HW01p

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Welcome to HW01p where the "p" stands for "practice" meaning you will use R to solve practical problems. This homework is due 11.59 PM Satuday 2/24/18.

You should have RStudio installed to edit this file. You will write code in places marked "TO-DO" to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won't learn that way.

To "hand in" the homework, you should compile or publish this file into a PDF that includes output of your code. Once it's done, push by the deadline.

R Basics

First, install the package testthat (a widely accepted testing suite for R) from https://github.com/r-lib/testthat using pacman. If you are using Windows, this will be a long install, but you have to go through it for some of the stuff we are doing in class. LINUX (or MAC) is preferred for coding. If you can't get it to work, install this package from CRAN (still using pacman), but this is not recommended long term.

```
pacman::p_load(testthat)
```

1. Use the seq function to create vector v consisting of all numbers from -100 to 100.

```
v = c(seq(-100, 100))
##
      [1] -100
                  -99
                        -98
                              -97
                                    -96
                                           -95
                                                 -94
                                                       -93
                                                             -92
                                                                   -91
                                                                          -90
                                                                                -89
                                                                                      -88
                                                                                            -87
##
     [15]
            -86
                  -85
                        -84
                              -83
                                    -82
                                           -81
                                                 -80
                                                       -79
                                                             -78
                                                                   -77
                                                                          -76
                                                                                -75
                                                                                      -74
                                                                                            -73
##
     [29]
            -72
                  -71
                        -70
                              -69
                                    -68
                                           -67
                                                 -66
                                                       -65
                                                             -64
                                                                   -63
                                                                          -62
                                                                                -61
                                                                                      -60
                                                                                            -59
##
     [43]
            -58
                  -57
                        -56
                              -55
                                    -54
                                           -53
                                                 -52
                                                       -51
                                                             -50
                                                                   -49
                                                                          -48
                                                                                -47
                                                                                      -46
                                                                                            -45
##
     [57]
            -44
                  -43
                        -42
                              -41
                                    -40
                                           -39
                                                 -38
                                                       -37
                                                             -36
                                                                   -35
                                                                          -34
                                                                                -33
                                                                                      -32
                                                                                            -31
##
     [71]
            -30
                  -29
                        -28
                              -27
                                    -26
                                           -25
                                                 -24
                                                       -23
                                                             -22
                                                                   -21
                                                                          -20
                                                                                -19
                                                                                            -17
                                                                                      -18
                                                        -9
                                                                     -7
##
     [85]
            -16
                  -15
                        -14
                              -13
                                    -12
                                           -11
                                                 -10
                                                              -8
                                                                           -6
                                                                                 -5
                                                                                       -4
                                                                                             -3
    [99]
                          0
                                       2
                                             3
                                                   4
                                                         5
                                                               6
                                                                      7
                                                                            8
                                                                                  9
##
             -2
                   -1
                                 1
                                                                                       10
                                                                                             11
##
   [113]
             12
                   13
                         14
                                15
                                      16
                                            17
                                                  18
                                                        19
                                                              20
                                                                     21
                                                                           22
                                                                                 23
                                                                                       24
                                                                                             25
   [127]
                   27
                                29
                                      30
                                                                                 37
##
             26
                         28
                                            31
                                                  32
                                                        33
                                                              34
                                                                     35
                                                                           36
                                                                                       38
                                                                                             39
   [141]
             40
                         42
                                            45
                                                        47
                                                                           50
                                                                                       52
                                                                                             53
##
                   41
                                43
                                      44
                                                  46
                                                              48
                                                                     49
                                                                                 51
##
   [155]
             54
                   55
                         56
                                      58
                                            59
                                                  60
                                                              62
                                                                     63
                                                                           64
                                                                                 65
                                                                                       66
                                57
                                                        61
                                                                                             67
## [169]
                         70
                                            73
                                                  74
                                                        75
                                                                           78
                                                                                 79
                                                                                       80
             68
                   69
                                71
                                      72
                                                              76
                                                                     77
                                                                                             81
## [183]
             82
                   83
                         84
                                85
                                      86
                                            87
                                                  88
                                                        89
                                                              90
                                                                     91
                                                                           92
                                                                                 93
                                                                                       94
                                                                                             95
## [197]
                                99
                                    100
             96
                         98
```

Test using the following code:

```
expect_equal(v, -100 : 100)
```

If there are any errors, the expect_equal function will tell you about them. If there are no errors, then it will be silent.

2. Create a function my_reverse which takes as required input a vector and returns the vector in reverse where the first entry is the last entry, etc. No function calls are allowed inside your function (otherwise

that would defeat the purpose of the exercise).

```
my_reverse = function(v){
  num_length = length(v)
  start = 1
  x = v
  if(is.vector(v) != TRUE) {
    warning("Input is not a vector!")
    while(0 < num_length) {</pre>
      v[start] = x[num_length]
      num_length = num_length -1
      start = start + 1
    }
  }
}
my_reverse(c(1,2,3,4,5))
## [1] 5 4 3 2 1
my_reverse(c('A', 'B', 'C'))
## [1] "C" "B" "A"
Test using the following code:
expect_equal(my_reverse(c("A", "B", "C")), c("C", "B", "A"))
expect_equal(my_reverse(v), rev(v))
  3. Let n = 50. Create a nxn matrix R of exactly 50% entries 0's, 25% 1's 25% 2's in random locations.
n = 50 \# n = 50
?matrix
## starting httpd help server ... done
R = matrix(sample((c(rep(0, 1250), rep(1,625), rep(2,625)))), n*n, nrow = n, ncol = n)
table(R)
## R
##
      0
            1
                 2
## 1250 625
              625
R
          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
##
##
    [1,]
                  0
                        0
                             0
                                   2
                                        2
                                              2
                                                   2
                                                         1
                                                               0
                                                                      0
                                                                                   0
   [2,]
             0
                  0
                        0
                             0
                                   0
                                        1
                                              2
                                                   0
                                                         2
                                                               0
                                                                      2
                                                                             2
                                                                                   0
##
   [3,]
             0
                  1
                        0
                             2
                                   0
                                        2
                                              0
                                                   0
                                                               0
                                                                      0
                                                                             2
                                                                                   2
                                                         1
                  2
                                        2
                                                   2
                                                                      2
                                                                                   0
##
   [4,]
             0
                        1
                             0
                                   2
                                              0
                                                         1
                                                               0
                                                                             0
##
    [5,]
             0
                  0
                        0
                             0
                                   0
                                        2
                                              0
                                                   0
                                                               0
                                                                      0
                                                                             0
                                                                                   0
                                                         1
             2
                                        2
                                                                      0
                                                                                   0
##
                  2
                        0
                             0
                                   2
                                              0
                                                   0
                                                         0
                                                               0
                                                                             0
   [6,]
   [7,]
##
             1
                  0
                        0
                             2
                                   0
                                        1
                                              0
                                                   2
                                                         0
                                                               0
                                                                      0
                                                                             0
                                                                                   0
                                                                      2
## [8,]
             0
                  1
                        0
                             1
                                   2
                                        0
                                              1
                                                   0
                                                               0
                                                                             1
                                                                                   0
                                                         1
## [9,]
             0
                  0
                        2
                             2
                                   0
                                        0
                                              0
                                                   0
                                                         0
                                                               0
                                                                      2
                                                                             0
                                                                                   0
             0
                  2
                        0
                                   2
                                        0
                                              0
                                                   2
                                                               1
                                                                      0
                                                                             0
                                                                                   0
## [10,]
                             1
                                                         1
## [11,]
             0
                  0
                        1
                             0
                                   0
                                        2
                                              0
                                                   1
                                                         0
                                                               0
                                                                      0
                                                                             0
                                                                                   2
```

