

$$\textcircled{1} \text{ a) } \begin{vmatrix} 2 & 3 \\ 1 & 5 \end{vmatrix} = 10 - 3 = 7 \therefore \underline{\underline{D=7}}$$

$$\text{b) } \begin{vmatrix} -2 & -4 \\ 3 & 6 \end{vmatrix} = -12 + 12 = 0 \therefore \underline{\underline{D=0}}$$

$$\text{c) } \begin{vmatrix} 3 & -1 & 1 \\ 2 & 1 & -1 \\ 1 & 4 & -2 \end{vmatrix} = -6 + 1 + 8 - 1 + 12 - 4 = 10 \therefore \underline{\underline{D=10}}$$

$$\text{d) } \begin{vmatrix} 3 & 2 & -1 \\ 2 & 3 & 1 \\ 1 & 1 & 4 \end{vmatrix} = 36 + 2 - 2 + 3 - 3 - 16 = 20 \therefore \underline{\underline{D=20}}$$

2) $A_{3 \times 3}$

$$\begin{cases} -3, & \text{se } i=j \\ 0, & \text{se } i \neq j \end{cases}$$

$$\begin{vmatrix} -3 & 0 & 0 \\ 0 & -3 & 0 \\ 0 & 0 & -3 \end{vmatrix}$$

$$\therefore -3 \cdot -3 \cdot -3 \\ D = -27$$

$$D(A) = ?$$

$$(A) = -27$$

3)

$$\begin{vmatrix} x & 1 & x \\ 3 & x & 4 \\ 1 & 3 & 3 \end{vmatrix} = -3$$

$$\hookrightarrow 3x^2 + 4 + 9x - x^2 - 12x - 9 = -3 \\ 2x^2 - 3x - 2 = 0$$

$$(-3)^2 - 4 \cdot 2 \cdot (-2) \\ 9 + 16$$

$$25$$

$$\frac{3 \pm 5}{4}$$

$$2$$

$$-1/2$$

$$\rightarrow x = \left\{ -\frac{1}{2}, 2 \right\}$$

(E)

4)

$$\begin{vmatrix} (x-1) & -1 & 0 \\ 0 & (x+1) & -1 \\ 2 & -1 & (x+1) \end{vmatrix} = 2$$

$$\rightarrow x(x^2 + x - 2) = 0$$

$$I. x^2 + x - 2 = 0$$

$$1^2 - 4 \cdot 1 \cdot (-2)$$

$$1 + 8$$

$$9$$

$$\rightarrow \frac{-1 \pm 3}{2} \quad \frac{2}{2} = 1$$

$$\frac{-1 - 3}{2} = -2$$

$$x^2 + x + x + 1(x-1)$$

$$x^3 + 2x^2 + x - x^2 - 2x - 1$$

$$x^3 + x^2 - x + 1 + 2 - x + 1 = 2$$

$$x^3 + x^2 - 2x = 0$$

$$II. x = 0$$

$$\therefore 0 + 1 - 2 = -1$$

$$(C) = -1$$

⑤ $A_{3 \times 2} \quad a_{ij} = 2i - 3j$

$B_{2 \times 3} \quad b_{jk} = K - j$

$$A = \begin{vmatrix} -1 & -4 \\ 1 & -2 \\ 3 & 0 \end{vmatrix}$$

$$B = \begin{vmatrix} 0 & 1 & 2 \\ -1 & 0 & 1 \end{vmatrix}$$

$A \cdot B$

$$0 + 4 - 1 + 0 - 2 - 4$$

$$0 + 2 \quad 1 + 0 \quad 2 - 2$$

$$0 + 0 \quad 3 + 0 \quad 6 + 0$$

$$\begin{vmatrix} 4 & -1 & -6 \\ 2 & 1 & 0 \\ 0 & 3 & 6 \end{vmatrix} =$$

$$24 - 0 - 36 - 0 - 0 + 12 = 0$$

$$\therefore D = 0$$

(C) 0

⑥ $\begin{vmatrix} 2 & 0 & -1 \\ -1 & 1 & 0 \end{vmatrix} \cdot \begin{vmatrix} 1 & -1 \\ -1 & 1 \\ 0 & 2 \end{vmatrix} =$

$$\begin{vmatrix} 2 & 1 & 0 & -1 & 0 \\ -2 & -1 & 0 & 1 & 0 \\ 0 & -2 & 0 & 2 & 0 \end{vmatrix}$$



$$\begin{vmatrix} 3 & -1 & -1 \\ -3 & 1 & 1 \\ -2 & 2 & 0 \end{vmatrix} =$$

$$0 + 2 + 6 - 2 - 6 - 0 = 0$$

$$D = 0$$

(C) 0