

Inequality in Market Design

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The work and open directions below focus on how we can harness market design to achieve more equitable outcomes for market participants. Some applications include rent control policies in housing markets, price floors in Iran’s kidney exchange (Dworczak, Kominers and Akbarpour (2020)), and allocation of food to food banks (Prendergast (2017)).

Reading through more of the literature on matching markets, combinatorial assignment, and market design more broadly, I’ve become more interested in the potential to design markets with equity as a primary objective. These works below all link to that goal, despite being applied in very different settings.

1. Redistribution through Markets

Price regulations, such as rent control and minimum wage laws, typically face tradeoffs between reducing inequality and maintaining efficient outcomes. In an age of dramatic inequality, it is critical to design markets with equity in mind.

Early work exploring this balance includes Weitzman (1977), who asks whether competitive prices or rationing in a one-commodity market is more effective at ensuring agents with the highest need receive the good. Weitzman focuses primarily on goods which are deemed a societal need, potentially including housing, food, or medical care. As in actual marketplaces, agents have both differing incomes and differing needs for the good. Intuitively, if income distribution is relatively egalitarian and agents’ needs vary widely, then competitive prices better identifies those agents with greater

need. On the other hand, if income inequality is high compared to the dispersion in need for the good, rationing is more effective.

Formally, Weitzman (1977) reach these results by parametrizing agents’ demand functions according to λ and ϵ , where λ represents the agent’s marginal value for money (falls as income rises) and ϵ represents the agent’s need for the good. Critically, these types are unobservable by the market designer, a problem which will arise again in later work as well.

Weitzman now considers two possible rules for allocating a fixed quantity of the good to each agent. Under competitive prices, the market designer sets a price to ensure market clearing. Under pure rationing, the market designer equally divides the good between all agents. Note that Dworczak, Kominers and Akbarpour (2020) build on this model by, among other improvements, considering more nuanced rationing schemes that allocate to a subset of agents or impose multiple price levels. Weitzman then may compute a loss for each method in meeting actual need, and compare the two schemes’ outcomes based on the prior distributions of λ and ϵ in the populace. This formalizes the intuition of when rationing or competitive prices better meet needs in the market.

Dworczak, Kominers and Akbarpour

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(2020) characterize the Pareto frontier of this tradeoff by framing price regulation as a market design problem, with buyers and sellers seeking to buy an indivisible good. They frame the Pareto frontier as determining the welfare-maximizing solution when agents have different valuations for money and for the good. (Roughly speaking, the valuation for money falls with an agent's wealth). They find that when there is significant inequality between buyers and sellers, optimal price controls take the form of a "tax" which charges buyers a lower price than that of sellers, then transfers the surplus to the poorer side of the market. When there is significant inequality between agents on one side of the market, price controls take a more complex form but may still be optimal.

The key obstacle which Dworczak, Kominers and Akbarpour (2020) overcomes, as was faced by earlier models such as Weitzman (1977), is that the market designer does not perfectly identify agents' needs, and hence setting a price at which the commodity is rationed helps to identify these needs.

One interesting novelty of the Dworczak, Kominers and Akbarpour (2020) model is their use of agents' differing marginal values for money, instead of the more standard approach of giving agents different Pareto weights to construct the Pareto frontier. The authors show that these two formulations are actually equivalent. Intuitively, an agent having a higher marginal utility for money is akin to a market designer placing greater weight on the money they are given in the final allocation. They show that agents' actions are fully characterized by their rate of substitution between the good and money.

The bulk of the paper describes the optimal mechanisms to address cross-side inequality (between sellers and buy-

ers) and same-side inequality (between agents on the same side of the market). The paper discusses applications in markets for kidney exchange (rather, the one market which runs in Iran), which is generally an example of same-side inequality among sellers. It also discusses applications in the housing rental market, which is generally an example of cross-side inequality.

The paper raises several interesting extensions. Most immediately, the model only studies an indivisible good without wealth effects. Both of these modeling assumptions could be extended. The model also neglects possible aftermarkets of trade between agents, which could be explicitly modeled. Finally, the rationing mechanism used to address same-side inequality is randomized; work on designing non-random mechanisms could be fruitful. It would also be interesting to find real-world examples where this randomization impacts participant behavior in measurable ways.

Akbarpour, Dworczak and Kominers (2020) approach the problem slightly differently, as one in which a market designer is allocating a public good of heterogeneous quality to buyers, and additionally deciding on the price. Also notable about the Akbarpour, Dworczak and Kominers (2020) model is that it weights the valuation of generating revenue with its own Pareto weight, reflecting the potential uses of that generated revenue. Finally, the work also introduces observable types which the market designer can condition on: one can think of these as observable demographics which are partially informative about a buyer's need or marginal utility of money. Akbarpour, Dworczak and Kominers (2020) is meant to be more "applied" than its predecessor, giving policymakers more concrete recommendations, and Piotr Dworczak has men-

tioned in a market design seminar that the authors are applying this paper's results to a model for vaccine distribution.

1. Vaccine Distribution

Pathak et al. (2020b) apply market design principles to the distribution of necessities such as vaccines and ventilators during the COVID-19 pandemic. They argue that the standard system in which states allocate vaccines, in which all individuals are ordered in one queue of priority, can harm disadvantaged communities, and often leads to discarding several ethical dimensions for the sake of ordering all individuals in one queue.