##	[12,]	0	1	1		0 1	0	2	0	0	2	2	2
##	[13,]	2	0	0		1 0	0	0	1	1	0	0	1
##	[14,]	0	0	0	1	0 0	0	0	1	1	0	0	1
##	[15,]	1	1	1	1	2 1	0	1	1	0	0	0	2
##	[16,]	1	0	0	2	1 1	0	2	2	2	0	0	2
##	[17,]	1	0	0	0	2 2	2	0	2	2	0	0	2
##	[18,]	0	0	0	1	0 0	0	0	0	0	1	0	2
##	[19,]	1	0	2	0	0 1	2	1	0	0	1	1	1
##	[20,]	1	1	0	0	2 1	1	0	2	1	2	0	1
##	[21,]	0	0	0		0 1	0	0	0	0	0	0	2
##	[22,]	0	1	0		0 2	0	2	1	1	0	2	2
##	[23,]	2	0	1		2 2	0	2	2	1	1	0	1
##	[24,]	2	1	0		0 1	0	1	1	2	0	0	1
##	[25,]	1	0	2		0 1	1	0	0	1	2	0	0
##	[26,]	0	1	2		2 0	2	0	0	0	2	0	0
##	[27,]	0	2	0		0 0	0	1	1	0	2	0	1
##	[28,]	0	1	0		2 0	2	0	1	0	2	1	2
##	[29,]	0	2	0		2 0	1	2	0	1	0	0	0
##	[30,]	2	1	1	0	0 0	0	1	1	2	0	2	0
##	[31,]	1	1	0	0	0 2	2	2	1	2	0	0	0
##	[32,]	0	2	2	2	0 0	0	1	0	1	0	0	2
##	[33,]	2	2	1	2	1 2	0	0	1	2	0	1	0
##	[34,]	0	1	2	0	1 0	0	0	1	1	2	2	0
##	[35,]	0	0	0	0	0 0	1	1	1	0	2	0	0
##	[36,]	0	1	1	2	0 0	0	1	1	2	0	0	0
##	[37,]	2	0	1		1 2	0	1	0	2	1	2	1
##	[38,]	0	0	0		2 0	0	0	0	0	0	1	0
##	[39,]	0	0	0		2 2	1	0	0	2	0	0	1
##	[40,]	0	0	0		2 0	0	1	1	2	2	0	0
		2	2			2 1	1	0	0		0	0	
##	[41,]			0						1			0
##	[42,]	1	2	1		2 0	1	2	0	1	1	1	0
##	[43,]	0	0	0		0 0	1	0	2	2	0	1	0
##	[44,]	1	2	2		0 0	2	0	0	1	0	1	2
##	[45,]	1	0	1		1 2	0	2	2	0	0	0	0
##	[46,]	1	0	0		0 0	1	1	1	0	1	0	0
##	[47,]	2	0	0		1 1	2	2	2	0	0	2	1
##	[48,]	0	0	0		0 0	1	1	0	0	2	2	2
##	[49,]	0	1	0	0	1 1	0	2	0	2	0	2	2
##	[50,]	0	0	1	0	0 0	0	0	2	0	0	0	1
##		[,14]	[,15]	[,16]	[,17]	[,18]	[,19]	[,20]	[,21]	[,22]	[,23]	[,24]	
##	[1,]	0	1	2	2	0	0	1	0	0	1	2	
##	[2,]	0	0	2	0	2	1	0	0	1	0	1	
##	[3,]	1	0	0	0	2	1	1	0	0	1	1	
##	[4,]	0	0	2	2	1	2	0	2	0	1	0	
##	[5,]	0	0	2	0	2		0	0	1	0	1	
##	[6,]	1	0	2	0			2	0	0	0	0	
##	[7,]	0	1	2	2		0	1	0	2	0	2	
##	[8,]	2	1	0	0		0	2	1	1	2	0	
##	[9,]	1	2	0	2		1	0	2	0	2	0	
##	[10,]	0	0	0	2		0	0	0	0	0	0	
##	[11,]	0	0	1				2	2			1	
		0	0	0	1 2		0	0	0	0	1	2	
##	[12,]												
##	[13,]	2	0	0	0		2	0	0	0	0	1	
##	[14,]	0	0	1	0	0	0	0	0	0	0	0	

##	[15,]	1	1	0	0	2	1	2	0	0	0	1
##	[16,]	0	0	2	2	2	1	2	0	0	0	0
##	[17,]	1	2	1	0	0	2	1	0	2	0	1
##	[18,]	1	0	2	0	0	2	0	0	1	0	0
##	[19,]	0	2	0	0	0	0	2	2	2	0	0
##	[20,]	2	2	0	0	1	0	2	1	2	0	0
##	[21,]	0	1	0	1	1	0	0	2	1	0	0
										2		
##	[22,]	0	1	0	1	0	0	2	0		2	1
##	[23,]	1	2	0	1	1	2	0	0	0	1	2
##	[24,]	1	1	1	0	1	2	1	2	2	0	0
##	[25,]	2	1	0	1	0	0	0	0	0	2	0
##	[26,]	0	1	0	0	2	0	2	0	0	2	1
##	[27,]	2	0	0	1	1	2	2	2	0	0	0
##	[28,]	2	1	2	0	0	2	0	0	1	2	1
##	[29,]	2	2	0	0	0	1	0	2	0	0	0
##	[30,]	0	0	2	1	0	1	2	0	1	2	0
##	[31,]	0	0	0	0	0	1	1	0	0	0	2
##	[32,]	1	0	0	1	0	1	1	0	2	0	2
##	[33,]	2	2	0	1	2	0	2	2	0	1	1
##	[34,]	2	1	0	1	1	0	2	0	2	2	1
##	[35,]	2	2				2	2	0	0	0	0
				1	0	1						
##	[36,]	0	1	1	1	2	1	0	0	0	1	1
##	[37,]	2	0	2	2	1	0	2	1	0	0	1
##	[38,]	0	0	0	0	0	2	0	0	0	2	2
##	[39,]	0	0	1	0	0	0	2	0	2	2	0
##	[40,]	2	2	0	2	0	2	0	2	2	1	0
##	[41,]	0	2	0	2	1	2	1	2	1	1	1
##	[42,]	0	0	1	2	1	1	0	0	1	1	0
##	[43,]	0	0	1	0	1	1	0	0	0	1	0
##	[44,]	0	0	0	2	2	1	0	0	0	0	2
##	[45,]	0	0	0	2	1	2	0	1	0	0	1
##	[46,]	2	2	0	1	0	1	0	1	1	0	2
##	[47,]	2	2	0	0	0	2	0	1	0	0	0
##	[48,]	0	1	1	1	0	0	1	0	1	0	0
##	[49,]	2	2	0	2	0	1	0		1	1	1
		1					1		1 2	2	0	0
##	[50,]		1	0	0	1		0				
##	F4 7	[,25]	[,26]	[,27]	[,28]	[,29]	[,30]	[,31]	[,32]	[,33]	[,34]	[,35]
##	[1,]	2	2	2	0	0	0	0	0	2	1	0
##	[2,]	1	0	0	0	0	0	0	2	2	1	0
##	[3,]	1	2	1	2	0	2	2	1	0	0	1
##	[4,]	2	0	1	2	1	0	0	1	0	0	0
##	[5,]	0	0	0	2	2	1	0	1	2	0	1
##	[6,]	0	2	0	0	2	0	2	0	0	2	2
##	[7,]	0	0	2	1	0	0	0	1	2	1	1
##	[8,]	1	1	2	0	2	1	2	2	0	0	2
##	[9,]	0	1	0	0	0	0	0	0	0	0	0
##	[10,]	1	1	0	2	0	1	0	1	2	0	0
##	[11,]	0	2	1	1	0	0	1	0	2	2	0
##	[12,]	0	0	2	0	0	0	0	0	0	0	0
##	[13,]	2	2	0	1	2	2	2	0	0	0	0
##	[14,]	0	0			0				0		0
				1	0		2	1	1		2	
##	[15,]	2	0	1	1	0	0	0	0	0	2	0
##	[16,]	0	0	0	1	1	1	2	0	1	2	0
##	[17,]	1	1	1	1	0	2	0	1	0	1	0

