

Spintronic Technology For Energy-Efficient In Memory Computing

Part 2 – Spintronic Fundamentals

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Lecture Outline

- 1 Brief Introduction
- 2 Spintronic Fundamentals: From Electron to GMR
- 3 Spintronic Fundamentals: Magnetization Dynamics
- 4 Spintronic Fundamentals: STT and LLGS Equation
- 5 Spintronic Devices and Applications
- 6 Summary

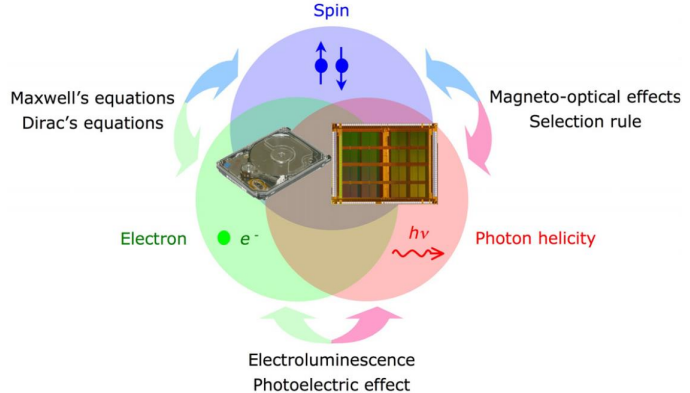


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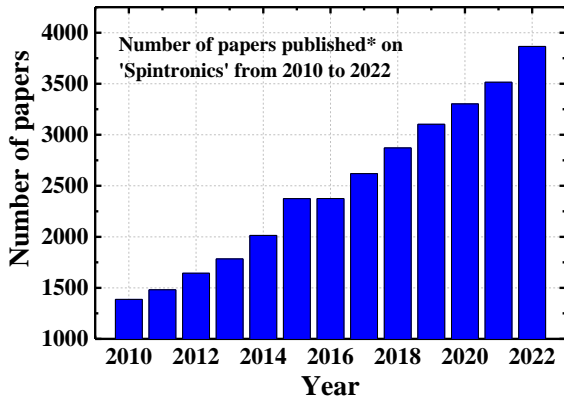
Spintronics

- Spintronics combines three information carriers: electron charge, **electron spin**, and photon.
- These carriers correspond to the three major fields of information technology:
 - ① data processing: it is done through electron transport
 - ② **data storage: it is achieved through a collection/assembly of electron spins**
 - ③ data transfer: it is accomplished through optical connections



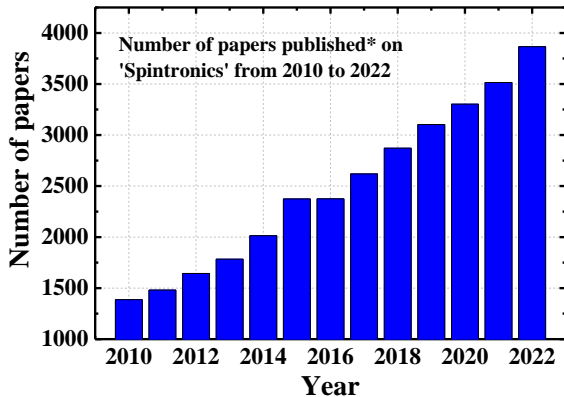
Source: Hirohata, A., & Takanashi, K. (2014). *J. of Physics D: Applied Physics*, 47(19), 193001.

- **Emerging information technologies require bigger data storage and faster processing**
 - Conventional semiconductor-based memories can not keep with the demand of emerging applications
- Spin-polarized electron transport has emerged as a faster alternative
- **The growth of spin transport devices using ferromagnetic and non-magnetic materials has generated a lot of interest among researchers.**



Source: Data obtained from Scopus data base by Esteban Garzón

- **Emerging information technologies require bigger data storage and faster processing**
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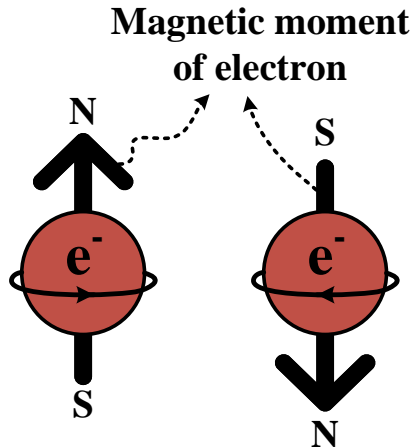
- Building blocks of magnetic memories:
 - 1 ferromagnetic materials
 - 2 spin-related phenomena

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Electron Spin and Magnetic Moment

- The **electron spin generates** a **magnetic moment** that is opposite to its **spin angular momentum**
 - Spin magnetic moment: $\vec{\mu}$
 - Angular momentum: \vec{S}
- Each **electron** can be seen as a **"tiny magnet"** that possesses a small magnetic moment.



