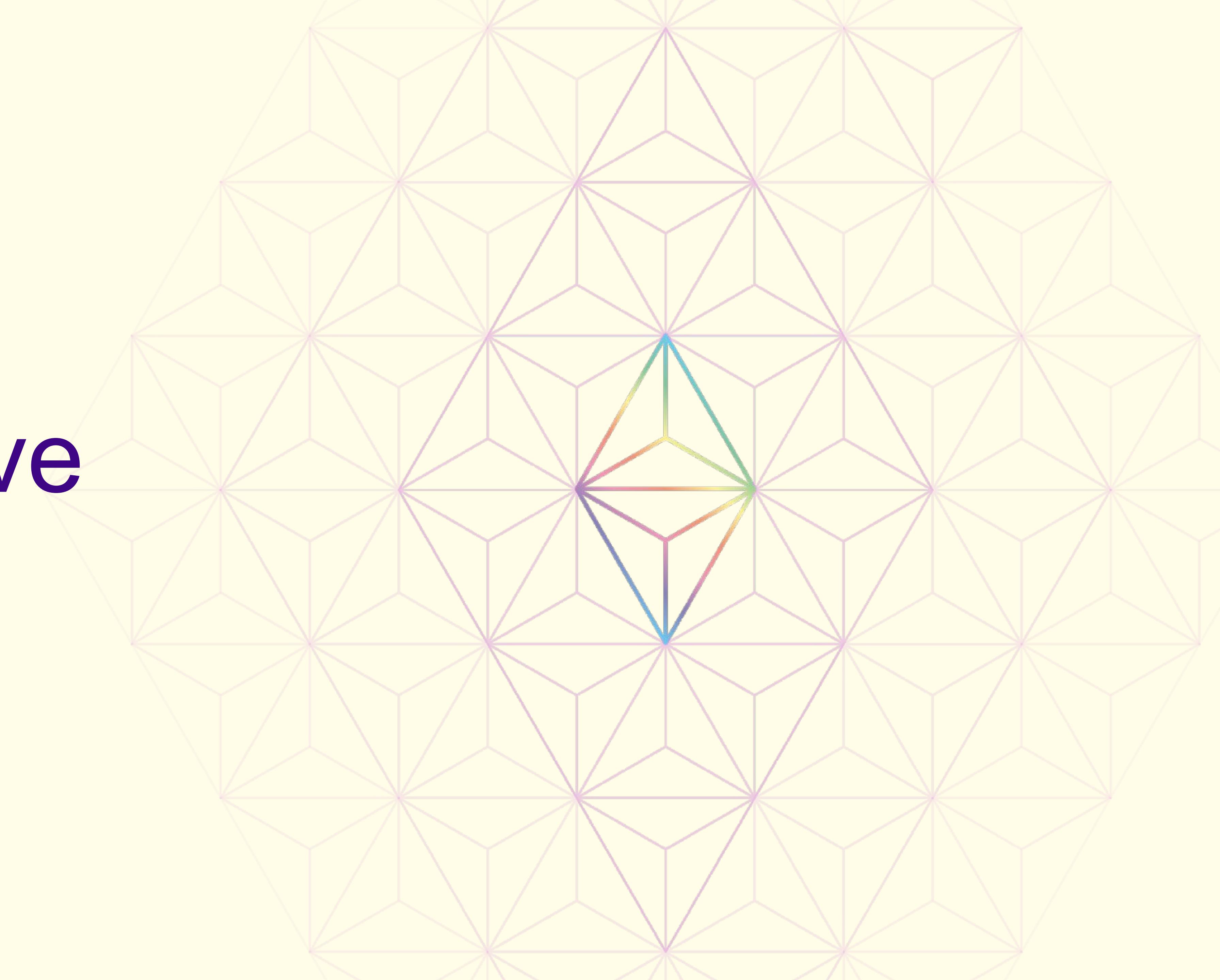
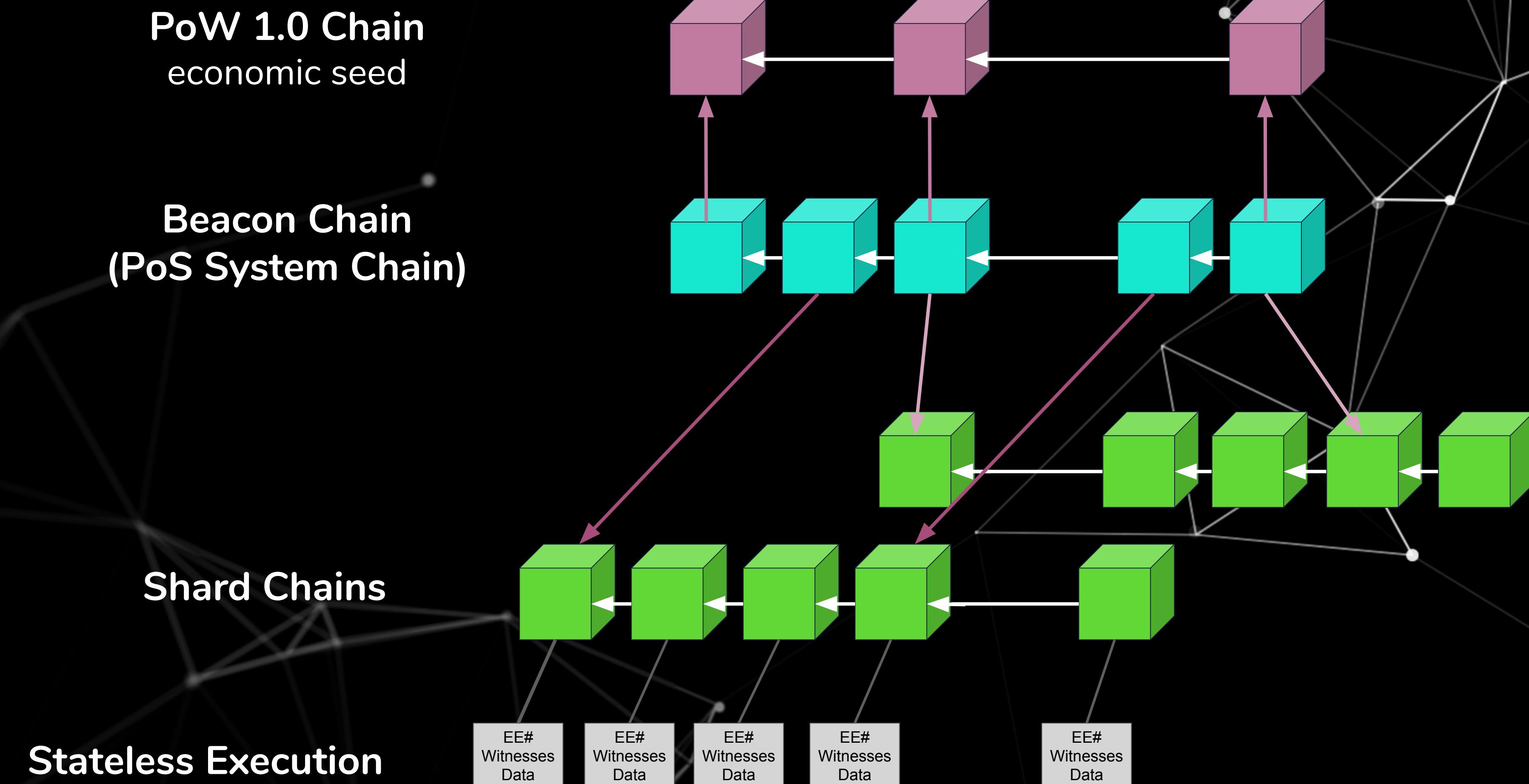


