

Design Analysis And Algorithms

Dijkstra's Shortest Path:

```
import java.util.Scanner;
import java.util.HashMap;
import java.util.ArrayList;
import java.util.List;
import java.util.Map;
import java.util.Set;
import java.util.Collections;
import java.util.HashSet;
class BinaryMinHeap<T> {
    private Map<T, Integer> nodePosition;
    private List<Node> heap;
    private int maxSize;

    public BinaryMinHeap(int maxSize) {
        this.nodePosition = new HashMap<>();
        this.heap = new ArrayList<>(maxSize);
        this.maxSize = maxSize;
    }

    public void add(int weight, T key) {
        if (nodePosition.containsKey(key)) {
            decrease(key, weight);
        } else {
            Node node = new Node();
            node.weight = weight;
            node.key = key;
            heap.add(node);
            nodePosition.put(key, heap.size() - 1);
            heapifyUp(heap.size() - 1);
        }
    }

    public void decrease(T key, int newWeight) {
        int position = nodePosition.get(key);
        Node node = heap.get(position);
        node.weight = newWeight;
        heapifyUp(position);
    }

    public boolean containsData(T key) {
        return nodePosition.containsKey(key);
    }
}
```

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```
public boolean empty() {
    return heap.isEmpty();
}

public Node extractMinNode() {
    Node minNode = heap.get(0);
    Node lastNode = heap.remove(heap.size() - 1);
    nodePosition.remove(minNode.key);
    if (!heap.isEmpty()) {
        heap.set(0, lastNode);
        nodePosition.put(lastNode.key, 0);
        heapifyDown(0);
    }
    return minNode;
}

public int getWeight(T key) {
    Integer position = nodePosition.get(key);
    if (position == null) {
        return Integer.MAX_VALUE;
    } else {
        return heap.get(position).weight;
    }
}

private void heapifyUp(int currentIndex) {
    int parentIndex = (currentIndex - 1) / 2;
    while (currentIndex > 0 && heap.get(currentIndex).weight < heap.get(parentIndex).weight) {
        swap(currentIndex, parentIndex);
        currentIndex = parentIndex;
        parentIndex = (currentIndex - 1) / 2;
    }
}

private void heapifyDown(int currentIndex) {
    int leftIndex = 2 * currentIndex + 1;
    int rightIndex = 2 * currentIndex + 2;
    int smallest = currentIndex;

    if (leftIndex < heap.size() && heap.get(leftIndex).weight < heap.get(smallest).weight) {
        smallest = leftIndex;
    }
    if (rightIndex < heap.size() && heap.get(rightIndex).weight < heap.get(smallest).weight) {
```

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```
        smallest = rightIndex;
    }

    if (smallest != currentIndex) {
        swap(currentIndex, smallest);
        heapifyDown(smallest);
    }
}

private void swap(int i, int j) {
    Node node1 = heap.get(i);
    Node node2 = heap.get(j);

    nodePosition.put(node1.key, j);
    nodePosition.put(node2.key, i);

    heap.set(i, node2);
    heap.set(j, node1);
}

public class Node {
    int weight;
    T key;
}

class Vertex<T> {
    private T data;
    private List<Edge<T>> edges;

    public Vertex(T data) {
        this.data = data;
        this.edges = new ArrayList<>();
    }

    public T getData() {
        return data;
    }

    public List<Edge<T>> getEdges() {
        return edges;
    }

    public void addEdge(Edge<T> edge) {
        edges.add(edge);
    }
}
```

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```
public void addBidirectionalEdge(Edge<T> edge) {
    edges.add(edge);
    Vertex<T> other = edge.getVertex1() == this ? edge.getVertex2() : edge.getVertex1();
    other.edges.add(edge);
}