Electron Spin and Magnetic Moment (Cont.)

$$\vec{\mu} = -\frac{g_e \mu_B}{\hbar} \vec{S}$$

$$\vec{\mu} = \gamma \vec{S}$$

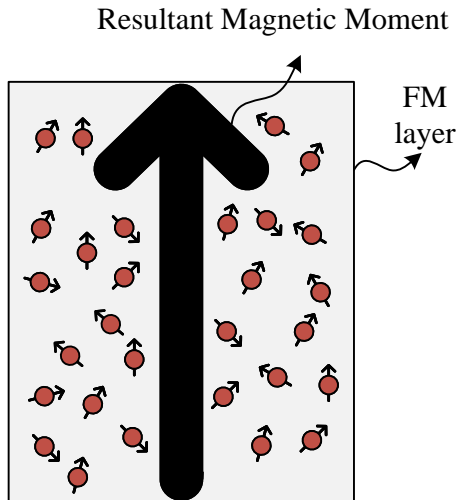
- $\gamma \rightarrow$ gyromagnetic ratio in $[\text{Rad s}^{-1} \text{T}^{-1}]$
- $\mu_B \rightarrow$ Bohr's Magneton $\approx 9.27 \times 10^{-24} [\text{A} \cdot \text{m}^2]$
- $g_e \rightarrow$ quantum mechanical electron dimensionless factor
 - $g_e = 2$ for electrons,
 - it depends on the material, e.g., $g_e \neq 2$ in semiconductors

- $\vec{S} = \pm \hbar/2$
 - It quantizes the angular momentum of spin
 - It depends on the orientation of the spin (from clockwise to anticlockwise or vice versa)
 - $\vec{\mu} = -\frac{g_e \mu_B}{\hbar} \left(\pm \frac{1}{2} \hbar \right) = \pm \frac{1}{2} g_e \mu_B (-1)$



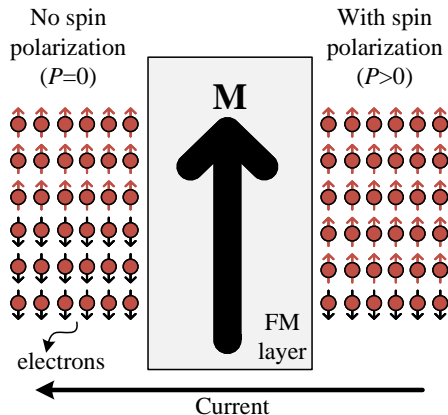
Magnetization

- Ferromagnetic materials (FM) with incomplete 3d orbitals are widely used in spintronics devices
 - Mn^{2+} , Fe^{3+} , Fe^{2+} , Co^{3+} , Co^{2+}
- Unpaired orbital electrons have magnetic moments that combine to form a resultant magnetic moment.
- **The net magnetic moment of bounded orbital electrons per unit volume defines the magnetization of an FM layer.**
$$\vec{M} = \frac{\sum_{i=1}^{Ne} \vec{\mu}_i}{Volume}$$
 - $\vec{\mu}_i$: individual magnetic moments of bounded electrons
 - Ne : total number of orbital electrons



Magnetization (Cont.)

- Bounded electrons in FM materials exchange magnetic moment with **free electrons**.
- **Spin magnetic moment** of free electrons is generated **in the direction of bulk magnetization during exchange**.
 - Spin filtering
- FM material acts as a filter passing either spin-up or spin-down electrons.
 - The majority of electrons end up with either spin orientation (spin-up in this example)