##	[18,]	1	0	2	0	0	1	1	0	0	0	0
##	[19,]	0	2	1	1	0	0	0	1	1	0	1
##	[20,]	1	0	0	2	0	2	0	2	2	2	0
##	[21,]	2	1	0	0	0	1	0	0	1	0	2
##	[22,]	2	1	1	0	0	1	0	0	0	1	0
##	[23,]	0	0	0	2	1	0	2	0	0	1	0
##	[24,]	1	2	2	2	2	1	2	0	1	2	2
##	[25,]	2	0	2	2	2	2	1	1	1	2	2
##	[26,]	1	2	0	2	1	0	2	0	2	0	2
##	[27,]	1	0	0	1	2	0	0	0	0	0	1
##	[28,]	0	2	0	0	2	0	2	0	0	0	1
##	[29,]	1	2	0	0	1	2	2	0	0	1	0
##	[30,]	0	2	0	0	0	0	2	1	2	0	1
##	[31,]	2	2	0	0	0	2	2	0	1	0	1
##	[32,]	0	1	0	2	0	1	0	0	0	0	1
## ##	[33,] [34,]	0	1 2	0 2	0 2	2 2	0	0	0	0 2	2	0 1
##	[35,]	0	0	2	0	1	0	1	1 1	2	1 1	0
##	[36,]	0	1	2	1	1	0	0	2	2	2	0
##	[37,]	2	1	2	1	0	2	1	0	1	1	0
##	[38,]	0	2	2	1	2	0	2	2	2	0	1
##	[39,]	1	0	0	0	0	2	2	0	1	0	0
##	[40,]	2	0	0	1	2	1	0	1	0	0	1
##	[41,]	2	2	0	2	1	0	1	2	2	2	1
##	[42,]	1	0	0	2	2	0	0	1	2	2	0
##	[43,]	2	0	0	1	0	2	2	0	2	0	1
##	[44,]	2	0	1	0	1	2	0	0	0	0	0
##	[45,]	1	2	2	2	0	0	0	2	2	0	2
##	[46,]	0	0	0	0	0	1	1	0	2	0	2
##	[47,]	0	2	0	2	0	0	2	0	0	2	0
##	[48,]	0	1	0	2	0	1	0	1	1	2	0
##	[49,]	0	2	1	1	0	0	2	1	0	0	2
##	[50,]	0	0	0	0	1	0	1	1	2	2	2
##	Γ4 7	[,36]	[,37]	[,38]	[,39]	[,40]	[,41]	[,42]	[,43]	[,44]	[,45]	[,46]
## ##	[1,] [2,]	1 2	1 1	0	2 2	0 1	1	0 1	1	0 2	1	0
##	[3,]	0	0	2	0	1	0	1	0	0	2	1
##	[4,]	0	0	0	1	0	0	1	1	2	2	1
##	[5,]	0	0	1	0	0	1	2	2	0	0	0
##	[6,]	0	0	0	2	2	0	2	2	0	1	0
##	[7,]	2	1	2	0	0	1	0	0	0	0	1
##	[8,]	1	0	0	0	2	2	2	0	1	2	2
##	[9,]	0	2	0	0	1	0	2	2	0	2	0
##	[10,]	0	0	0	0	2	0	0	1	1	0	1
##	[11,]	0	0	1	0	2	0	0	0	1	0	0
##	[12,]	0	2	2	2	0	2	2	0	2	2	1
##	[13,]	1	1	0	0	0	1	2	0	1	1	1
##	[14,]	0	1	0	2	2	0	0	1	0	0	1
##	[15,]	0	2	1	0	2	2	0	0	0	2	2
##	[16,]	0	0	0	0	0	0	0	0	0	0	1
##	[17,]	0	0	0	0	0	0	2	2	0	0	0
## ##	[18,]	0	2	0	2	0	2	1	0	1	1	1
##	[19,] [20,]	2 2	0	2	1 2	1 0	1 0	2	0	0	0 1	1 0
##	[∠∪,]	2	U	U	2	U	U	U	U	U	1	U

##	[21,]	2	2	0	0	2	2	2	0	2	1	0
##	[22,]	0	1	0	0	2	0	1	0	2	2	2
##	[23,]	1	0	2	0	0	2	0	0	1	0	0
##	[24,]	0	1	2	2	0	1	1	2	1	2	0
##	[25,]	0	0	1	0	0	0	0	0	0	2	0
##	[26,]	1	0	0	2	0	0	1	2	1	0	0
##	[27,]	0	0	1	0	0	2	1	2	0	2	1
##	[28,]	0	0	2	2	1	2	0	0	1	1	0
##	[29,]	1	2	0	0	1	1	0	0	0	0	0
##	[30,]	1	0	0	1	2	2	2	0	2	0	0
##	[31,]	0	0	1	1	2	2	0	2	1	0	0
##	[32,]	1	0	0	1	1	2	0	2	0	0	2
##	[33,]	1	1	1	1	0	1	2	0	2	0	0
##	[34,]	0	2	2	2	1	1	2	0	2	2	1
##	[35,]	0	0	1	0	0	0	1	2	2	0	0
##	[36,]	1	0	0	0	2	0	0	1	0	0	0
##	[37,]	1	1	1	1	1	0	0	0	2	0	0
##	[38,]	2	1	2	0	2	0	1	0	2	0	0
##	[39,]	0	0	2	0	1	1	0	2	0	0	2
##	[40,]	0	1	1	0	0	0	2	2	0	2	0
##	[41,]	2	0	2	1	0	2	1	0	2	1	0
##	[42,]	0	2	0	0	0	0	1	0	0	1	0
##	[43,]	0	0	1	1	2	1	0	0	2	1	1
##	[44,]	1	2	2	0	1	2	2	2	0	1	1
##	[45,]	2	0	2	0	1	2	0	1	2	0	1
##	[46,]	0	0			2	2	0				
				1	1				0	1	1	2
##	[47,]	0	1	0	1	0	1 0	1	2 1	1	1	0
##	[48,]	1	2	0	0	()	()	0			0	1
	F 4 6 7	_				0				1		1
##	[49,]	0	0	2	1	0	1	1	0	0	0	0
##	[49,] [50,]	0	0 2	2 1	1 2							
	[50,]	0 [,47]	0	2 1 [,49]	1	0	1	1	0	0	0	0
##		0	0 2	2 1	1 2	0	1	1	0	0	0	0
## ##	[50,]	0 [,47]	0 2 [,48]	2 1 [,49]	1 2 [,50]	0	1	1	0	0	0	0
## ## ##	[50,] [1,] [2,]	0 [,47] 0	0 2 [,48] 1	2 1 [,49] 0 1	1 2 [,50] 1	0	1	1	0	0	0	0
## ## ## ##	[50,] [1,] [2,] [3,]	0 [,47] 0 2	0 2 [,48] 1 0	2 1 [,49] 0 1 2	1 2 [,50] 1 1 0	0	1	1	0	0	0	0
## ## ## ## ##	[50,] [1,] [2,] [3,] [4,]	0 [,47] 0 2 2 0	0 2 [,48] 1 0 1	2 1 [,49] 0 1 2 2	1 2 [,50] 1 1 0	0	1	1	0	0	0	0
## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,]	0 [,47] 0 2 2 2 0	0 2 [,48] 1 0 1	2 1 [,49] 0 1 2 2 1	1 2 [,50] 1 1 0 0	0	1	1	0	0	0	0
## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,]	0 [,47] 0 2 2 0 0	0 2 [,48] 1 0 1 0	2 1 [,49] 0 1 2 2 1 1	1 2 [,50] 1 1 0 0	0	1	1	0	0	0	0
## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,]	0 [,47] 0 2 2 0 0 0	0 2 [,48] 1 0 1 0 1 2	2 1 [,49] 0 1 2 2 1 1	1 2 [,50] 1 1 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,]	0 [,47] 0 2 2 0 0 0 2	0 2 [,48] 1 0 1 0 1 2	2 1 [,49] 0 1 2 2 1 1 0 2	1 2 [,50] 1 1 0 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,]	0 [,47] 0 2 2 0 0 0 2 0	0 2 [,48] 1 0 1 0 1 2 0 2	2 1 [,49] 0 1 2 2 1 1 0 2	1 2 [,50] 1 1 0 0 0 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,]	0 [,47] 0 2 2 0 0 0 2 0 0	0 2 [,48] 1 0 1 2 0 2 1	2 1 [,49] 0 1 2 2 1 1 0 2 1	1 2 [,50] 1 1 0 0 0 0 0 2 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,]	0 [,47] 0 2 2 0 0 0 2 0 0	0 2 [,48] 1 0 1 2 0 2 1 0	2 1 [,49] 0 1 2 2 1 1 0 2 1	1 2 [,50] 1 1 0 0 0 0 0 0 2 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,]	0 [,47] 0 2 2 0 0 0 2 0 0 1 1	0 2 [,48] 1 0 1 2 0 2 1 0 1 2	2 1 [,49] 0 1 2 2 1 1 0 2 1 0	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,]	0 [,47] 0 2 2 0 0 0 2 0 0 1 1 1 2	0 2 [,48] 1 0 1 2 0 2 1 0 1 2	2 1 [,49] 0 1 2 2 1 1 0 2 1 0 2	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 1 2	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,]	0 [,47] 0 2 2 0 0 0 2 0 0 1 1 1 2	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0	2 1 [,49] 0 1 2 2 1 1 0 2 1 0 2 1 1	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 1 2 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2	0 2 [,48] 1 0 1 0 1 2 0 2 1 0 1 2 0 1 2	2 1 [,49] 0 1 2 2 1 1 0 2 1 0 2 1 1 0	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0	2 1 [,49] 0 1 2 2 1 1 0 2 1 0 1 1 0	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2	0 2 [,48] 1 0 1 0 1 2 0 2 1 0 1 2 0 1 2	2 1 [,49] 0 1 2 2 1 0 2 1 0 2 0 1 1 1 2	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0	2 1 [,49] 0 1 2 2 1 1 0 2 1 0 1 1 0	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0 1	2 1 [,49] 0 1 2 2 1 0 2 1 0 2 0 1 1 1 2	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0 1	2 1 [,49] 0 1 2 2 1 0 2 1 0 2 0 1 1 2 0	1 2 [,50] 1 1 0 0 0 0 0 0 1 2 0 0 0 0 1 2 1 2 1 2	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,] [20,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2 0 1 1 1	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0 1 1 0 1 1 0 1 0	2 1 [,49] 0 1 2 2 1 0 2 1 0 1 1 0 2 0 1 1 2 2 1	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0 0	0	1	1	0	0	0	0
######################################	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,] [20,] [21,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2 0 0	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0 1 2 0 1 0 1	2 1 [,49] 0 1 2 2 1 0 2 1 0 1 1 0 2 0 1 1 0 0 2 1 0 0 1 0 0 0 1 0 0 0 0	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0 0 0	0	1	1	0	0	0	0
## ## ## ## ## ## ## ## ## ## ## ## ##	[50,] [1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,] [20,]	0 [,47] 0 2 2 0 0 0 2 0 1 1 1 2 0 2 0 1 1 1	0 2 [,48] 1 0 1 2 0 2 1 0 1 2 0 1 2 0 1 1 0 1 1 0 1 0	2 1 [,49] 0 1 2 2 1 0 2 1 0 1 1 0 2 0 1 1 2 2 1	1 2 [,50] 1 1 0 0 0 0 0 2 0 0 0 1 2 0 0 0 0	0	1	1	0	0	0	0

```
## [24,]
               2
                                    0
## [25,]
               2
                      1
                             1
                                    2
## [26,]
               0
                      0
                             0
                                    0
## [27,]
               2
                             1
                                    0
                      1
                      2
## [28,]
               0
                             1
                                    2
## [29,]
               0
                      1
                             2
                                    0
## [30,]
               2
                      1
                             0
## [31,]
                      2
                             0
                                    0
               1
## [32,]
               2
                      1
                             0
                                    0
## [33,]
                      0
                             2
                                    2
               1
## [34,]
               1
                      1
                             0
                                    2
                             0
## [35,]
               1
                      1
                                    1
## [36,]
                      2
                             0
               1
                                    1
## [37,]
                      0
                             0
                                    0
               1
## [38,]
               2
                      2
                             2
                                    1
                      2
## [39,]
               0
                             0
                                    0
## [40,]
               1
                      2
                             0
                                    1
                      0
                                    0
## [41,]
               2
                             0
## [42,]
               0
                      0
                             0
                                    2
## [43,]
               0
                      1
                             1
                                    1
## [44,]
               2
                      0
                             1
                                    0
## [45,]
               1
                      0
                             0
                             0
## [46,]
                      0
                                    0
               1
## [47,]
               1
                      1
                             0
                                    0
                                    0
## [48,]
               0
                      2
                             0
## [49,]
               1
                      0
                             0
                                    2
## [50,]
               1
                      1
                             1
                                    1
```

