Chapter 1

Introduction

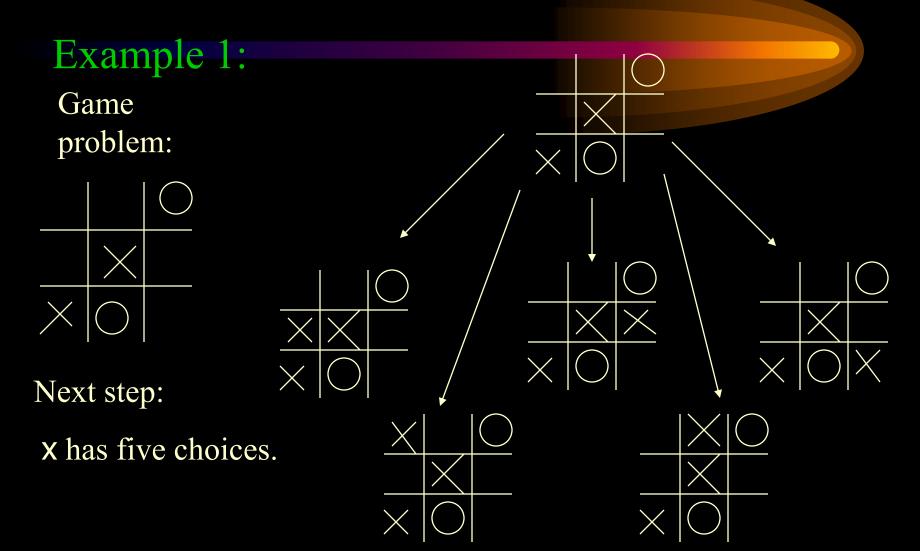
- Introduce most used data structures and algorithms
- Prerequisite of other courses
- Introduce algorithm analysis
- Review Java and C++

1. Introduce most used data structures and algorithms.

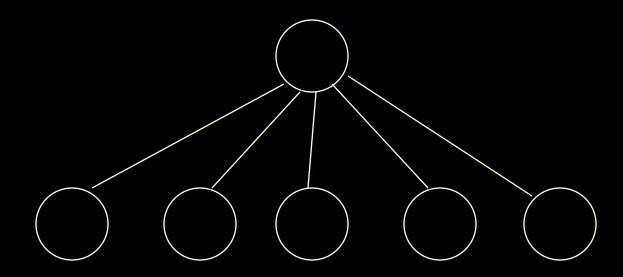
Use proper data structures to solve different problems.

Example:

- Game problem
- Management of library catalogue by computer
- Management of the traffic lights in intersections
- The book : selection problem solve a popular word puzzle



Example 1 uses a tree structure.



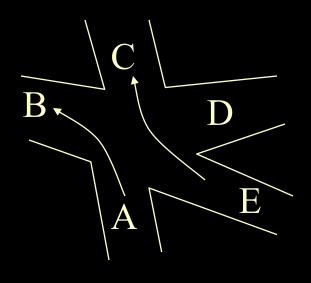
Example 2: Management of library catalogue by computer

书名	作者名	登录号	分类	出版年月
D.S.	Sartaj Sahni	000001	computer	2000.1

It is a linear list.

Example 3:

Management of the traffic lights in intersections



C, E are one-way road, there are 13 path to go.

Can go at the same time:

Cannot go at the same time:

$$E \rightarrow B \quad A \rightarrow D$$

- 2. Prerequisite of other courses:
- Principles of compiling: use stack to compute expression and implement recursive procedure
- Operating System: use queue to implement job scheduling
- Database: use B-tree, B+ tree to organize, store and load massive data in the hard memory.

• • •

3. Basic methods of algorithm analysis standards of the performance of an algorithm: time complexity, space complexity, and accuracy example: sorting $a_1, a_2, a_3, \dots, a_{n-1}, a_n$ $n-1+n-2+...+2+1=n(n-1)/2=(n^2-n)/2$ $O(n^2)$ $O(n*log_2n)$ 4. Review Java and C++

1. Data

is the carrier of information.

Data is a set of numbers, characters, and other symbols

- that can be used to describe the objective things.
- These symbols can be input into computers, identified and processed by the computer program.

```
Data can divided into two classes:

numerical data: int, float, complex,.....
non-numerical data: character, string,
graph, voice...
```

2. Data structure

A data structure is a data object together with the relationships among the data members that compose the object

 $Data_Structure = \{D,R\}$

D is a data object,

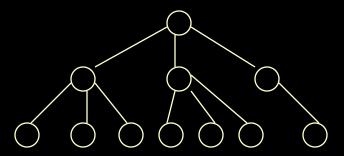
R is a limited set of relationships of all the data members in D.

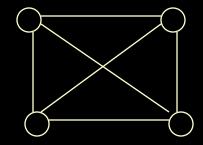
Linear structure



Data structure

Non-linear structure





数据结构涉及三个方面:

数据的逻辑结构-----从用户视图看,是面向问题的。 数据的物理结构-----从具体实现视图看,是面向计算机的。 相关的操作及其实现。

Example:

学生表:逻辑结构----线性表

物理结构----数组,拉链

操作----插入,删除,查找

1. Data type

Definition: is a set of values together with a operation set that operate on these values.

Example:

```
int type
```

```
value set: \{...,-2,-1,0,1,2,...\}
```

Most of the programming languages provide a group of predefined data type.

```
Atom data type — int, float, double.....

Structure data type—array, struct,.....
```

2. ADTs: Abstract Data Types

是将类型和与这个类型有关的操作集合封装在一起的数据模型。

Abstract: is a method used to hide the information.

Example:

```
int x;
    :
    x=735;
    :
abstract of int data type
assignment
```

```
float x, y;
:
x=x*y+3.0;
:
abstract of float data type operation
```

Abstract data type:

is a new programming method that

part the usage and implementation, in order to encapsulate and hide the information.

思想:

将数据类型的使用与它的表示(机内存储)、实现(机内操作的实现)分开。更确切的说,把一个数据类型的表示及在这个类型上的操作实现封装到一个程序模块中,用户不必知道它。

ADT NaturalNunber is

• **objects:** 一个整数的有序子集合,它开始于0,结束于机器能表示的最大整数 (MAXINT)。

• Function:

- Zero():NaturalNumber
- IsZero(x):Boolean
- Add(x,y):NaturalNumber
- Equal(x,y):Boolean
- Successor(x):NaturalNumber
- Subtract(x,y):NaturalNumber
- end NaturalNumber

3. OO:

```
object-oriented=object+class+inherit+
communicate
```

object: attribute values+ operates

```
example: rectangle: 一个几何对象
```

attribute values: 左上角坐标, 右下角坐标, 边线颜色, 内部颜色

operates : move(x,y);

setEdgeColor(c);

setInterColor(c) ;

class: objects of same attributes and operates.

an instance is an object of the class.

different object has deferent attribute
value

Inherit:

base class—integrate the same part (including attributes and operations) in all the derived classes

derived class—add the specific attributes and operations

Example: base class—polygon derived class—quadrilateral,triangular

Communication: each class object communicate with others using messages.

Message: instructions that one class object used in order to require another class object to perform some operation.

Algorithm definition

Algorithm: an operation sequence of soluting a problem

Characteristic: 1.finite

- 2. deterministic
- 3. initial action
- 4. sequence ends

Algorithm definition

Program: is written by languages that can be performed by machine.

can't satisfy the finiteness.

For example, OS.

Algorithm: has multiple descriptive methods, such as language, graph, table.

Algorithm definition

1. Exponents

$$X^A X^B = X^{A+B}$$

$$X^A/X^B = X^{A-B}$$

$$(X^A)^B = X^{AB}$$

$$X^{N} + X^{N} = 2X^{N}$$

$$2^{N} + 2^{N} = 2^{N+1}$$

2. Logarithms (all logarithms are to the base 2)

DEFINITION:

$$X^A = B$$
 if and only if $log_X B = A$

THEOREM 1.1

$$log_AB = log_CB/log_CA$$
; A, B, C > 0, A != 1

THEOREM 1.2

$$logAB = log A + log B; A, B > 0$$

3. Series

$$\sum_{i=0}^{N} 2^{i} = 1 + 2^{1} + 2^{2} + \dots + 2^{N} = 2^{N+1} - 1$$

$$\sum_{i=1}^{N} i = 1 + 2 + 3 + \dots + N = (N+1)*N/2$$

4. Modular Arithmetic

We say that A is congruent to B modular N,

written $A \equiv B \pmod{N}$, if N divides A-B.

