

exercicio_2

May 9, 2022

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
from scipy.interpolate import interp1d
import pandas as pd
```

```
[ ]: def C_converge(C_t,d,tau,F_max):

    k = 0

    while k < 100:

        Ks = (4*C_t - 1)/(4*C_t - 4) + 0.675/C_t

        C_p = tau*np.pi*d**2/(8*F_max*Ks)

        error = ((C_p-C_t)**2)**0.5

        C_t = (C_p+C_t)/2

        if error <= C_t*0.01:
            return C_t
```

```
[ ]: # constantes

Su = 1250e6
Su_lim = 0.80
Su_vida_inf = 0.44
Sy_lim = 0.65
F_min = 250
F_max = 500
Fs = 1.1 * F_max
delta_p = 25e-3
G = 79e9
E = 207e9
rho = 7700
```

```
[ ]: # plotagem diagrama de goodman

fig = plt.figure(figsize=[16, 9])
fig.suptitle('Diagrama de Goodman modificado', fontsize=16)

linha_sobrecarga_1 = np.array(
    ([0,Su_vida_inf],
     [Su_lim,Su_lim])
)

linha_sobrecarga_2 = np.array(
    ([0,Sy_lim],
     [Su_lim,Sy_lim])
)

linha_carga = np.array(
    ([0,0],
     [Su_lim*(F_min/F_max),Su_lim])
)

# Plotando 2D

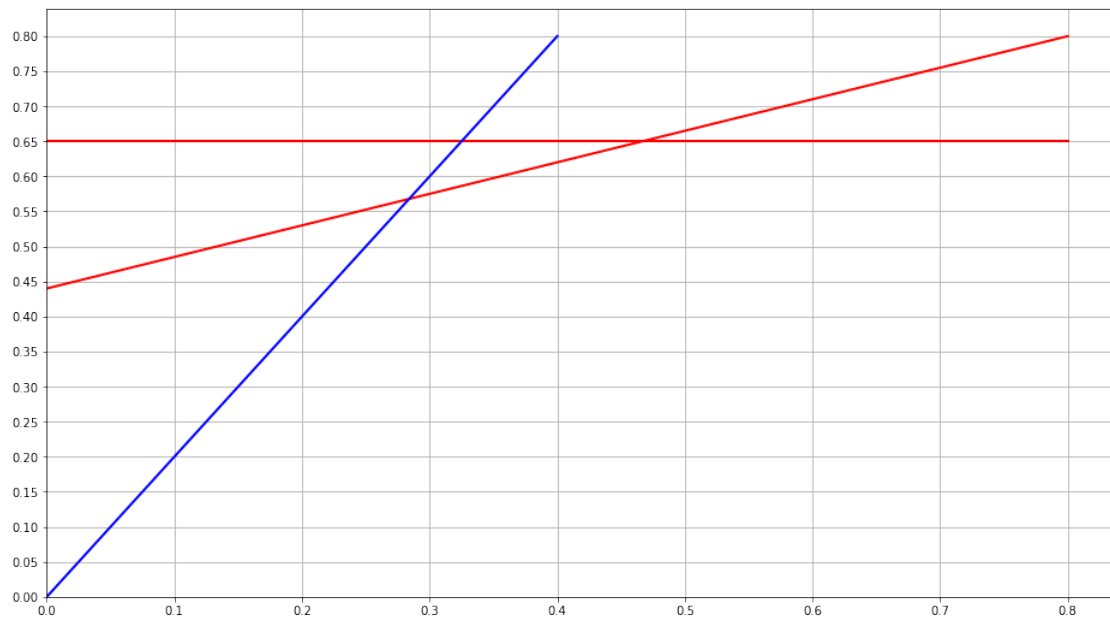
ax = fig.add_subplot(1, 1, 1)

ax.plot(linha_sobrecarga_1[:,0], linha_sobrecarga_1[:,1], 'r', linewidth=2)
ax.plot(linha_sobrecarga_2[:,0], linha_sobrecarga_2[:,1], 'r', linewidth=2)
ax.plot(linha_carga[:,0], linha_carga[:,1], 'b', linewidth=2)

ax.set_xlim(0)
ax.set_ylim(0)
ax.locator_params(axis='y', nbins=20)
ax.grid()

plt.show()
```

Diagrama de Goodman



```
[ ]: # encontrando tensão limite

tensao_max_teorico = 0.52 * Su

f_seguranca = 0.1

f_mola_solida = 0.1

tensao_max = tensao_max_teorico/(1+f_seguranca)/(1+f_mola_solida)
print('{:.2e} MPa'.format(tensao_max/1e6))
```

5.37e+02 MPa