Test using the following and write two more tests as specified below:

```
expect_equal(dim(R), c(n, n))
?unique
#TO-DO test that the only unique values are 0, 1, 2
expect_equal(n*n, sum(c(R) == 0) + sum(c(R) == 1) + sum(c(R) == 2))
#TO-DO test that there are exactly 625 2's
expect_equal(625, sum(c(R)==2))
```

4. Randomly punch holes (i.e. NA) values in this matrix so that approximately 30% of the entries are missing.

```
R = replace(matrix(sample((c(rep(0, 1250), rep(1,625), rep(2,625))))), n*n, nrow = n, ncol = n), sample(1,625), rep(2,625)))
table(R)
## R
##
     0
          1
              2
## 862 443 445
R
          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
##
##
    [1,]
             0
                   0
                         0
                                   NA
                                          2
                                                      1
                                                           0
                                                                 NA
                                                                         2
                                                                               NA
##
    [2,]
             2
                  NA
                        NA
                               0
                                    0
                                          1
                                                1
                                                      2
                                                           2
                                                                 NA
                                                                        NA
                                                                               NA
                                                                                      NA
##
    [3,]
            NA
                   0
                         1
                             NA
                                   NA
                                          0
                                                0
                                                      2
                                                          NA
                                                                  1
                                                                         2
                                                                                1
                                                                                      NA
   [4,]
##
                              2
                                    0
                                                     0
                                                                  0
             0
                   1
                        NA
                                         NA
                                                1
                                                           0
                                                                        NA
                                                                               NA
                                                                                       1
##
   [5,]
             1
                   2
                         2
                             NA
                                    0
                                          0
                                                          NA
                                                                  0
                                                                         2
                                                                                2
                                                                                       0
```

##	[6,]	NA	0	0	0	2	NA	2	1	NA	0	NA	NA	0
##	[7,]	NA	NA	1	0	NA	2	0	2	2	2	NA	0	NA
##	[8,]	1	2	0	0	1	1	1	NA	NA	NA	2	NA	0
##	[9,]	1	2	2	2	0	0	2	2	0	2	NA	0	0
##	[10,]	0	0	0	1	NA	NA	NA	2	0	2	2	NA	NA
##	[11,]	2	NA	2	1	NA	NA	NA	0	0	0	1	2	1
##	[12,]	2	1	1	NA	1	1	0	NA	1	1	1	2	NA
##	[13,]	1	2	1	1	0	0	NA	0	2	NA	0	NA	0
##	[14,]	NA	0	NA	2	2	1	0	0	2	0	NA	0	0
##	[15,]	0	1	NA	NA	NA	2	NA	1	0	1	NA	0	0
##	[16,]	0	2	2	0	0	NA	NA	0	NA	NA	NA	2	1
##	[17,]	0	0	0	0	NA	NA	1	1	0	NA	0	NA	0
##	[18,]	2	0	0	1	0	NA	0	1	0	1	NA	1	NA
##	[19,]	0	0	0	1	2	0	0	0	0	2	NA	NA	NA
##	[20,]	2	1	2	0	NA	0	0	1	2	2	2	NA	0
##	[21,]	NA	NA	1	0	2	0	1	2	0	2	NA	0	0
##	[22,]	0	2	NA	NA	NA	1	NA	1	0	2	NA	2	NA
##	[23,]	0	NA	NA	NA	2	0	0	NA	1	0	0	NA	0 2
## ##	[24,] [25,]	1 0	0 2	0	NA O	1 0	NA 2	O NA	NA O	1 1	1 0	NA NA	NA 2	
##	[26,]	1	2	2	0	0	0	NA 1	1	0	1	NA NA	1	0 1
##	[27,]	2	NA	0	NA	NA	2	0	0	NA	NA	0	2	1
##	[28,]	2	NA	0	1	NA	NA	0	0	NA	NA	2	NA	0
##	[29,]	1	1	NA	NA	0	0	2	0	NA	0	0	1	0
##	[30,]	NA	1	0	2	0	0	0	0	2	0	NA	NA	NA
##	[31,]	1	0	1	0	1	2	2	NA	1	1	1	1	0
##	[32,]	1	1	1	2	2	1	1	2	ΝA	2	1	2	0
##	[33,]	1	NA	NA	NA	NA	0	0	1	NA	0	NA	2	2
##	[34,]	1	1	0	2	NA	2	NA	2	NA	1	1	0	0
##	[35,]	NA	0	0	1	NA	NA	0	0	NA	NA	2	1	NA
##	[36,]	0	NA	1	NA	1	2	0	NA	NA	0	NA	2	0
##	[37,]	NA	0	1	NA	0	0	2	0	0	1	0	2	0
##	[38,]	NA	NA	NA	2	1	0	0	NA	NA	1	0	2	0
##	[39,]	NA	0	2	0	1	2	0	0	0	0	1	0	NA
##	[40,]	0	NA	1	0	NA	NA	0	0	0	0	0	NA	2
##	[41,]	2	0	NA	NA	NA	2	0	NA	1	0	0	1	0
##	[42,]	0	1	NA	NA	0	2	NA	NA	NA	0	0	1	0
	[43,]	NA	0	2	NA	1	0	0	0	0	1	0	0	0
	[44,]	0	NA	2	0	1	NA	1	NA	1	1	NA	0	NA
	[45,]	NA	0	NA	0	1	NA	1	1	2	2	2	0	0
	[46,]	O	0	1	0	NA	2	0	NA 1	1	2	2	1	1
	[47,] [48,]	NA NA	NA NA	NA	1 NA	NA O	NA 2	NA O	1 1	O N A	1 2	0 0	2	1
##	[49,]	NA NA	0	0 1	NA NA	NA	1	NA	2	NA 1	2	2	2	0 1
##	[50,]	1	NA	2	NA	NA	0	0	1	NA	1	1	NA	0
##	[00,]	[,14]						[,19]			[,22]			
##	[1,]	NA	2	٠, -	2	NA NA	0	NA	0		1	NA		1
##	[2,]	NA	0		NA	NA	NA	2	0	1	0	NA		
##	[3,]	NA	NA		0	2	0	1	NA		NA	2		1
##	[4,]	0	0		NA	0	1	NA	1		1	2		
##	[5,]	0	0		0	0	1	0	2		2	NA		1
##	[6,]	NA	0		1	NA	NA	2	0	2	0	1		
##	[7,]	1	0		0	NA	2	2	0	0	0	2		0
##	[8,]	2	2		NA	NA	1	NA	0	0	0	0		0

