

5.1  $x \vee x \wedge y = x$

$x \wedge y$  means that it must be an element of  $x$  and  $y$

$x \vee x \wedge y$  means that it must be an element of  $x$  or  $x$  and  $y$

an element of  $x \wedge y$  is always an element of  $x$ . Therefore  $x \vee x \wedge y = x$

2.  $x \vee x \wedge y = x \vee (x \wedge y)$  (Associativity)  
 $x \vee (x \wedge y) = x$  (law of absorption)

6.1

1	$(p \vee q) \rightarrow q$	(A)
2	$p$	(A)
3	$p \vee q$	( $\vee$ -I, 1)
4	$q$	( $\rightarrow$ -E, 1, 3)
5	$p \wedge q$	( $\wedge$ -I, 2, 4)
6	$\neg(p \wedge q)$	( $\rightarrow$ -I, 1-5)

2.

1	$(p \rightarrow q) \wedge (p \rightarrow \neg r)$	(A)
2	$p$	(A)
3	$p \rightarrow q$	( $\wedge$ -E, 1)
4	$p \rightarrow r$	( $\wedge$ -E, 1, 2)
5	$q$	( $\rightarrow$ -E, 2, 3)
6	$r$	( $\rightarrow$ -E, 2, 4)
7	$q \wedge r$	( $\wedge$ -I, 5, 6)
8	$p \rightarrow q \wedge r$	( $\rightarrow$ -I, 2, 7)
9	$((p \rightarrow q) \wedge (p \rightarrow r)) \rightarrow (p \rightarrow (q \wedge r))$	( $\rightarrow$ -I, 1, 8)

7.1

1	$p \vee q$	(A)
2	$\neg p$	(A)
3	$p$	(A)
4	$\bot$	( $\rightarrow$ -E, 2, 3)
5	$q$	( $\rightarrow$ -E, 4)
6	$p \rightarrow q$	( $\rightarrow$ -I, 3, 5)
7	$q$	(A)
8	$q \rightarrow q$	( $\rightarrow$ -I, 7, 7)
9	$q$	( $\vee$ -E, 1, 6, 8)
10	$\neg p \rightarrow q$	( $\rightarrow$ -I, 2, 9)
11	$(p \vee q) \rightarrow (\neg p \rightarrow q)$	( $\rightarrow$ -I, 1, 10)