

ACSE Labs10

Lab Report

姓名：廖冠勳

系級：電信

學號：0860306

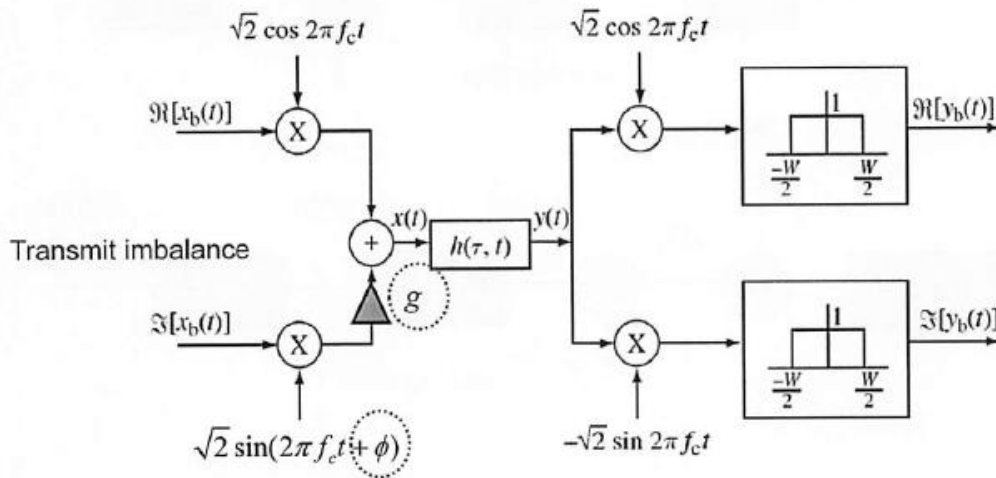
Lab 10 - RF Impairments

A. Goal of Experiment :

- To Realize the Characteristic of Communication System, including of transmit IQ imbalance, carrier frequenc offset.
- Use IQ imbalance compensation technique to eliminate the imbalance effect in the transmittor .
- Realize a carrier frequency offset system ,then plot its constellation diagram then observe it.

B. Background of experiment :

- Effect of IQ Imbalance :
 - Principle of IQ Imblance :



Signal at analog side will encounter a phase shift and additional gain due to analog circuit property, which will arise a IQ imbalance effect in the transmitting side. The effect of the IQ imbalance is listed as below.

The IQ imbalance factor g and Φ will cause gain and phase shift in the a_Q part this effect can be derived as below.

$$\begin{aligned}
 x(t) &= a_I(t) \cos(\omega t) + a_Q(t) g \sin(\omega t + \Phi) \\
 &= a_I(t) \frac{e^{j\omega t} + e^{-j\omega t}}{2} + jga_Q(t) \frac{e^{j(\omega t + \Phi)} - e^{-j(\omega t + \Phi)}}{2}
 \end{aligned}$$

Then we make a equivalent equation of the above formulation :

$$\begin{aligned} LPF\{2x(t)e^{-j\omega t}\} &= a_I + ja_Q(t)e^{j\phi} = \alpha [a_I(t) + ja_Q(t)] + \beta [a_I(t) - ja_Q(t)] \\ &= \alpha a(t) + \beta a^*(t) \end{aligned}$$

Note :

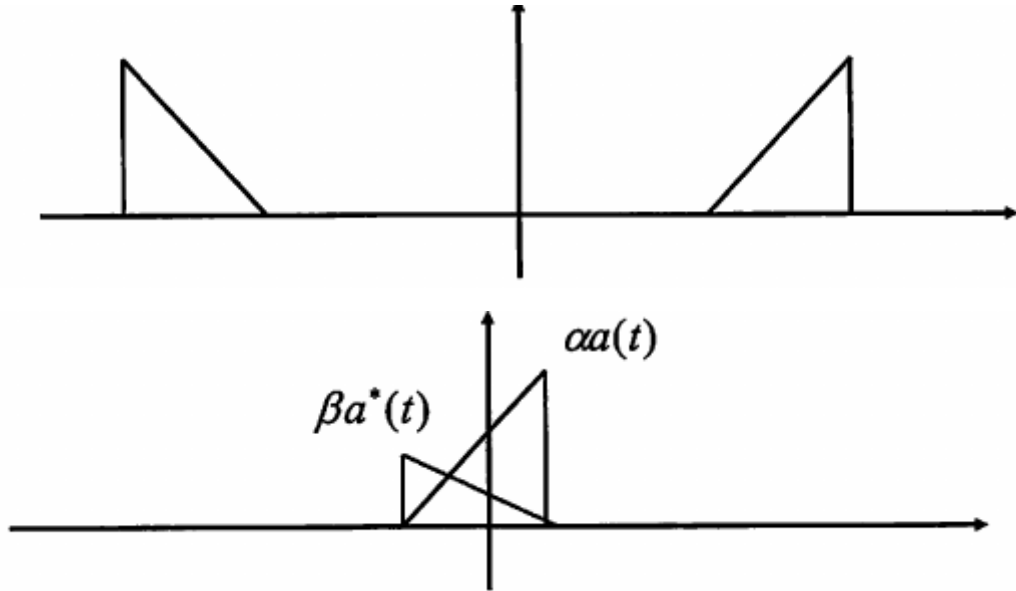
We can use the formula above to generate the received signal to verify our system result.

$$\begin{aligned} x(t) &= a_I(t) \cos(\omega t) - a_Q(t) g \sin(\omega t + \phi) \\ &= \alpha a(t) + \beta a^*(t) \end{aligned}$$

Where

$$\alpha = \frac{1}{2}(1 + ge^{j\phi}) \text{ and } \beta = \frac{1}{2}(1 - ge^{j\phi})$$

When $\alpha=1$, β will be 0, so the effect of the IQ imbalance is that the imbalance signal can be viewed as linear combination of two spectrum signal in the symmetric side of spectrum.



IQ imbalance will cause the sin part of signal a gain and phase shift.

■ Compensate the effect of IQ Imbalance :

From the IQ imbalance signal we make the form as below :

$$x(t) = a_I(t) \cos(\omega t) + a_Q(t) g \sin(\omega t + \phi)$$

By the equation of sin and cos:

$$\sin(\omega t + \phi) = \sin(\omega t) \cos(\phi) + \cos(\omega t) \sin(\phi)$$

Then we can rewrite the IQ Imbalance function :

$$\begin{aligned} x(t) &= a_I(t) \cos(\omega t) - a_Q(t) g \sin(\omega t + \phi) \\ &= [a_I(t) - g \sin \phi a_Q(t)] \cos(\omega t) - g \cos \phi a_Q(t) \sin(\omega t) \\ &= a_I^E(t) \cos(\omega t) - a_Q^E(t) \sin(\omega t) \end{aligned}$$

Then we can represent the above form as below :

$$\begin{bmatrix} a_I^E(t) \\ a_Q^E(t) \end{bmatrix} = \begin{bmatrix} 1 & -g \sin \phi \\ 0 & g \cos \phi \end{bmatrix} \begin{bmatrix} a_I(t) \\ a_Q(t) \end{bmatrix} \Rightarrow a^E(t) = H a(t)$$

With this matrix multiplication form we can use the matrix inverse property to get the original signal $a(t)$:

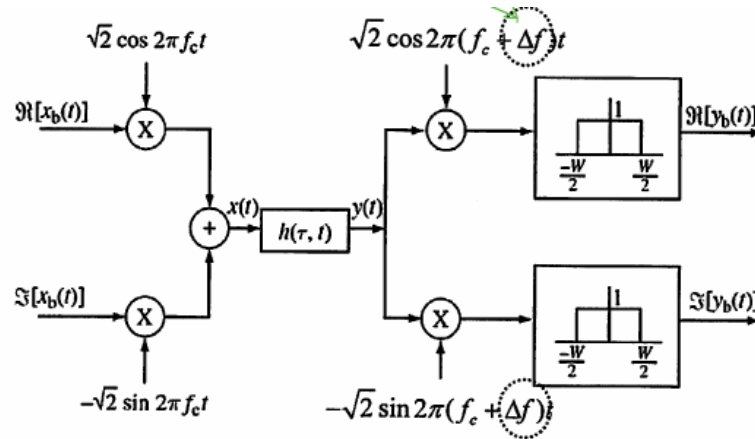
$$H^{-1} a^E(t) = a(t)$$

Where

$$a^E = \begin{bmatrix} a_I^E(t) \\ a_Q^E(t) \end{bmatrix}$$

- Effect of Carrier Frequency Offset (CFO):

- Principle of the CFO effect



Without loss of generality, we can represent the transmission signal as below :

$$\text{Real}\{a(t)e^{j\omega t}\}$$

The CFO effect in the receiver can be represented as :

$$e^{-j(\omega + \Delta\omega)t}$$

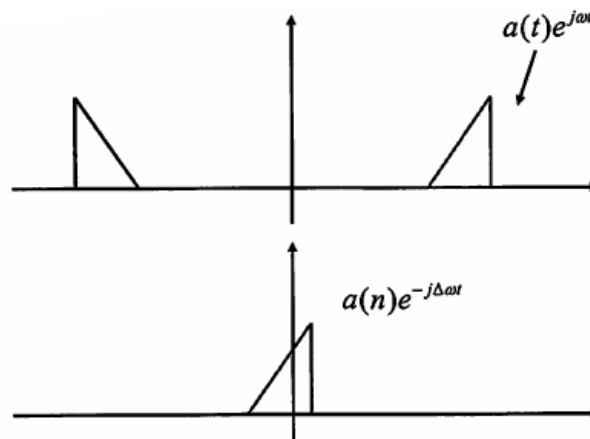
Therefore, the received signal can be written as :

$$\text{Real}\{a(t)e^{j\omega t}\} \times e^{-j(\omega + \Delta\omega)t}$$

Simplify this formula for convenience :

$$a(t)e^{j\omega t} \times e^{-j(\omega + \Delta\omega)t} = a(t)e^{-j\Delta\omega t}$$

We can observe that this signal will be rotated in the time domain, this will make the signal in frequency domain shift its FFT signal.



C. Experiment result and analysis :

● Practice Experiment Result :

■ Practice 1 - IQ imbalance

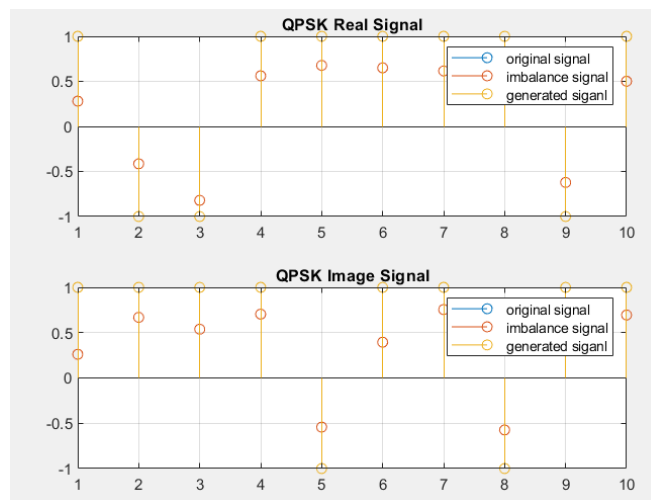
◆ Notation of Practice 1 :

From background of this experiment, we can utilize the below formula to generated the signal to verify our received signal which is indicated as generated signal in the graph.

$$x(t) = a_I(t) \cos(wt) - a_Q(t) g \sin(wt + \emptyset)$$

◆ 10 points transmission and receive signal:

- $g = 1 \quad \Phi = 1$

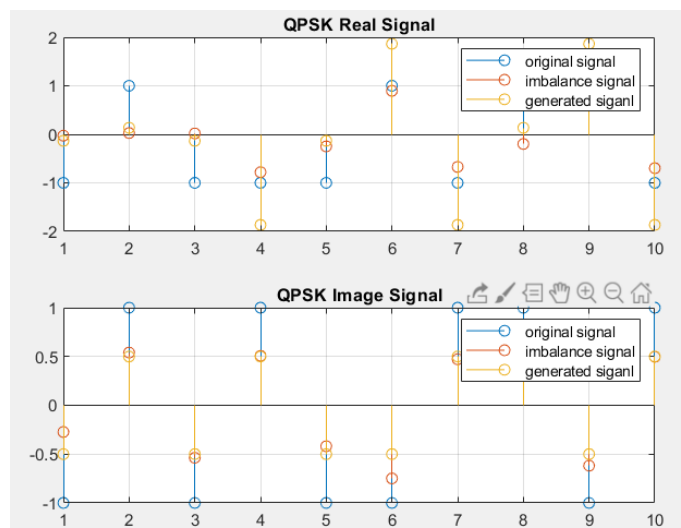


From the $a_I(t) \cos(wt) + a_Q(t) g \sin(wt + \emptyset)$, we use parameters in title then we can get

$$a_I(t) \cos(wt) + a_Q(t) * 1 * \sin(wt + 0) = a_I(t) \cos(wt) + a_Q(t) \sin(wt)$$

This result indicate that we can get original signal as show above.

- $g = 1 \quad \Phi = \pi/3$



We utilize the formula mentioned in the background and parameters in the title again then we can get :

$$a_I(t) \cos(\omega t) + a_Q(t) * 1.5 * \sin(\omega t + \pi/3)$$

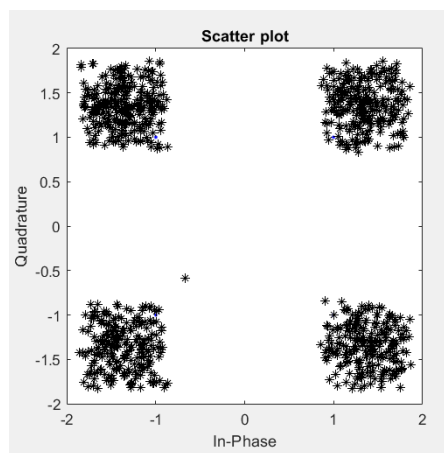
From this result , we can observe the imaginary part of this signal is multiplied by the gain of imbalance factor and is shifted the phase cause of phase imbalance.

◆ 1000 points :

- Notation of this part :

We use more points then plot its constellation graph to get the distribution of received signal then compare it with original signal.

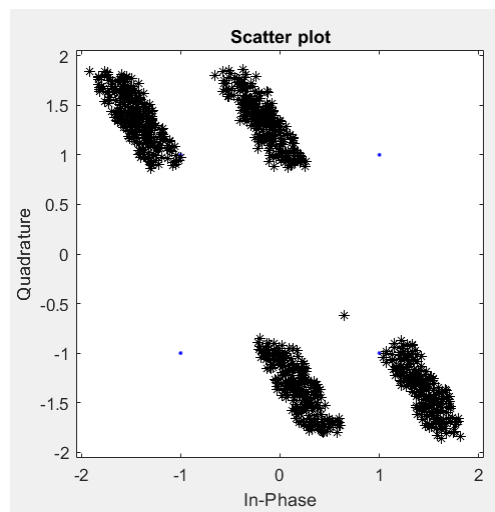
- $g = 1 \quad \Phi = 0$



Similar to the above result we can get received signal distributed around its original signal.

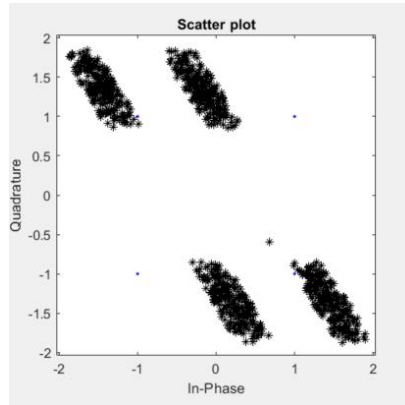
$$a_I(t) \cos(\omega t) + a_Q(t) * 1 * \sin(\omega t + 0) = a_I(t) \cos(\omega t) + a_Q(t) \sin(\omega t)$$

- $g = 1 \quad \Phi = \pi/3$



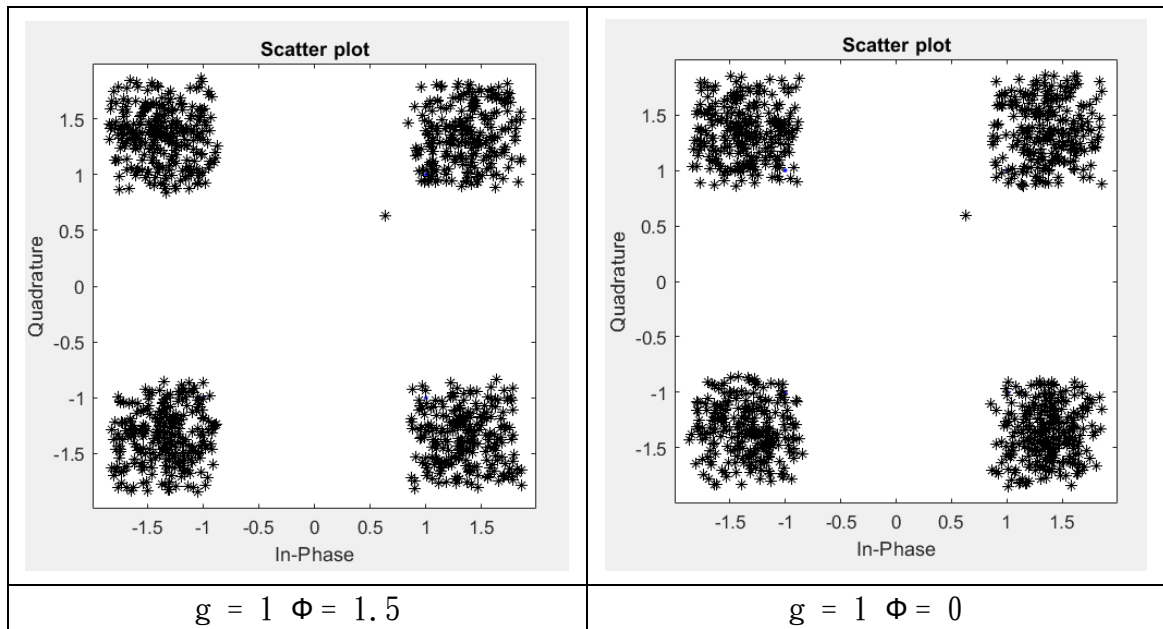
From background we can get $a_I(t) \cos(\omega t) + a_Q(t) * 1.5 * \sin(\omega t + \pi/3)$. In this situation , we can observe that the shifted phase rotate the signal in the constellation graph.

- $g = 1.5 \quad \Phi = \pi/3$



We can compare this result to the previous one, there is a small gain in the diagram.