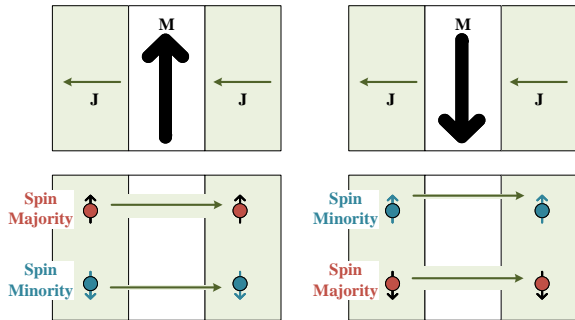
Spin Polarized Current

- Spin-polarized current (I_S) can be defined as:

$$I_S = I_{\uparrow} - I_{\downarrow}$$

$$I_S = P I_C$$

- $I_{\uparrow(\downarrow)}$: current in a material due to electrons with a spin-up (spin-down)
- I_C : electric current resulting from the charge flow through the FM
- P : spin polarization factor of FM
- Note: if $P = 0$, $I_{\uparrow} = I_{\downarrow}$
 - non-magnetic (NM) material, which lacks any specific spin orientation among the majority of electrons



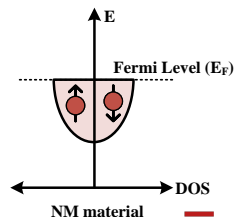
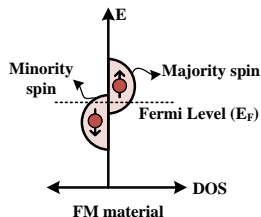
Energy Bands and Density of States – A Simplified View

- In **FM** the **density of states** (DOS) can exhibit an **asymmetry** due to the spin-splitting of the **energy levels**.
 - larger for one spin direction than the other
 - **net magnetic moment** (\vec{M}) can be **attributed** to a different population of **spin-up and spin-down electrons** near Fermi energy level
- In a NM material, the density of states typically exhibits a symmetric distribution around the Fermi level.

- P of a FM can also be written as:

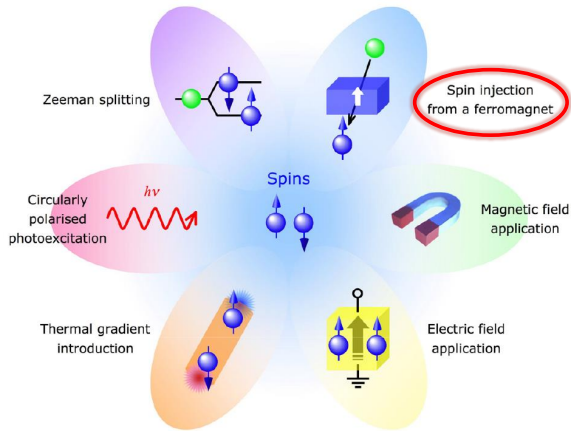
$$P = \frac{N_{\uparrow}(E_F) - N_{\downarrow}(E_F)}{N_{\uparrow}(E_F) + N_{\downarrow}(E_F)}$$

- $N_{\uparrow}(E_F)$ and $N_{\downarrow}(E_F)$: number of electrons at Fermi energy of spin-up and spin-down orientation, respectively.



Spin Generation

- Spin-polarized electrons can be generated in non-magnetic materials through various methods including:
 - **Spin injection from a ferromagnet**
 - Magnetic field
 - Electric field
 - Circularly polarized photoexcitation
 - Thermal gradient
 - Zeeman splitting
- **The most common method is spin injection from a ferromagnetic material attached to a non-magnetic metal or semiconductor**



Source: Hirohata, A., & Takanashi, K. (2014). *J. of Physics D: Applied Physics* 47(19), 193001.

Electrical Spin Injection

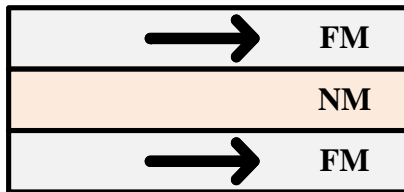
- Spin injection from FM to NM is fundamental for spintronic devices
- Proposed by Aronov in 1976
- Studied by Johnson and Silsbee in 1980s
- Formalisms for spin-dependent injection and transport developed by Valet and Fert in 1993 and Rashba in 2000.



Albert Fert (Nobel Prize in Physics - 2007)

Understanding the Giant Magnetoresistance Effect in Spin Valves

- A **spin valve** is a **basic spin-based device** that comprises two ferromagnetic (FM) layers and a non-magnetic (NM) spacer layer.
 - The **resistance** of a spin valve can be **changed between** two values by aligning or misaligning the **magnetization orientation of the two FM layers**.
 - The FM layers have different magnetic coercivity levels and are distinguished as a free layer (FL) and a pinned layer (PL).