# Phase 0 Deep Dive

EF Research Team

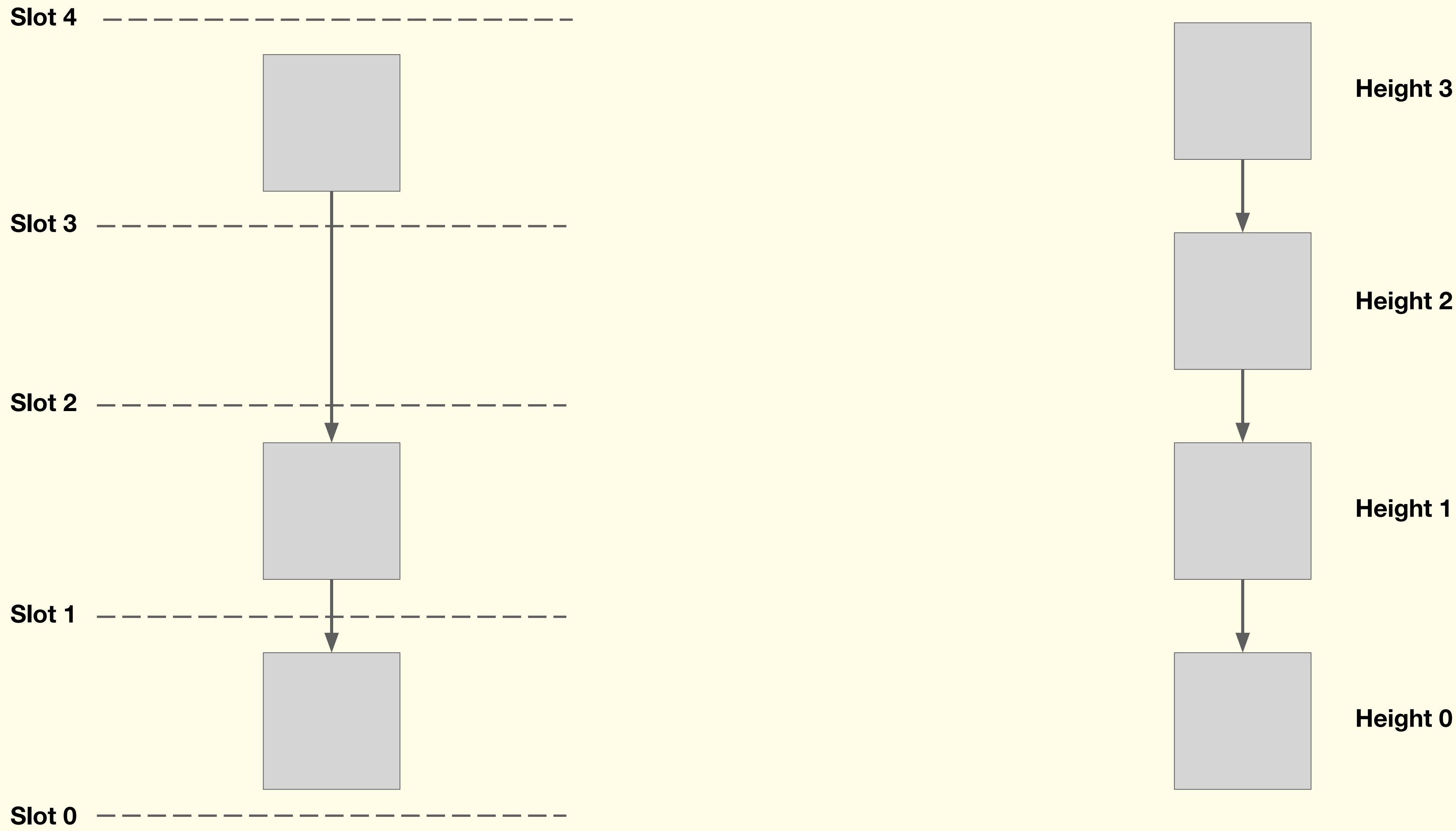




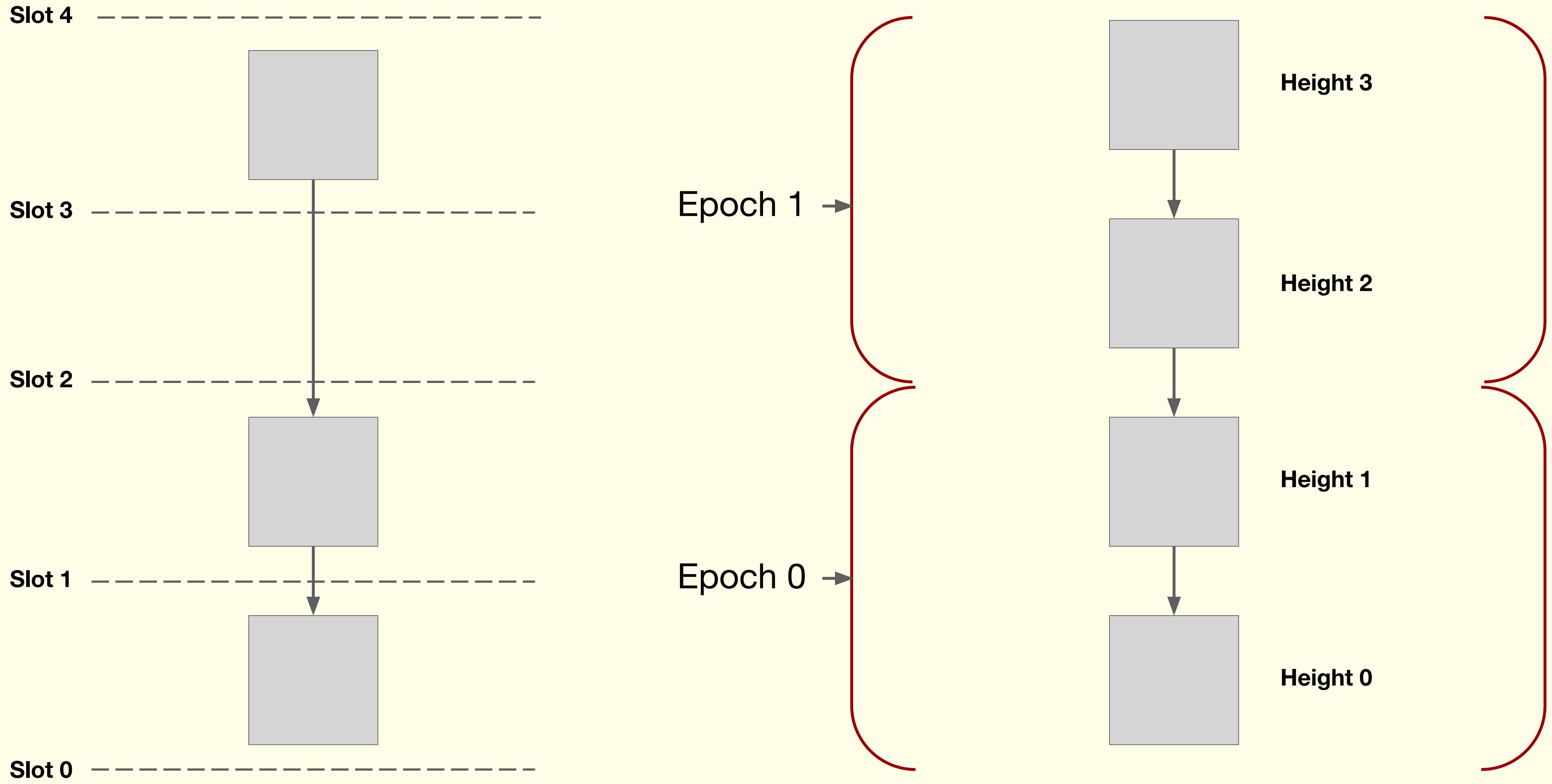


FFG applied to PoS

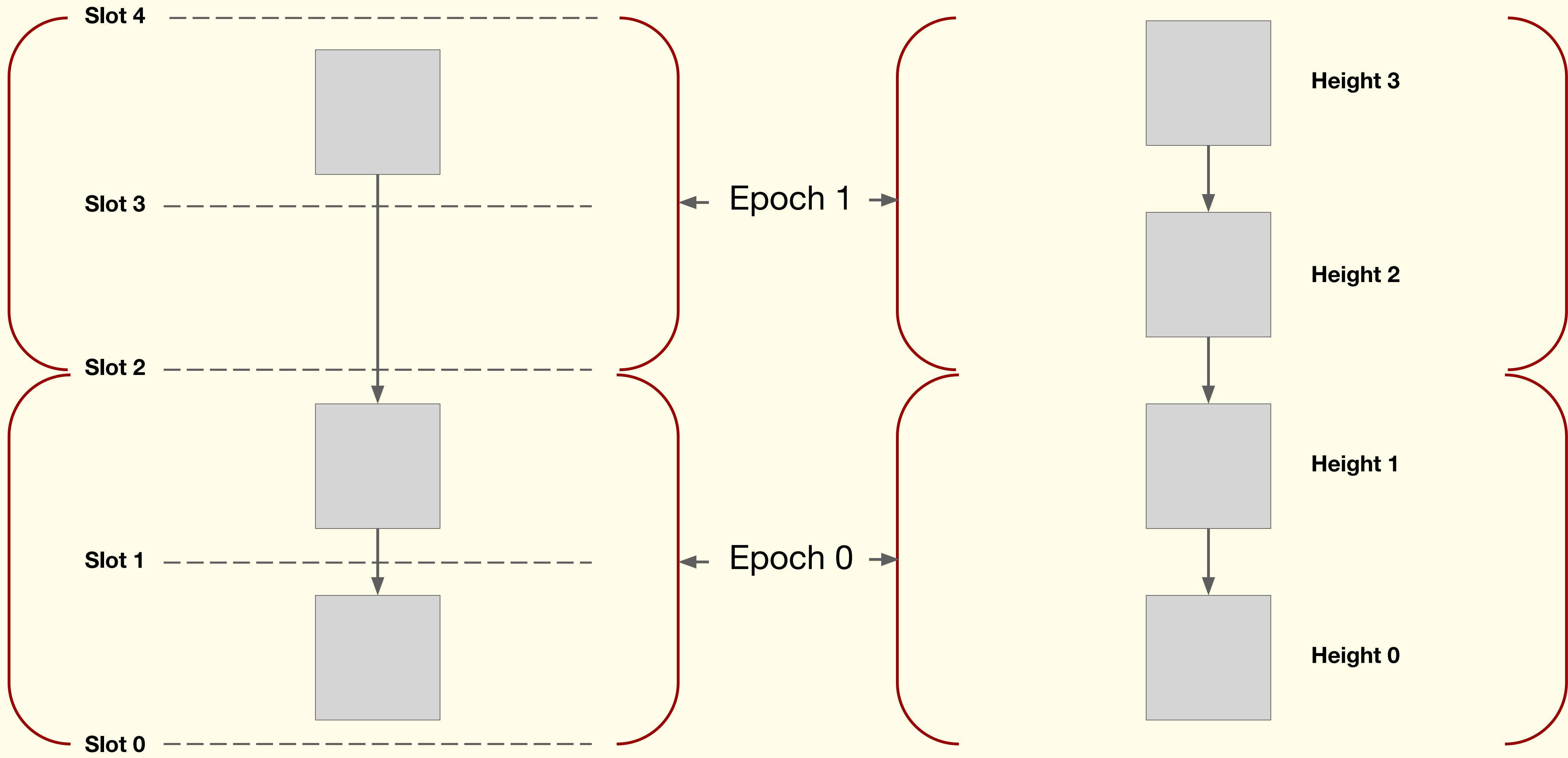
# Slots vs Blockheight



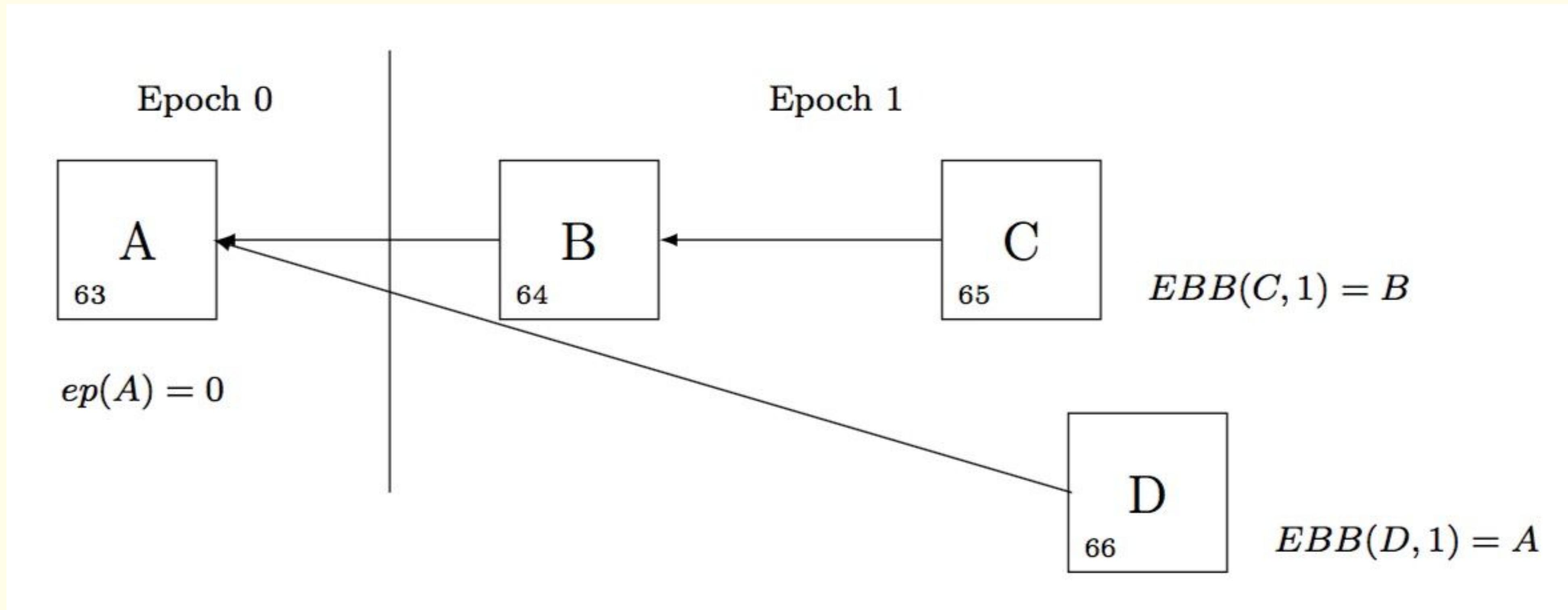
# Slots vs Blockheight



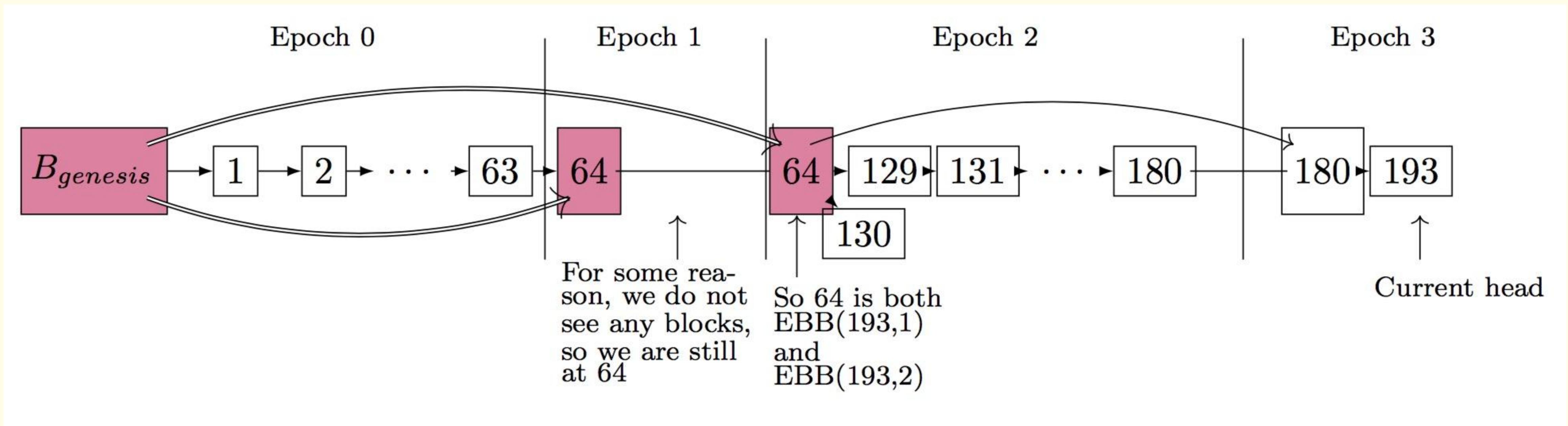
# Slots vs Blockheight



# Checkpoints



# (Block, Epoch) -- Paired Justification



# Justification Rules

**Definition 4.2.** We say that there is a *supermajority link* from pair  $(A, j')$  to pair  $(B, j)$  if the attestations with checkpoint edge  $(A, j') \xrightarrow{v} (B, j)$  have total stake more than  $\frac{2N}{3}$ . In this case, we write  $(A, j') \xrightarrow{j} (B, j)$ .

Given a view  $G$ , a block  $B$ , and an epoch  $j$ , we say that the pair  $(B, j)$  is *justified in  $G$* , or equivalently that  $B$  is justified in  $G$  during epoch  $j$ , if:

- $B = B_{\text{genesis}}, j = 0$ ; or
- for some justified pair  $(A, j')$ ,  $(A, j') \xrightarrow{j} (B, j)$ .

We use  $J(G)$  to denote the set of justified pairs in  $G$ .

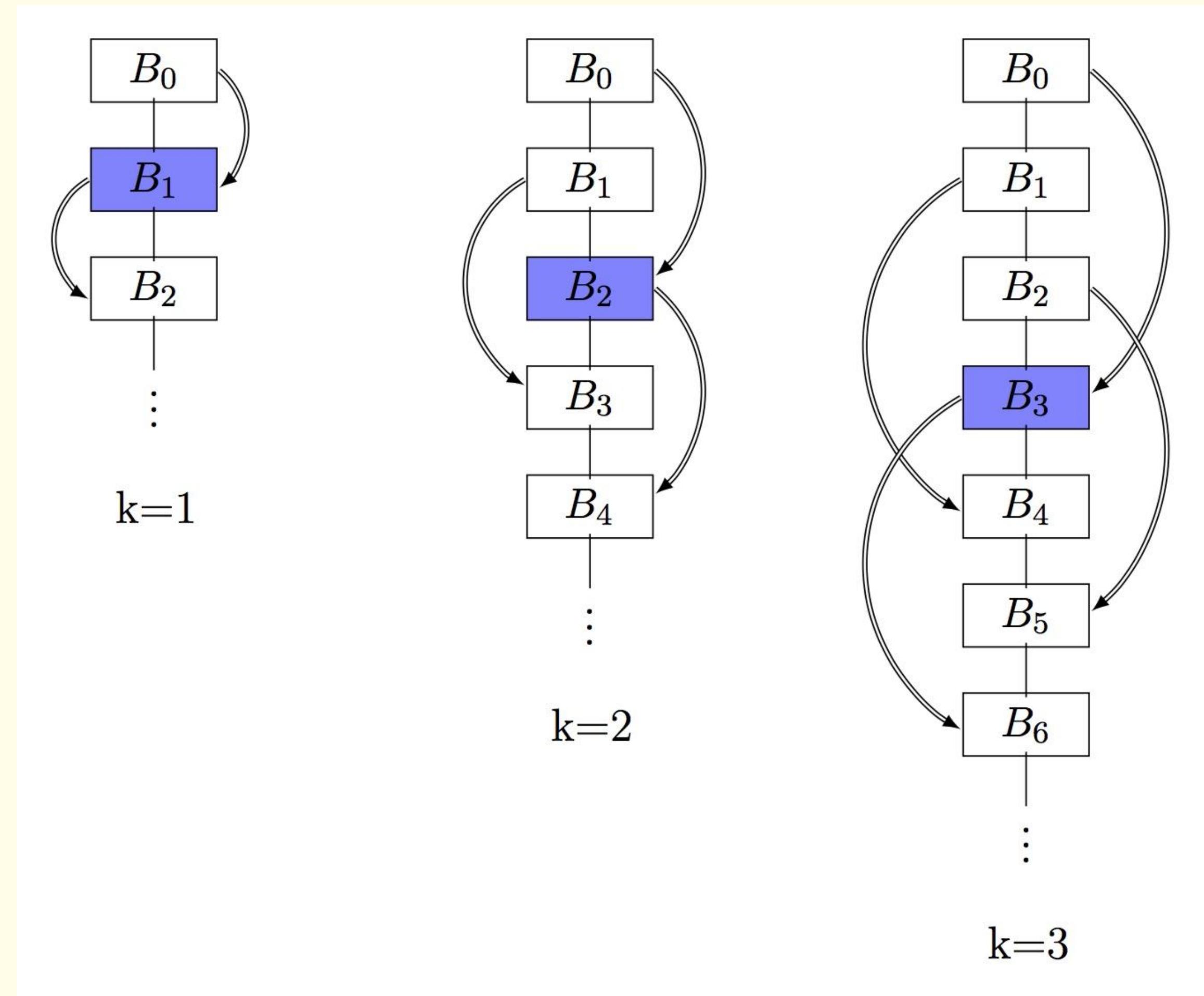
## Finalization Rules

**Definition 4.4.** For a view  $G$ , we say that  $(B_0, j)$  is *finalized*<sup>6</sup> if there is an integer  $k \geq 1$  and blocks  $B_1, \dots, B_k$  such that:

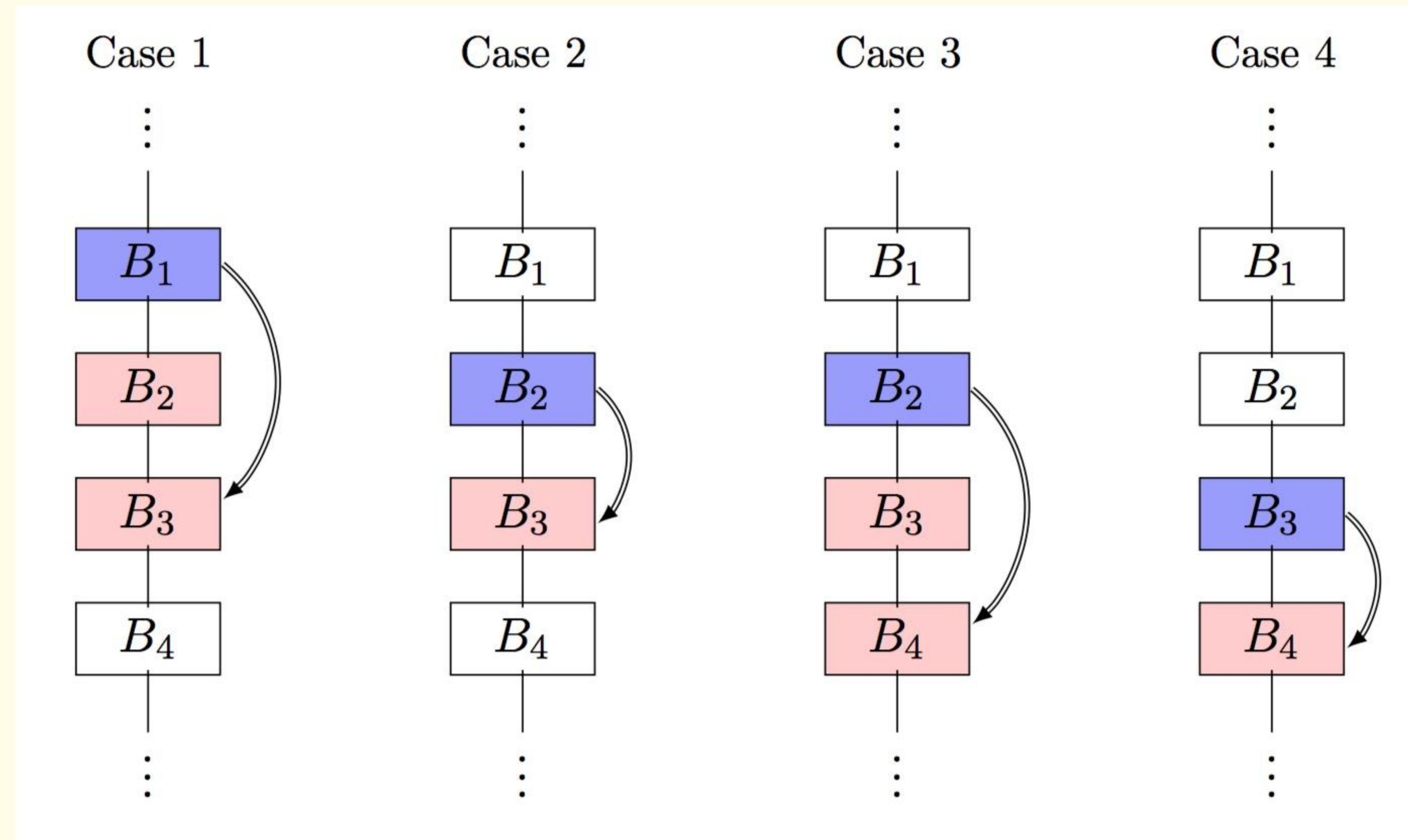
- $(B_0, j), (B_1, j+1), \dots, (B_k, j+k)$  are adjacent epoch boundary pairs in  $\text{chain}(B_k)$ ;
- $(B_0, j), (B_1, j+1), \dots, (B_k, j+k)$  are all in  $J(G)$ ;
- $(B_0, j) \xrightarrow{\downarrow} (B_k, j+k)$ .

We define  $F(G)$  to be the set of finalized pairs in the view  $G$ ; we also say that a block  $B$  is *finalized* if  $(B, j) \in F(G)$  for any epoch  $j$ .