@Override
public String toString() {
    return data.toString();
}
}

class Edge<T> {
    private Vertex<T> vertex1;
    private Vertex<T> vertex2;
    private int weight;

    public Edge(Vertex<T> vertex1, Vertex<T> vertex2, int weight) {
        this.vertex1 = vertex1;
        this.vertex2 = vertex2;
        this.weight = weight;
    }

    public Vertex<T> getVertex1() {
        return vertex1;
    }

    public Vertex<T> getVertex2() {
        return vertex2;
    }

    public int getWeight() {
        return weight;
    }
}

class Graph<T> {
    private List<Vertex<T>> vertices;

    public Graph() {
        vertices = new ArrayList<>();
    }
}
```

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```
public void addVertex(Vertex<T> vertex) {
    vertices.add(vertex);
}

public List<Vertex<T>> getAllVertex() {
    return vertices;
}
}

public class DijkstraShortestPath {

    public Map<Vertex<Integer>, Map<Integer, List<Vertex<Integer>>>> shortestPath(Graph<Integer>
graph, Vertex<Integer> sourceVertex) {
        BinaryMinHeap<Vertex<Integer>> minHeap = new
BinaryMinHeap<>(graph.getAllVertex().size());
        Map<Vertex<Integer>, Integer> distance = new HashMap<>();
        Map<Vertex<Integer>, Vertex<Integer>> parent = new HashMap<>();
        Map<Vertex<Integer>, Map<Integer, List<Vertex<Integer>>>> paths = new HashMap<>();

        for (Vertex<Integer> vertex : graph.getAllVertex()) {
            int initialDistance = (vertex == sourceVertex) ? 0 : Integer.MAX_VALUE;
            minHeap.add(initialDistance, vertex);
        }

        minHeap.decrease(sourceVertex, 0);
        distance.put(sourceVertex, 0);
        parent.put(sourceVertex, null);

        while (!minHeap.empty()) {
            BinaryMinHeap<Vertex<Integer>>.Node heapNode = minHeap.extractMinNode();
            Vertex<Integer> current = heapNode.key;
            distance.put(current, heapNode.weight);

            for (Edge<Integer> edge : current.getEdges()) {
                Vertex<Integer> adjacent = getVertexForEdge(current, edge);

                if (!minHeap.containsData(adjacent)) {
                    continue;
                }

                int newDistance = distance.get(current) + edge.getWeight();

                if (minHeap.getWeight(adjacent) > newDistance) {
                    minHeap.decrease(adjacent, newDistance);
                }
            }
        }
    }
}
```

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```
parent.put(adjacent, current);

List<Vertex<Integer>> path = new ArrayList<>();
Vertex<Integer> temp = adjacent;
while (temp != sourceVertex) {
    path.add(temp);
    temp = parent.get(temp);
}
path.add(sourceVertex);
Collections.reverse(path);

Map<Integer, List<Vertex<Integer>>> pathsForAdjacent = new HashMap<>();
pathsForAdjacent.put(newDistance, path);
paths.put(adjacent, pathsForAdjacent);
}
}
}

return paths;
}

private Vertex<Integer> getVertexForEdge(Vertex<Integer> v, Edge<Integer> e) {
    return e.getVertex1().equals(v) ? e.getVertex2() : e.getVertex1();
}

public static void main(String[] args) {
    Scanner scanner = new Scanner(System.in);

    Graph<Integer> graph = new Graph<>();
    Map<Integer, Vertex<Integer>> vertexMap = new HashMap<>();

    System.out.print("Enter the number of vertices: ");
    int numVertices = scanner.nextInt();

    System.out.println("Enter the vertices (integer values):");
    for (int i = 0; i < numVertices; i++) {
        int vertexValue = scanner.nextInt();
        Vertex<Integer> vertex = new Vertex<>(vertexValue);
        graph.addVertex(vertex);
        vertexMap.put(vertexValue, vertex);
    }

