

# Multi-Objective Monte Carlo Tree Search for Real-Time Games

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**Abstract—Abstract...**

## I. INTRODUCTION

Here it goes, the introduction.

## II. MONTE CARLO TREE SEARCH

Monte Carlo Tree Search (MCTS) is a tree search algorithm that was originally applied to board games, concretely to the two-players game of Go. This game is played in a square grid board, with a size of  $19 \times 19$  in the original game, and  $9 \times 9$  in its reduced version. The game is played in turns, and the objective is to surround the opponent's stones by placing stones in any available position in the board. Due to the very large branching factor of Go, this game is considered the drosophila of Game AI, and MCTS players have reached professional level play in the reduced board size version [1]. After its success in Go, MCTS has been used extensively by many researchers in this and different domains. An extensive survey of MCTS methods, variations and applications, has been written by Browne et al. [2].

MCTS is considered to be an *anytime* algorithm, as it is able to provide a valid next move to choose at any moment in time. This is true independently from how many iterations the algorithm was able to make (although, in general, more iterations usually produce better results). This differs from other algorithms (such as  $A^*$ ) that normally provide the next ply only after they have finished. This makes MCTS a suitable candidate for real-time domains, where the decision time budget is limited, affecting the number of iterations that can be performed.

MCTS is an algorithm that builds a tree in memory. Each node in the tree maintains statistics that indicate how often a move is played from a given state ( $N(s, a)$ ), how many times each move is played from there ( $N(s)$ ) and the average reward ( $Q(s, a)$ ) obtained after applying move  $a$  in state  $s$ . The tree is built iteratively by simulating actions in the game, making move choices based on the statistics store in the nodes.

Each iteration of MCTS can be divided into several steps [3]: *Tree selection*, *Expansion*, *Monte Carlo simulation* and *Back-propagation* (all summarized in Figure 1). When the algorithm starts, the tree is formed only by the root node, which holds the current state of the game. During the *selection*

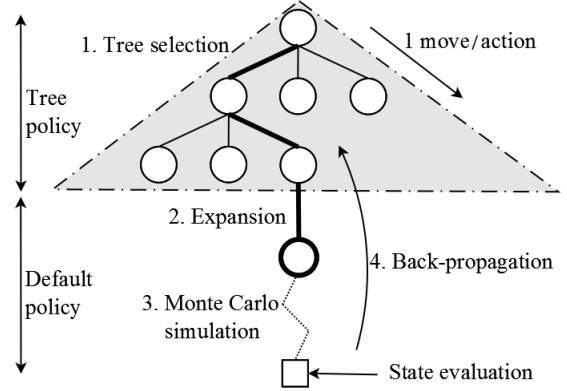


Fig. 1: MCTS algorithm steps.

step, the tree is navigated from the root until a maximum depth or the end of the game has been reached.

In every one of this action decisions, MCTS balances between exploitation and exploration. In other words, this chooses between taking an action that leads to states with the best outcome found so far, and performing a move to go to less explored game states, respectively. In order to achieve this, MCTS uses Upper Confidence Bound (UCB1, see Equation 1) as a *Tree Policy*.

$$a^* = \arg \max_{a \in A(s)} \left\{ Q(s, a) + C \sqrt{\frac{\ln N(s)}{N(s, a)}} \right\} \quad (1)$$

The balance between exploration and exploitation is achieved by setting the value of  $C$ . Higher values of  $C$  weight more the second term of the UCB1 Equation 1, giving preference to those actions that have been explored less, at the expense of taking actions with the highest average reward  $Q(s, a)$ . A commonly used value is  $\sqrt{2}$ , as it balances both facets of the search when the rewards are normalized between 0 and 1. It is worth noting that MCTS, when combined with UCB1 reaches asymptotically logarithmic regret [4].

If, during the *tree selection* phase, a node has less children than the available number of actions from a given position, a new node is added as a child of the current one (*expansion* phase) and the *simulation* step starts. At this point, MCTS executes a Monte Carlo simulation (or roll-out; *default policy*) from the expanded node. This is performed by choosing random (either uniformly random, or biased) actions until the game end or a pre-defined depth is reached, where the state of the game is evaluated.

Finally, during the *back-propagation* step, the statistics  $N(s)$ ,  $N(s, a)$  and  $Q(s, a)$  are updated for each node visited,

using the reward obtained in the evaluation of the state. These steps are executed in a loop until a termination criteria is met (such as number of iterations).