Understanding the Giant Magnetoresistance Effect in Spin Valves

- The **Giant Magnetoresistance (GMR)** effect refers to the **phenomenon of resistance change in a spin valve**

- normalized difference in resistance between parallel (R_P) and antiparallel (R_{AP}) magnetization configurations of FM layers:

$$GMR = \frac{R_{AP} - R_P}{R_P}$$

- The **GMR effect** is based on the concept of **two-channel theory**, proposed by Mott in 1935-36 (explains the magnetoresistance of a spin valve)

The Electrical Conductivity of Transition Metals

By N. F. MOTT, H. H. Wills Physical Laboratory, University of Bristol

(Communicated by R. H. Fowler, F.R.S.—Received September 23, 1935)

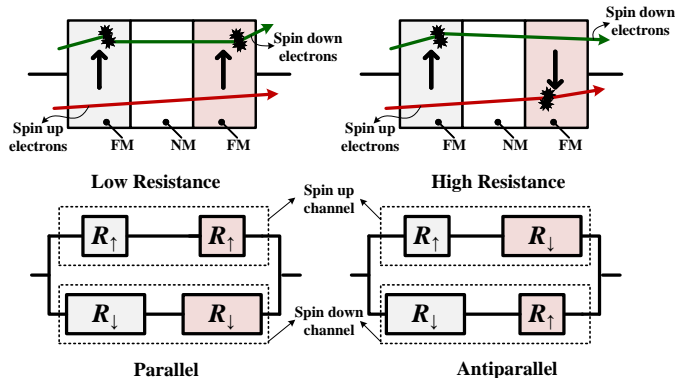
Source: N. F. Mott, *The Electrical Conductivity of Transition Metals*, Proc. Royal Soc.

London. A 153, pp. 699-717 (1936)



GMR – Two-Channel Theory

- Metal conduction occurs in independent spin-up and spin-down channels
- In FM metal, both channels exhibit different conductivities due to spin-dependent scattering of electrons
- Low probability (high probability) of scattering occurs when electron flowing through FM has spin orientation similar (different) to magnetization orientation of FM



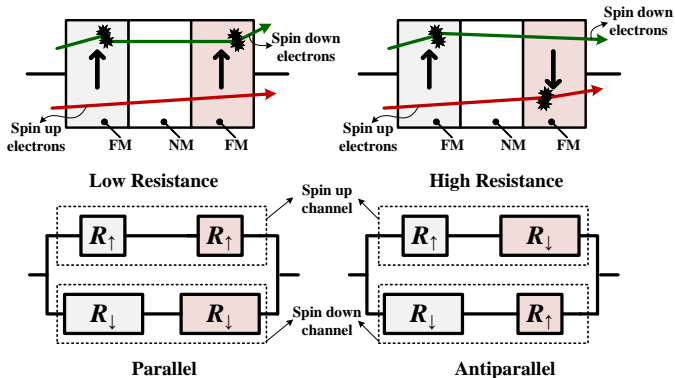
GMR – Two-Channel Theory (Cont.)

- Resistance is lower when magnetization orientation of two FM layers is parallel.

$$R_P = \frac{2 R_{\uparrow} R_{\downarrow}}{R_{\uparrow} + R_{\downarrow}}$$

- Resistance is higher when magnetization orientation of two FM layers is in antiparallel.

$$R_{AP} = \frac{R_{\uparrow} + R_{\downarrow}}{2}$$



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Magnetization Dynamics

Gyromagnetic Precession

- The ratio of the spin magnetic moment ($\vec{\mu}_S$) to its spin angular momentum (\vec{S}) is referred to as the gyromagnetic ratio

$$\vec{\mu}_S = -\gamma \vec{S} \quad (1)$$

- “The equation for the rotational motion of a rigid body in classical mechanics:”

$$\frac{d\vec{L}}{dt} \rightarrow \frac{d\vec{S}}{dt} = \vec{\tau} \quad (2)$$

- \vec{L} : is the angular momentum of the body
- $\vec{\tau}$: is the torque on an electron
- When an external magnetizing field (\vec{H}) is applied:

$$\vec{\tau} = \frac{d\vec{S}}{dt} = (\vec{\mu}_S \times \vec{H}) \quad (3)$$



Magnetization Dynamics

Gyromagnetic Precession

- Using (1) and (3):

$$\frac{d\vec{\mu}_S}{dt} = -\gamma \left(\vec{\mu}_S \times \vec{H} \right) \quad (4)$$