    System.out.print("Enter the number of edges: ");
    int numEdges = scanner.nextInt();
```

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```
System.out.println("Enter the edges in the format 'vertex1 vertex2 weight':");
for (int i = 0; i < numEdges; i++) {
    int vertex1 = scanner.nextInt();
    int vertex2 = scanner.nextInt();
    int weight = scanner.nextInt();
    Vertex<Integer> v1 = vertexMap.get(vertex1);
    Vertex<Integer> v2 = vertexMap.get(vertex2);
    Edge<Integer> edge = new Edge<>(v1, v2, weight);
    v1.addEdge(edge);
    v2.addEdge(edge);
}

DijkstraShortestPath dijkstra = new DijkstraShortestPath();

System.out.print("Enter the source vertex: ");
int sourceVertexValue = scanner.nextInt();
Vertex<Integer> sourceVertex = vertexMap.get(sourceVertexValue);

if (sourceVertex == null) {
    System.out.println("Invalid source vertex.");
    return;
}

Map<Vertex<Integer>, Map<Integer, List<Vertex<Integer>>>> shortestPaths =
dijkstra.shortestPath(graph, sourceVertex);

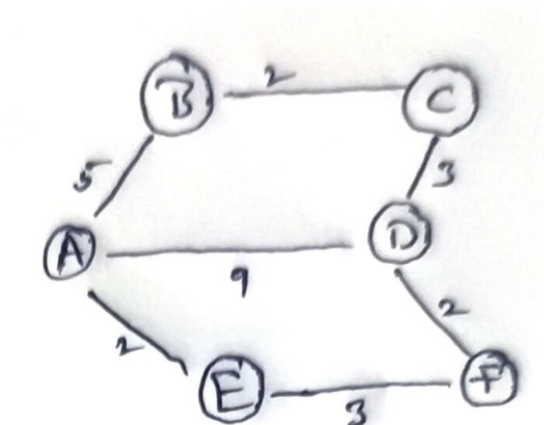
System.out.println("Shortest paths and their total distances from " + sourceVertexValue + ":");
for (Map.Entry<Vertex<Integer>, Map<Integer, List<Vertex<Integer>>>> entry :
shortestPaths.entrySet()) {
    Vertex<Integer> destination = entry.getKey();
    System.out.println("To " + destination.getData() + ":");
    Map<Integer, List<Vertex<Integer>>> paths = entry.getValue();
    for (Map.Entry<Integer, List<Vertex<Integer>>> pathEntry : paths.entrySet()) {
        System.out.println("  Distance: " + pathEntry.getKey() + " Path: " + pathEntry.getValue());
    }
}
}
```

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Output:

```
root@iPhone12promax:~# java DijkstraShortestPath
Enter the number of vertices: 6
Enter the vertices (characters a, b, c, ...):
a b c d e f
Enter the number of edges: 7
Enter the edges in the format 'vertex1 vertex2 weight':
a b 5
a d 9
a e 2
b c 2
c d 3
d f 2
e f 3
Enter the source vertex: b
Shortest paths and their total distances from b:
To c:
  Distance: 2 Path: [b, c]
To e:
  Distance: 7 Path: [b, a, e]
To a:
  Distance: 5 Path: [b, a]
To f:
  Distance: 7 Path: [b, c, d, f]
To d:
  Distance: 5 Path: [b, c, d]
root@iPhone12promax:~#
```

Graph:



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Prims Algorithm:

```
import java.util.Scanner;
import java.util.HashMap;
import java.util.ArrayList;
import java.util.List;
import java.util.Map;
import java.util.Collections;
import java.util.HashSet;
import java.util.Set;
class BinaryMinHeap<T> {
    private Map<T, Integer> nodePosition;
    private List<Node> heap;
    private int maxSize;

    public BinaryMinHeap(int maxSize) {
        this.nodePosition = new HashMap<>();
        this.heap = new ArrayList<>(maxSize);
        this.maxSize = maxSize;
    }

    public void add(int weight, T key) {
        if (nodePosition.containsKey(key)) {
            decrease(key, weight);
        } else {
            Node node = new Node();
            node.weight = weight;
            node.key = key;
            heap.add(node);
            nodePosition.put(key, heap.size() - 1);
            heapifyUp(heap.size() - 1);
        }
    }

    public void decrease(T key, int newWeight) {
        int position = nodePosition.get(key);
        Node node = heap.get(position);
        node.weight = newWeight;
        heapifyUp(position);
    }

    public boolean containsData(T key) {
```