MCTS has been employed extensively in real-time games in the literature. A clear example of this is the popular real-time game *Ms. PacMan*. The objective of this game is to control Ms. PacMan to clear the maze by eating all pills, without being captured by the ghosts. An important feature of this game is that it is *open-ended*, as an end game situation is, most of the time, far ahead in the future and can not be devised by the algorithm during its iterations. The consequence of this is that MCTS, in its vanilla form, it is not able to know if a given ply will lead to a win or a loss game end state. Robles et al [5] solved this problem by including hand-coded heuristics that guided MCTS simulations towards more promising portions of the search space. Other authors also included domain knowledge to bias the search in MCTS, such as in [6], [7].

MCTS has also been applied to single-player games, like SameGame [8], where the player's goal is to destroy contiguous tiles of the same colour, distributed in a rectangular grid. Another use of MCTS is in the popular puzzle Morpion Solitaire [9], a connection game where the goal is to link nodes of a graph with straight lines that must contain at least five vertices. Finally, the PTSP has also been addressed with MCTS, both in the single-objective [10], [11] and the multi-objective versions [12]. These papers describe the entries that won both editions of the PTSP Competition.

It is worthwhile mentioning that in most cases found in the literature, MCTS techniques have been used with some kind of heuristic that guides the Monte Carlo simulations or the tree selection policy. In the algorithm proposed in this paper, simulations are purely random, as the objective is to compare the search abilities of the different algorithms. The intention is therefore to keep the heuristics to a minimum, and the existing pieces of domain knowledge are shared by all the algorithms presented (as in the case of the score function for MO-PTSP, described later).

### III. MULTI-OBJECTIVE OPTIMIZATION

A multi-objective optimization problem (MOOP) represents a scenario where two or more objective functions are to be optimized (either maximized or minimized). The general form of a MOOP is formally described as a maximization function  $F_m(x)$ , that transforms points in the decision space ( $X$ ) to points in the solution space ( $F$ ). The elements of the decision space are vectors of  $n$  variables of the form  $x = (x_1, x_2, \dots, x_n)$ , while elements in the solution space are vectors with a dimension  $m$ :  $F_m(x) = (f_1(x), f_2(x), \dots, f_m(x))$ . Therefore, each solution provides  $m$  different scores (or rewards, or fitness) that are meant to be optimized. Without loss of generality, it is assumed from now on that all objectives must be maximized.

It is said that a solution  $F_m(x)$  *dominates* another solution  $F_m(y)$  if:

- 1)  $F_m(x)$  is not worse than  $F_m(y)$  in all objectives for all  $i = 1, 2, \dots, m$ .

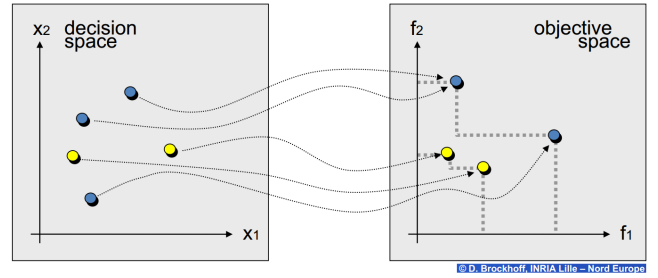


Fig. 2: Decision and Solution spaces in a MOOP with two variables ( $x_1$  and  $x_2$ ) and two objectives ( $f_1$  and  $f_2$ ). In the objective space, yellow dots are non-optimal objective vectors, while blue dots form the Pareto-optimal front.

- 2) At least one objective of  $F_m(x)$  is better than its analogous counterpart in  $F_m(y)$ .

When this two conditions apply, it is said that  $F_m(x) \preceq F_m(y)$  ( $F_m(x)$  dominates  $F_m(y)$ ), and  $F_m(x)$  is non-dominated by  $F_m(y)$ . The *dominance* condition provides a partial ordering between points in the solution space: if  $F_m(x) \preceq F_m(y)$ , then  $F_m(x)$  is considered to be better than  $F_m(y)$ .

However, there are some cases where it cannot be said that  $F_m(x) \preceq F_m(y)$  or  $F_m(y) \preceq F_m(x)$ . This situation occurs when one of the objectives is better in  $F_m(x)$  but a different objective is better in  $F_m(y)$  (for instance, when  $F_1(x) < F_1(y)$  but  $F_2(x) > F_2(y)$ ). In this case, it is said that these solutions are non-dominated with respect to each other. Solutions that are not dominated by each other are grouped in a *non-dominated set*. Given a non-dominated set  $P$ , it is said that  $P$  is the *optimal Pareto front* if there is no other solution in the solution space that dominates any member of  $P$ . The relation between decision and objective space, dominance and Pareto fronts is depicted in Figure 2.