```
[ ]: # estabelecendo um diâmetro alvo

C_t = 10

Kw = (4*C_t - 1)/(4*C_t - 4) + 0.615/C_t

d_alvo = (8*F_max*C_t*Kw/(np.pi*tensao_max))**0.5

print('{:.2e} mm'.format(d_alvo*1e3))
```

5.21e+00 mm

```
[ ]: k = (F_max-F_min)/delta_p
k
```

```
[ ]: 10000.0
```

```
[ ]: # iterando diâmetros para achar a melhor solução

d_mm_list = np.linspace(4,18,num=15,dtype=int)

C_list = []
D_list = []
Nt_list = []
Lf_D_list = []
delta_Lf_list = []
V_list = []
P_list = []
fn_list = []
d_list = []

for i,d_mm in enumerate(d_mm_list):

    d = d_mm*1e-3

    C = C_converge(C_t,d,tensao_max,F_max)

    D = C * d

    N = d * G/(8 * C**3 * k)

    N_t = N + 2

    Ls = N_t * d

    delta = Fs/k

    L_f = Ls + delta

    Lf_D = L_f/D

    delta_Lf = delta/L_f

    V = (np.pi * d **2 / 4) * 2*np.pi *D/2

    P = V * rho

    fn = 353e3*d/(N*D**2) * 60
```

```

C_list.append(C)
D_list.append(D)
Nt_list.append(N_t)
Lf_D_list.append(Lf_D)
delta_Lf_list.append(delta_Lf)
V_list.append(V)
P_list.append(P)
fn_list.append(fn)
d_list.append(d)

df = pd.DataFrame(np.vstack((
    d_list,
    C_list,
    D_list,
    Nt_list,
    Lf_D_list,
    delta_Lf_list,
    V_list,
    P_list,
    fn_list
)).T, columns=[
    'd',
    'C',
    'D',
    'Nt',
    'Lf/D',
    'delta/Lf',
    'V',
    'P',
    'fn'
])

df

```

```

[ ]:

```

	d	C	D	Nt	Lf/D	delta/Lf	V \
0	0.004	5.183055	0.020732	30.368715	8.512106	0.311659	8.184752e-07
1	0.005	9.089688	0.045448	8.574461	2.153480	0.561957	2.803488e-06
2	0.006	13.643828	0.081863	4.332811	0.989420	0.679039	7.271596e-06
3	0.007	19.137260	0.133961	2.986270	0.566613	0.724601	1.619622e-05
4	0.008	25.441376	0.203531	2.479739	0.367698	0.734922	3.214033e-05
5	0.009	32.584411	0.293260	2.256892	0.256810	0.730295	5.861073e-05
6	0.010	40.566833	0.405668	2.147919	0.188526	0.719150	1.000946e-04
7	0.011	49.388901	0.543278	2.090166	0.143558	0.705202	1.621986e-04
8	0.012	59.050764	0.708609	2.057550	0.112461	0.690169	2.517729e-04
9	0.013	69.552513	0.904183	2.038154	0.090132	0.674880	3.770358e-04
10	0.014	80.894207	1.132519	2.026116	0.073611	0.659744	5.476982e-04
11	0.015	93.075886	1.396138	2.018370	0.061080	0.644968	7.750875e-04

12	0.016	106.097575	1.697561	2.013229	0.051375	0.630650	1.072272e-03
13	0.017	119.959294	2.039308	2.009725	0.043723	0.616832	1.454188e-03
14	0.018	134.661056	2.423899	2.007279	0.037597	0.603527	1.937757e-03

	P	fn
0	0.006302	6.947918e+06
1	0.021587	7.798262e+06
2	0.055991	8.128728e+06
3	0.124711	8.376692e+06
4	0.247481	8.526081e+06
5	0.451303	8.628071e+06
6	0.770729	8.700815e+06
7	1.248929	8.754530e+06
8	1.938651	8.795325e+06
9	2.903176	8.827037e+06
10	4.217276	8.852179e+06
11	5.968173	8.872449e+06
12	8.256498	8.889029e+06
13	11.197244	8.902765e+06
14	14.920728	8.914271e+06

```
[ ]: # Análise gráfica

# plotagem do peso em função do diametro

fig = plt.figure(figsize=[16, 9])
fig.suptitle('Peso em função do diametro do fio', fontsize=16)