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```
        return nodePosition.containsKey(key);
    }

    public boolean empty() {
        return heap.isEmpty();
    }

    public Node extractMinNode() {
        Node minNode = heap.get(0);
        Node lastNode = heap.remove(heap.size() - 1);
        nodePosition.remove(minNode.key);
        if (!heap.isEmpty()) {
            heap.set(0, lastNode);
            nodePosition.put(lastNode.key, 0);
            heapifyDown(0);
        }
        return minNode;
    }

    public int getWeight(T key) {
        Integer position = nodePosition.get(key);
        if (position == null) {
            return Integer.MAX_VALUE;
        } else {
            return heap.get(position).weight;
        }
    }

    private void heapifyUp(int currentIndex) {
        int parentIndex = (currentIndex - 1) / 2;
        while (currentIndex > 0 && heap.get(currentIndex).weight < heap.get(parentIndex).weight) {
            swap(currentIndex, parentIndex);
            currentIndex = parentIndex;
            parentIndex = (currentIndex - 1) / 2;
        }
    }

    private void heapifyDown(int currentIndex) {
        int leftIndex = 2 * currentIndex + 1;
        int rightIndex = 2 * currentIndex + 2;
        int smallest = currentIndex;

        if (leftIndex < heap.size() && heap.get(leftIndex).weight < heap.get(smallest).weight) {
            smallest = leftIndex;
        }
```

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```
}
if (rightIndex < heap.size() && heap.get(rightIndex).weight < heap.get(smallest).weight) {
    smallest = rightIndex;
}

if (smallest != currentIndex) {
    swap(currentIndex, smallest);
    heapifyDown(smallest);
}
}

private void swap(int i, int j) {
    Node node1 = heap.get(i);
    Node node2 = heap.get(j);

    nodePosition.put(node1.key, j);
    nodePosition.put(node2.key, i);

    heap.set(i, node2);
    heap.set(j, node1);
}

public class Node {
    int weight;
    T key;
}

class Vertex<T> {
    private T data;
    private List<Edge<T>> edges;

    public Vertex(T data) {
        this.data = data;
        this.edges = new ArrayList<>();
    }

    public T getData() {
        return data;
    }

    public List<Edge<T>> getEdges() {
        return edges;
    }
}
```

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```
public void addEdge(Edge<T> edge) {
    edges.add(edge);
}

public void addBidirectionalEdge(Edge<T> edge) {
    edges.add(edge);
    Vertex<T> other = edge.getVertex1() == this ? edge.getVertex2() : edge.getVertex1();
    other.edges.add(edge);
}

@Override
public String toString() {
    return data.toString();
}
}

class Edge<T> {
    private Vertex<T> vertex1;
    private Vertex<T> vertex2;
    private int weight;

    public Edge(Vertex<T> vertex1, Vertex<T> vertex2, int weight) {
        this.vertex1 = vertex1;
        this.vertex2 = vertex2;
        this.weight = weight;
    }

