

Tarea 16

Vectores y Valores propios

$$\begin{pmatrix} -2 & -2 \\ -5 & 1 \end{pmatrix} \quad \begin{pmatrix} -2\lambda & -2 \\ -5 & -1\lambda \end{pmatrix} \quad \begin{aligned} &(-2-\lambda)(1-\lambda) - (-5)(-2) \\ &= -2\lambda + 2\lambda - \lambda + \lambda^2 - 10 \\ &\lambda^2 + 1\lambda - 12 \end{aligned}$$

$$\lambda^2 + \lambda - 12 = 0$$

$$(\lambda + 4)(\lambda - 3) = 0$$

$$\lambda + 4 = 0 \quad \lambda - 3 = 0$$

$$\lambda_1 = -4 \quad \lambda_2 = 3$$

Polinomio
Característico

Valores propios.

$$\text{Valores propios. } \begin{pmatrix} 2x & -2y \\ -5x & 5y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

②

$$\begin{pmatrix} -9 & 7 \\ -7 & 5 \end{pmatrix} \quad \begin{pmatrix} -9-\lambda & 7 \\ -7-\lambda & 5 \end{pmatrix} \quad \begin{aligned} &(-9-\lambda)(5-\lambda) - (7)(-7) \\ &= 63\lambda - 35 \end{aligned}$$

Polinomio.
Característico

$$63\lambda - 35 = 0$$

$$\lambda 63 - 35 = 0$$

$$\lambda 63 = 0 \quad \lambda 35 = 0$$

$$\begin{pmatrix} -9 & 7 \\ -7 & 5 \end{pmatrix} \quad \begin{pmatrix} -9+63 & 7-35 \\ 7 & 5 \end{pmatrix}$$

$$\begin{pmatrix} -34 & -28 \\ 7 & 5 \end{pmatrix} \quad \begin{pmatrix} 26 \\ 12 \end{pmatrix}$$

③

$$\begin{pmatrix} -3 & 0 \\ 0 & -3 \end{pmatrix} = \begin{pmatrix} -3-\lambda & 0 \\ 0 & -3-\lambda \end{pmatrix} = (-3-\lambda)(-3-\lambda) - (0)(0) = 9\lambda + 0$$

$$9\lambda + 0 = 0$$

$$(\lambda + 9)(\lambda + 0) = 0$$

$$\lambda = 9 \quad \lambda = 0$$

$$\begin{pmatrix} -3+9 & 0+0 \\ 0 & -3 \end{pmatrix} = \begin{pmatrix} 6x & 0y \\ 0x & -3y \end{pmatrix} = \begin{pmatrix} 6x \\ -3y \end{pmatrix}$$

$$3) \begin{pmatrix} 3 & 2 \\ -5 & 1 \end{pmatrix} = 3 - \lambda \quad 2 = (3 + \lambda)(1 - \lambda) - (2)(-5)$$

$$3\lambda + -10 //$$

$$9\lambda + -10 = 0$$

$$(\lambda + 9)(\lambda - 10)$$

$$\lambda = 9 \quad \lambda = -10$$

$$\begin{pmatrix} 3+9 & 2-10 \\ -5 & 1 \end{pmatrix} = \begin{pmatrix} 12 & -8 \\ -5 & 1 \end{pmatrix} = \begin{pmatrix} -2x \\ -4y \end{pmatrix}$$