DDT Math Write Up

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$$\frac{dT_{h}}{dt} = -\frac{\dot{Q}_{h}}{m_{h}C_{ph}} + \frac{V^{2}R_{h}}{R_{sys}^{2}}$$

$$\frac{dT_{a1}}{dt} = \frac{\dot{Q}_{h}}{2m_{a1}C_{pc}} - \frac{\dot{m}}{m_{a1}}T_{a1} + \frac{\dot{m}}{m_{a1}}T_{a4}$$

$$\frac{dT_{a1}}{dt} = \frac{\dot{Q}_{h}}{2m_{a2}C_{pc}} - \frac{\dot{m}}{m_{a2}}T_{a2} + \frac{\dot{m}}{m_{a2}}T_{a1}$$

$$\frac{dT_{a1}}{dt} = -\frac{\dot{Q}_{ab}}{2m_{a3}C_{pc}} - \frac{\dot{m}}{m_{a3}}T_{a3} + \frac{\dot{m}}{m_{a3}}T_{a2}$$

$$\frac{dT_{a1}}{dt} = -\frac{\dot{Q}_{ab}}{2m_{a4}C_{pc}} - \frac{\dot{m}}{m_{a4}}T_{a4} + \frac{\dot{m}}{m_{b1}}T_{b4}$$

$$\frac{dT_{a1}}{dt} = \frac{\dot{Q}_{ab}}{2m_{b1}C_{pc}} - \frac{\dot{m}}{m_{b1}}T_{b1} + \frac{\dot{m}}{m_{b1}}T_{b4}$$

$$\frac{dT_{a1}}{dt} = \frac{\dot{Q}_{ab}}{2m_{b2}C_{pc}} - \frac{\dot{m}}{m_{b2}}T_{b2} + \frac{\dot{m}}{m_{b2}}T_{b1}$$

$$\frac{dT_{a1}}{dt} = -\frac{\dot{Q}_{bc}}{2m_{b3}C_{pc}} - \frac{\dot{m}}{m_{b3}}T_{b3} + \frac{\dot{m}}{m_{b3}}T_{b2}$$

$$\frac{dT_{a1}}{dt} = -\frac{\dot{Q}_{bc}}{2m_{b4}C_{pc}} - \frac{\dot{m}}{m_{b4}}T_{b4} + \frac{\dot{m}}{m_{b4}}T_{b3}$$

$$\frac{dT_{a1}}{dt} = \frac{\dot{Q}_{bc}}{2m_{c1}C_{pc}} - \frac{\dot{m}}{m_{c1}}T_{c1} + \frac{\dot{m}}{m_{c1}}T_{in}$$

$$\frac{dT_{a1}}{dt} = \frac{\dot{Q}_{bc}}{2m_{c2}C_{pc}} - \frac{\dot{m}}{m_{c2}}T_{c2} + \frac{\dot{m}}{m_{c2}}T_{c1}$$

$$\dot{Q}_h = -h_h A_h l_H \frac{(T_{a1} - T_{a2})}{ln(\frac{T_h - T_{a1}}{T_h - T_{a2}})}$$

$$\dot{Q_{ab}} = -h_{ab}\pi d_{ab}l_{ab}\frac{(T_{a3} - T_{b2}) - (T_{a4} - T_{b1})}{ln(\frac{T_{a3} - T_{b2}}{T_{a4} - T_{b1}})}$$

$$\dot{Q_{bc}} = -h_{bc}\pi d_{bc}l_{bc}\frac{(T_{b3}-T_{c2})-(T_{b4}-T_{c1})}{ln(\frac{T_{b3}-T_{c2}}{T_{b4}-T_{c1}})}$$