    public Vertex<T> getVertex1() {
        return vertex1;
    }

    public Vertex<T> getVertex2() {
        return vertex2;
    }

    public int getWeight() {
        return weight;
    }
}

class Graph<T> {
    private List<Vertex<T>> vertices;
```

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```
public Graph() {
    vertices = new ArrayList<>();
}

public void addVertex(Vertex<T> vertex) {
    vertices.add(vertex);
}

public List<Vertex<T>> getAllVertex() {
    return vertices;
}
}

class PrimMinimumSpanningTree<T> {
    private Map<Vertex<T>, Vertex<T>> parent;
    private Map<Vertex<T>, Integer> key;
    private Set<Vertex<T>> visitedVertices;
    private BinaryMinHeap<Vertex<T>> minHeap;

    public Map<Vertex<T>, List<Edge<T>>> minimumSpanningTree(Graph<T> graph, Vertex<T>
startVertex) {
        this.parent = new HashMap<>();
        this.key = new HashMap<>();
        this.visitedVertices = new HashSet<>();
        this.minHeap = new BinaryMinHeap<>(graph.getAllVertex().size());

        Map<Vertex<T>, List<Edge<T>>> minimumSpanningTree = new HashMap<>();

        for (Vertex<T> vertex : graph.getAllVertex()) {
            key.put(vertex, Integer.MAX_VALUE);
            minHeap.add(Integer.MAX_VALUE, vertex);
        }

        minHeap.decrease(startVertex, 0);
        key.put(startVertex, 0);
        parent.put(startVertex, null);

        while (!minHeap.empty()) {
            BinaryMinHeap<Vertex<T>>.Node heapNode = minHeap.extractMinNode();
            Vertex<T> currentVertex = heapNode.key;
            visitedVertices.add(currentVertex);

            if (parent.get(currentVertex) != null) {
                Vertex<T> start = parent.get(currentVertex);
```

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```
Edge<T> minimumSpanningTreeEdge = findEdge(graph, start, currentVertex);
minimumSpanningTree.computeIfAbsent(start, k -> new
ArrayList<>()).add(minimumSpanningTreeEdge);
}

for (Edge<T> edge : currentVertex.getEdges()) {
    Vertex<T> adjacentVertex = getOtherVertex(edge, currentVertex);
    if (!visitedVertices.contains(adjacentVertex)) {
        int weight = edge.getWeight();
        if (key.get(adjacentVertex) > weight) {
            minHeap.decrease(adjacentVertex, weight);
            key.put(adjacentVertex, weight);
            parent.put(adjacentVertex, currentVertex);
        }
    }
}
return minimumSpanningTree;
}

public Vertex<T> getOtherVertex(Edge<T> edge, Vertex<T> currentVertex) {
    return edge.getVertex1().equals(currentVertex) ? edge.getVertex2() : edge.getVertex1();
}

private Edge<T> findEdge(Graph<T> graph, Vertex<T> start, Vertex<T> end) {
    for (Edge<T> edge : start.getEdges()) {
        Vertex<T> adjacent = getOtherVertex(edge, start);
        if (adjacent.equals(end)) {
            return edge;
        }
    }
    return null;
}

public class PrimAlgorithm {
    public static void main(String[] args) {
        Scanner scanner = new Scanner(System.in);
        Graph<Character> graph = new Graph<>();
        Map<Character, Vertex<Character>> vertexMap = new HashMap<>();
        System.out.print("Enter the number of vertices: ");
        int numVertices = scanner.nextInt();
        System.out.println("Enter the vertices (characters a, b, c, ...):");
        for (int i = 0; i < numVertices; i++) {
            char vertexValue = scanner.next().charAt(0);
            Vertex<Character> vertex = new Vertex<>(vertexValue);
            graph.addVertex(vertex);
        }
    }
}
```

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```
vertexMap.put(vertexValue, vertex);
}
System.out.print("Enter the number of edges: ");
int numEdges = scanner.nextInt();
System.out.println("Enter the edges in the format 'vertex1 vertex2 weight:");
for (int i = 0; i < numEdges; i++) {
    char vertex1 = scanner.next().charAt(0);
    char vertex2 = scanner.next().charAt(0);
    int weight = scanner.nextInt();

    Vertex<Character> v1 = vertexMap.get(vertex1);
    Vertex<Character> v2 = vertexMap.get(vertex2);

    Edge<Character> edge = new Edge<>(v1, v2, weight);
    v1.addEdge(edge);
    v2.addEdge(edge);
}
PrimMinimumSpanningTree<Character> prim = new PrimMinimumSpanningTree<>();

System.out.print("Enter the source vertex: ");
char sourceVertexValue = scanner.next().charAt(0);
Vertex<Character> sourceVertex = vertexMap.get(sourceVertexValue);

if (sourceVertex == null) {
    System.out.println("Invalid source vertex.");
    return;
}

Map<Vertex<Character>, List<Edge<Character>>> minimumSpanningTree =
prim.minimumSpanningTree(graph, sourceVertex);

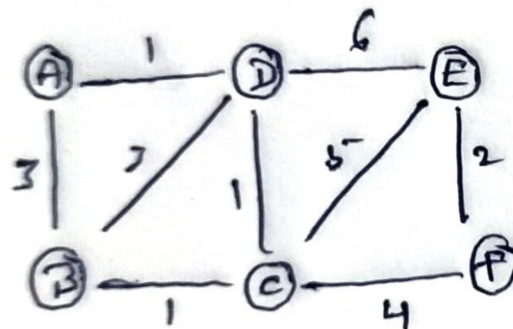
System.out.println("Minimum Spanning Tree Edges from " + sourceVertexValue + " :");
for (Map.Entry<Vertex<Character>, List<Edge<Character>>> entry :
minimumSpanningTree.entrySet()) {
    Vertex<Character> startVertex = entry.getKey();
    System.out.println("From " + startVertex.getData() + " :");
    List<Edge<Character>> edges = entry.getValue();
    for (Edge<Character> edge : edges) {
        Vertex<Character> otherVertex = prim.getOtherVertex(edge, startVertex);
        System.out.println(" To " + otherVertex.getData() + " Weight: " + edge.getWeight());
    }
} }
```

