^2 c_{12}^2 + 2 l_1 l_2 c_1 c_{12} \\ t_y'^2 = l_1^2 s_1^2 + l_2^2 s_{12}^2 + 2 l_1 l_2 s_1 s_{12} \end{cases}$$

$$t_x'^2 + t_y'^2 = l_1^2 + l_2^2 + 2 l_1 l_2 \underbrace{(c_1 c_{12} + s_1 s_{12})}_{c_2}$$

$$c_2 = \frac{t_x'^2 + t_y'^2 - l_1^2 - l_2^2}{2 l_1 l_2}$$

$$\theta_2 = \pm \arccos \left( \frac{t_x'^2 + t_y'^2 - l_1^2 - l_2^2}{2 l_1 l_2} \right)$$

$$\begin{aligned} c_1 c_{12} + s_1 s_{12} &= c(\theta_1 - (\theta_1 + \theta_3)) = \\ &= c(\theta_1 - \theta_2 - \theta_3) = \\ &= c(-\theta_2) = c(\theta_2) \end{aligned}$$

$$\theta_1 + \theta_2 + \theta_3 = \arctan^2(\theta_2, a_x)$$

$$\theta_3 = \arctan^2(\theta_2, a_x) - \theta_1 - \theta_2$$

$$\begin{matrix} 0 & 1 \\ 1 & 2 \end{matrix} T \cdot \begin{matrix} 1 \\ 2 \end{matrix} T = [m' \ s' \ a' \ t'] \Leftrightarrow \begin{bmatrix} c_1 & -s_1 & 0 & l_1 c_1 \\ s_1 & c_1 & 0 & l_1 s_1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} =$$

$$= \begin{bmatrix} m_x' & s_x' & a_x' & t_x' \\ m_y' & s_y' & a_y' & t_y' \\ m_z' & s_z' & a_z' & t_z' \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} c_2 & s_2 & 0 & l_2 \\ s_2 & c_2 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$