They instead propose a system of "reserves", in which a number of items (in our case, vaccines) are allocated to each category of priority individuals. For example, 20% of doses might be allocated to minority communities, 20% to first-responders, and the remaining 60% be open to all. Pathak et al. (2020b) identify several axioms that any such system should satisfy, then fully characterize these reserve systems. They show that these reserve systems are cutoff equilibria, and link these characterizations to the classic deferred-acceptance algorithm.

Most interesting in the paper is the consequences of their work for underprivileged groups who have their own reserve allotted; the authors characterize which reserve equilibria are likely to be best for these groups. This paper is quite impressive in that Pathak et al. (2020b) have advised Massachusetts and Tennessee in revising their vaccine allotment systems in just the past year. Pathak et al. (2020a) simulate current vaccine distribution policy to forecast the share of vaccines that will be delivered to Black and Indigenous communities. They compare this share of vaccines to a reserve system in which 40% of vac-

cines are reserved for socioeconomically disadvantaged communities, under their reserve system proposed in Pathak et al. (2020b). Indeed, the proposed change delivers more vaccines to Black and Indigenous communities.

2. Other Papers to Read

- Scheuer, F. (2014): "Entrepreneurial taxation with endogenous entry," *American Economic Journal: Economic Policy*, 6, 126–63.
- Maybe: Saez, E., and Stantcheva, S. (2016). Generalized social marginal welfare weights for optimal tax theory. *American Economic Review*, 106(1), 24–45.
- Kominers, S. and Teytelboym, A.: "More Equal by Design: Economic Design Responses to Inequality". (Forthcoming book).
- Condorelli 2013.

3. Miscellaneous Ideas to Follow

(Some scattered ideas that I'm still working through).

- In a larger vein, it remains to model these markets in conjunction with much of the literature on taxation and macroeconomic redistribution. What might happen if we have a government tax collector who can directly observe incomes, and another market designer (the subject of Akbarpour, Dworczak and Kominers (2020)) who cannot? How do their optimal mechanisms interact?
- Alternative rationing devices: how can we ration in Dworczak, Kominers and Akbarpour (2020), say, to ensure better ex-post fairness?

What if this allocation is repeated several times? I still don't see how a different rationing mechanism would improve ex-post fairness here; the problem still seems somewhat unavoidable to me, but I think I'm missing something.

- Akbarpour, Dworczak and Kominers (2020) value revenue generation by attaching it its own Pareto weight, representing the value of revenue to the market designer. Can we model revenue redistribution more explicitly? Does that buy us anything?
- Total off-the-wall idea: Pathak et al. (2020*b*) develop some results in the theory of reserves, when there are various categories of a good in reserve, and agents are eligible for each reserve based on what categories they fall into. What if goods in the reserves are heterogeneous in quality, and agents have preferences over the quality of goods? This extension would be analogous to the way that Akbarpour, Dworczak and Kominers (2020) extended Condorelli (2013), expanding the work to include items of heterogeneous quality. That said, I'm not quite sure what the real-world analogy would be here. The original model of Pathak et al. (2020*b*) focused on medical supplies such as vaccines and ventilators; I'm not sure how salient preferences over quality are in this domain.
- The importance of revenue generation in Akbarpour, Dworczak and Kominers (2020) (optimal mechanisms differ based on the Pareto weight of revenue generation) reflects the similar importance of that revenue generation witnessed in

most congestion pricing models. Often, how the revenue is spent almost completely determines whether a congestion toll is progressive or regressive. Can we apply frameworks like that of Akbarpour, Dworczak and Kominers (2020) to congestion pricing? Unlike the intended use, though, this isn't quite distributing an "essential" good, as many of these motivating examples do.

- Externalities? Redistribution with differential externalities by group. Or e.g. schooling has externalities.
- Approximately optimal mechanisms? Those with unknown distributions that must be learned?

4. Open Questions

- 1) In cases of significant same-side inequality, the optimal mechanism proposed by Dworczak, Kominers and Akbarpour (2020) is a randomized mechanism, in which some agents can only trade with a given probability. As the authors point out, randomized rationing in practice can be particularly harmful to poorer individuals, who may have less tolerance for uncertainty. Meanwhile, there is also a long tradition in computer science of trying to "de-randomize" randomized algorithms. **Can we model the harm to poorer agents in this model that results from randomization? Can we develop a mechanism that "trades off" efficiency for less randomization? Could these answers change if the good is divisible?**

To put this in more formal terms, perhaps the question is that of ex-post versus ex-ante fairness. **If this game is repeated, can we**

explicitly choose which agents are rationed to reduce ex-post unfairness? Are there established metrics of ex-post fairness which we can use to evaluate this metric? Existing metrics may come from Lien et al. (2014), who roughly measure ex-post fairness as an “expected minimum fill rate”, that is, the expected minimal utility among customers served.

- 2) For a fairly technical extension, in the accompanying seminar talk for Akbarpour, Dworzak and Kominers (2020), Piotr Dworzak notes that their work only considers the case when there are a finite number of different label groups i (the observable characteristics), but their work could likely be extended to the continuous case (when Pareto weights are continuous). This could be an interesting technical extension, but I’m not sure what the real-world analogue of interest would be here. Feasibility: decent; novelty: eh; bearing on real world: unclear.
- 3) Very interesting: taking Akbarpour, Dworzak and Kominers (2020) or Dworzak, Kominers and Akbarpour (2020) as a departure point, what if there are different externalities by group? Motivating question is the distribution of vaccines here, but one could imagine others.

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