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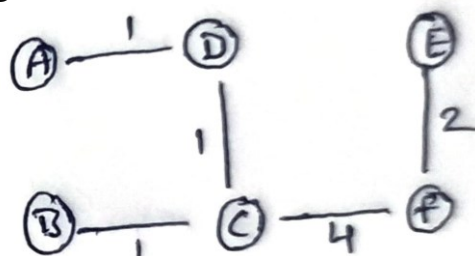
Output:

```
root@iPhone12promax:~# java PrimAlgorithm
Enter the number of vertices: 6
Enter the vertices (characters a, b, c, ...):
a b c d e f
Enter the number of edges: 9
Enter the edges in the format 'vertex1 vertex2 weight':
a b 3
a d 1
b c 1
b d 3
c d 1
c e 5
c f 4
d e 6
e f 2
Enter the source vertex: c
Minimum Spanning Tree Edges from c:
From d:
  To a Weight: 1
From f:
  To e Weight: 2
From c:
  To b Weight: 1
  To d Weight: 1
  To f Weight: 4
```

Graph:



Minimum Spanning Tree:



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Kruskals Algorithm:

```
import java.util.Scanner;
import java.util.HashMap;
import java.util.ArrayList;
import java.util.List;
import java.util.Map;
import java.util.Collections;
```

```
class Edge<T> {
    private Vertex<T> vertex1;
    private Vertex<T> vertex2;
    private int weight;

    public Edge(Vertex<T> vertex1, Vertex<T> vertex2, int weight) {
        this.vertex1 = vertex1;
        this.vertex2 = vertex2;
        this.weight = weight;
    }

    public Vertex<T> getVertex1() {
        return vertex1;
    }

    public Vertex<T> getVertex2() {
        return vertex2;
    }

    public int getWeight() {
        return weight;
    }
}
```

```
class Vertex<T> {
    private T data;
    private List<Edge<T>> edges;

    public Vertex(T data) {
        this.data = data;
        this.edges = new ArrayList<>();
    }
}
```

