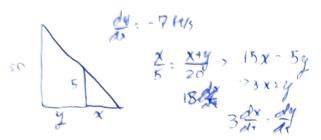


Math 1A Worksheet #20

Name

1. A street light is mounted 20 feet above a ground at the top of a pole. A 5 foot-tall teenager runs towards the pole at a rate of 7 feet per second. At what rate is the length of her shadow shrinking while she is 28 feet from the pole? (your answer should be negative)



St = 7/3 Ft/s

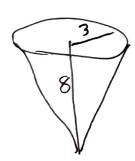
2. A red car is positioned 50 kilometers due east of a blue car. Suddenly, both cars start moving: the red car moves at a constant rate of 20 km/h east, while the blue car moves at a constant rate of 30 km/h north. At what rate is the distance between the two cars increasing 3 hours after the two cars start moving?

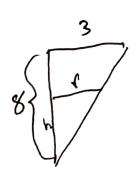
what rate is the distance between the two cars increasing 3 nours after the two cars start moving:

$$\frac{1}{x+50} = \sqrt{(x+50)^2 + y^2}$$

$$\frac{dD}{dx} = \sqrt{(x+50)^$$

3. A fluid is being pumped into an inverted conical tank at a constant rate of 10,000 cm³/min. Suppose that the tank has height 8 m and the diameter of the top is 6 m. What is the rate at which the water level is rising when the height of the water is 4 m?





4. Estimate the following quantities using linear approximation via a tangent line. A hint is provided for the first part.

- (a) $e^{-0.1}$ (use the tangent line to $y = e^x$ at (x, y) = (0, 1))
- (b) $\sin(3.24)$ (recall that $\pi \approx 3.14$).
- (c) $\sqrt{9.001}$
- (d) 1.999³

(d) 1.999°

A.) $y' = e^{x}$, y'(0) = 1, x tangent y = x + 1; $e^{-0.1} \approx 0.9$ B) $y' = \sin(x)$; $y'(\pi) = (\cos(\pi) = -1)$ tangent $y = -x + \pi$ Sin(3.24) ≈ 0.1 C.) $y = \pi$; $y'(x) = \frac{1}{2\pi}$; $y'(9) = \frac{1}{6}$; tangent $y = \frac{1}{6}(x - 9) + 3$; $\sqrt{9.001} \approx 3 + \frac{1}{6090}$ d.) $y' = x^{3}$; $y'(x) = 3x^{2}$; $y'(2) = \frac{1}{12}$; tangent $y = \frac{1}{2}(x - 2) + 4$; $1.909^{3} \approx 8 - 0.012$ $y' = \frac{1}{2}(x - 2) + 8$

5. Let u, v be functions of x. Recall that the differential dx is defined as an independent variable, and the differential du is defined by the equation du = u'(x)dx. So du depends on x and dx. Prove the following identities.

(a)
$$d(u+v) = du + dv$$

(b)
$$d(uv) = v du + u dv$$

(a)
$$d(u+v) = du+dv$$

(b) $d(uv) = v \ du+u \ dv$ Product Rule
(c) $d\left(\frac{u}{v}\right) = \frac{v \ du-u \ dv}{v^2}$. Quotient Rule.