##	[9,]	2	1	1	0	0	1	NA	0	NA	1	NA
##	[10,]	2	1	NA	NA	1	1	2	0	2	0	1
##	[11,]	NA	NA	1	1	0	0	NA	1	0	2	0
##	[12,]	1	0	1	1	1	1	NA	1	NA	NA	NA
##	[13,]	2	0	0	0	2	0	1	2	1	0	2
##	[14,]	0	1	0	NA	2	0	1	NA	0	1	NA
##	[15,]	NA	0	2	2	1	1	1	0	0	0	2
##	[16,]	2	0	0	1	0	NA	NA	0	0	0	1
##	[17,]	0	0	0	0	2	0	0	2	1	0	1
##	[18,]	1	1	1	0	0	1	0	2	0	2	NA
##	[19,]	0	0	1	0	2	1	0	NA	1	NA	0
##	[20,]	1	2	0	NA	2	0	1	2	2	1	1
##	[21,]	0	1	1	2	2	0	0	1	0	1	0
##	[22,]	1	0	0	NA	1	2	1	1	0	0	0
##	[23,]	NA	0	0	0	2	NA	NA	0	NA	NA	NA
##	[24,]	0	0	2	1	NA	NA	0	NA	2	0	2
##	[25,]	0	1	NA	0	0	0	0	2	NA	0	0
##	[26,]	2	NA	0	0	0	0	1	0	0	1	1
##	[27,]	1	NA	0	0	0	1	NA	0	0	0	2
##	[28,]	NA	0	NA	NA	NA	NA	0	2	NA	1	NA
##	[29,]	NA	2	NA	1	0	0	0	1	0	NA	0
##	[30,]	NA	NA	2	0	0	0	NA	2	1	1	NA
##	[31,]	1	2	2	0	0	NA	NA	1	NA	2	0
##	[32,]	NA	2	NA	NA	2	NA	NA	NA	2	0	1
##	[33,]	2	NA	2	1	0	2	NA	NA	2	2	0
##	[34,]	0	1	0	0	NA	2	0	2	2	0	NA
##	[35,]	2	2	1	NA	NA	2	0	0	0	NA	0
##	[36,]	0	0	0	2	1	NA	0	0	0	2	1
##	[37,]	2	0	NA	2	2	2	NA	0	2	2	NA
##	[38,]	2	0	0	NA	1	0	1	1	1	0	0
##	[39,]	NA	NA	NA	1	NA	0	0	2	1	NA	0
##	[40,]	2	1	2	0	1	NA	0	0	NA	1	NA
##	[41,]	0	2	0	NA	0	1	NA	1	0	0	NA
##	[42,]	1	2	NA	NA	NA	2	2	0	2	2	0
##	[43,]	0	2	NA	NA	0	NA	1	1	0	2	NA
##	[44,]	NA	0	0	NA	NA 1	2	0	NA	1	2	O
##	[45,]	0	2	1	2	1	1 NA	NA	1 NA	0		NA
	[46,] [47,]	O N A	O	0	0	1 N A	NA 2	0	NA MA	NA NA	1	NA
## ##	[48,]	NA NA	NA NA	NA	0	NA O	2	0	NA O	NA 1	0 1	0 1
##	[49,]	0	1	NA	0	1	1	2	0	NA	0	2
##	[50,]	0	NA	NA	0	1	2	NA	0	0	2	0
##	[50,]			[,27]								
##	[1,]	2	2	NA	NA	0	0	NA	0	0	0	1
##	[2,]	NA	NA	0	1	NA	NA	2	NA	2	2	2
##	[3,]	NA	2	1	0	2	0	1	2	2	NA	0
##	[4,]	0	2	0	2	NA	NA	0	2	2	2	2
##	[5,]	1	0	0	2	2	NA	NA	2	0	1	0
##	[6,]	2	2	0	0	NA	0	NA	NA	2	1	0
##	[7,]	NA	NA	NA	0	2	0	NA	0	0	NA	NA
##	[8,]	NA	0	NA	NA	2	2	0	2	2	NA	NA
##	[9,]	0	2	0	NA	NA	NA	NA	0	1	0	2
##	[10,]	NA	0	0	NA	NA	0	NA	0	1	0	NA
##	[11,]	NA	0	1	0	NA	2	NA	NA	2	0	0

##	[12,]	2	0	2	0	NA	0	0	1	1	NA	0
##	[13,]	NA	0	2	0	NA	1	1	0	NA	0	0
##	[14,]	0	2	1	0	2	0	NA	NA	1	NA	2
##	[15,]	0	0	0	1	2	1	0	0	NA	2	NA
##	[16,]	1	0	1	NA	0	NA	0	1	1	NA	0
##	[17,]	1	0	2	1	2	NA	0	NA	0	NA	2
##	[18,]	2	2	0	0	2	NA	NA	NA	0	2	NA
##	[19,]	2	1	0	2	NA	0	NA	0	1	2	1
##	[20,]	NA	NA	0	2	NA	NA	2	0	0	1	NA
##	[21,]	0	0	1	1	NA	0	NA	0	1	1	NA
##	[22,]	NA	NA	NA	0	2	NA	NA	1	1	2	0
## ##	[23,]	NA 2	1 2	0	NA NA	NA 1	NA O	NA O	1	NA O	NA O	2 1
##	[24,] [25,]	NA	NA	1 2	NA 1	1 2	NA	0	0	NA	NA	NA
##	[26,]	0	0	NA	0	0	0	0	0	0	NA	0
##	[27,]	0	0	0	NA	1	NA	1	1	NA	1	2
##	[28,]	NA	NA	0	1	0	0	0	0	NA	NA	NA
##	[29,]	1	1	NA	0	NA	0	0	1	2	0	NA
##	[30,]	1	1	2	1	NA	0	2	NA	2	0	NA
##	[31,]	2	2	NA	NA	2	2	0	1	0	NA	0
##	[32,]	2	2	NA	NA	NA	0	NA	NA	2	NA	0
##	[33,]	0	1	2	1	NA	2	0	1	1	NA	0
##	[34,]	0	NA	2	NA	0	2	2	NA	2	NA	1
##	[35,]	NA	NA	0	NA	1	0	NA	NA	NA	2	NA
##	[36,]	0	0	0	2	1	2	2	NA	NA	NA	0
##	[37,]	NA	NA	0	0	1	2	0	NA	1	2	1
##	[38,]	NA	0	0	NA	NA	NA	1	0	0	NA	0
##	[39,]	0	NA	NA	2	NA	0	1	0	NA	NA	NA
##	[40,]	1	1	0	NA	0	0	NA	NA	0	0	1
##	[41,]	0	2	2	0	0	0	0	0	0	0	NA
##	[42,]	NA	NA	0	2	2	0	2	0	0	0	0
##	[43,]	1	NA	NA	NA	NA	NA	2	0	2	0	1
##	[44,]	1	0	2	NA	NA	NA	0	1	NA	1	2
##	[45,]	NA	0	2 MA	O M A	0	NA	NA 1	2	1	1 N A	0
## ##	[46,] [47,]	2 NA	1 NA	NA 1	NA 2	2	2	1 2	0	2 NA	NA O	2 NA
##	[48,]	NA	1	2	1	NA	NA	NA	1	0	1	NA
##	[49,]	0	0	NA	2	0	NA	1	NA	1	NA	1
##	[50,]	0	0	NA	NA	0	NA	0	0	NA	2	0
##	[00,]								[,43]			
##	[1,]	0	0	2	0	1	0	0	0	NA	NA	NA
##	[2,]	NA	0	0	1	1	0	2	2	0	0	0
##	[3,]	NA	0	0	2	0	0	2	0	0	2	0
##	[4,]	0	0	1	NA	0	0	NA	2	NA	0	NA
##	[5,]	NA	NA	1	0	1	1	NA	2	0	NA	NA
##	[6,]	2	NA	2	0	0	NA	NA	2	0	NA	NA
##	[7,]	NA	2	NA	0	1	0	NA	0	NA	0	NA
##	[8,]	NA	0	0	2	1	1	NA	NA	NA	NA	0
##	[9,]	0	2	NA	NA	0	0	0	NA	NA	NA	1
##	[10,]	0	0	0	2	NA	0	1	0	2	0	0
##	[11,]	NA	2	0	NA	2	NA	0	NA	0	0	2
##	[12,]	0	NA	2	NA	1	1	NA	NA	0	1	0
##	[13,]	1	0	NA	NA	2	0	0	1	NA	2	0
##	[14,]	NA	0	2	NA	0	0	0	NA	1	0	0

шш	[4E]	0	0	1	4	NT A	NT A	0	0	NT A	1	NT A
## ##	[15,]	0 1	0	1 NA	1 NA	NA O	NA NA	0	2 1	NA 1	1	NA
##	[16,] [17,]		1	0	0		NA NA		0	1		0
##	[18,]	NA O	1	1	1	0	NA	0	0	NA	NA NA	NA
##	[19,]	NA	0	NA	NA	NA	0	2	NA	1	1	NA
##	[20,]	1	2	NA	0	1	1	2	1	0	NA	NA
##	[21,]	0	1	0	1	2	2	0	NA	1	0	0
##	[22,]	NA	NA	0	NA	NA	1	NA	2	1	0	2
##	[23,]	NA	2	0	0	2	1	0	0	0	0	NA
##	[24,]	NA NA	0	NA	2	0	1	NA	NA	1	2	0
##	[25,]	1	2	NA	NA	NA	NA	NA	NA	NA	NA	1
##	[26,]	0	0	0	2	NA	1	1	0	NA	1	0
##	[27,]	0	0	1	0	NA	2	0	2	0	NA	1
##	[28,]	0	NA	0	2	0	0	NA	0	NA	2	0
##	[29,]	0	0	1	NA	NA	1	2	NA	0	NA	NA
##	[30,]	0	0	0	0	NA	2	1	2	NA	0	1
##	[31,]	NA	NA	2	NA	2	0	2	NA	2	NA	NA
##	[32,]	0	1	NA	2	NA	2	0	1	0	NA	0
##	[33,]	NA	2	NA	NA	0	0	NA	0	2	NA	1
##	[34,]	2	0	0	2	2	0	0	NA	0	2	1
##	[35,]	NA	2	0	NA	0	NA	NA	2	0	NA	NA
##	[36,]	2	NA	NA	0	0	0	2	0	NA	1	NA
##	[37,]	NA	0	NA	1	NA	NA	2	NA	0	0	NA
##	[38,]	0	0	0	0	NA	0	0	1	1	0	0
##	[39,]	0	2	NA	0	1	NA	0	NA	NA	NA	0
##	[40,]	2	0	0	0	0	0	0	2	2	1	2
##	[41,]	0	NA	0	0	NA	NA	0	2	1	NA	NA
##	[42,]	0	1	2	NA	NA	NA	NA	0	2	NA	NA
##	[43,]	1	0	1	0	0	0	NA	0	NA	NA	0
##	[44,]	0	NA	0	0	2	1	NA	NA	0	0	1
##	[45,]	NA	2	1	2	2	1	0	0	NA	NA	0
##	[46,]	2	1	NA	NA	2	0	2	NA	2	0	NA
##	[47,]	0	0	2	1	NA	NA	NA	2	0	2	0
##	[48,]	NA	NA	NA	2	0	0	1	1	0	1	NA
##	[49,]	1	0	1	0	0	1	2	NA	2	1	1
##	[50,]	NA	2	NA	NA	NA	0	2	0	0	2	2
##		[,47]	[,48]	[,49]	[,50]							
##	[1,]	2	1	2	0							
##	[2,]	2	0	2	NA							
##	[3,]	1	NA	2	0							
##	[4,]	NA	0	NA	NA							
##	[5,]	0	1	1	0							
##	[6,]	NA	0	2	1							
##	[7,]	0	1	1 0	0							
## ##	[8,] [9,]	2 MA	NA O		NA 2							
##	[10,]	NA NA	0	NA O	2							
##	[11,]	2	0	NA	1							
##	[12,]	2	2	0	1							
##	[13,]	NA	0	0	2							
##	[14,]	1	NA	1	0							
##	[15,]	0	1	1	NA							
##	[16,]	NA	1	2	0							
	[17,]	1	0	NA	2							
	_ ,_	_	,		_							

```
## [18,]
              0
                      1
                             0
                                    0
## [19,]
                      2
                                    0
              NA
                             1
## [20,]
              0
                      0
                           NA
                                   NA
## [21,]
                             0
                                   NA
              NA
                    NA
## [22,]
              NA
                      0
                             0
                                    2
## [23,]
                      0
                             2
               1
                                    0
## [24,]
               0
                      0
                           NA
                                   NA
## [25,]
               1
                      1
                             0
                                    1
## [26,]
               1
                      0
                             0
                                   NA
                      2
                                   2
## [27,]
               0
                           NA
## [28,]
              NA
                      0
                             2
                                   NA
                      2
## [29,]
              NA
                             1
                                   NA
## [30,]
               1
                      0
                           NA
                                    1
               2
## [31,]
                      0
                             1
                                    1
## [32,]
               2
                      2
                           NA
                                    2
## [33,]
               1
                      0
                            0
                                    0
## [34,]
                      0
                                    0
               0
                           NA
## [35,]
              NA
                    NA
                                    2
                            1
## [36,]
                                    0
             NA
                    NA
                           NA
## [37,]
             NA
                      2
                           NA
                                    2
## [38,]
               0
                    NA
                             0
                                   NA
## [39,]
               2
                    NA
                             2
                                    0
## [40,]
                      0
                             2
              NA
                                    1
## [41.]
               0
                           NA
                      1
                                   NA
                             2
                                   NA
## [42,]
               2
                      2
## [43,]
               2
                      0
                             1
                                   0
## [44,]
               0
                             0
                      1
                                   NA
## [45,]
               0
                    NA
                             1
                                   NA
## [46,]
               0
                                    0
                    NA
                             1
## [47,]
              NA
                      1
                             2
                                    1
## [48,]
               0
                      0
                             0
                                    0
## [49,]
               0
                      2
                             0
                                   NA
## [50,]
                             0
                                    2
```

Test using the following code. Note this test may fail 1/100 times.

```
num_missing_in_R = sum(is.na(c(R)))
expect_lt(num_missing_in_R, qbinom(0.995, n^2, 0.3))
expect_gt(num_missing_in_R, qbinom(0.005, n^2, 0.3))
```