# Plotando 2D

ax = fig.add_subplot(1, 1, 1)

ax.plot(d_list,
        df['P'],
        'o',
        d_list,
        df['P'],
        '-',
        color='b',
        )

ax.locator_params(axis='y', nbins=30)
ax.locator_params(axis='x', nbins=30)
ax.grid()

plt.show()
```

```

# análise de flambagem

fig = plt.figure(figsize=[16, 9])
fig.suptitle('Análise de flambagem', fontsize=16)

flambagem_seed = np.array((
    [5.2,0.75],
    [10,0.1375],
    [9,0.1625],
    [6,0.3667],
    [8,0.2],
    [7,0.252]
))

flambagem_eval = np.linspace(
    min(flambagem_seed[:,0]),
    max(flambagem_seed[:,0]),
    num=200
)

# Análise de flambagem

fig = plt.figure(figsize=[16, 9])
fig.suptitle('Análise de flambagem', fontsize=16)

# Plotando 2D

ax = fig.add_subplot(1, 1, 1)

f2 = interp1d(
    flambagem_seed[:,0],
    flambagem_seed[:,1],
    kind='cubic'
)

curva_A = f2(flambagem_eval) # use interpolation function returned by
↪ `interp1d`

ax.plot(flambagem_seed[:,0],
        flambagem_seed[:,1],
        'o',
        flambagem_eval,
        curva_A,
        '-',
        color='r',
        label='curva de flambagem A')

```

```

)

ax.plot(df['Lf/D'],
        df['delta/Lf'],
        'o',
        df['Lf/D'],
        df['delta/Lf'],
        '-',
        color='b',
        label='curva experimental'
)

ax.locator_params(axis='y', nbins=30)
ax.locator_params(axis='x', nbins=30)
ax.grid()
ax.legend()

plt.show()

# Análise de frequência natural

fig = plt.figure(figsize=[16, 9])
fig.suptitle('frequência natural em função do diametro', fontsize=16)

# Plotando 2D

ax = fig.add_subplot(1, 1, 1)

ax.plot(d_list,
        df['fn'],
        'o',
        d_list,
        df['fn'],
        '-',
        color='b',
        label="curva experimental"
)

ax.plot([0,max(d_list)],
        [650,650],
        '-',
        color='r',
        label = 'Frequência da aplicação'
)

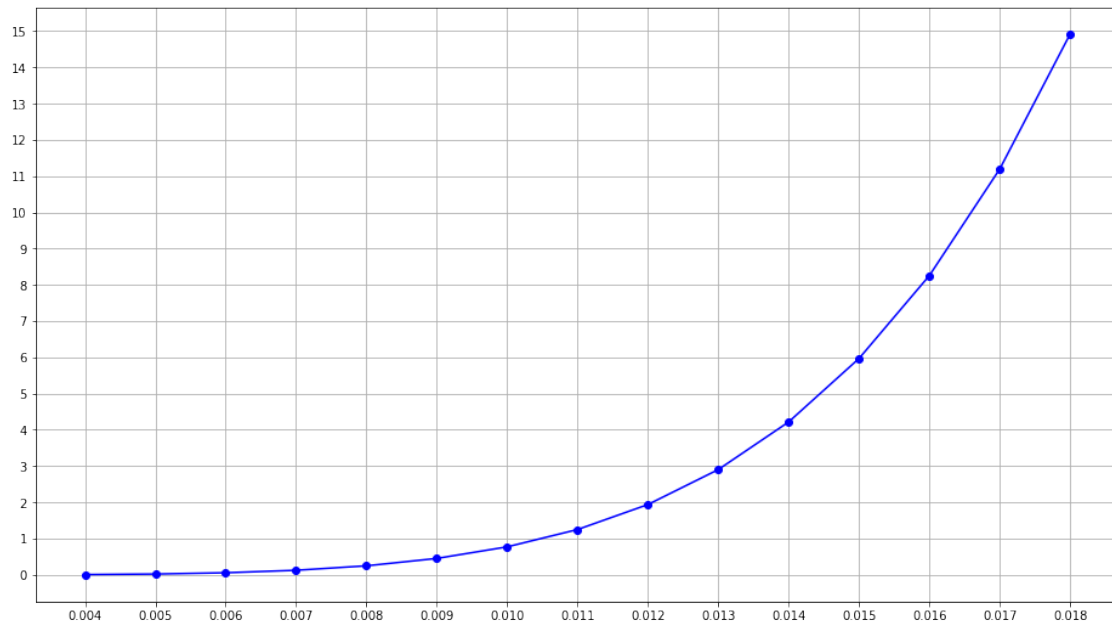
ax.locator_params(axis='y', nbins=30)
ax.locator_params(axis='x', nbins=30)

```



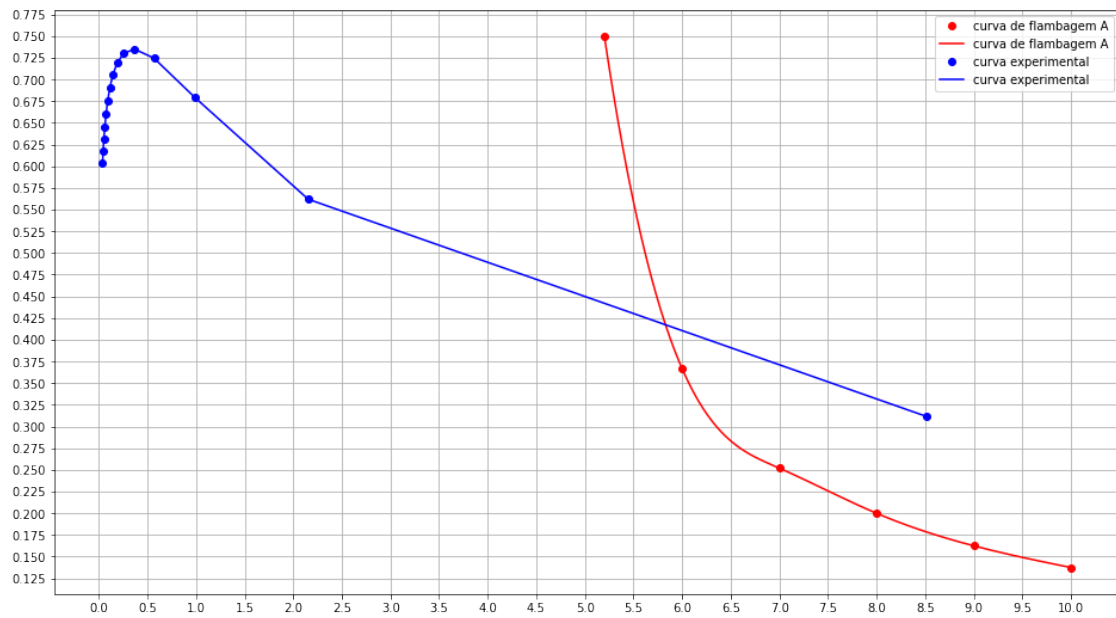
```
ax.grid()  
ax.legend()  
  