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```
public T getData() {
    return data;
}

public List<Edge<T>> getEdges() {
    return edges;
}

public void addEdge(Edge<T> edge) {
    edges.add(edge);
}
}

class BinaryMinHeap<T> {
    // Private inner class to hold the edges and their positions
    private class Node {
        Edge<T> edge;
        int position;
    }

    private Map<Edge<T>, Integer> nodePosition;
    private List<Node> heap;

    public BinaryMinHeap() {
        this.nodePosition = new HashMap<>();
        this.heap = new ArrayList<>();
    }

    public void add(Edge<T> edge) {
        Node node = new Node();
        node.edge = edge;
        nodePosition.put(edge, heap.size());
        heap.add(node);
        heapifyUp(heap.size() - 1);
    }

    public Edge<T> extractMin() {
        Node minNode = heap.get(0);
        Edge<T> minEdge = minNode.edge;
        Node lastNode = heap.remove(heap.size() - 1);

        if (!heap.isEmpty()) {
            heap.set(0, lastNode);
            nodePosition.put(lastNode.edge, 0);
        }
    }
}
```

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```
        heapifyDown(0);
    }

    return minEdge;
}

public boolean isEmpty() {
    return heap.isEmpty();
}

private void heapifyUp(int currentIndex) {
    int parentIndex = (currentIndex - 1) / 2;
    while (currentIndex > 0 && heap.get(currentIndex).edge.getWeight() <
heap.get(parentIndex).edge.getWeight()) {
        swap(currentIndex, parentIndex);
        currentIndex = parentIndex;
        parentIndex = (currentIndex - 1) / 2;
    }
}

private void heapifyDown(int currentIndex) {
    int leftIndex = 2 * currentIndex + 1;
    int rightIndex = 2 * currentIndex + 2;
    int smallest = currentIndex;

    if (leftIndex < heap.size() && heap.get(leftIndex).edge.getWeight() <
heap.get(smallest).edge.getWeight()) {
        smallest = leftIndex;
    }

    if (rightIndex < heap.size() && heap.get(rightIndex).edge.getWeight() <
heap.get(smallest).edge.getWeight()) {
        smallest = rightIndex;
    }

    if (smallest != currentIndex) {
        swap(currentIndex, smallest);
        heapifyDown(smallest);
    }
}

private void swap(int i, int j) {
    Node node1 = heap.get(i);
    Node node2 = heap.get(j);
```

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```
nodePosition.put(node1.edge, j);
nodePosition.put(node2.edge, i);

heap.set(i, node2);
heap.set(j, node1);
}
}

class DisjointSet<T> {
    private Map<Vertex<T>, Vertex<T>> parent;
    private Map<Vertex<T>, Integer> rank;

    public DisjointSet(List<Vertex<T>> vertices) {
        parent = new HashMap<>();
        rank = new HashMap<>();

        for (Vertex<T> vertex : vertices) {
            parent.put(vertex, vertex);
            rank.put(vertex, 0);
        }
    }

    public Vertex<T> find(Vertex<T> vertex) {
        if (vertex != parent.get(vertex)) {
            parent.put(vertex, find(parent.get(vertex)));
        }
        return parent.get(vertex);
    }

    public void union(Vertex<T> x, Vertex<T> y) {
        Vertex<T> rootX = find(x);
        Vertex<T> rootY = find(y);

        if (rootX == rootY) {
            return;
        }

        if (rank.get(rootX) < rank.get(rootY)) {
            parent.put(rootX, rootY);
        } else if (rank.get(rootX) > rank.get(rootY)) {
            parent.put(rootY, rootX);
        } else {
            parent.put(rootY, rootX);
            rank.put(rootX, rank.get(rootX) + 1);
        }
    }
}
```

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```
    }  
  }  
}
```

```
class KruskalMinimumSpanningTree<T> {  
  public List<Edge<T>> minimumSpanningTree(List<Vertex<T>> vertices, List<Edge<T>> edges) {  
    BinaryMinHeap<T> minHeap = new BinaryMinHeap<>();  
  
    for (Edge<T> edge : edges) {  
      minHeap.add(edge);  
    }  
  
    List<Edge<T>> mst = new ArrayList<>();  
    DisjointSet<T> disjointSet = new DisjointSet<>(vertices);  
  
    while (!minHeap.isEmpty()) {  
      Edge<T> edge = minHeap.extractMin();  
      Vertex<T> root1 = disjointSet.find(edge.getVertex1());  
      Vertex<T> root2 = disjointSet.find(edge.getVertex2());  
  
      if (root1 != root2) {  
        mst.add(edge);  
        disjointSet.union(root1, root2);  
      }  
    }  
  
    return mst;  
  }  
}
```

```
public class KruskalAlgorithm {  
  public static void main(String[] args) {  
    Scanner scanner = new Scanner(System.in);  
  
    List<Vertex<Character>> vertices = new ArrayList<>();  
    List<Edge<Character>> edges = new ArrayList<>();  
  
    System.out.print("Enter the number of vertices (a, b, c, ...): ");  
    int numVertices = scanner.nextInt();  
  
    System.out.println("Enter the vertices (character values):");  
    for (int i = 0; i < numVertices; i++) {  
      char vertexValue = scanner.next().charAt(0);  
      Vertex<Character> vertex = new Vertex<>(vertexValue);
```