# k-finality rule



# finality cases in eth2 (k=2)



# Finality related fields in state

## BeaconState

```
class BeaconState(Container):
    ...
    ...
    # Finality
    justification_bits: Bitvector[JUSTIFICATION_BITS_LENGTH] # Bit set for every recent justified epoch
    previous_justified_checkpoint: Checkpoint # Previous epoch snapshot
    current_justified_checkpoint: Checkpoint
    finalized_checkpoint: Checkpoint
```

---

## Checkpoint

```
class Checkpoint(Container):
    epoch: Epoch
    root: Hash
```

```
def process_justification_and_finalization(state: BeaconState) -> None:
    if get_current_epoch(state) <= GENESIS_EPOCH + 1:
        return

    previous_epoch = get_previous_epoch(state)
    current_epoch = get_current_epoch(state)
    old_previous_justified_checkpoint = state.previous_justified_checkpoint
    old_current_justified_checkpoint = state.current_justified_checkpoint

    # Process justifications
    state.previous_justified_checkpoint = state.current_justified_checkpoint
    state.justification_bits[1:] = state.justification_bits[:-1]
    state.justification_bits[0] = 0b0
    matching_target_attestations = get_matching_target_attestations(state, previous_epoch) # Previous epoch
    if get_attesting_balance(state, matching_target_attestations) * 3 >= get_total_active_balance(state):
        state.current_justified_checkpoint = Checkpoint(epoch=previous_epoch,
                                                       root=get_block_root(state, previous_epoch))

        state.justification_bits[1] = 0b1
        matching_target_attestations = get_matching_target_attestations(state, current_epoch) # Current epoch
        if get_attesting_balance(state, matching_target_attestations) * 3 >= get_total_active_balance(state):
            state.current_justified_checkpoint = Checkpoint(epoch=current_epoch,
                                                               root=get_block_root(state, current_epoch))
            state.justification_bits[0] = 0b1

    # Process finalizations
    bits = state.justification_bits
    # The 2nd/3rd/4th most recent epochs are justified, the 2nd using the 4th as source
    if all(bits[1:4]) and old_previous_justified_checkpoint.epoch + 3 == current_epoch:
        state.finalized_checkpoint = old_previous_justified_checkpoint
    # The 2nd/3rd most recent epochs are justified, the 2nd using the 3rd as source
    if all(bits[1:3]) and old_previous_justified_checkpoint.epoch + 2 == current_epoch:
        state.finalized_checkpoint = old_previous_justified_checkpoint
    # The 1st/2nd/3rd most recent epochs are justified, the 1st using the 3rd as source
    if all(bits[0:3]) and old_current_justified_checkpoint.epoch + 2 == current_epoch:
        state.finalized_checkpoint = old_current_justified_checkpoint
    # The 1st/2nd most recent epochs are justified, the 1st using the 2nd as source
    if all(bits[0:2]) and old_current_justified_checkpoint.epoch + 1 == current_epoch:
        state.finalized_checkpoint = old_current_justified_checkpoint
```

# Slashing Conditions

**Definition 4.5.** We define the following *slashing conditions*:

- (S1) No validator makes two distinct attestations  $\alpha_1, \alpha_2$  with  $\text{aep}(\text{LE}(\alpha_1)) = \text{aep}(\text{LE}(\alpha_2))$ . Note this condition is equivalent to  $\text{ep}(\alpha_1) = \text{ep}(\alpha_2)$ .
- (S2) No validator makes two distinct attestations  $\alpha_1, \alpha_2$  with
$$\text{aep}(\text{LJ}(\alpha_1)) < \text{aep}(\text{LJ}(\alpha_2)) < \text{aep}(\text{LE}(\alpha_2)) < \text{aep}(\text{LE}(\alpha_1)).$$

# Slashing Conditions

## ↳ **is\_slashable\_attestation\_data**

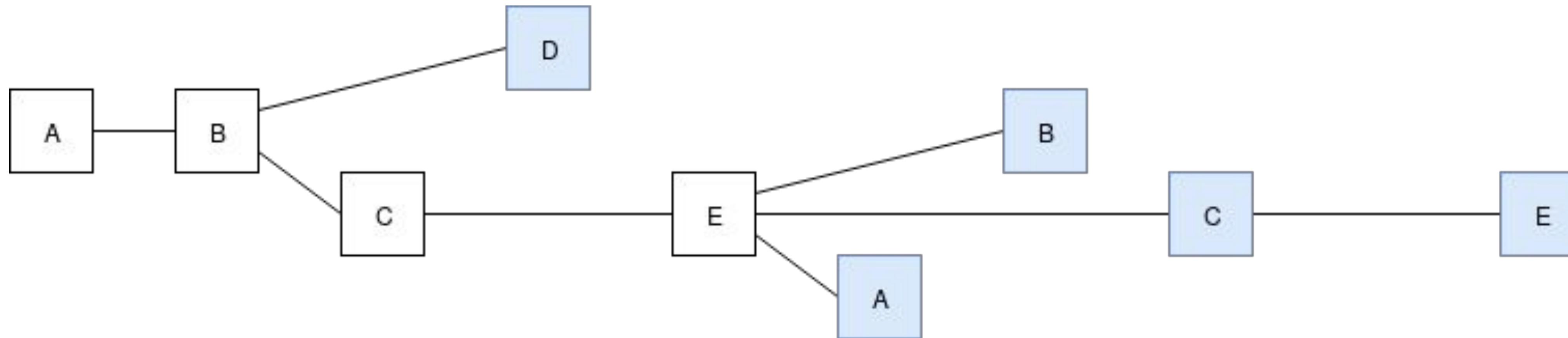
```
def is_slashable_attestation_data(data_1: AttestationData, data_2: AttestationData) -> bool:  
    """  
        Check if ``data_1`` and ``data_2`` are slashable according to Casper FFG rules.  
    """  
  
    return (  
        # Double vote  
        (data_1 != data_2 and data_1.target.epoch == data_2.target.epoch) or  
        # Surround vote  
        (data_1.source.epoch < data_2.source.epoch and data_2.target.epoch < data_1.target.epoch)  
    )
```

## What is LMD GHOST?



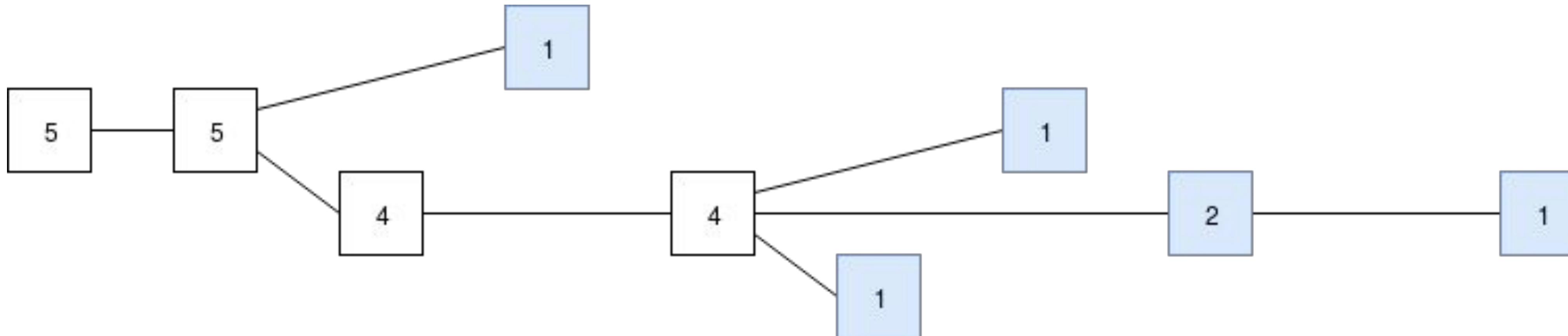
## LMD GHOST fork choice rule

- Adaptation of GHOST (Sompolinsky et al, 2013) to a proof of stake context
- Idea: look only at latest messages of each node as evidence of what chain that node favors
- Assume for now “simple model” where blocks and messages are the same thing

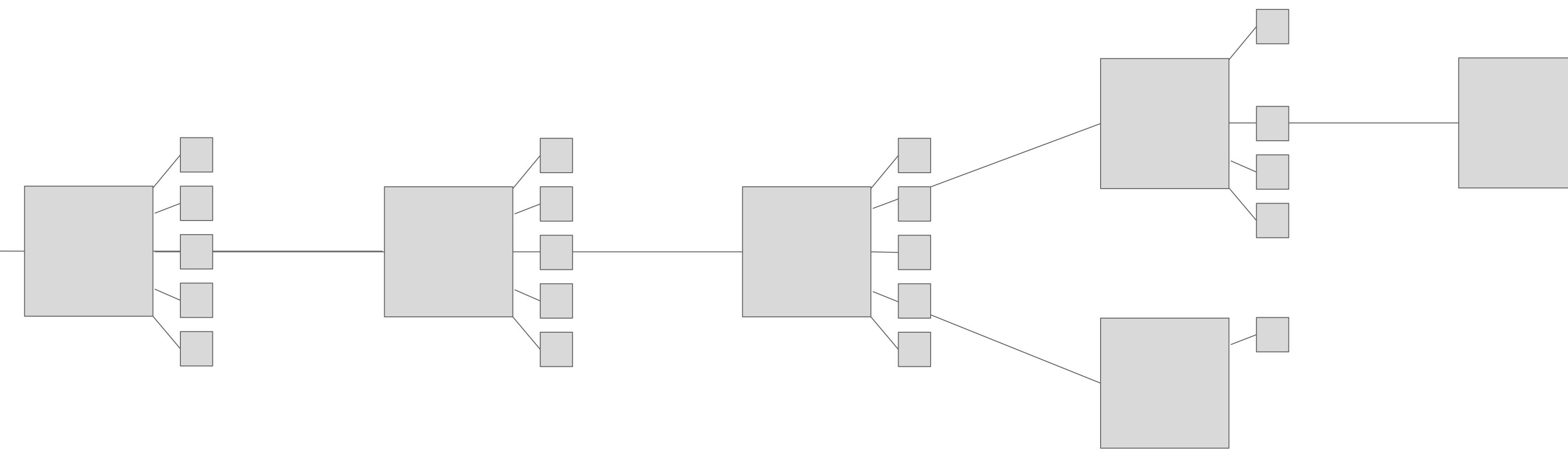


## LMD GHOST fork choice rule

- As in GHOST, start from genesis, walk up the tree, at each branch choose the child that has more latest-messages supporting it (directly or indirectly)