5. Sort the rows matrix R by the largest row sum to lowest. See 2/3 way through practice lecture 3 for a hint.

```
#TO-DO
n = 50
M = replace(matrix(sample((c(rep(0, 1250), rep(1,625), rep(2,625)))),n*n, nrow = n, ncol = n), sample(
rowSums(M, na.rm =TRUE)

## [1] 24 23 25 32 37 18 24 23 34 28 20 19 23 22 18 27 29 23 25 29 37 20 27

## [24] 33 26 23 27 28 22 25 31 25 32 33 30 18 20 28 31 23 28 26 29 27 29 24

## [47] 24 26 22 31

R = M[order(rowSums(M, na.rm = TRUE), decreasing = T), ]
rowSums(R, na.rm = TRUE)

## [1] 37 37 34 33 33 32 32 31 31 31 30 29 29 29 29 28 28 28 28 27 27 27 27

## [24] 26 26 26 25 25 25 25 24 24 24 24 23 23 23 23 23 23 22 22 22 20 20 20
```

```
## [47] 19 18 18 18
```

Test using the following code.

```
for (i in 2 : n){
  expect_gte(sum(R[i - 1, ], na.rm = TRUE), sum(R[i, ], na.rm = TRUE))
}
```

6. Create a vector v consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 10.

```
#TO-DO
?rnorm
#smaple(x, size, replace = TRUE/FALSE, prob = NULL)
v = rnorm(1000, mean = -10, sd = sqrt(10))
```

Find the average of v and the standard error of v.

```
#TO-DO
average = mean(v)
standard_error = sd(v)/ (sqrt(length(v)))
```

Find the 5%ile of v and use the qnorm function as part of a test to ensure it is correct based on probability theory.

```
#TO-DO
?qnorm
#expect_equal(as.numeric(quantile(v, .05)), expected = qnorm(.05, mean = -10, sd = sqrt(10)))
```

Find the sample quantile corresponding to the value -7000 of v and use the pnorm function as part of a test to ensure it is correct based on probability theory.

```
#TO-DO
#expect_equal(..., tol = )
```

7. Create a list named my_list with keys "A", "B", ... where the entries are arrays of size 1, 2 x 2, 3 x 3 x 3, etc. Fill the array with the numbers 1, 2, 3, etc. Make 8 entries.

```
#TO-DO
enteries = 8
key = 'A'
my_list = list()
keys = c("A", "B", "C", "D", "E", "F", "G", "H")
for(i in 1:enteries) {
   key = keys[i]
   my_list[[key]] = array(seq(1,i), dim = c(rep(i, i)))
}
```

Test with the following uncomprehensive tests:

```
expect_equal(my_list$A[1], 1)
expect_equal(my_list[[2]][, 1], 1 : 2)
expect_equal(dim(my_list[["H"]]), rep(8, 8))
```

Run the following code:

```
lapply(my_list, object.size)
```

```
## $A
## 208 bytes
##
## $B
```

```
## 216 bytes
##
## $C
## 336 bytes
##
## $D
## 1232 bytes
##
## $E
## 12728 bytes
##
## $F
## 186848 bytes
##
## $G
## 3294400 bytes
##
## $H
## 67109088 bytes
?lapply
?object.size
```

Use ?lapply and ?object.size to read about what these functions do. Then explain the output you see above. For the later arrays, does it make sense given the dimensions of the arrays?

Answer here in English. object.size gives an estimate of how much memory is being used in each key of my list.

lapply returns the keys and the bytes the correspond with each key. It seems obivious that as the dimensions increase, so does the memory.

Now cleanup the namespace by deleting all stored objects and functions:

```
#TO-DO
rm(list = ls())
```

Basic Binary Classification Modeling

8. Load the famous iris data frame into the namespace. Provide a summary of the columns and write a few descriptive sentences about the distributions using the code below and in English.

```
#TO-DO
data(iris)
head(iris)
```

```
##
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1
               5.1
                            3.5
                                          1.4
                                                       0.2
                                                            setosa
## 2
               4.9
                            3.0
                                          1.4
                                                       0.2
                                                            setosa
## 3
               4.7
                            3.2
                                          1.3
                                                       0.2
                                                            setosa
               4.6
                            3.1
                                                       0.2
## 4
                                          1.5
                                                            setosa
## 5
                            3.6
                                                       0.2
               5.0
                                          1.4
                                                             setosa
## 6
               5.4
                            3.9
                                          1.7
                                                       0.4
                                                            setosa
```

The outcome metric is Species. This is what we will be trying to predict. However, we have only done binary classification in class (i.e. two classes). Thus the first order of business is to drop one class. Let's drop the level "virginica" from the data frame.

```
iris = iris[iris$Species != "virginica", ]
str(iris)
## 'data.frame':
                     100 obs. of 5 variables:
## $ Sepal.Length: num 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
## $ Sepal.Width : num 3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
## $ Petal.Length: num 1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
## $ Petal.Width : num 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
                  : Factor w/ 3 levels "setosa", "versicolor", ...: 1 1 1 1 1 1 1 1 1 1 ...
vec_two_factors = as.factor(c('setosa', 'versicolor'))
SpeciesV2 = factor(iris$Species, levels = vec_two_factors)
iris$Species = NULL
iris = cbind(iris, SpeciesV2)
iris
##
       Sepal.Length Sepal.Width Petal.Length Petal.Width SpeciesV2
## 1
                 5.1
                             3.5
                                           1.4
                                                       0.2
                                                                setosa
## 2
                 4.9
                             3.0
                                           1.4
                                                       0.2
                                                                setosa
## 3
                 4.7
                             3.2
                                                       0.2
                                           1.3
                                                                setosa
## 4
                 4.6
                             3.1
                                           1.5
                                                       0.2
                                                                setosa
## 5
                5.0
                             3.6
                                           1.4
                                                       0.2
                                                                setosa
## 6
                5.4
                             3.9
                                           1.7
                                                       0.4
                                                                setosa
## 7
                4.6
                             3.4
                                           1.4
                                                       0.3
                                                                setosa
## 8
                5.0
                             3.4
                                           1.5
                                                       0.2
                                                                setosa
## 9
                4.4
                             2.9
                                           1.4
                                                       0.2
                                                                setosa
## 10
                4.9
                             3.1
                                           1.5
                                                       0.1
                                                                setosa
## 11
                5.4
                             3.7
                                           1.5
                                                       0.2
                                                                setosa
## 12
                4.8
                             3.4
                                           1.6
                                                       0.2
                                                                setosa
## 13
                4.8
                                           1.4
                             3.0
                                                       0.1
                                                                setosa
## 14
                4.3
                             3.0
                                           1.1
                                                       0.1
                                                                setosa
## 15
                5.8
                             4.0
                                           1.2
                                                       0.2
                                                                setosa
## 16
                5.7
                             4.4
                                           1.5
                                                       0.4
                                                                setosa
## 17
                5.4
                             3.9
                                           1.3
                                                       0.4
                                                                setosa
## 18
                5.1
                             3.5
                                           1.4
                                                       0.3
                                                                setosa
## 19
                5.7
                             3.8
                                           1.7
                                                       0.3
                                                                setosa
## 20
                5.1
                             3.8
                                                       0.3
                                           1.5
                                                                setosa
## 21
                5.4
                             3.4
                                           1.7
                                                       0.2
                                                                setosa
## 22
                5.1
                             3.7
                                           1.5
                                                       0.4
                                                                setosa
## 23
                4.6
                             3.6
                                           1.0
                                                       0.2
                                                                setosa
## 24
                5.1
                             3.3
                                           1.7
                                                       0.5
                                                                setosa
## 25
                4.8
                             3.4
                                           1.9
                                                       0.2
                                                                setosa
## 26
                5.0
                             3.0
                                           1.6
                                                       0.2
                                                                setosa
## 27
                5.0
                             3.4
                                           1.6
                                                       0.4
                                                                setosa
## 28
                5.2
                             3.5
                                           1.5
                                                       0.2
                                                                setosa
## 29
                5.2
                             3.4
                                           1.4
                                                       0.2
                                                                setosa
## 30
                4.7
                             3.2
                                           1.6
                                                       0.2
                                                                setosa
## 31
                4.8
                             3.1
                                           1.6
                                                       0.2
                                                                setosa
## 32
                5.4
                                           1.5
                                                                setosa
                             3.4
                                                       0.4
## 33
                5.2
                             4.1
                                           1.5
                                                       0.1
                                                                setosa
                             4.2
## 34
                5.5
                                           1.4
                                                       0.2
                                                                setosa
## 35
                4.9
                             3.1
                                           1.5
                                                       0.2
                                                                setosa
## 36
                             3.2
                5.0
                                           1.2
                                                       0.2
                                                                setosa
```