plt.show()
```

Peso em função do diametro do fio

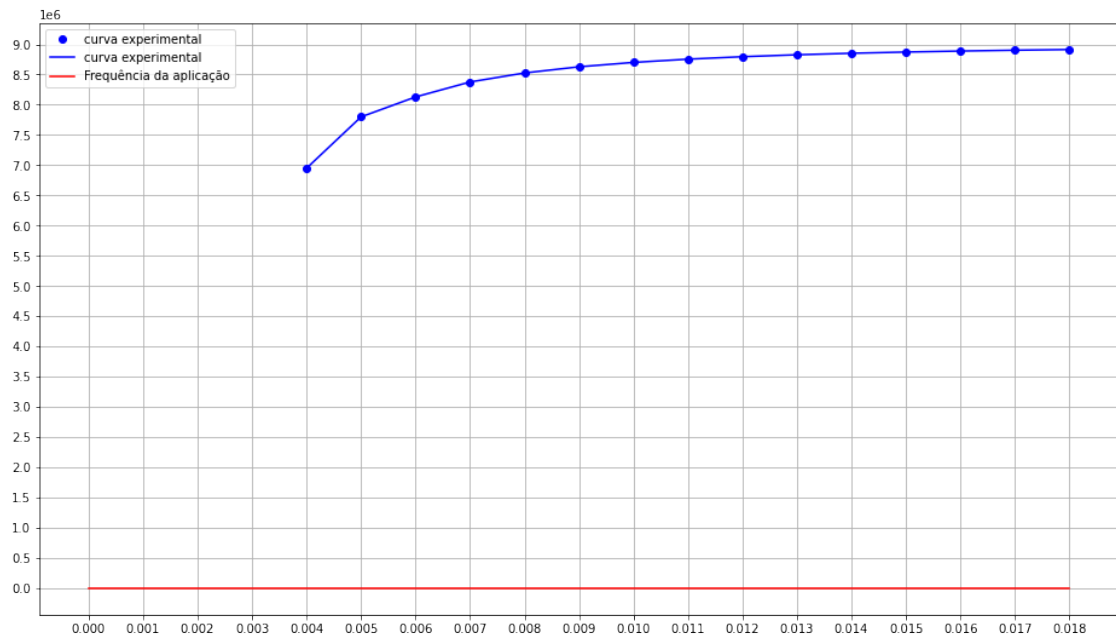


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Análise de flambagem



frequência natural em função do diametro



[]: