

Question 5) Charlotte's test

Let use bit notation ie True = 1, False = 0.

∴ There are exactly three trues among five consecutive questions.

∴ 3 1's and 2 0's. XORing all gives 1.

∴ 5 consecutive bits:  $\boxed{1} \boxed{2} \boxed{3} \boxed{4} \boxed{5}$  XOR<sub>1</sub> = 1 (Given)

∴ Next 5 consecutive bit:  $\boxed{2} \boxed{3} \boxed{4} \boxed{5} \boxed{6}$

$$\begin{aligned}\therefore \text{XOR}_2 &= \text{XOR}_1 \oplus \boxed{1} \oplus \boxed{6} \\ &= 1 \text{ (Given)}\end{aligned}$$

$$\therefore \text{As XOR}_1 = 1, 1 \oplus \boxed{1} \oplus \boxed{6} = 1$$

$$\begin{aligned}\therefore \boxed{1} \oplus \boxed{6} &= 1 \oplus 1 \\ &= 0\end{aligned}$$

∴ After every four questions, the answer repeats.

∴ As 1<sup>st</sup> is ~~true~~<sub>false</sub>, 6<sup>th</sup>, 11<sup>th</sup>, ... 96<sup>th</sup> are ~~true~~<sub>false</sub>.

∴ As 100<sup>th</sup> is ~~true~~<sub>false</sub>, 95<sup>th</sup>, 90<sup>th</sup>, ... 5<sup>th</sup> are ~~true~~<sub>false</sub>.

∴ As 1<sup>st</sup> and 5<sup>th</sup> are ~~true~~<sub>false</sub>, 2<sup>nd</sup>, 3<sup>rd</sup> and 4<sup>th</sup> must be true.

∴ The sequence of answer is: FTTTFFTTTF... TTF

∴ a) 6<sup>th</sup> question answer is false

b) There are total 60 ~~true~~ answers. Questions with answer true.

c) By following sequence Charlotte can score 100.