

# Occupancy Networks: Learning 3D Reconstruction in Function Space

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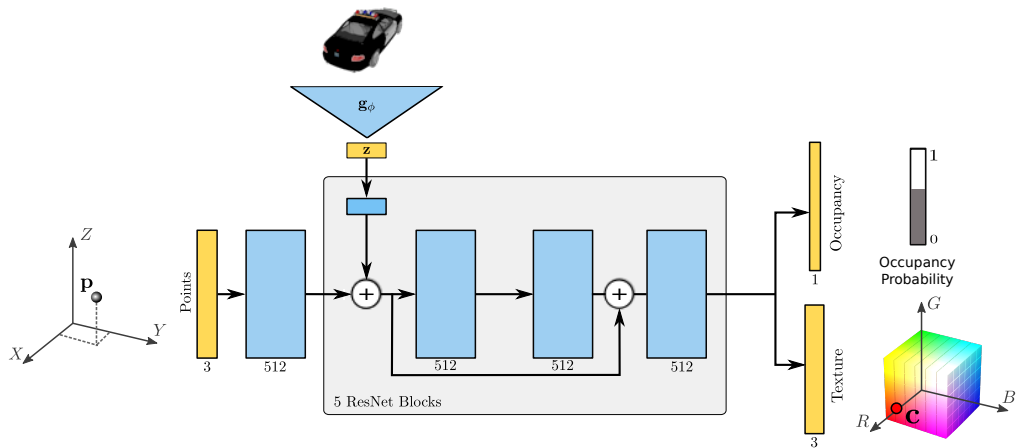


# Differentiable Volumetric Rendering: Learning Implicit 3D Representations without 3D Supervision

[Niemeyer, Mescheder, Oechsle & Geiger, In Review]



# Architecture



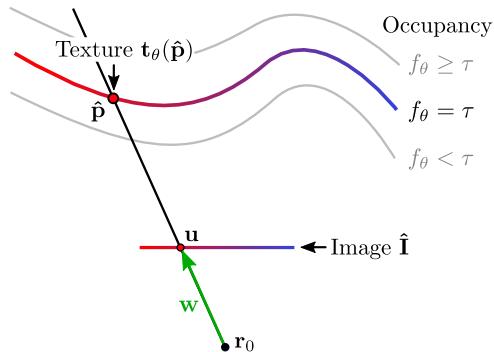
# Forward Pass

(Rendering)

# Differentiable Volumetric Rendering

## Forward Pass:

- For all pixels  $\mathbf{u}$
- Find surface point  $\hat{\mathbf{p}}$  along ray  $\mathbf{w}$  via ray marching and root finding
- Evaluate texture field  $\mathbf{t}_\theta(\hat{\mathbf{p}})$  at  $\hat{\mathbf{p}}$
- Insert color  $\mathbf{t}_\theta(\hat{\mathbf{p}})$  at pixel  $\mathbf{u}$



# Backward Pass

(Differentiation)

# Differentiable Volumetric Rendering

## Backward Pass:

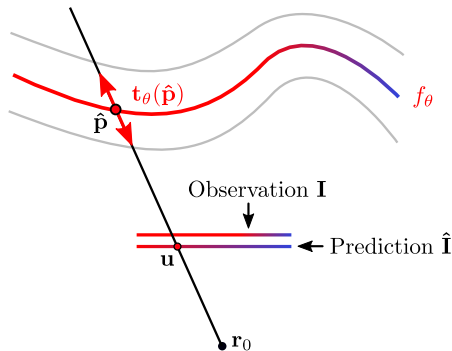
- Image Observation  $\mathbf{I}$
- Loss  $\mathcal{L}(\hat{\mathbf{I}}, \mathbf{I}) = \sum_{\mathbf{u}} \|\hat{\mathbf{I}}_{\mathbf{u}} - \mathbf{I}_{\mathbf{u}}\|$
- Gradient of loss function:

$$\frac{\partial \mathcal{L}}{\partial \theta} = \sum_{\mathbf{u}} \frac{\partial \mathcal{L}}{\partial \hat{\mathbf{I}}_{\mathbf{u}}} \cdot \frac{\partial \hat{\mathbf{I}}_{\mathbf{u}}}{\partial \theta}$$

$$\frac{\partial \hat{\mathbf{I}}_{\mathbf{u}}}{\partial \theta} = \frac{\partial \mathbf{t}_{\theta}(\hat{\mathbf{p}})}{\partial \theta} + \frac{\partial \mathbf{t}_{\theta}(\hat{\mathbf{p}})}{\partial \hat{\mathbf{p}}} \cdot \frac{\partial \hat{\mathbf{p}}}{\partial \theta}$$

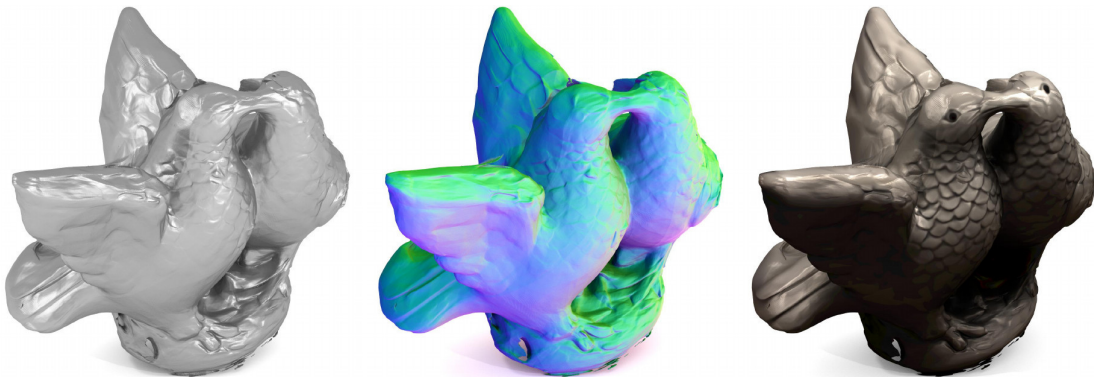
- Differentiation of  $f_{\theta}(\hat{\mathbf{p}}) = \tau$  yields:

$$\frac{\partial \hat{\mathbf{p}}}{\partial \theta} = -\mathbf{w} \left( \frac{\partial f_{\theta}(\hat{\mathbf{p}})}{\partial \hat{\mathbf{p}}} \cdot \mathbf{w} \right)^{-1} \frac{\partial f_{\theta}(\hat{\mathbf{p}})}{\partial \theta}$$



⇒ **Analytic solution** and **no need** for storing **intermediate results**

# Results





# Thank you!

<http://autonomousvision.github.io>



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