- From a macroscopic point of view, the total magnetization \vec{M} is defined as the sum of the individual magnetic moments per unit volume. Rewriting (4):

$$\sum_{i=1}^N \frac{d\vec{\mu}_{S,i}}{dt} = -\gamma \left(\sum_{i=1}^N \vec{\mu}_{S,i} \right) \times \vec{H}$$

- Now we can define the **precessional motion** (a.k.a **gyromagnetic precession**)

$$\frac{d\vec{M}}{dt} = -\gamma \left(\vec{M} \times \vec{H} \right) \quad (5)$$

- Note: considering all fields (internal and external)

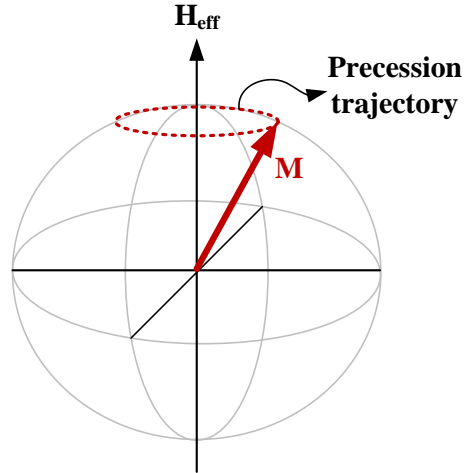
$$\frac{d\vec{M}}{dt} = -\gamma \left(\vec{M} \times \vec{H}_{eff} \right) \quad (6)$$



Magnetization Dynamics

Gyromagnetic Precession

- Example: simplified (not a complete picture) dynamics of the gyromagnetic precession of magnetic moment \vec{M} around the effective magnetic field \vec{H}_{eff}



Magnetization Dynamics

Landau-Lifshitz damping term

- Previous gyromagnetic precession equation **incomplete in explaining magnetization dynamics**

$$\frac{d\vec{M}}{dt} = -\gamma \left(\vec{M} \times \vec{H}_{eff} \right)$$

- Shown in the 1950s: **The magnetization, \vec{M} , returns to its equilibrium** when no field, \vec{H}_{eff} , is applied.
- Precession angle decreases to zero at equilibrium, aligning \vec{M} with \vec{H}_{eff}

- To explain this phenomenon, Lev **Landau** and Evgeny **Lifshitz** introduced the damping term (DLL):

$$\vec{D}_{LL} = -\frac{\alpha_{LL}}{M_S} \vec{M} \times \left(\vec{M} \times \vec{H}_{eff} \right) \quad (7)$$

M_S : saturation magnetization

α_{LL} : Landau-Lifshitz damping coefficient

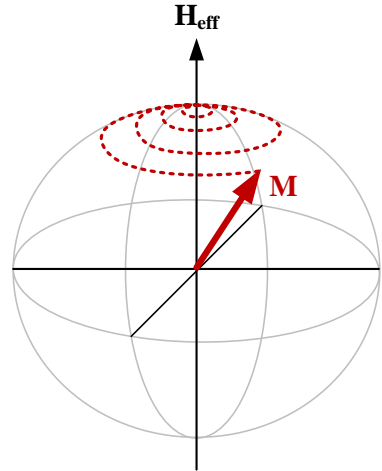
Magnetization Dynamics

Landau-Lifshitz damping term

- We can rewrite the magnetization dynamics including DLL term

$$\frac{d\vec{M}}{dt} = -\gamma_{LL} \left(\vec{M} \times \vec{H}_{eff} \right) - \frac{\alpha_{LL}}{M_S} \vec{M} \times \left(\vec{M} \times \vec{H}_{eff} \right) \quad (8)$$

- This is the Landau-Lifshitz (LL) equation.
- Note: An increased damping should result in a deceleration of magnetization motion



Magnetization Dynamics

Gilbert damping term

- In 1955, Gilbert introduced an alternative damping term.

$$\vec{D}_G = \frac{\alpha_G}{M_S} \left(\vec{M} \times \frac{d\vec{M}}{dt} \right) \quad (9)$$

- α_G : Gilbert damping coefficient

- Gilbert equation for magnetization dynamics:

$$\frac{d\vec{M}}{dt} = -\gamma_G \left(\vec{M} \times \vec{H}_{eff} \right) + \frac{\alpha_G}{M_S} \left(\vec{M} \times \frac{d\vec{M}}{dt} \right) \quad (10)$$