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```
vertices.add(vertex);
}

System.out.print("Enter the number of edges: ");
int numEdges = scanner.nextInt();

System.out.println("Enter the edges in the format 'vertex1 vertex2 weight':");
for (int i = 0; i < numEdges; i++) {
    char vertex1 = scanner.next().charAt(0);
    char vertex2 = scanner.next().charAt(0);
    int weight = scanner.nextInt();

    Vertex<Character> v1 = null;
    Vertex<Character> v2 = null;
    for (Vertex<Character> v : vertices) {
        if (v.getData() == vertex1) {
            v1 = v;
        }
        if (v.getData() == vertex2) {
            v2 = v;
        }
    }

    if (v1 != null && v2 != null) {
        Edge<Character> edge = new Edge<>(v1, v2, weight);
        edges.add(edge);
    } else {
        System.out.println("Invalid edge vertices!");
    }
}

KruskalMinimumSpanningTree<Character> kruskal = new KruskalMinimumSpanningTree<>();
List<Edge<Character>> minimumSpanningTree = kruskal.minimumSpanningTree(vertices,
edges);

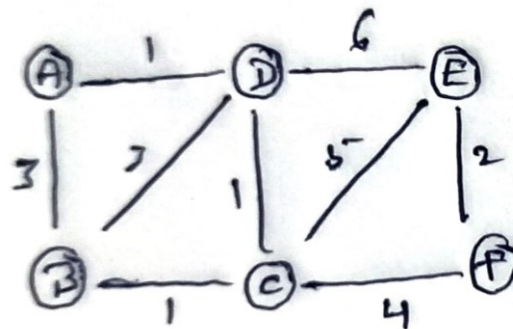
System.out.println("Minimum Spanning Tree Edges:");
for (Edge<Character> edge : minimumSpanningTree) {
    System.out.println("From " + edge.getVertex1().getData() + " To " +
edge.getVertex2().getData() + " Weight: " + edge.getWeight());
}
}
```

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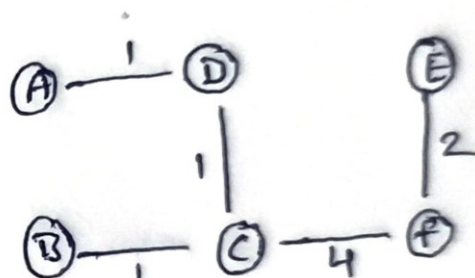
Output:

```
root@iPhone12promax:~# javac KruskalAlgorithm.java
root@iPhone12promax:~# java KruskalAlgorithm
Enter the number of vertices (a, b, c, ...): 6
Enter the vertices (character values):
a b c d e f
Enter the number of edges: 9
Enter the edges in the format 'vertex1 vertex2 weight':
a b 3
a d 1
b c 1
b d 3
c d 1
c e 5
c f 4
d e 6
e f 2
Minimum Spanning Tree Edges:
From a To d Weight: 1
From c To d Weight: 1
From b To c Weight: 1
From e To f Weight: 2
From c To f Weight: 4
```

Graph:



Minimum Spanning Tree:



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