

Lecture 4: 2/7/18

Supervised

Learning

$\mathcal{D}, \mathcal{H}, \mathcal{A}$

$$g = \mathcal{A}(\mathcal{D}, \mathcal{H})$$

→ this is a model.

How to get predictions or fits?

$$\mathcal{D} = \{ \langle \vec{x}_i, y_i \rangle \}_{i=1 \dots n}$$

$$g = \mathcal{A}(\mathcal{D}, \mathcal{H})$$

→ "fit"

$$\hat{y}_i = g(\vec{x}_i)$$

is called sample fit

$\{ \hat{y}_1, \dots, \hat{y}_n \}$ is sample fit/prediction

$$\approx \{ y_1, \dots, y_n \}$$

How to predict for new data/observation: \vec{x}^* ?

$$\hat{y}^* = g(\vec{x}^*)$$

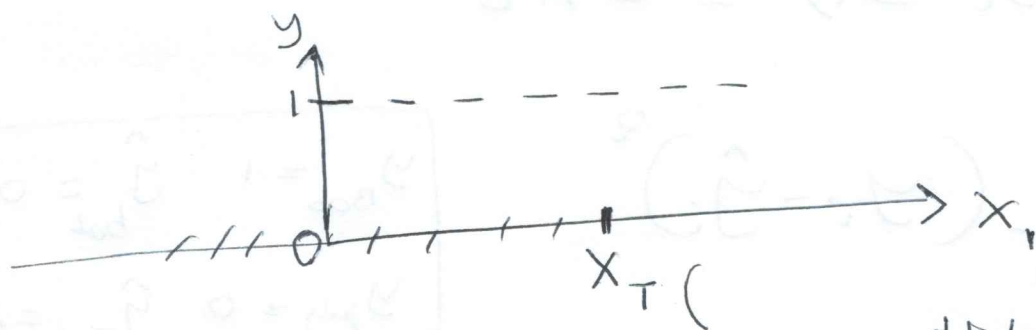
$y \in \{0, 1\}$ is binary.

let's use only

X_1 (salary, con

$$\mathcal{H} = \{$$

Let's graph.



$$\mathcal{H} = \{ \mathbb{1}_{x > x_T} : x_T \in \mathbb{R} \}$$

↓
is every possible
functions that
look like

Note

$$\mathbb{1}_A = \begin{cases} 1 & \text{if } A \\ 0 & \text{if } A^c \end{cases}$$

$$\mathbb{1}_{x > 10} = \begin{cases} 1 & \text{of } x > 10 \\ 0 & \text{of } x \leq 10 \end{cases}$$

→ This is called
parameter

Now

$$\mathcal{H} = \{ \mathbb{1}_{x > x_T} : x_T \in \{x_1, \dots, x_n\} \}$$

Some error function:

$$\text{Err}(\vec{y}, \hat{\vec{y}}) > 0$$

sum of absolute error: $\text{SAE} = \sum_{i=1}^n |y_i - \hat{y}_i|$

Mean Abs Error.

$$\text{MAE} = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| : \text{called mischaracterization}$$

sum of square error: SSE error. $\text{SSE} = \sum_{i=1}^n (y_i - \hat{y}_i)^2 = \text{SAE}$

$$\text{Mean of Square error: } \text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$SSE = \sum_{i=1}^n (y_i - \hat{y}_i)^2 = SAE$$

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$\begin{array}{ll} y_{\text{Bob}} = 1 & \hat{y}_{\text{Bob}} = 0 \\ y_{\text{July}} = 0 & \hat{y}_{\text{July}} = 1 \end{array}$$

$$MAE = \frac{1}{n} \sum |y_i - \hat{y}_i|$$

$$\leq \frac{1}{n} \sum_{i=1}^n \mathbb{1}_{y_i \neq \hat{y}_i}$$

$$SSE(h) = \sum_{i=1}^n (y_i - h(\vec{x}_i))^2$$

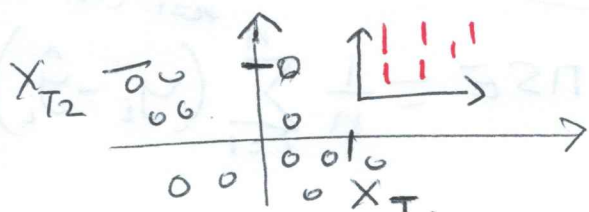
$$g = \arg \min \{ SSE \}$$

$$g = \arg \min \{ SSE(h) \} \Leftrightarrow X_T^* = \arg \min \left\{ \sum (y_i - \frac{1}{n} \sum_{i=1}^n y_i) \right\}$$

It would be a "great research" \pm every possible.