Magnetization Dynamics

Landau-Lifshitz-Gilbert Equation

- Two equations:
 - Landau-Lifshitz
 - Gilbert
- Both equations are mathematically equivalent
- **The Gilbert form has been demonstrated to be more precise for a wide number of the damping constants**
 - As a result, the majority of literature considers the Gilbert gyromagnetic ratio

- After some math (cross product of both sides of equation with \vec{M}) and simplifications ($\vec{M} \cdot \frac{d\vec{M}}{dt} = 0$), we can obtain:

$$\frac{d\vec{M}}{dt} = -|\gamma_{LL}| \left(\vec{M} \times \vec{H}_{eff} \right) - \frac{|\gamma_{LL}| \alpha}{M_S} \vec{M} \times \left(\vec{M} \times \vec{H}_{eff} \right)$$

- where: $\gamma_{LL} = \gamma / (1 + \alpha^2)$

$$\frac{d\vec{M}}{dt} = -|\gamma| \left(\vec{M} \times \vec{H}_{eff} \right) + \frac{\alpha}{M_S} \left(\vec{M} \times \frac{d\vec{M}}{dt} \right)$$

Magnetization Dynamics

Landau-Lifshitz-Gilbert Equation

- The simplified magnetization equations of a magnetic moment \vec{m} in presence of torque generating by an external field and damping:

- Note:

$$\vec{M} = \vec{m} M_S$$

- \vec{m} : unit vector of \vec{M}

$$\frac{d\vec{m}}{dt} = -\gamma_{LL} \left(\vec{m} \times \vec{H}_{eff} \right) - \alpha \gamma_{LL} \vec{m} \times \left(\vec{m} \times \vec{H}_{eff} \right) \quad (11)$$

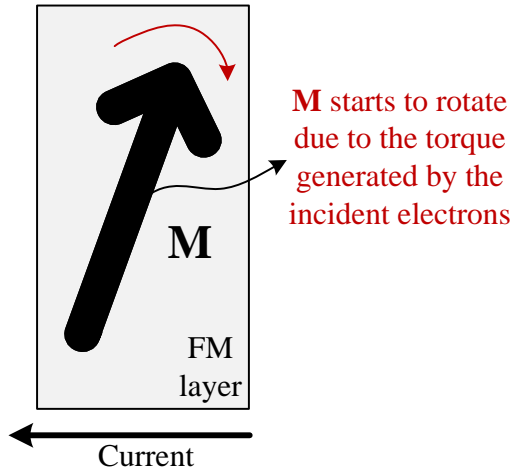
$$\frac{d\vec{m}}{dt} = -\gamma \left(\vec{m} \times \vec{H}_{eff} \right) + \alpha \left(\vec{m} \times \frac{d\vec{m}}{dt} \right) \quad (12)$$



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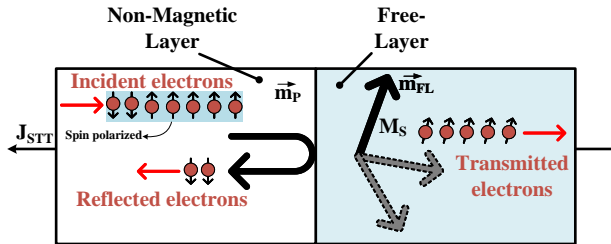
Spin-Transfer Torque

- FM layer serves as a spin filter while also absorbing the spin angular momentum of incident electrons.
- The change in spin angular momentum of the incident electrons \Rightarrow change in spin angular momentum of orbital electrons in an FM.
- Therefore, this change in the orbital electrons acts as a **torque** on the magnetization \vec{M} of the FM layer



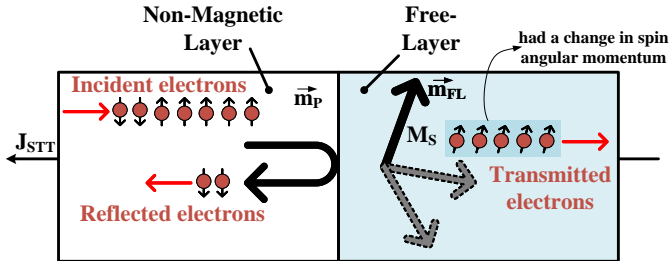
Spin-Transfer Torque

- Consider a single ferromagnetic layer:
 - Free-Layer (FL): can change its magnetization direction under the influence of spin-polarized current.
 - The FL has a saturation magnetization M_S and a unit vector \vec{m}_{FL} that points toward its magnetization direction
- A current density J_{STT} is applied
 - Spin-polarization unit vector of the current represented as \vec{m}_P
- “Scattering”** at the interface of the non-magnetic (NM) layer and FL.