As many Pareto front can be formed by several points in the solution space, it is important to devise a mechanism to assess the quality of a given front. A possibility is to use the Hypervolume Indicator (HV): given a Pareto front  $P$ ,  $HV(P)$  is defined as the volume of the objective space dominated by  $P$ . More formally,  $HV(P) = \mu(\{x \in \mathbb{R}^d : \exists r \in P \text{ s.t. } r \preceq x\})$ , where  $\mu$  is the de Lebesgue measure on  $\mathbb{R}^d$ . If the objectives are to be maximized, the higher the  $HV(P)$ , the better the front calculated. Figure 3 shows an example of  $HV(P)$  where the objective dimension space is 2.

For more extensive descriptions, definitions, properties and multi-objective optimization in general, the reader can consult the work by K. Deb [13].

Many different algorithms have been proposed to tackle multi-objective optimization problems in the literature. One of the most widely known and used methods is the weighted-sum approach. The procedure consists of giving a weight to each one of the objective and produce a single result as the linear combination of objectives and weights. By varying the weights provided, it is possible to converge to different solutions of the optimal Pareto front, if this is convex. However, K. Deb [13] explains how linear scalarization approaches fail in

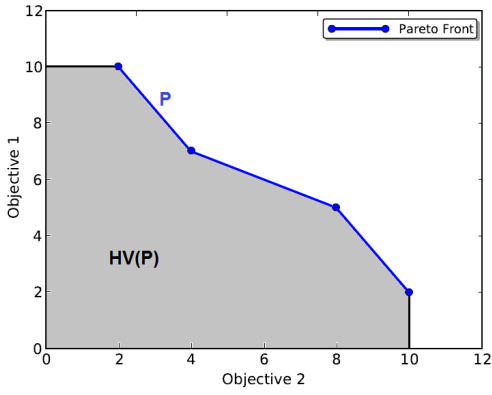


Fig. 3:  $HV(P)$  of a given pareto front  $P$ .

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**Algorithm 1** NSGA-2 Algorithm.

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1: function NSGA-2
2:    $P = \text{NewRandomPopulation}$ 
3:   while Termination criteria not met do
4:      $R = P \cup Q$ 
5:      $F = \text{FASTNONDOMINATEDSORT}(R)$ 
6:     while  $|P| < N$  do
7:        $\text{CROWDINGDISTANCEASSIGNMENT}(F_i)$ 
8:        $P = P \cup F_i$ 
9:      $\text{SORT}(P)$ 
10:     $P = P[0 : N]$ 
11:     $Q = \text{breed}(P)$ 

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those scenarios where the optimal Pareto front is non-convex.

A popular choice for multi-objective optimization problems are evolutionary multi-objective optimization (EMOA) algorithms [14], [15]. One of the most well known algorithms in the literature is the Non-dominated Sorting Evolutionary Algorithm 2 (NSGA-2), which pseudocode is shown in Algorithm 1. As in any evolutionary algorithm, NSGA-2 evolves a set of individuals or solutions to the problem, with the difference that here they are ranked according to dominance criteria and crowding distance (distances between members of the pareto fronts). A full description of the algorithm can be found in [16].

The three main pillars of the NSGA-2 algorithm are:

- A *fast non-dominated sorting* algorithm, that ranks the individuals of the population and groups them in Pareto fronts.
- A *crowding distance*, assigned to each one of the individuals, that measures how close it is to its neighbours. The selection genetic operator chooses individuals based on the ranks of the individuals and their crowding distance.
- *Elitism*, implemented so the algorithm automatically promotes the best  $N$  individuals to the next generation.

A more recent approach, developed by Q. Zhang, is the Multi-Objective Evolutionary Algorithm based on Decomposition (MOEA/D) [17], that decomposes the problem into several single optimization sub-problems and an evolutionary algorithm optimizes them all simultaneously. Information is shared between neighbouring sub-problems in order to guide

evolution. The authors show that MOEA/D performs similarly than, and sometimes even outperforms, NSGA-II in the scenarios tested.

Reinforcement Learning (RL) algorithms have also tackled Multi-objective optimization in some scenarios. RL [18] is a broad field in Machine Learning that studies real-time planning and control situations where an agent has to find out the actions (or sequences of actions) that should be applied in order to maximize the reward from the environment.