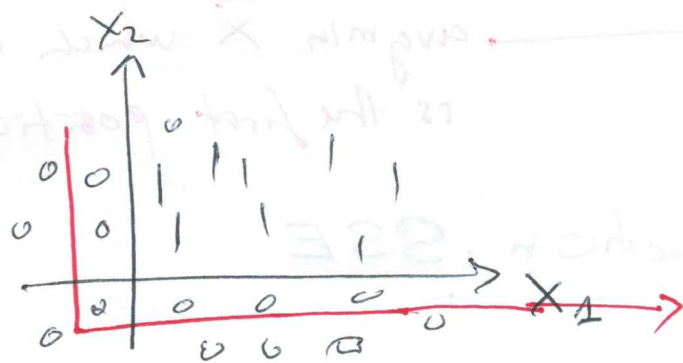
Now we have X_1, X_2 both continuous.

$$\mathcal{H} = \left\{ \mathbb{1}_{X_1 > X_T} \mathbb{1}_{X_2 > X_{T_2}} : \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} \in \mathbb{R}^2 \right\}$$

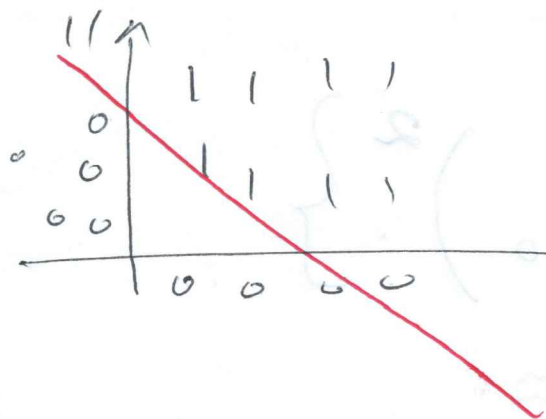


Let say your data looks like this:

8
650



arbitrary bad.



Best to do.

$a+bx$ - line.

Now:

$$H = \left\{ \mathbb{1}_{x_2 > a+bx} : \begin{bmatrix} a \\ b \end{bmatrix} \in \mathbb{R}^2 \right\}$$

$$= \left\{ \mathbb{1}_{a+bx - x_2 < 0} : \begin{bmatrix} a \\ b \end{bmatrix} \in \mathbb{R}^2 \right\}$$

$$= \left\{ \mathbb{1}_{-a-bx + x_2 > 0} : \begin{bmatrix} a \\ b \end{bmatrix} \in \mathbb{R} \right\}$$

linear
classification

$$= \left\{ \mathbb{1}_{w_0 + w_1 x_1 + w_2 x_2 > 0} : \begin{bmatrix} w_0 \\ w_1 \\ w_2 \end{bmatrix} \in \mathbb{R}^3 \right\}$$

$$= \left\{ \mathbb{1}_{w_0 + \vec{w} \cdot \vec{x} > 0} : w_0 \in \mathbb{R}, \vec{w} \in \mathbb{R}^2 \right\}$$

$$\text{let } \vec{x} = [1, x_1, x_2]$$

$$= \{ \mathbb{1}_{\vec{w} \cdot \vec{x} > 0} : \vec{w} \in \mathbb{R}^3 \}$$

argmin \vec{x} which a 1
is the first position

Use same error function, SSE

$$g = \text{argmin} \{ \text{SSE}(h) \}$$



$$\vec{w} = \text{argmin} \left\{ \sum_{i=1}^n \left(\mathbb{1}_{\vec{w} \cdot \vec{x}_i > 0}^{y_i} \right)^2 \right\}$$

This is Hard Problem.