Spin-Transfer Torque

- Transmitted electrons had a change in spin angular momentum
 - During this stage, there is a **transfer of spin angular momentum** between the FL and the incident electrons
- The **change of magnetization direction of the FL** takes place only if there is enough **torque** by the incident electrons.

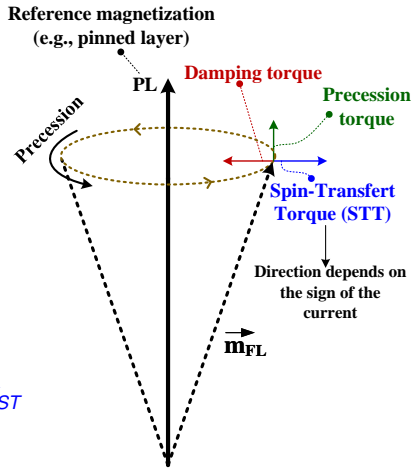


Slonczewski's torque and LLGS equation

- The torque acting on the FL is known as **Slonczewski's torque**
 - Slonczewski's torque aids or opposes damping torque to decide FM free layer's magnetization
 - Along with STT torque we have the precession torque, which acts of the precessional motion of the \vec{m}_{FL}
 - The torques **only exhibit their effect** when the **magnetization** of the system is in a **non-equilibrium position**.

$$\frac{d\vec{m}_{FL}}{dt} = -\gamma_{LL} \left(\vec{m}_{FL} \times \vec{H}_{eff} \right) - \alpha \gamma_{LL} \vec{m}_{FL} \times \left(\vec{m}_{FL} \times \vec{H}_{eff} \right) + \vec{\tau}_{ST}$$

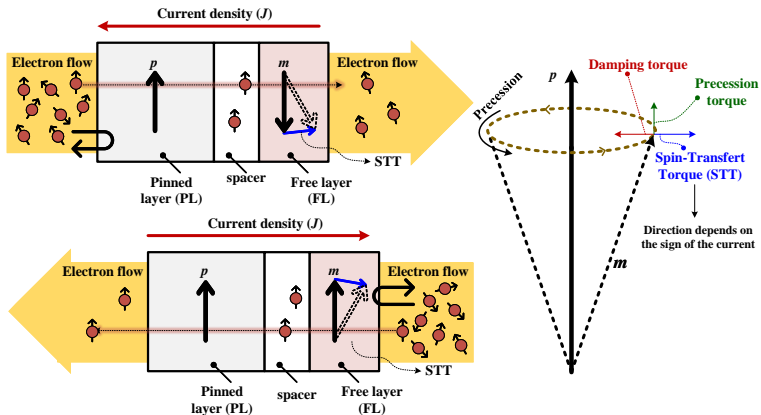
$\vec{\tau}_{ST}$ is the STT term defined as:
 $\sigma I \vec{m}_{FL} \times (\vec{m}_{FL} \times \vec{m}_{PL})$



Example of FL magnetization switching:
Here

STT in Multilayers

- Two switching transitions
 - Anti-Parallel (AP) to Parallel (P) – top fig
 - P to AP – bottom fig
- AP \rightarrow P
 - **Current** (electron) flow from FL (PL) to PL (FL)
 - “easier” to switch (need less current than P \rightarrow AP)
- P \rightarrow AP
 - **Current** (electron) flow from PL (FL) to FL (PL)
 - “harder” to switch (need more current than AP \rightarrow P)

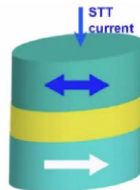
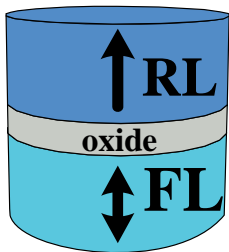


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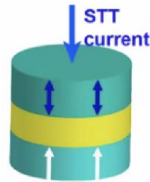


Spintronic Devices

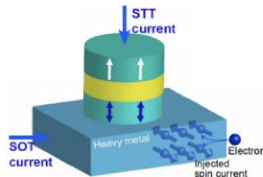
- Magnetic tunnel junction (MTJ): two FMs (RL and FL) separated by an oxide barrier
- Two stable states: parallel (low-resistance) and antiparallel (high resistance)



