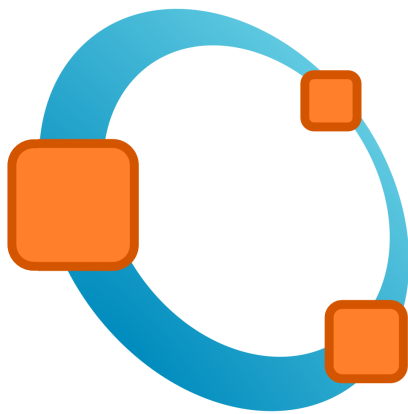


GNU Octave

A high-level interactive language for numerical computations
Edition 4 for Octave version 4.4.1
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Free Your Numbers

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This is the fourth edition of the Octave documentation, and is consistent with version 4.4.1 of Octave.

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