■ Practice 2 - IQ imbalance Compensation : (1000 points)



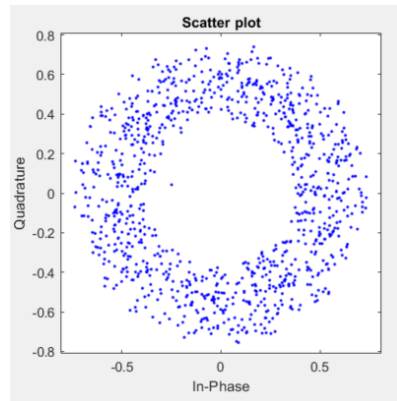
From the background $H^{-1} a^E(t) = a(t)$ indicate that we can add this compensation block to eliminate the effect of IQ imbalance. The result of this experiment verify the equation we have derived.

Therefore, we can test the communication system while offline time to get the gain and phase shift of the communication system to design this matrix for compensation.

$$H = \begin{bmatrix} 1 & -g \sin \Phi \\ 0 & g \cos \Phi \end{bmatrix}$$

It' s a useful technuque to solve such this problem.

■ Practice 3 - Carrier Frequency Offset :



CFO is a common problem in the communication system. By the derived equation above :

$$a(t)e^{j\omega t} \times e^{-j(\omega+\Delta\omega)t} = a(t)e^{-j\Delta\omega t}$$

The $e^{-j\Delta\omega t}$ term can form a circle in the constellation graph. Which make QPSK signal to form the donut shape showed in above graph.

● Home work Experiment Result :

■ Derive of home work :

① 经过 $\cos(\omega_c - \omega_{IF})t$

$$\left\{ \alpha [a_I(t) + j a_Q(t)] + \beta [a_I(t) - j a_Q(t)] \right\} \cos\left(\frac{\omega_c - \omega_{IF}}{\gamma} t\right)$$

$$\stackrel{\omega_c - \omega_{IF} = \gamma}{=} \left\{ \alpha [a_I(t) + e^{j\frac{\pi}{2}} a_Q(t)] + \beta [a_I(t) - e^{j\frac{\pi}{2}} a_Q(t)] \right\} \frac{e^{j\gamma t} + e^{-j\gamma t}}{2}$$

$$= a_I(t) [\alpha + \beta] \cdot \frac{e^{j\gamma t} + e^{-j\gamma t}}{2} + j \cdot a_Q(t) [\alpha - \beta] e^{j\frac{\pi}{2}} \cdot \frac{e^{j\gamma t} + e^{-j\gamma t}}{2}$$

$$\alpha + \beta = 1$$

$$\alpha - \beta = j e^{j\phi}$$

$$= a_I(t) \cdot \frac{e^{j\gamma t} + e^{-j\gamma t}}{2} + j \cdot a_Q(t) e^{j\phi} e^{j\frac{\pi}{2}} \cdot \frac{e^{j\gamma t} + e^{-j\gamma t}}{2}$$