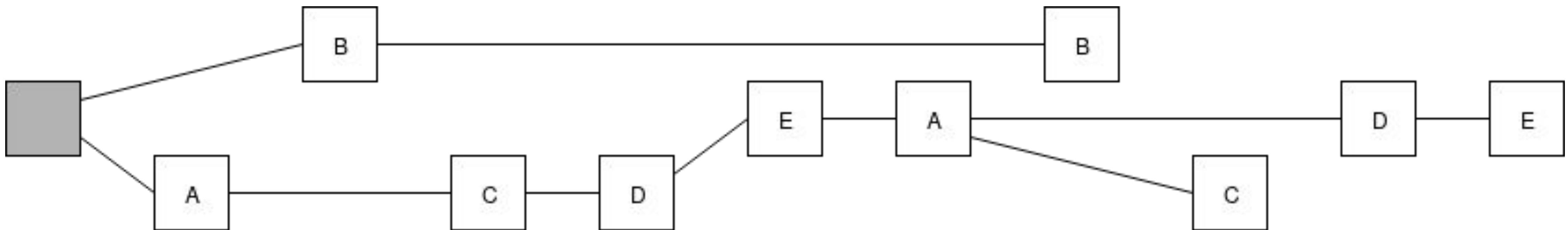


# Why LMD GHOST: Parallel confirmations



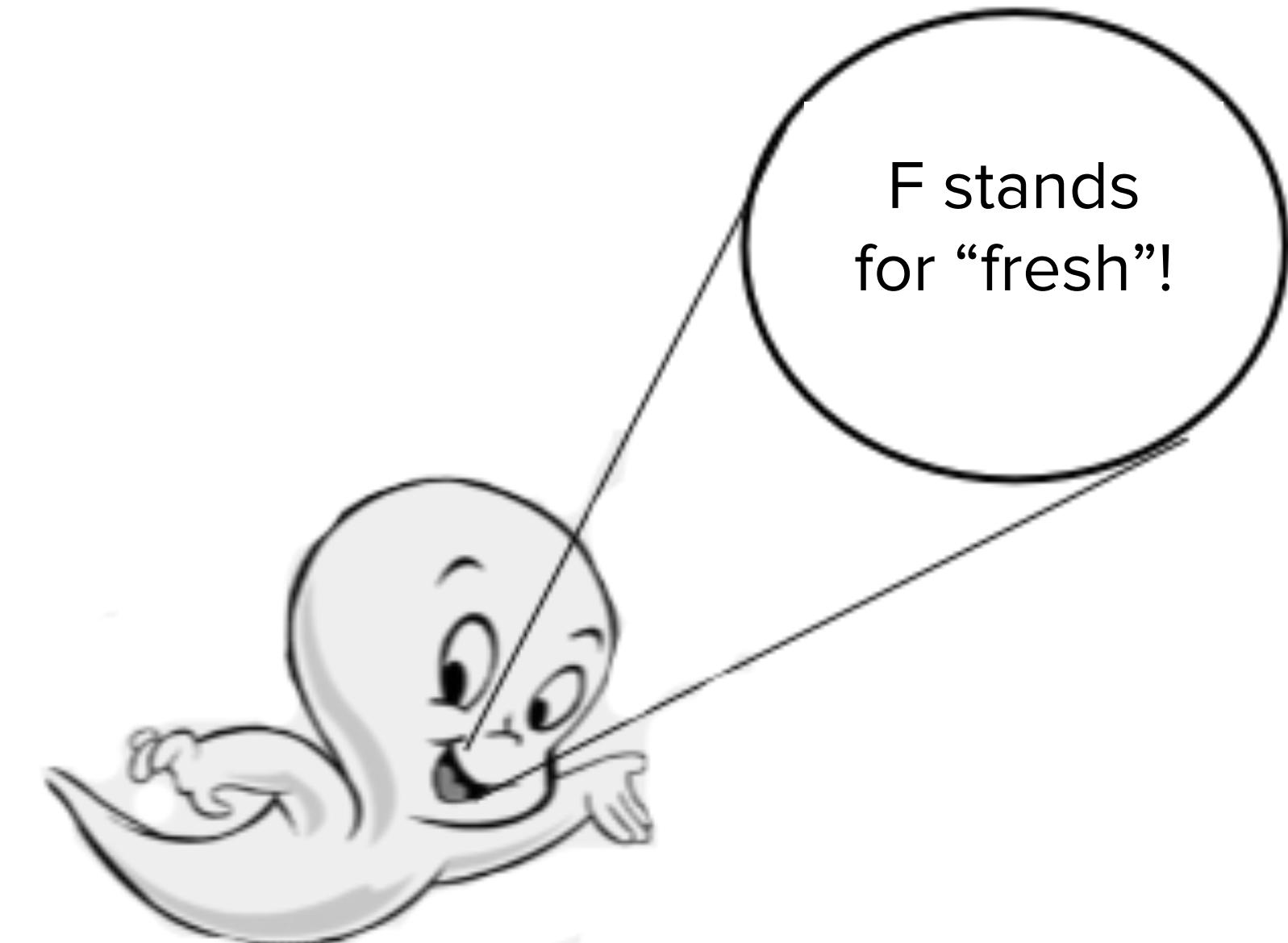
## Why LMD GHOST?

- Longest chain rules cannot take into account info from frequent parallel attestations
- Minority can never “beat” majority, regardless of how many messages they send
- This property is useful for CBC Casper



## Saved message attacks

- A validator can make max one vote per epoch (if more they get slashed)
  - Problem: a validator can not vote for N epochs, then suddenly make N votes all at once
- 
- Worst case: traditional GHOST (can influence fork choice by N)
  - Middle case: LMD GHOST (can influence fork choice by 1 but go back-and-forth N times; can allow some anti-liveness attacks)
  - Best case: FMD GHOST (clients only look at messages tagged with the current or previous epoch; prevents saving more than 1)



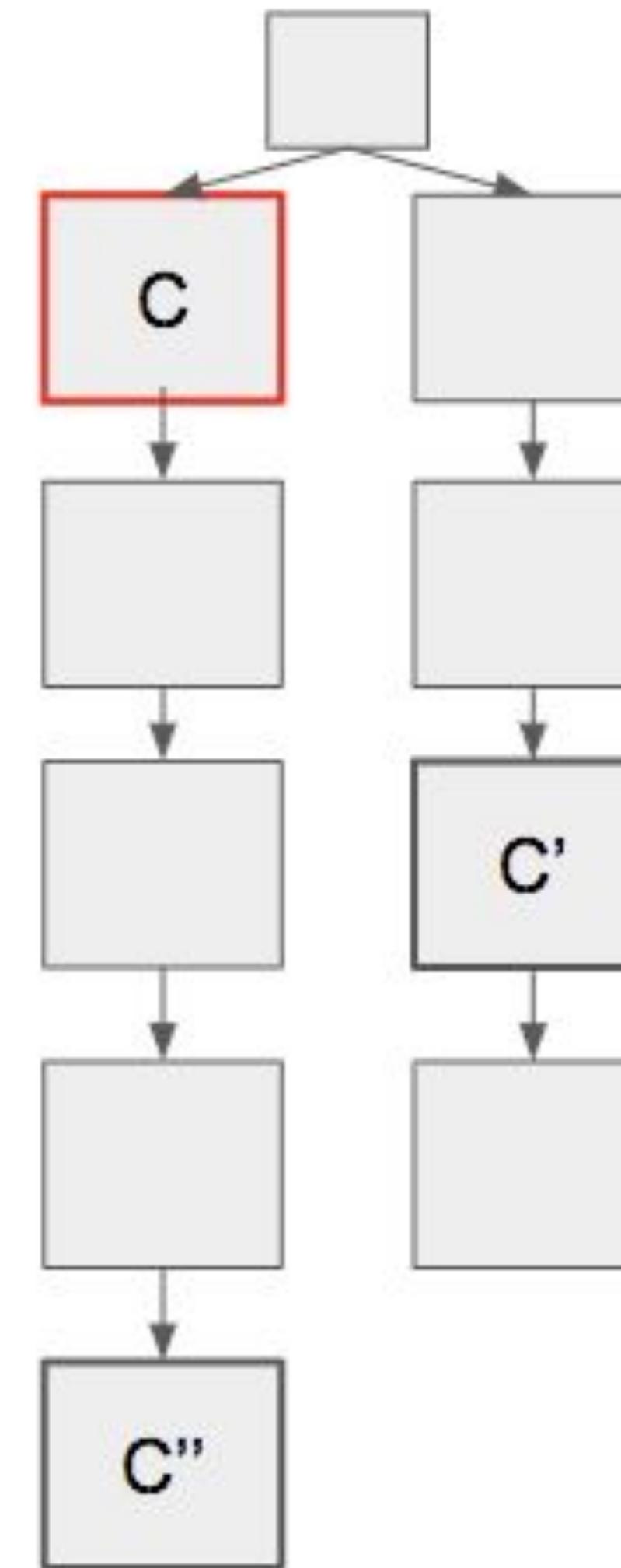
# Interaction between LMD GHOST and FFG

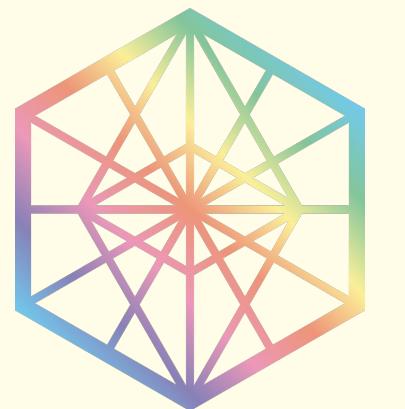
The “real” fork choice rule:

- First select the last finalized block  $B_1$  you were aware of (maybe the genesis)
- Then select the highest-epoch justified block  $B_2$  that is a descendant of  $B_1$
- Then use LMD GHOST starting from  $B_2$  to find the head

# Interaction between LMD GHOST and FFG

- This does open room for some kinds of “bounce” attacks
- General solution: if a client sees a checkpoint that is NOT in the current canonical chain become justified, it delays when it switches chains
  - Idea 1: usually switch only on epoch boundaries (credit Ryuya Nakamura)
  - Idea 2:  $h(B_1) + N$ 'th checkpoint can be used only from height  $h(B_1) + 3N$ ; this ensures that there are periods of 3 epochs in which to finalize a new checkpoint





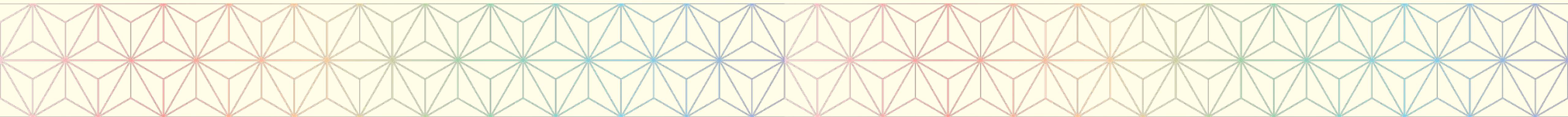
# Randomness in Ethereum 2.0

Dankrad Feist  
Ethereum Foundation (Eth2.0 Research)

# Randomness in Ethereum 2.0

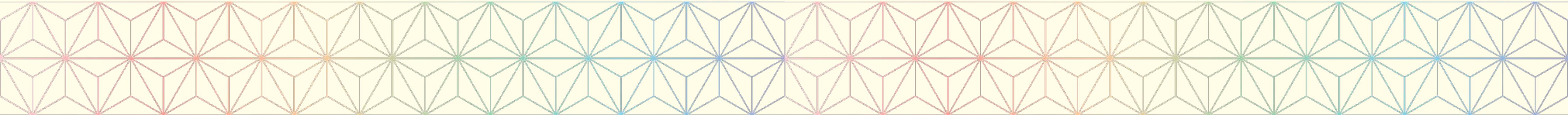
```
int getRandomNumber()
{
    return 4; // chosen by fair dice roll.
              // guaranteed to be random.
}
```

- Why randomness is critical in Proof of Stake
- RANDAO
- RANDAO issues
- Randomness using verifiable delay functions



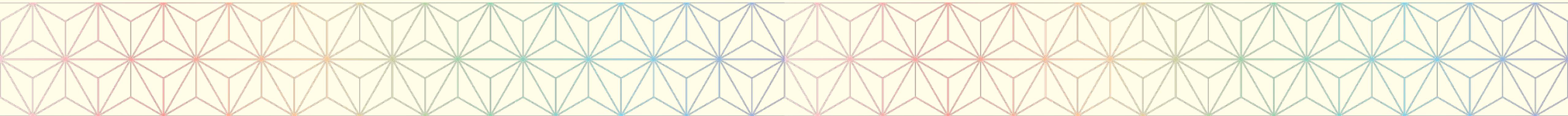
# Randomness in Proof of Stake

- Select proposers
- Select committees
- Provide randomness on-chain



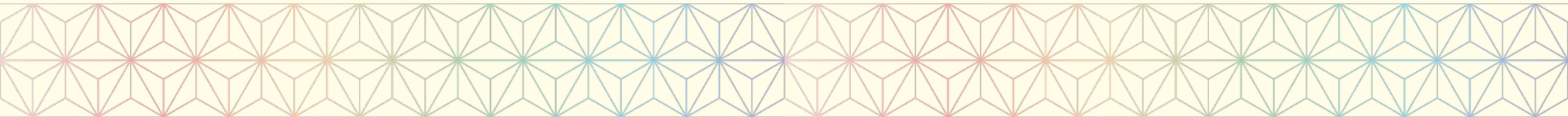
# Why is unpredictable, unbiased randomness required?

