1. A program has a 30% of code that can be parallelized. Since this program is going to be run for a long time, ¿should you invest in a 2 CPU, 4 CPU or 8 CPU server?

For n = 2 and s = 0.70

$$\frac{1}{.7 + \frac{1 - .7}{2}} = \frac{1}{.7 + \frac{.3}{2}} = \frac{1}{0.85} = 1.1765x$$

For n = 4 and s = 0.70

$$\frac{1}{.7 + \frac{1 - .7}{4}} = \frac{1}{.7 + \frac{.3}{4}} = \frac{1}{0.775} = 1.2903x$$

For n = 8 and s = 0.70

$$\frac{1}{.7 + \frac{1 - .7}{8}} = \frac{1}{.7 + \frac{.3}{8}} = \frac{1}{0.7375} = 1.3559x$$

It would be recommended to invest (according to time investment) on the 8 CPU server, as it offers the higher speedup factor. However, the 4 CPU server can also be regarded as a possible solution as it has the best improvement of all 3 possible solutions (investing from 2 to 4 servers adds up to the speedup factor 0.1138x, while investing from a 4 to an 8 CPU server only adds 0.0656x). In other words, depending on the priority of the client (highest speedup factor or better cost-relation), the 4 or 8 CPU are viable alternatives.

2. Would it be better to have a program with 10% parallelism and 8 CPUs, 20% with 4 or 25% with 2?

For n = 8 and s = 0.90

$$\frac{1}{.9 + \frac{1 - .9}{8}} = \frac{1}{.9 + \frac{.1}{8}} = \frac{1}{0.9125} = 1.0959x$$

For n = 4 and s = 0.80

$$\frac{1}{.8 + \frac{1 - .8}{4}} = \frac{1}{.8 + \frac{.2}{4}} = \frac{1}{0.85} = 1.1765x$$

For n = 2 and s = 0.75

$$\frac{1}{.5 + \frac{1 - .75}{2}} = \frac{1}{.75 + \frac{.25}{2}} = \frac{1}{0.875} = 1.1429x$$

The best alternative would be a 4 CPU device with a 20% paralleled code.

3. Consider you have a program that takes 10 hours to run on a 1 core CPU. You only need to run it once, and you have an 8 CPU computer. Optimizing 5% of the code takes 20 minutes. The code can be optimized to be at most 35% parallel. How much time should you invest optimizing the code so the time for optimization+running is the lowest.

For n = 8 and s = 0.95

$$\frac{1}{.95 + \frac{1 - .95}{8}} = \frac{1}{.95 + \frac{.05}{8}} = \frac{1}{0.9563} = 1.0457x$$

$$\frac{10}{1.0457} = 9.5630 \ hr \rightarrow 0.5630 \ hr = 33.78 \ min$$

$$9 hr + 33.78 min + 4(5 min) = 9 hr 53.78 min$$

For n = 8 and s = 0.90

$$\frac{1}{.90 + \frac{1 - .90}{8}} = \frac{1}{.90 + \frac{.10}{8}} = \frac{1}{0.9125} = 1.0959x$$

$$\frac{10}{1.0959} = 9.1249 \ hr \rightarrow 0.1249 \ hr = 7.494 \ min$$

$$9 hr + 7.494 min + 4(10 min) = 9 hr 47.494 min$$

For n = 8 and s = 0.85

$$\frac{1}{.85 + \frac{1 - .85}{9}} = \frac{1}{.85 + \frac{.15}{9}} = \frac{1}{0.8688} = 1.1510x$$

$$\frac{10}{1.1510} = 8.6881 \ hr \to 0.6881 \ hr = 41.286 \ min$$

$$8 hr + 41.286 min + 4(15 min) = 9 hr 41.286 min$$

For n = 8 and s = 0.80

$$\frac{1}{.80 + \frac{1 - .80}{8}} = \frac{1}{.80 + \frac{.20}{8}} = \frac{1}{0.8250} = 1.2121x$$

$$\frac{10}{1.2121} = 8.2501 \, hr \to 0.2501 \, hr = 15.006 \, min$$

$$8 hr + 15.006 min + 4(20 min) = 9 hr 35.006 min$$

For n = 8 and s = 0.75

$$\frac{1}{.75 + \frac{1 - .75}{8}} = \frac{1}{.75 + \frac{.25}{8}} = \frac{1}{0.78125} = \mathbf{1.28}x$$

$$\frac{10}{1.28} = 7.8125 \, hr \to 0.8125 \, hr = 48.75 \, min$$

$$7 hr + 48.75 min + 4(25 min) = 9 hr 28.75 min$$

For n = 8 and s = 0.70

$$\frac{1}{.70 + \frac{1 - .70}{8}} = \frac{1}{.70 + \frac{.3}{8}} = \frac{1}{0.7375} = \mathbf{1.3560}x$$

$$\frac{10}{1.3560} = 7.3746 \ hr \rightarrow 0.3746 \ hr = 22.476 \ min$$

$$7 hr + 22.476 min + 4(30 min) = 9 hr 22.476 min$$

For n = 8 and s = 0.65

$$\frac{1}{.65 + \frac{1 - .65}{8}} = \frac{1}{.65 + \frac{.35}{8}} = \frac{1}{0..6938} = \mathbf{1.4413}x$$

$$\frac{10}{1.4413} = 6.9382 \ hr \to 0.9382 \ hr = 56.29 \ min$$

$$6 hr + 56.29 min + 4(35 min) = 9 hr 16.29 min$$

With a limit of 35% regarding the maximum code optimization, the best optimization+running time is found when the code has been optimized up to a 35% (the maximum percentage allowed by this exercise).