## 27		2 5	1 0	0.0
## 37	5.5	3.5	1.3	0.2 setosa
## 38	4.9	3.6	1.4	0.1 setosa
## 39	4.4	3.0	1.3	0.2 setosa
## 40	5.1	3.4	1.5	0.2 setosa
## 41	5.0	3.5	1.3	0.3 setosa
## 42	4.5	2.3	1.3	0.3 setosa
## 43	4.4	3.2	1.3	0.2 setosa
## 44	5.0	3.5	1.6	0.6 setosa
## 45	5.1	3.8	1.9	0.4 setosa
## 46	4.8	3.0	1.4	0.3 setosa
## 47	5.1	3.8	1.6	0.2 setosa
## 48	4.6	3.2	1.4	0.2 setosa
## 49	5.3	3.7	1.5	0.2 setosa
## 50	5.0	3.3	1.4	0.2 setosa
## 51	7.0	3.2	4.7	1.4 versicolor
## 52	6.4	3.2	4.5	1.5 versicolor
## 53	6.9	3.1	4.9	1.5 versicolor
## 54	5.5	2.3	4.0	1.3 versicolor
## 55	6.5	2.8	4.6	1.5 versicolor
## 56	5.7	2.8	4.5	1.3 versicolor
## 57	6.3	3.3	4.7	1.6 versicolor
## 58	4.9	2.4	3.3	1.0 versicolor
## 59	6.6	2.9	4.6	1.3 versicolor
## 60	5.2	2.7	3.9	1.4 versicolor
## 61	5.0	2.0	3.5	1.0 versicolor
## 62	5.9	3.0	4.2	1.5 versicolor
## 63	6.0	2.2	4.0	1.0 versicolor
## 64	6.1	2.9	4.7	1.4 versicolor
## 65	5.6	2.9	3.6	1.3 versicolor
## 66	6.7	3.1	4.4	1.4 versicolor
## 67	5.6	3.0	4.5	1.5 versicolor
## 68	5.8	2.7	4.1	1.0 versicolor
## 69	6.2	2.2	4.5	1.5 versicolor
## 70	5.6	2.5	3.9	1.1 versicolor
## 71	5.9	3.2	4.8	1.8 versicolor
## 72	6.1	2.8	4.0	1.3 versicolor
## 73	6.3	2.5	4.9	1.5 versicolor
## 74	6.1	2.8	4.7	1.2 versicolor
## 75	6.4	2.9	4.3	1.3 versicolor
## 76	6.6	3.0	4.4	1.4 versicolor
## 77	6.8	2.8	4.8	1.4 versicolor
## 78	6.7	3.0	5.0	1.7 versicolor
## 79	6.0	2.9	4.5	1.5 versicolor
## 80	5.7	2.6	3.5	1.0 versicolor
## 81	5.5	2.4	3.8	1.1 versicolor
## 82	5.5	2.4	3.7	1.0 versicolor
## 83	5.8	2.7	3.9	1.2 versicolor
## 84	6.0	2.7	5.1	1.6 versicolor
## 85	5.4	3.0	4.5	1.5 versicolor
## 86	6.0	3.4	4.5	1.6 versicolor
## 87	6.7	3.1	4.7	1.5 versicolor
## 88	6.3	2.3	4.4	1.3 versicolor
## 89	5.6	3.0	4.1	1.3 versicolor
## 99 ## 90	5.5	2.5	4.0	1.3 versicolor
π# ∂∪	5.5	∠.∪	4.0	1.0 AGISICOTOL

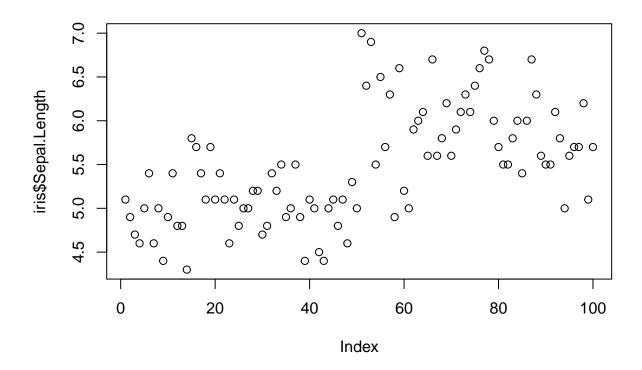
```
## 91
                5.5
                             2.6
                                           4.4
                                                        1.2 versicolor
## 92
                6.1
                             3.0
                                           4.6
                                                        1.4 versicolor
                                                        1.2 versicolor
## 93
                5.8
                             2.6
                                           4.0
                             2.3
## 94
                5.0
                                           3.3
                                                        1.0 versicolor
## 95
                5.6
                             2.7
                                           4.2
                                                        1.3 versicolor
## 96
                                           4.2
                                                        1.2 versicolor
                5.7
                             3.0
## 97
                             2.9
                                           4.2
                                                        1.3 versicolor
                5.7
## 98
                6.2
                             2.9
                                           4.3
                                                        1.3 versicolor
## 99
                5.1
                             2.5
                                           3.0
                                                        1.1 versicolor
## 100
                5.7
                             2.8
                                           4.1
                                                        1.3 versicolor
```

Now create a vector y that is length the number of remaining rows in the data frame whose entries are 0 if "setosa" and 1 if "versicolor".

```
#TO-DO
y = nrow(iris)
for(i in 1:nrow(iris)) {
   if(iris$SpeciesV2[i] == "setosa") {
      y[i] = 0
   } else {
      y[i] = 1
   }
}
```

9. Fit a threshold model to y using the feature Sepal.Length. Try to write your own code to do this. What is the estimated value of the threshold parameter? What is the total number of errors this model makes?

```
#TO-DO
x_1 = as.matrix(cbind(iris[, 1, drop = FALSE]))
MAX_ITER = 100
w = 0
for(iter in 1: MAX_ITER) {
    for(i in 1:nrow(x_1)) {
        x_i = x_1[i]
        y_Hat_I = ifelse(sum(x_i * w) > 0, 1, 0)
        y_i = y[i]
        w = w + (y_i - y_Hat_I) *x_i
    }
}
plot(iris$Sepal.Length)
```



```
y_Hat_I = ifelse(x_1 %% w > 0, 1, 0)
sum(y != y_Hat_I)/ length(y)
## [1] 0.5
Does this make sense given the following summaries:
summary(iris[iris$Species == "setosa", "Sepal.Length"])
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
     4.300
             4.800
                      5.000
                                               5.800
##
                              5.006
                                       5.200
#summary(iris[iris$Species == "virginica", "Sepal.Length"])
summary(iris[iris$Species == "versicolor", "Sepal.Length"])
                               Mean 3rd Qu.
##
      Min. 1st Qu.
                     Median
                                                Max.
##
     4.900
             5.600
                      5.900
                              5.936
                                       6.300
                                               7.000
```

Write your answer here in English. Given the summaries, it does make sense. We are able to visualize the line between setosa and versicolor. The min and max are about the same, concluding that there is some error due to the fact that the data is not linearly seperable (which is shown when plotting the data).

10. Fit a perceptron model explaining y using all three features. Try to write your own code to do this. Provide the estimated parameters (i.e. the four entries of the weight vector)? What is the total number of errors this model makes?

```
#TO-DO: Perceptron mode
#if the result from using all features is 0, than it may be separable
```

```
x_2 = as.matrix(cbind(y, iris[ , 1, drop = FALSE], iris[ , 2, drop = FALSE], iris[ , 3, drop = FALSE],

MAX_ITER = 100
w = rep(0,5)
for(iter in 1: MAX_ITER) {
    for(i in 1:nrow(x_2)) {
        x_i = x_2[i, ]
        y_Hat_I = ifelse(sum(x_i*w) > 0, 1, 0)
        y_i = y[i]
        w = w + (y_i - y_Hat_I) * x_i
    }
}
#error-rate: the result is 0, so the 4 features together make it separable

y_Hat = ifelse(x_2 %*% w > 0, 1, 0)
sum(y != y_Hat) / length(y)

## [1] 0
```