An RL problem can be defined as a tuple  $(S, A, T, R, \pi)$ .  $S$  is the set of possible states in the problem (or game), and  $s_0$  is the initial state.  $A$  is the set of available actions the agent can make at any given time, and the transition model  $T(s_i, a_i, s_{i+1})$  determines the probability of reaching the state  $s_{i+1}$  when action  $a_i$  is applied in state  $s_i$ . The reward function  $R(s_i)$  provides a single value (*reward*) that the agent must optimize, representing the desirability of the state  $s_i$  reached. Finally, a decision policy  $\pi(s_i) = a_i$  determines which actions  $a_i$  must be chosen from each state  $s_i \in S$ . One of the most important challenges in RL, as shown in Section II, is the trade-off between exploration and exploitation. The decision policy can choose between following actions that provided good rewards in the past and exploring new parts of the search space by selecting new actions.

Multi-objective Reinforcement Learning (MORL) [19] changes this definition by using instead a vector  $R = r_0, r_1, \dots, r_n$  as rewards of the problem. Thus, MORL problems differ from RL in having more than one objective objectives ( $n$ ) that must be maximized. If the objectives are independent or they do not oppose each other, scalarization technique approaches, as described above, could be suitable to tackle the problem. Essentially, this would mean to use a conventional RL algorithm on a single objective obtained by a weighted-sum of the multiple rewards. However, this is not always the case, as it is usual that the objectives are in conflict and the policy ( $\pi$ ) must balance among them.

According to how  $\pi$  approaches this problem, Vamplew et al. [19] proposed the following distinction for MORL: *single-policy* algorithms are those that provide a preference order in the objectives available (given by the user or by the nature of the problem). An example of this type of algorithm can be found at [20], where the authors introduce an order of preference in the objectives treated and constraint the value of the rewards desired. Scalarization approaches would also fit in this category, as the work performed by S. Natarajan et al. [21].

The second type of algorithms, *multiple-policy*, target to approximate the optimal Pareto front of the problem. An example of this type of algorithm is the one given by L. Barrett [22], who propose the Convex Hull Iteration Algorithm. This algorithm provides the optimal policy for any linear preference function, by learning all policies that define the convex hull of the Pareto front.

#### IV. MULTI-OBJECTIVE MONTE CARLO TREE SEARCH

Adapting MCTS into Multi-Objective Monte Carlo Tree Search (MO-MCTS) requires the obvious modification of

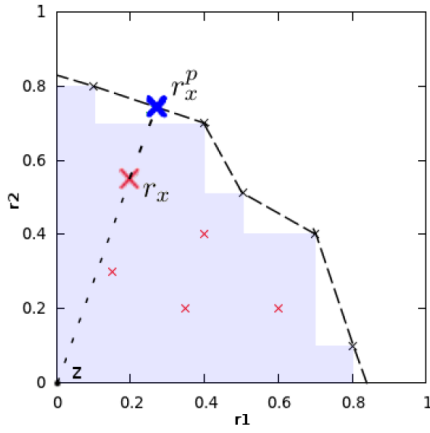


Fig. 4:  $r_x^p$  is the projection of the  $r_x$  value on the piecewise linear surface (discontinuous line). The shadowed surface represents  $HV(P)$ . From [23].

dealing with multiple rewards instead of just one. As these are collected at the end of a Monte Carlo simulation, the reward value  $r$  now becomes a vector  $R = r_0, r_1, \dots, r_n$ , where  $n$  is the number of objectives to optimize. Derived from this change, the average value  $Q(s, a)$  becomes a vector that stores the average reward of each objective. Note that the other statistics ( $N(s, a)$  and  $N(s)$ ) do not need to change, as this are just node and action counters. The important question to answer next is how to adapt the vector  $Q(s, a)$  to use it in the UCB1 formula (Equation 1).

An initial attempt on Multi-Objective MCTS was addressed by W. Wang and Michele Sebag [23], [24]. In their work, the authors employ a mechanism, based on the HV calculation, to replace the UCB1 equation. The algorithm keeps a Pareto archive ( $P$ ) with the best solutions found in game end states. Every node in the tree defines  $\bar{r}_{sa}$  as a vector of UCB1 values, in which each  $\bar{r}_{sa,i}$  is the result of calculating UCB1 for each particular objective  $i$ .