② 经过 $e^{-j\omega_{IF}k}$

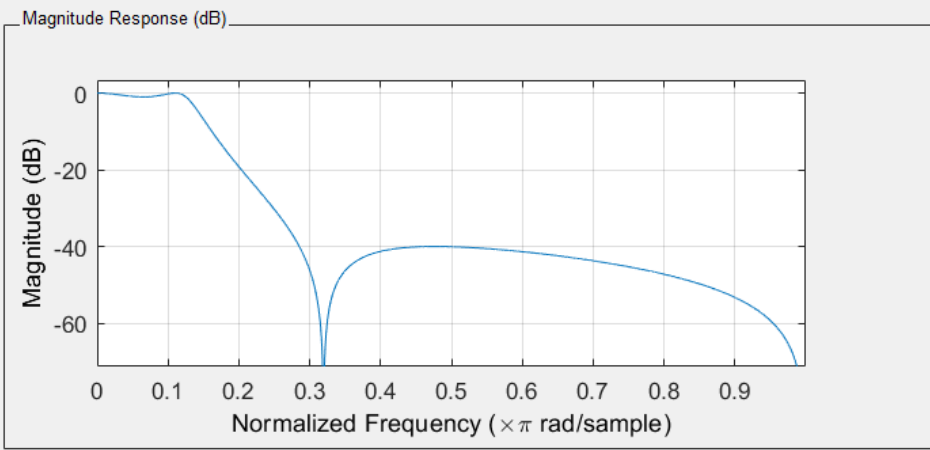
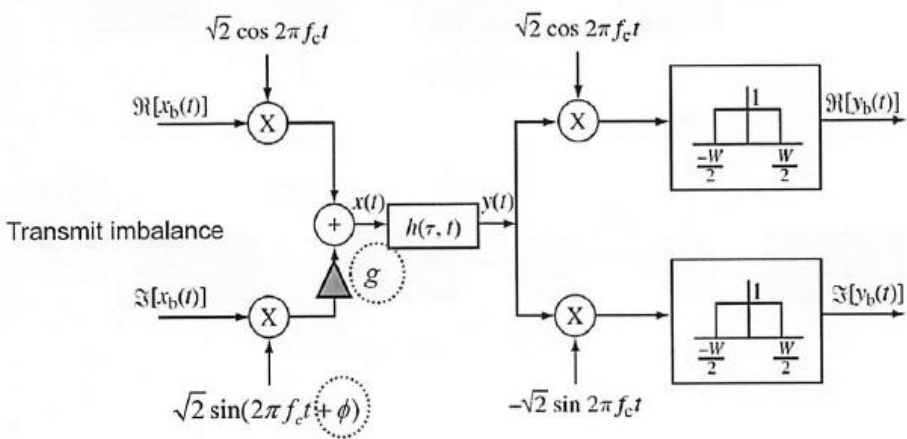
$$a_I(k) \frac{e^{j\gamma k} + e^{-j\gamma k}}{2} e^{-j\omega_{IF}k} + j a_Q(k) e^{j\phi} e^{j\frac{\pi}{2}} \cdot \frac{e^{j\gamma k} + e^{-j\gamma k}}{2} e^{-j\omega_{IF}k}$$

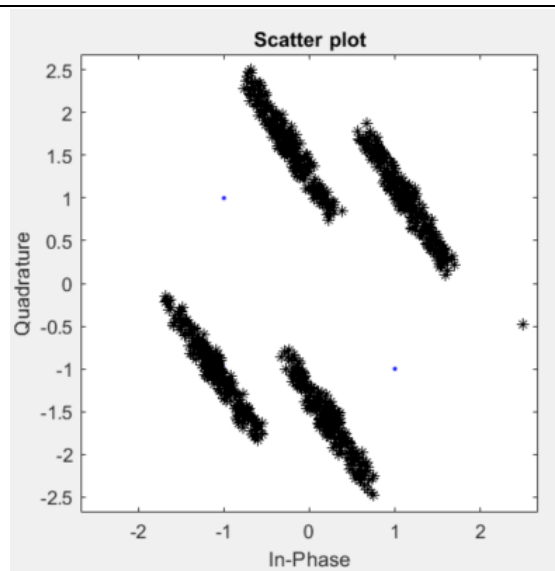
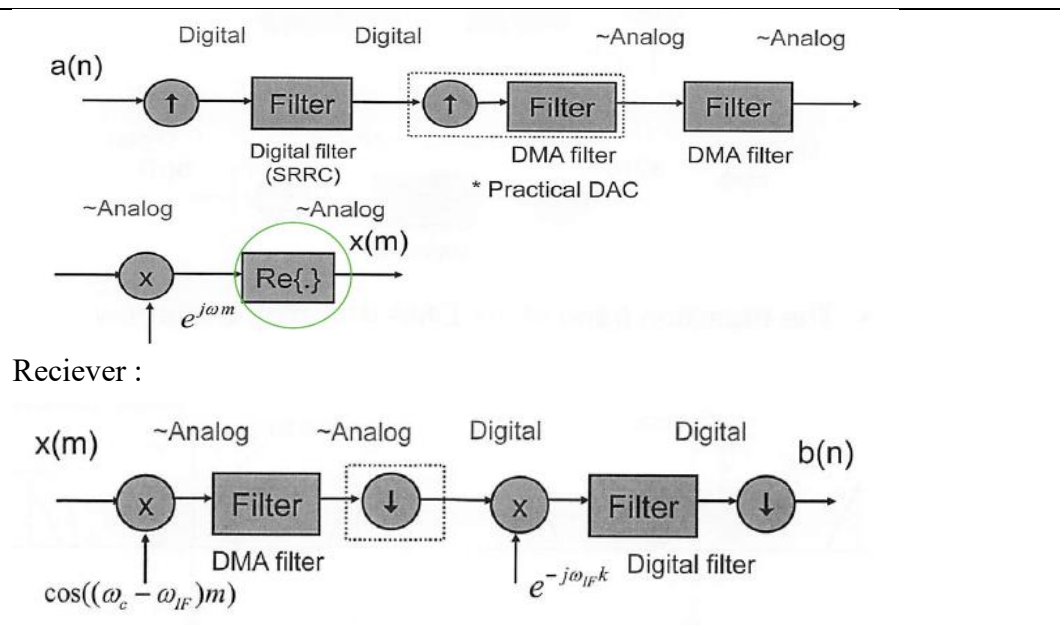
$$\stackrel{\substack{\text{LPF} \Rightarrow \omega_c \text{ 足够大} \\ \gamma = \omega_c - 2\omega_{IF}}}{=} a_I(k) \frac{e^{j(\omega_c - 2\omega_{IF})k} + e^{-j\omega_c k}}{2} + j a_Q(k) e^{j\phi} e^{j\frac{\pi}{2}} \cdot \frac{e^{j(\omega_c - 2\omega_{IF})k} + e^{-j\omega_c k}}{2}$$