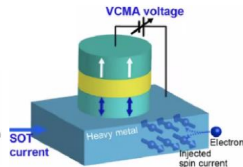
STT-iMTJ



STT-pMTJ



SOT + STT



SOT + VCMA

Source: W. Zhao, "Roadmap for the future MTJs", Beihang Spintronics Interdisciplinary Center. 2021

Spintronic Applications

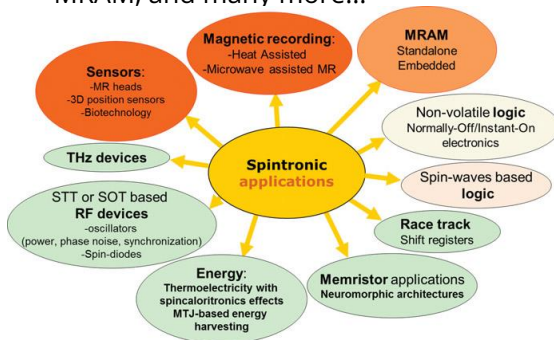
- Two spintronics roadmaps presented in 2019 and 2020

J1. Dieny, Bernard, et al. "The SpinTronicFactory roadmap: A European community view." (2019).

J2. Dieny, Bernard, et al. "Opportunities and challenges for spintronics in the microelectronics industry." Nature Electronics 3.8 (2020): 446-459.

- Spintronics applications:

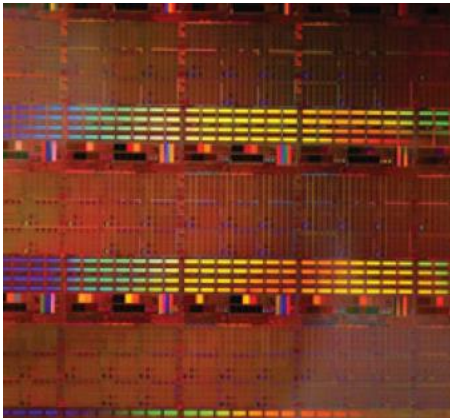
- Logic Devices,
- RF devices,
- Magnetic Sensors,
- MRAM, and many more...



Source: imec, "The SpinTronicFactory roadmap", 2019

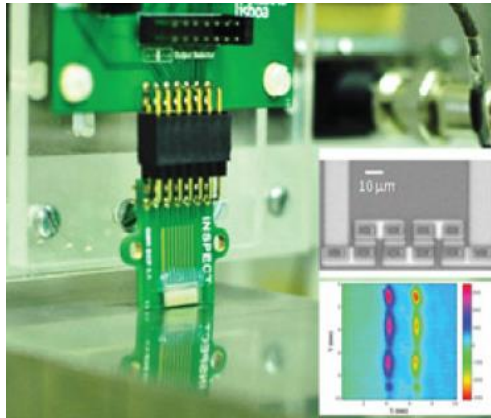
Spintronic Applications

Prototypes



**Integrated circuit exploiting hybrid
CMOS/Magnetic technology**

Source: imec, "The SpinTronicFactory roadmap", 2019



**Array of MTJ sensors for non-
destructive testing**

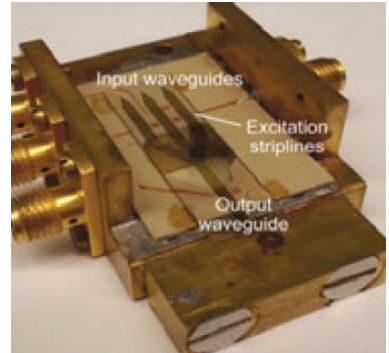
Spintronic Applications

Prototypes



PCB board for STT RF emitters

Source: imec, "The SpinTronicFactory roadmap", 2019



Spin wave majority gate

Spintronic Applications

pillars, motivation to MRAM a big phase that states we are focusing to focus on memories!

Four main pillars according to the Spintronics European community view ([Here](#))

Memories

Magnetic Sensors

Radio-frequency and microwaves devices

Logic and non-Boolean devices



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Summary

- This Lecture covered the basics of STT and magnetization dynamics.
- Spin-polarized transport through NM materials is explained, including spin polarization, filtering, and injection.
- The mathematical formalism of magnetization dynamics was also introduced
- The LLG equation, magnetization damping, magnetization precession, and STT are explained
- It provides an overview on spintronic devices and applications.
- **Overall, this part provides an overview of the Spintronic fundamentals that serves as a foundation for understanding the remaining of this course.**