Example: $81 \equiv 61 \equiv 1 \pmod{10}$

5. The P Word (证明方法)

1). Proof by Induction

The first step is proving a base case.

the Next stap an inductive hypothesis is assumed.

theorem is assumed to be true for all cases up to some limit k. Using this assumption, the theorem is then shown to be true for the next value, which is typically k+1. This proves the theorem (as long as k is finite).

Example: 例如 等比级数的和以及整数平方和的证明等.

2). Proof by Contradiction

Proof by contradiction proceeds by assuming that the theorem is false and showing that this assumption implies that some known property is false, and hence the original assumption was erroneous.

Example: proof that there is an infinite number of primes

1. Recursive

example:

define a function f, valid on nonnegative integers

$$f(x) = \begin{cases} 0 & x = 0 \\ 2f(x-1) + x^2 & x > 0 \end{cases}$$
$$f(1) = 1, f(2) = 6, f(3) = 21, f(4) = 58$$

```
public static int f ( int x)
{    if ( x = = 0) //base case
        return 0;
    else return 2*f(x-1) + x*x; //recursive call
}
```

A nonterminating recursive method: public static int bad(int n) $\{ if (n = 0) \}$

```
{ if ( n = = 0)
    return 0;
    else return bad( n/3 + 1) + n-1;
}
```

two fundamental rules of recursion:

- 1) Base cases.
- 2) Making progress.

- 2. 1) direct recursive
 - 2) indirect recursive

Example 1 factorial function f(n)=n!

$$f(n) = \begin{cases} 1 & n \le 1 \text{ (base)} \\ n*f(n-1) & n \ge 1 \text{ (recursive component)} \end{cases}$$

```
f(5)=5f(4)=5*4f(3)=5*4*3f(2)=5*4*3*2f(1)=120

static long factorial (int n)

{ if (n <= 1) return 1; else return n* factorial(n-1)}
```

```
public class ComputeFactorial
   public static void main( String[ ] args )
     System.out. Println("please enter a nonnegative integer");
      int n = MyInput.readInt( );
       System.out.println("Factorial of " + n +" is " + factorial( n ) );
   static long factorial (int n)
   \{ if (n \le 1) return 1; \}
     else return n*factorial(n-1);
```

Example 2: Compute Fibonacci number 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, ... fib(0) = 0;

fib(n) = fib(n-2) + fib(n-1); n>=2

```
public static long fib(long n)
{     if ( ( n == 0) || ( n == 1 ) )
         return n;
     else
        return fib(n-1) + fib(n-2);
}
```

Compute fib(4):

fib(1) = 1;

```
public class ComputeFibonacci
  public static void main( String args[ ])
     System.out.println("Enter an index for the Fibonacci number");
      int n = MyInput.readInt();
      System.out.println("Fibonacci number at index "+ n + " is " +
                           fib(n);
    public static long fib(long n)
       if ((n = = 0) || (n = = 1))
          return 1;
       else
          return fib(n-1) + fib(n-2);
```

Example 3:

```
computes the sum of the elements a[0] through a[n-1] a[0], a[1], ..., a[n-2], a[n-1]
```

```
public static int Rsum(int[] a , int n)
\{ if (n>0) \}
     return Rsum(a,n-1)+a[n-1];
  return 0;
Rs(a,4)---->Rs(a,3)+a[3]
             Rs(a,2)+a[2]
             Rs(a,1)+a[1]
             Rs(a,0)+a[0]
```

Example 4:

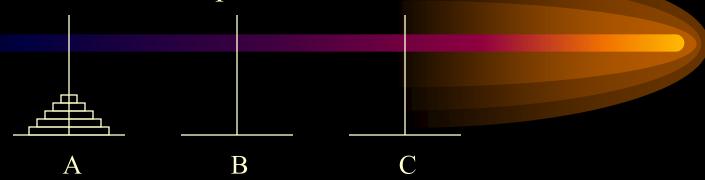
Permutation

{a,b,c}: abc, acb, bac, bca, cab, cba permutation of n elements has n!

下面在黑板上来分析该问题:

```
public static void perm(Char[] list, int k, int m)
   int i;
   if (k==m) { for (i=0; i\le m; i++) cout << list[i];
                 cout << endl; }
   else{ for (i=k; i<=m; i++)
            { swap(list[k], list[i]);
              perm(list, k+1, m);
              swap(list[k], list[i]);
```

Example 5 : Hanoi tower problem



```
if ( n==1)
    Move disk 1 from the fromTower to the toTower;
else
{ moveDISKs(n-1, fromTower, auxTower, toTower);
    Move disk n from the fromTower to the toTower;
    moveDISKs(n-1, auxTower, toTower, fromTower);
}
```

```
public class TowersOfHanoi
  public static void main(String[] args)
     System.out.printLn("Enter number of disks");
     int n = MyInput.readInt();
     System.out.printLn( "The move are:");
     moveDISKs(n, 'A', 'B', 'C');
  public static void moveDISKs(int n, char fromTower, char
                                toTower, char auxTower)
  \{ if (n=1) \}
      System.out.printLn( "move disk " + n + "from "+
                          fromTower +" to" + toTower);
    else
      moveDISKs(n-1, fromTower, auxTower, toTower);
      System.out.printLn( "Move disk " + n + "from " +
                          fromTower + " to " + toTower );
      moveDISKs(n-1, auxTower, toTower, fromTower);
```

Throughout this text, we will describe algorithms and data structures that are type independent.

```
IntCell — nongeneric class

MomoryCell — generic class
```

```
1. IntCell class
public class IntCell
{ public IntCell(){ this (0); }
   public IntCell( int initialValue )
     { storedValue = initialValue; }
   public int read ( ) { return storedValue; }
   public void write ( int x ) { storedValue = x; }
   private int storedValue;
```

1) public and private

```
memble of public: may be accessed by any method in any class.
```

member of private: may only be accessed by methods in its class.

```
specifier is omitted (package-friendly visibility):
```

a data member whose visibility specifier is omitted is visible to other classes in the same package.

2) constructor

A class may define methods that describe how an instance of the class is constructed; these are called constructors.

If no constructor is explicitly defined, one that initializes the fields using language defaults is automatically generated.

3) This

In many cases, the zero-parameter constructor can be implemented by calling another constructor.

By using this, we avoid replicating code logic in separate constructors.

• A different use of this is as a reference to the object being acted upon.

1) static and main

The main method must be static, meaning that it applies to the TestIntCell class instead of a single instance of the class.

Each class may declare a main method that will be used when the java interpreter is called for that class.

复习一下static

2) Object creation.

Objects are created by using new.

```
3) Method calls.
m.write(5);
m.read()

m.storedValue //be illegal
```

2. MemoryCell class

design a class that works for any type of Object.

```
example: sorting of array a_0, a_1, a_2, a_3, \dots a_{n-1}
```

• C++: use templete

```
program1.1:
```

```
int Abc(int a,int b,int c)
{return a+b+b*c+(a+b-c)/(a+b)+4;}

program1.2:
float Abc(float a,float b,float c)
{return a+b+b*c+(a+b-c)/(a+b)+4;}
```

program1.1 and 1.2 differ only in the data type of the formal parameters and of the value returned.

We can write a generic code in which the data type is a variable whose value is determined by the compiler. This generic code is written using the template statement in program 1.3

Program1.3

```
template < class T > T Abc(T a,T b,T c) {return a+b+b*c+(a+b-c)/(a+b)+4; } From this generic code the compiler can construct 1.1 by substituting int for T and 1.2 by substituting float for T.
```

- Java:
 - use inheritance(pre-java 5)
 all objects are subclasses of Object.

```
public class MemoryCell
{ public Object read()
    { return storedValue; }
   public void write(Object x)
    { storedValue = x; }
   private Object storedValue;
              A generic MemoryCell class (pre-java 5)
       1.5
```

Two problem:

```
First problem: We must downcast to the correct type
 public class TestMemoryCell
    public static void main( String [ ] args )
       MemoryCell m = new MemoryCell ( );
        m.write("37");
        string val = (String) m.read();
        System.out.println("Contents are: " + val)
       Using the generic MemoryCell class (pre-Jave 5)
       the read method for MemoryCell returns an Object.
```

Second problem Although all objects are subclasses of Object, the primitive types boolean, short, char, byte, int, long, float, double are not objects. Thus we cannot directly use MemoryCell to store a primitive value.

We must use wrapper class provide by Jave. Wrapper class store a single primitive value and can be used wherever an Object is need.

the wrapper class provides a method that can be used to access the primitive value it stores.

two example:

a) For the Integer wrapper, this method is named intValue.

```
public class Integer
{    public Integer(int x)
    {       value = x; }
    public int intValue()
    {       return value; }
}
```

```
public class wrapperdemo
  public static void main ( String [ ] args )
        MemoryCell m = new Memorycell ( );
        m.write ( new Integer ( 37 ) );
        Integer wrapperVal = (Integer) m. Read();
        int val = wrapperVal . intValue ( );
        System . Out . Println ("Contents are: "+ val);
```

1.7 An illustration of Integer wrapper class

To get the int value that is hidden inside the Integer object, we must convert the result of read back to an Integer, and then use mathod intValue access the value. This involves using a type conversion.

2) Java 5 supports generic classes that are very easy to use

1.9 Generic implementation of the MemoryCell class

- When a generic class is specified, the class declaration includes one or more type parameters after the class name
- User can create types such as GenericMemoryCell<String>
 GenericMemoryCell<Integer>
 - but can not create GenericMemoryCell<int>
- Inside the GenericMemoryCell class declaration, we can declare fields of the generic type and methods that use the generic type as a parameter or return type

Interfaces can also be declared as generic.
 prior to Java 5, the Comparable interface was not generic.
 In Java 5, the Comparable class is generic.

```
package java.lang;
public interface Comparable<AnyType>
{    public int compareTo ( AnyType other );
}
```

1.10 Comparable interface, Java 5 version which is generic

```
class BoxingDemo
  public static void main ( String [ ] args )
      GenericMemoryCell<Integer> m =
                 new GenericMemoryCell<Integer>();
       m. Write (37); insert a call to the Integer constructor behind the scenes m. Write (37);
       int val = m . Read();
                                                                        scenes
       System . Out . Println ("contents are: "+ val);
```

1.11 Autoboxing and unboxing

**编译程序在箭头处分别调用Integer构造函数与intValue方法

b) Implementing Generic findMax

The MemoryCell class required no special properties of Object; the only operations performed were reference assignments, which are always available.

Finding the maximum item in an array of items does require a special property; we must be able to compare two items and decide which is larger.

```
Comparable findMax (Comparable [] a)
    Comparable \max Value = a[0];
    for (int i = 1; i < a.length; i++)
     if (maxValue.lessThan (a[i]))
         maxValue = a[i];
    return max Value;
```

a generic findMax algorithm.

Notice that the objects that are manipulated are not Object, But instead are Comparable.

Comparable is an interface.

In java, an interface declares a set of methods that must be implemented.

- In this example, any class that is Comparable must provide an implementation of lessThan
- A class that is Comparable must also declare so by using the implements clause.

```
public interface Comparable
{ int lessThan( Comparable rhs );
} compareTo
```

```
Comparable findMax (Comparable [] a)
    Comparable max Value = a[0];
    for (int i = 1; i < a.length; i++)
      if ( maxValue.compareTo(a[i])<0 )
         maxValue = a[i];
     return maxValue;
         a generic findMax algorithm.
```

```
In the book:
Class FindMaxDemo
    public static comparable findMax( Comparable [ ] arr )
       int maxIndex = 0;
       for (int i = 1; i < arr.length; i++)
          if (arr[i].compareTo(arr[maxIndex]) > 0)
                 maxIndex = i;
        return arr[ maxIndex ];
    public static void main ( String [ ] args )
       Shape [] sh1 = \{ new Circle(2.0), new Square(3.0),
                         new Rectangle( 3.0, 4.0 ) }
       String [ ] sta = { "Joe", "Bob", "Bill", "Zeke" };
       System.out.println( findMax( sh1 ) );
       System.out.println( findMax( st1 ));
```

```
//another Example:
public interface Comparable
  public int compareTo(object o );
public class Max
  public static Comparable max( Comparable o1, Comparable o2)
   { if (o1. compareTo(o2) > 0)
          return o1;
       else return o2;
```

```
class Circle
{ private double radius;
   public Circle() { radius = 1.0; }
   public Circle( double r ) { radius = r; }
   public double getRadius ( ) { return radius; }
   public void set Radius (double newRadius)
     { radius = newRadius; }
   public double findArea()
     { return radius * radius * 3.14159; }
```

class ComparableCircle extends Circle implements Comparable public ComparableCircle (double r) super (r); public int compareTo (object o) if (getRadius() > ((Circle) o).getRadius()) return 1; else if (getRadius () < ((Circle) o) . getRadius ()) return -1; else return 0;

```
public class TestInterface
  public static void main( String[] args )
      ComparableCircle circle1 = new ComparableCircle(5);
      ComparableCircle circle2 = new ComparableCircle(4);
      Comparable circle = Max . max (circle1, circle2);
      System.out.println ("The max circle's radius is "+
                     ( ( Circle ) circle ) . getRadius ( ) );
      System.out.println (circle);
} //another Example
```

Java的异常处理提供对运行时错误的语言级处理机制。

1. 三类error

语法error, 语义error, 逻辑 error

1) 语法error

通常在编译时发现, 又称编译错。

如: 标识符未声明, 类型不匹配, 缺少分号等。

2) 语义error

只有到程序运行时才发现,又称运行错。

如:除数为0,数组下标越界等。

打开的文件不存在, 网络连接中断等。

3) 逻辑 error

运行结果与期望值不符。这类错误最难确定与排除。

- 2. 运行时的error又分为两类(根据错误的性质)
 - 1) 错误(error)-----运行时遇到硬件或OS错误。

2) 异常(exception)-----硬件与OS都正常,程序遇到的运行错。 如,除数为0,网络连接中断,打开文件发现文件不存在等。

- 3. Java的异常处理
 - 1) 异常处理语句

```
try
  语句1
            //存在潜在异常的代码
catch(异常类 异常对象)
  语句2
           //捕获到异常并进行处理的代码
finally
            //最后必须执行的代码,无论是否捕获到异常
  语句3
```

```
public class Try2
   public static void main( string args[ ])
   \{ \text{ int } i = 0; \text{ int } a[] = \{ 5,6,7,8 \}; 
      for(i = 0; i < 5; i++)
      { try
          { system.out.print("a[" + i + "]/" + i + " = " + (a[i]/i));
         catch(ArrayIndexOutOfBoundsException e)
          { system.out.print("捕获数组下标越界异常!"); }
         catch( ArithmeticException e)
             system.out.print("捕获算术异常!") }
         catch(Exception e)
             system.out.print("捕获" + e.getMessage() + "异常!");
                                  //显示异常信息
         finally
            system.out.println("i = "+i); }
      } //for
      system.out.println("继续!");
```

运行结果为:

捕获算术异常! i=0

$$a[1]/1 = 6$$
 $i = 1$

$$a[2]/2 = 3$$
 $i = 2$

$$a[3]/3 = 2$$
 $i = 3$

捕获数组下标越界异常! i=4

继续!

- 2) 抛出异常
- 抛出自定义异常对象

throw 异常对象

由throw语句抛出的异常也必须由try语句捕获并处理。

```
example
 public void set(int age)
   if(age > 0 \&\& age < 100)
     this.age = age;
   else
     throw new Exception ("IllegaAgeData"); //抛出异常
抛出异常和处理可以在一个方法中,也可分别在不同的方法中。
一般而言,一个方法通过throw抛出异常,由方法的调用者捕获
并处理该异常对象。
```

```
public void set ( int age )
  try
  \{ \text{ if (age > 0 \&\& age < 100)} \}
         this . age = age;
     else throw new Exception ("IllegalAgeData");
  catch (Exception e)
       system . Out . Println ( e . toString ( ) );
```

方法声明抛出异常的throws子句example
 public void removeAny() throws Underflow
 if (isEmpty())
 throw new Underflow();

import java.io.*

1. Basic Stream Operations

System.in standard input;

System.out standard output

System.err standard error

output in java: is done almost exclusively by String concatenation, with no built-in formatting.

use toString

input in java: reading formatted input

is to read a single line into a String object using readLine. The readLine method reads until it encounters a line terminator or end of file.

To use readLine, we must first construct a BufferedReader object from an InputStreamReader object that itself constructed from System.in.

```
import java.io.*;
public class DivideByTwo
 public static void main(String args)
     bufferedReader in = new BufferedReader( new
                          InputStreamReader (System.in);
      int x;
      String oneLine;
      System.out.println("Enter an integer:");
      try
      { oneLine = in.readLine(); // IOException
        x = Integer.parseInt( oneLine ); //NumberFormatException
        System.out.println("Half of x is" + (x/2));
       catch(Exception e)
          { system.out.println(e); }
```

Recall that to read a single primitive type, such as an int:

- 1) use readLine to read the line as a String.
- 2) then apply a method to generate the primitive type from the String. For int, we can use parseInt.

2. The StringTokenizer Object

Sometimes we have several items on a line. For instance, suppose each line has two **int**s.

Java provides the **StringTokenizer** object to separate a **String** into **tokens**.

```
Input and Output
import java.io.*
import java.util.*;
public class MaxTest
 public static void main( String [ ] args )
     BufferedReader in = new BufferedReader
                 ( new InputStreamReader( System.in ) );
     String oneLine;
     StringTokenizer str;
     int x; int y;
     System.out.println("Enter 2 ints on one line: ");
     try
        oneLine = in.readLine();
        str = new StringTokenizer( oneLine );
        if( str . countTokens( ) != 2 )
            throw new NumberFormatException();
        x = Integer . parseInt( str . nextToken( ) );
        y = Integer . parseInt( str . nextToken( ) );
        System.out.println("Max: " + Math.max(x, y));
    catch (Exception e)
           System.err.println("Error: need two ints"); } }
```

- To use StringTokenizer, provide the Import directive import java.util.*;
- By default, tokens are separated by white space.

example:

"I am learning Java now"

3. Sequential Files

One of the basic rules of java is that what works for terminal I/O as works for files.

To deal with a file:

```
System.in----> InputstringReader----> BufferedReader

construct construct BufferedReader

filename----> FileReader construct construct sometime construct sometime construct construct sometime construct sometime construct sometime construct construct sometime construct construct sometime construct construct sometime construct construct construct sometime construct constru
```

```
import java.io.*;
public class ListFiles
   public static void main( String [ ] args )
      if (args.length = = 0)
         System.out.println("No files specified");
      for (int i = 0; i < args.length; i++)
         listFile( args[i]);
   public static void listFile( String fileName )
       FileReader theFile;
       BufferedReader fileIn = null;
       String oneLine;
       Systnm.out.println("FILE: " + fileName );
```

```
try
   theFile = new FileReader( fileName );
   fileIn = new BufferedReader( theFile );
   while( ( oneLine = fineIn.readLine( ) ) != null )
        System.out.println( oneLine );
catch( exception e)
     System.out.println( e ); }
// close the stream
try
   if(fileIn!=null)
       fileIn.close( );
catch( IOException e ) { }
```

Code Organization

Packages
 package DataStructures;

Most of our classes will be found in a package named DataStructures. This includes the Overflow and Underflow exception classes.

Chapter 1

Exercises:

- 1. Write a recursive method that returns the number of 1's in the binary representation of N. Use the fact that is equal to the number of 1's in the representation of N/2, plus 1, if N is odd.
- 2. Write the routines wise the following declarations:

```
public void permute( String str );
private void permute( char [ ] str, int low, int high )
```

The first routine is a driver that calls the second and prints all the permutations of the characters in String str. If str is "abc", then the strings that are output are abc, acb, bac, bca, cab, and cba. Use recursion for the second routine.

- 3. 已知a[n]为整型数组,试写出实现下列运算的递归算法。
 - 1) 求数组a中的最大整数。
 - 2) 求n个整数的平均值。

Chapter 1

- 4. Write a recursive method that calculates and returns the length of a linked list.
- 5. Check recursively if the following objects are palindromes:
 - a. A word
 - b. a sentence (ignoring blanks, lower- and uppercase differences, and punctuation marks so that "Madam, I'm Adam" is accepted as a palindrome)

Chapter 1

实习题:

1. 找出从自然数 1, 2, ..., n 中任取r个数的所有组合, 编一个递归算法...

```
例子: n=5 12345
    r = 3 5 4 3
              5 4 2
              5 4 1
              5 3 2
              5 3 1
              5 2 1
              4 3 2
              4 3 1
              4 2 1
              3 2 1
```

2. 实现Hanoi塔