$$\left[\begin{array}{l} \gamma - \omega_{IF} = \omega_c - \omega_{IF} - \omega_{IF} = \omega_c - 2\omega_{IF} \\ \gamma + \omega_{IF} = \omega_c - \omega_{IF} + \omega_{IF} = \omega_c \end{array} \right]$$

$$= \frac{1}{2} e^{j(-2\omega_{IF})k} a_I(k) + \frac{1}{2} e^{j(2\omega_{IF})k} j \cdot e^{j\phi} a_Q(k)$$

■ Experiment result :

Signal Type	QPSK
Carrier Frequency	
DAC UP factor	
DMA UP factor	
	16 = sampling rate of the DAC / symbol rate
	4 = sampling rate for DMA filter / sampling rate of the DAC
DMA Filter Pass and stop Freq	 <div> <div> Filter Order <input type="radio"/> Specify order: 10 <input checked="" type="radio"/> Minimum order </div> <div> Options Match exactly: both </div> <div> Frequency Specifications Units: Normalized (0 to 1) Fs: 48000 wpass: 1/8 wstop: 1/4+3/4/4 </div> <div> Magnitude Specifications Units: dB Apass: 1 Astop: 40 </div> </div>
System Architecture	<p>All system view :</p>  <p>Transmitter :</p>



From the derived equation, we can get:

$$\frac{1}{2} e^{-j2\omega_{IF}k} [a_I(k) + j * g * e^{j\Phi} * a_Q(k)]$$

Unlike practice 1:

$$x(t) = a_I(t) \cos(\omega t) - a_Q(t) g \sin(\omega t + \phi)$$

The term of $\frac{1}{2} e^{-j2\omega_{IF}k}$ will make both real and imaginary part of signal be rotated. The reason is that both blocks in IF receiver will contribute the rotation term.

The diagrams illustrate the rotation term in the IF receiver. The first block shows a multiplier (X) with an input from the left and a feedback input from below labeled $\cos((\omega_c - \omega_{IF})m)$. The second block shows a multiplier (X) with an input from the left and a feedback input from below labeled $e^{-j\omega_{IF}k}$.