The next step is to define the value for each pair of state and action,  $W(s, a)$ , as in Equation 2.  $\bar{r}_{sa}^p$  is the projection of  $\bar{r}_{sa}$  into the piecewise linear surface defined by the Pareto archive  $P$  (see Figure 4). Then,  $HV(P \cup \bar{r}_{sa})$  is declared as the HV of  $P$  plus the point  $\bar{r}_{sa}$ . If  $\bar{r}_{sa}$  is dominated by  $P$ , the distance between  $\bar{r}_{sa}$  and  $\bar{r}_{sa}^p$  is subtracted from the HV calculation. The tree policy selects actions based on a maximization of the value of  $W(s, a)$ .

$$W(s, a) = \begin{cases} HV(P \cup \bar{r}_{sa}) - dist(\bar{r}_{sa}^p, \bar{r}_{sa}) & \text{Otherwise} \\ HV(P \cup \bar{r}_{sa}) & \text{if } \bar{r}_{sa} \preceq P \end{cases} \quad (2)$$

The proposed algorithm was employed successfully in two domains: the DST and the Grid Scheduling problem, matching state of the art results in both domains, at the expense of a high computational cost.

As mentioned before, the objective of this paper is to propose an MO-MCTS algorithm that is suitable for real-time domains. Although the work discussed here is influenced by Wang's approach, some modifications need to be done in order

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**Algorithm 2** Pareto MO-MCTS node update.

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1: function UPDATE( $node, \bar{r}, dominated = false$ )
2:    $node.Visits = node.Visits + 1$ 
3:    $node.\bar{R} = node.\bar{R} + \bar{r}$ 
4:   if ! $dominated$  then
5:     if  $node.P \preceq \bar{r}$  then
6:        $dominated = true$ 
7:     else
8:        $node.P = node.P \cup \bar{r}$ 
9:   UPDATE( $node.parent, \bar{r}, dominated$ )

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to overcome the high computational cost involved by their approach.

In the algorithm proposed in this paper, the vector  $\bar{r}$  of rewards that was obtained at the end of an Monte Carlo simulation is back-propagated through the nodes visited in the last iteration until the root is reached. In the vanilla algorithm, each node would use this vector  $\bar{r}$  to update its own accumulated reward vector  $\bar{R}$ . Instead of doing this, each node in the MO-MCTS algorithm keeps a local Pareto front ( $P$ ), updated at each iteration with the reward vector  $\bar{r}$  obtained at the end of the simulation. Algorithm 2 describes how the node statistics are updated.

In this algorithm, if  $\bar{r}$  is not dominated by the local Pareto front, it is added to the front and  $\bar{r}$  is propagated to its parent. In case  $\bar{r}$  is dominated by the node's Pareto front, the local Pareto front and there is no need to keep this propagation up the tree.

Three observations can be made about the mechanism described here:

- Each node in the tree has an estimate of the quality of the solutions reachable from there, both as an average (as in the baseline MCTS) and as the best case scenario (by keeping the non-dominated front  $P$ ).
- By construction, if a reward  $\bar{r}$  is dominated by the local front of a node, it is a given that it will be dominated by the nodes above in the tree, so there is no need to update the fronts of the upper nodes, producing little cost in the efficiency of the algorithm.
- It is easy to infer, from the last point, that the Pareto front of a node cannot be worse than the front of its children (in other words, the front of a child will never dominate that of its parent). Therefore, the root of the tree contains the best non-dominated front ever found during the search.

This last detail is important for two main reasons. First of all, the algorithm allows the root to store information indicating which is the action to take in order to converge to any specific solution in the front discovered. This information can be used, when all iterations have been performed, to select the move to perform next. If weights for the different objectives are provided, this weights can be used to select the desired solution in the Pareto front of the root node, and hence select the action that leads to that point. Secondly, the root's Pareto front can be used to measure the global quality of the search using the hypervolume calculation.

Finally, the information stored at each node regarding the



local Pareto front can be used to substitute  $Q(s, a)$  in the UCB1 equation. The quality of a given pair  $(s, a)$  can be obtained by measuring the HV of the Pareto front stored in the node reached from state  $s$  after applying action  $a$ . This can be defined as  $Q(s, a) = HV(P)/N(s)$ , and the Upper Confidence Bound equation, referred to here as *MO-UCB*, is described as in Equation 3).

$$a^* = \arg \max_{a \in A(s)} \left\{ HV(P)/N(s) + C \sqrt{\frac{\ln N(s)}{N(s, a)}} \right\} \quad (3)$$

## V. BENCHMARKS

## VI. EXPERIMENTATION

## VII. CONCLUSIONS AND FUTURE WORK

## ACKNOWLEDGMENTS

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**Spyridon Samothrakis** is currently pursuing a PhD in Computational Intelligence and Games at the University of Essex. His interests include game theory, computational neuroscience, evolutionary algorithms and consciousness.



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