- **Select proposers**
  - Fairness
  - Protection against DOS attacks
- **Select committees**
  - Need honest committees or else will suffer from too many fraud proofs
- **Provide randomness on-chain**
  - Applications might attach huge value to random numbers
  - If attacks are possible, this will degrade the randomness for everyone



# Why is unpredictable, unbiased randomness required?

- **Select committees**
  - We want to minimize the probability for dishonest committees
- **Crosslinks** to shards in eth2.0 are made based on crosslink committee votes
  - A bad committee can create a link to an invalid or non-existent block
    - Fraud proof potentially means reverting beacon chain
  - E.g. probability of bad committee of size 128 is  $5 \cdot 10^{-15}$  ( $\frac{2}{3}$  honesty assumption)
    - But what if attacker can bias committee sampling?

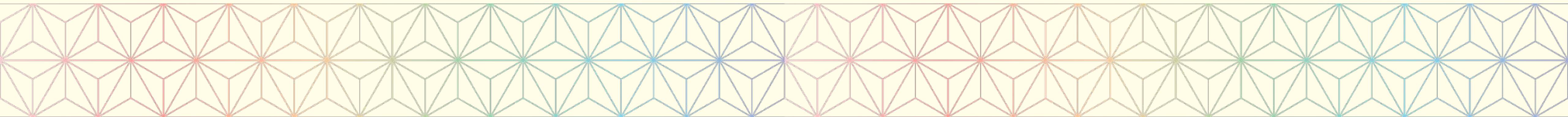


# Idea

n people want to generate a random number

- They all go into a room
- Each person contributes one value  $x_i$
- Compute  $\text{XOR}(x_1, x_2, \dots)$

Problem: The last player can just change their value after having seen the other choices, until they get a favourable output (grinding)



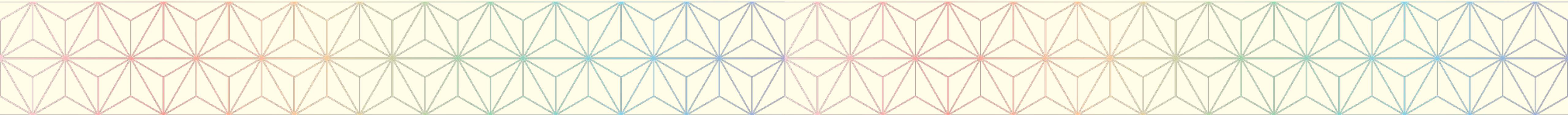
# Commit-reveal — basis for RANDAO

n people want to generate a random number

- They all go into a room
- Each person commits to one value  $x_i$ , commits by telling everyone  $\text{hash}(x_i)$
- Compute  $\text{XOR } (x_1, x_2, \dots)$

Nice! This cannot be manipulated

But: Anyone can stop the process by not revealing their preimage  $x_i$



# RANDAO in practice

e = epoch



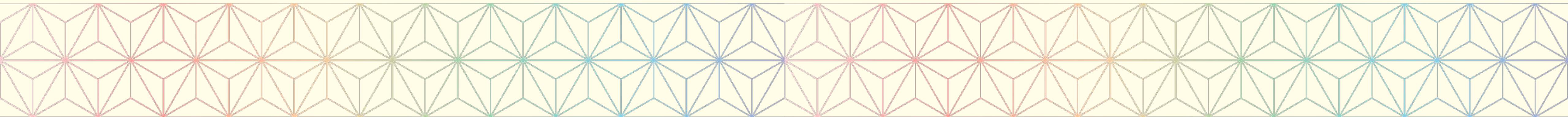
mix = hash (hash (reveal1) XOR hash (reveal2))

XOR hash (reveal3) XOR hash (reveal4)

XOR hash (reveal5) ...

# Problems with RANDAO

- Last revealer can choose to not produce a block
  - “Get another roll if I don’t like the result”
  - If I control validators with several slots in a row, more bias is possible
- A chain that uses RANDAO + Longest chain as fork choice can be completely taken over by an attacker with 36% stake (ethresear.ch analysis by Vitalik)

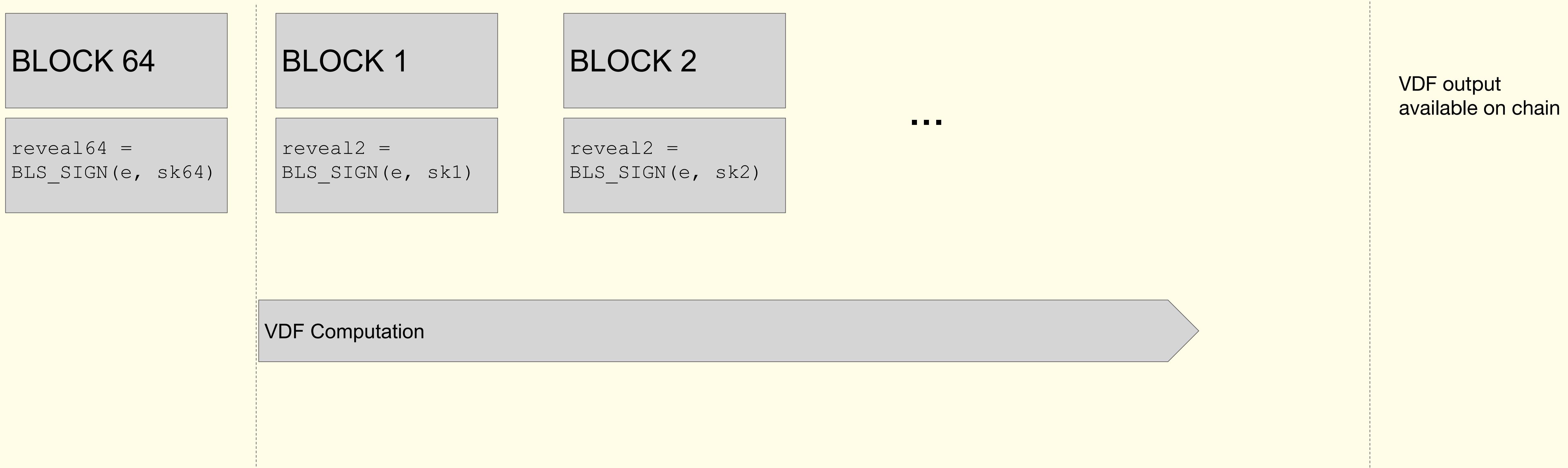


# Outlook: Verifiable delay functions

- . Verifiable delay function (VDF): A function  $y, \pi = f(x)$ , such that
  - . Computing  $f(x)$  takes a long serial time
  - . Checking the result  $y$  using the proof  $\pi$  is fast
- . Example: Computing  $x^{(2^T)} \bmod m$  where  $m = p \cdot q$  is an RSA modulus of unknown factorization

By using the VDF output on RANDAO, the last revealer loses the advantage

# Outlook: Verifiable delay functions



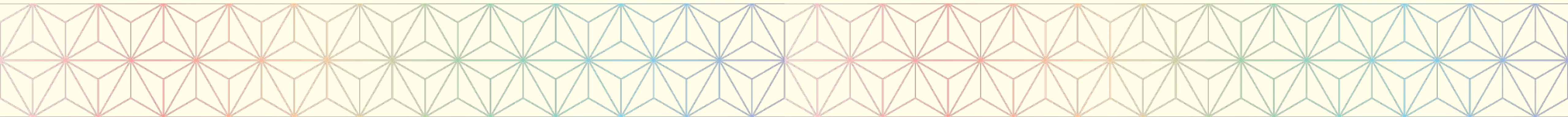
Last revealer has to make decision before being able to know VDF result

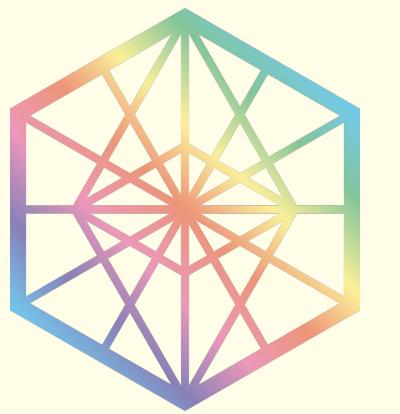
# YOU FOUND A STAR

Speaker Track



**dropparty.tech**

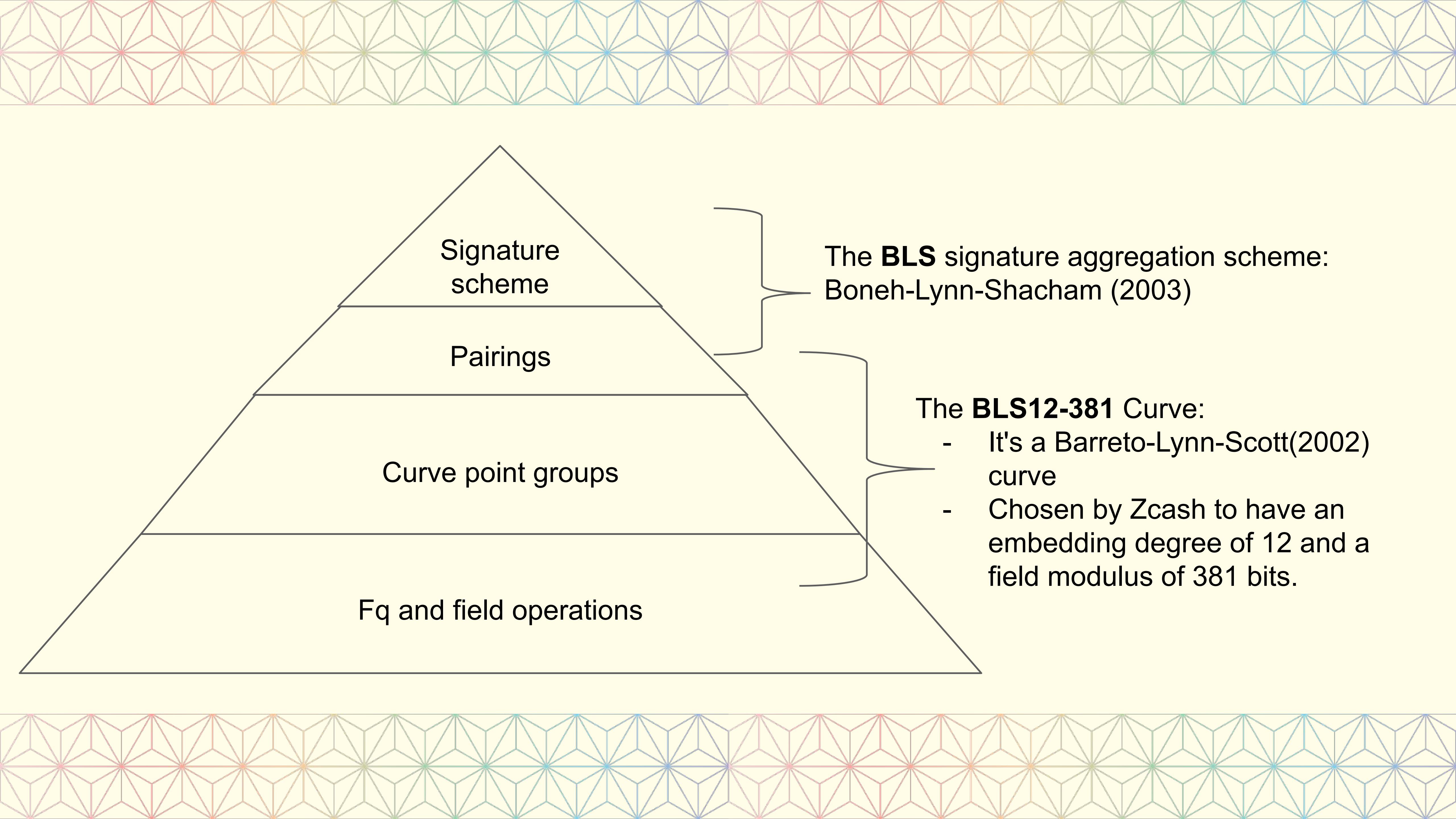




## BLS Signatures and Aggregation

Chih-Cheng Liang





## Operations of Prime Fields

Consider  $F_{13}$ , i.e.  $q=13$

### Addition

$$11 + 12 = 10 \quad \text{mod } 13$$

### Subtraction

$$5 - 7 = 11 \quad \text{mod } 13$$

### Multiplication

$$2 * 8 = 3 \quad \text{mod } 13$$

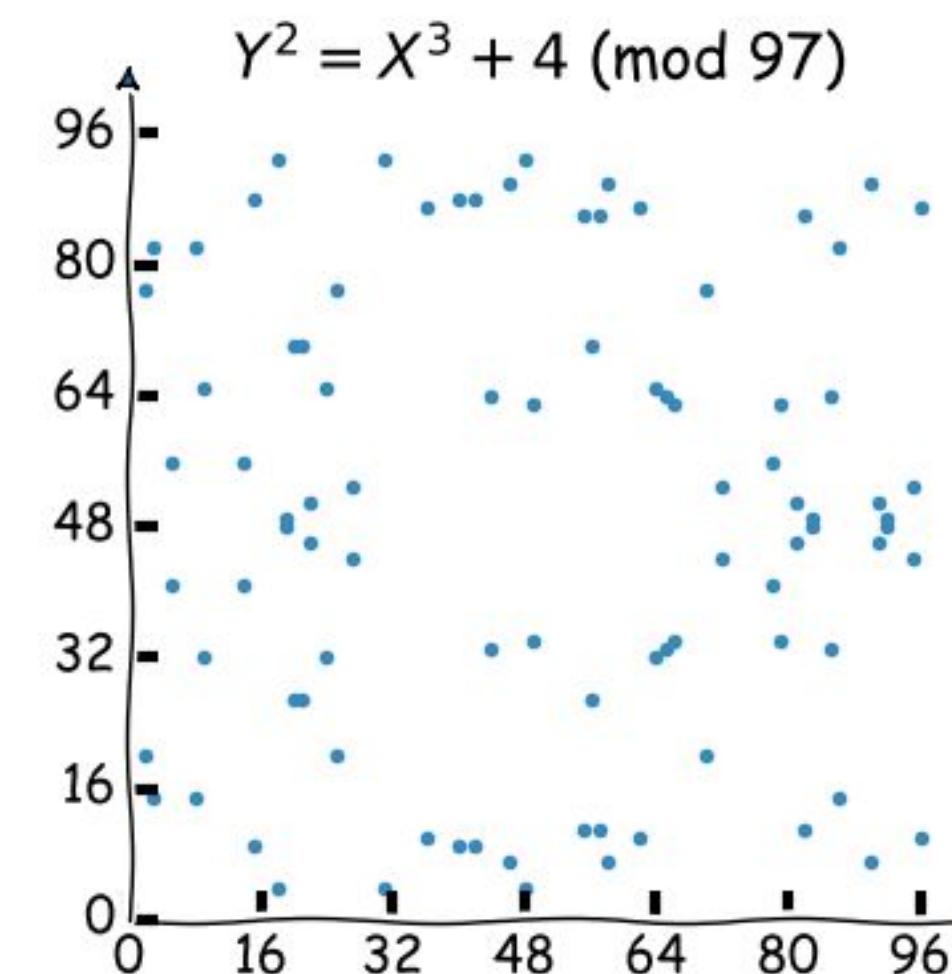
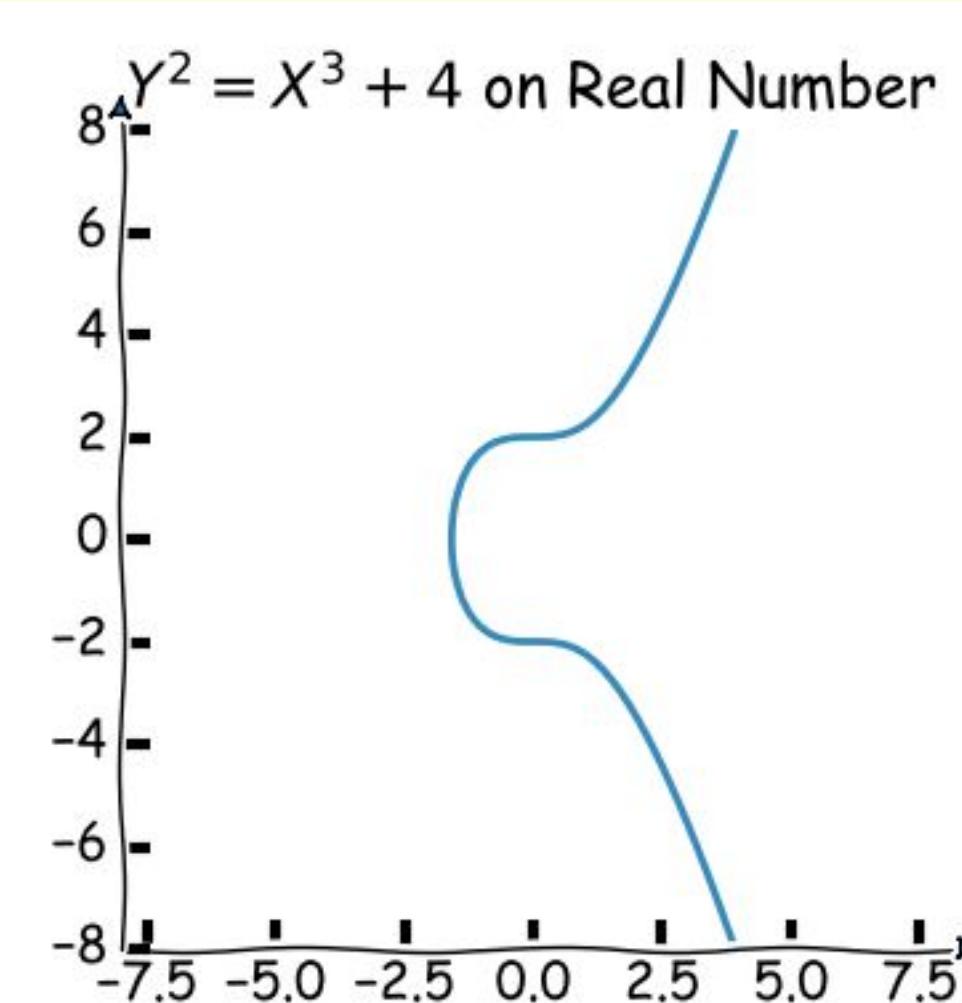
### Division

$$10 / 3 = 10 * (3)^{-1} = 10 * 3^{11} = 12 \quad \text{mod } 13$$

```
>>> from py_ecc.fields.field_elements import FQ
>>> class F13(FQ):
...     field_modulus = 13
...
>>> F13(10) / F13(3)
12
```

A **curve** is an equation of the form:

$$y^2 = x^3 + ax + b$$

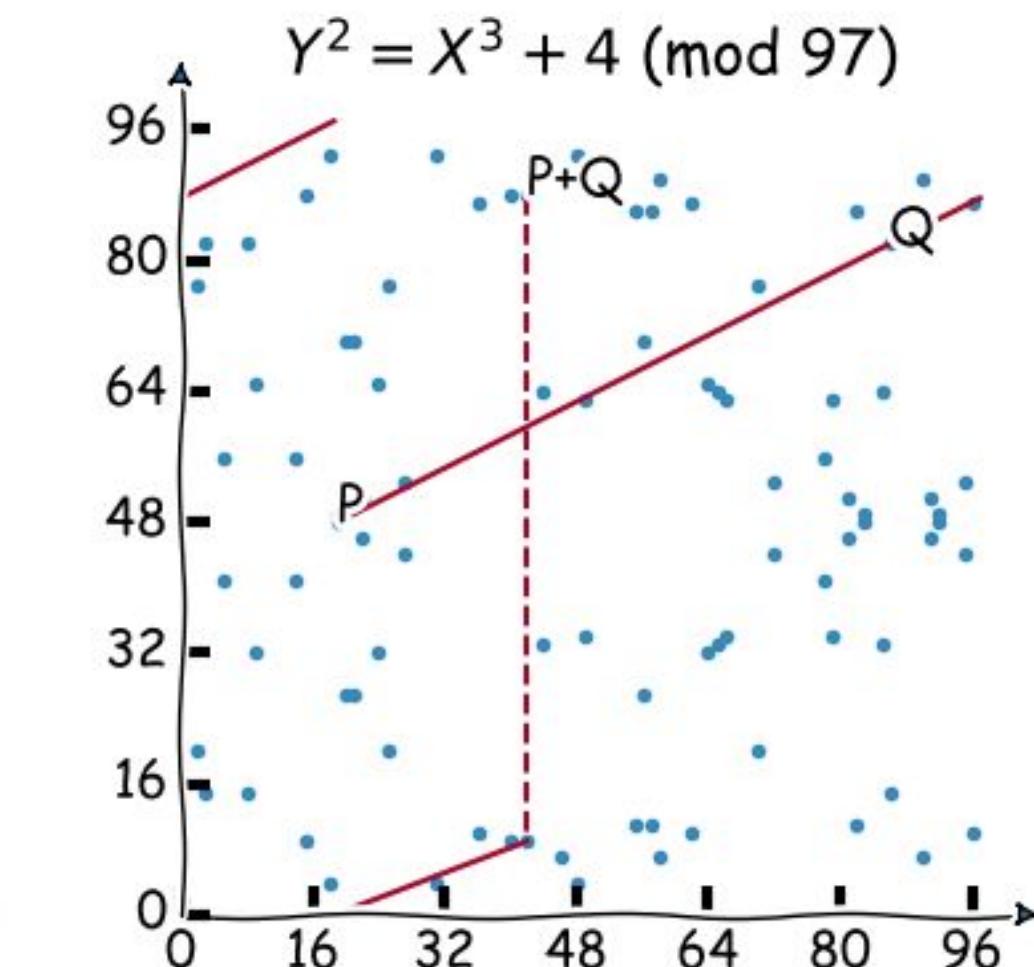
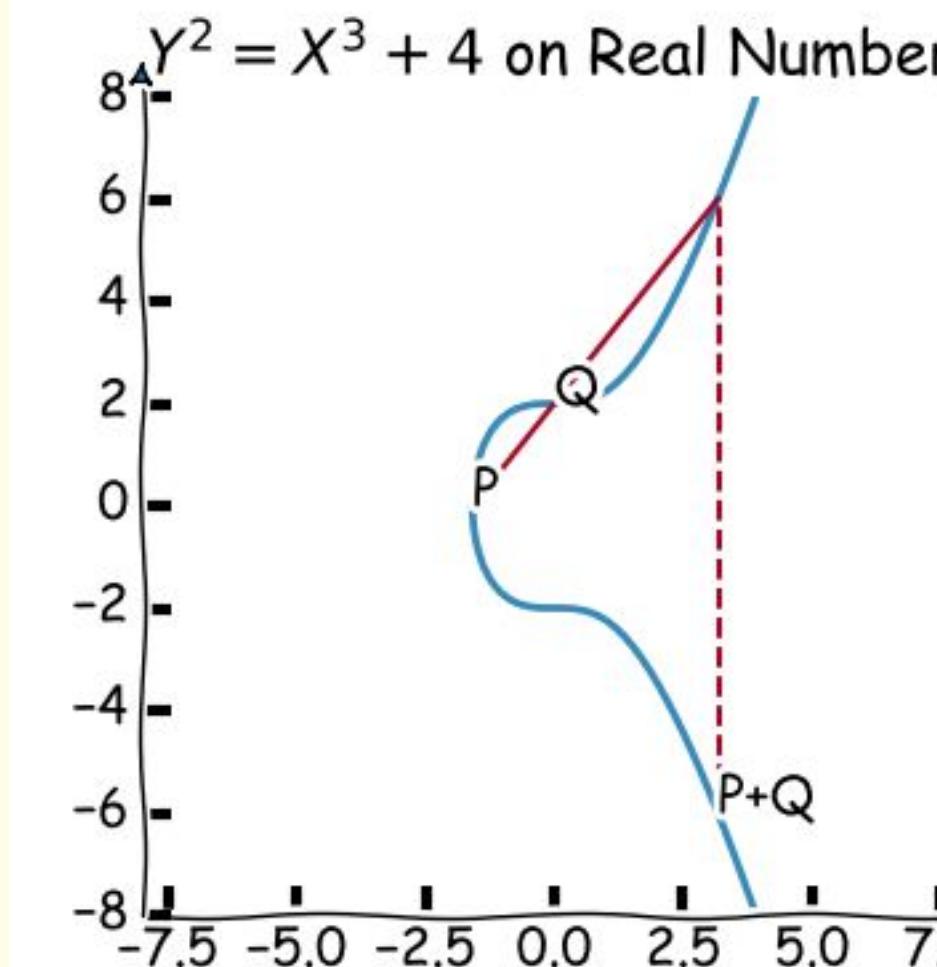


A **point** on the curve has x and y coordinates. It can be *compressed* by specifying only x plus 1 bit to infer y.

P: (x, y)

You can **add** a point to another point

P+Q



You can **multiply** a point with an integer

$$\begin{aligned} 10P &= P + P + P + P + P + \\ &\quad P + P + P + P + P \end{aligned}$$

When people see this...

The integer can be used as a secret

Q := 10P

They can't figure out this.

## The pairing function



48 bytes 

$$\langle G_1 \rangle \\ G_1, 2G_1, \dots, (r-1)G_1$$

$$E(F_q) := y^2 = x^3 + 4$$

$F_q$  48 bytes

$q \approx 2^{381}$

Field elements

Curves



96 bytes 

$$\langle G_2 \rangle \\ G_2, 2G_2, \dots, (r-1)G_2 \\ E'(F_{q^2}) := y^2 = x^3 + 4(i+1)$$

$F_{q^2}$  96 bytes

$$e(P + R, Q + S) \\ = e(P, Q)e(P, S)e(R, Q)e(R, S)$$

Curve point subgroup  
generated by the  
generator

**Private Key**

$k$

32 bytes

**Hash to  $G_2$**

**Public Key**

$P = k \cdot G_1$

48 bytes

$H(m)$

**Sign**

$S = k \cdot H(m)$  96 bytes

**Verify**

$e(G_1, S) == e(P, H(m))$

$$\begin{aligned}
 & e(G_1, S) \\
 &= e(G_1, k \cdot H(m)) \\
 &= e(k \cdot G_1, H(m)) \\
 &= e(P, H(m))
 \end{aligned}$$

**Aggregate multiple signatures**

$$S_{123} = S_1 + S_2 + S_3$$

$$P_{123} = P_1 + P_2 + P_3$$

**Verify multiple signatures**

$$e(G_1, S_{123}) == e(P_{123}, H(m))$$

## Attestation: An aggregation example

```
aggregationBits: '0x63e301'
```

```
data:
```

```
...
```

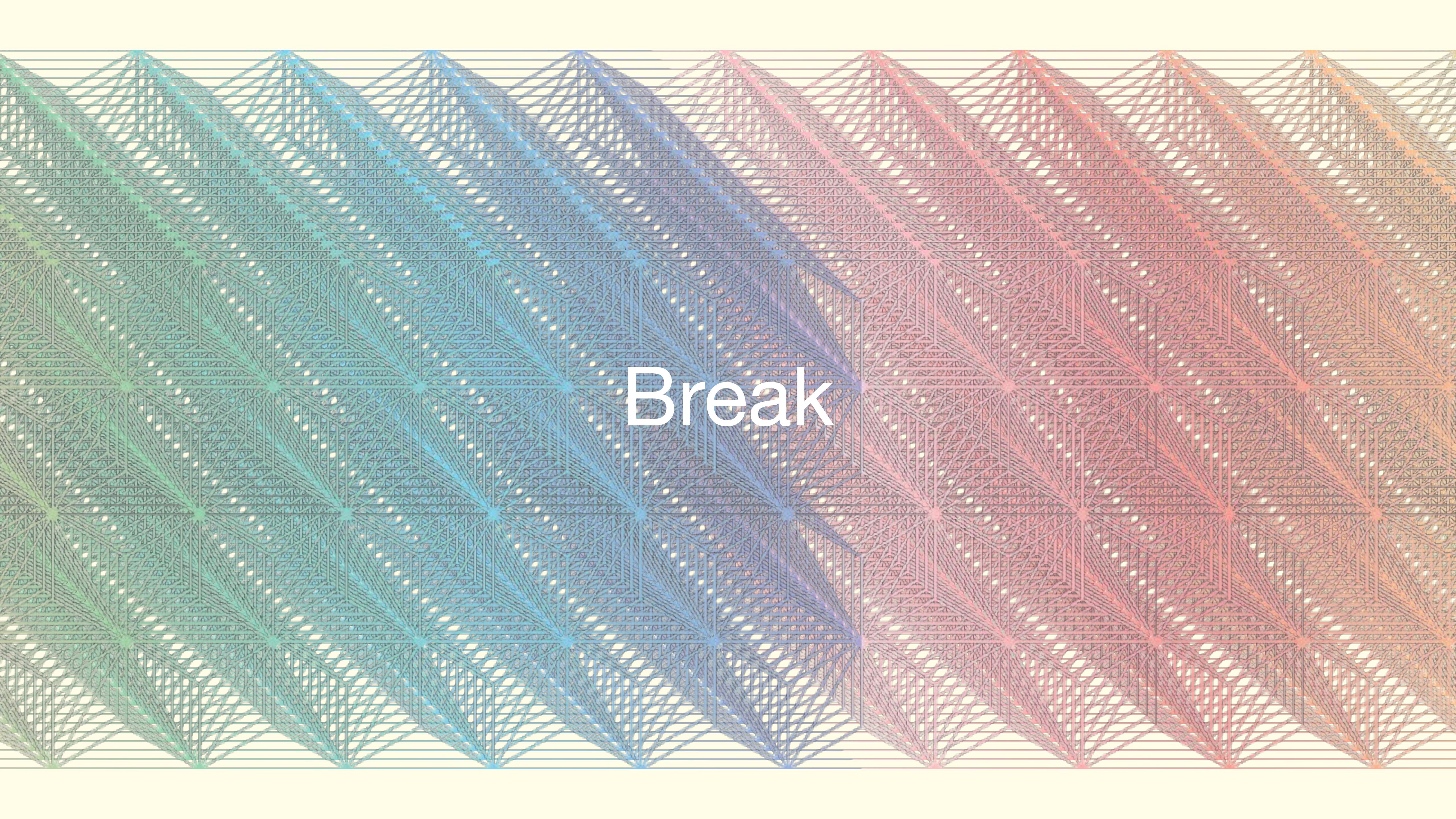
```
signature: >-
```

```
0x63e7c50e0894483e0e7974b2a22dd5c0facb  
853ae8cffcae1657301e36b55299438c760e6b  
18a7e85b74ffce0697f028de9c4b633dcde21e  
3a0caf3d686b98f565d2ea80a3aa63588515a8  
d46e2af8a84144953dd1abe4b7f586291e1490  
b1d9
```

This is '0b1100011110001100000001' in binary.  
The i'th position records if the i'th validator has voted.

A client uses this information to  
lookup the public keys of the  
voting validators.

Always 96 bytes, no matter  
how many votes it  
aggregated.



Break

# Life of An Ethereum Beacon Chain Validator

Spec v.0.8.3 - 2019 August 24th

Ethereum Research

Hsiao-Wei Wang



hwwhww



icebearhww



# Life of An Ethereum Beacon Chain Validator

1. Two main factors of validator status transition

Status epoch

Slashed

2. Rate-limiting entry/exits queues
3. Lifecycle

# Validator Status

1. Activation Eligibility
2. Activation
3. Exit
4. Withdrawable

**the validator will be able to withdraw to EEs in phase 2**

# Validator Status Epoch

```
class Validator(Container):
    pubkey: BLSPubkey
    withdrawal_credentials: Hash # Commitment to pubkey for withdrawals and transfers
    effective_balance: Gwei # Balance at stake
    slashed: boolean
    # Status epochs
    activation_eligibility_epoch: Epoch # When criteria for activation were met
    activation_epoch: Epoch
    exit_epoch: Epoch
    withdrawable_epoch: Epoch # When validator can withdraw or transfer funds
```

status epoch default value = FAR\_FUTURE\_EPOCH = Epoch(2\*\*64 - 1)

# Validator Status Epoch: example

activation\_eligibility\_epoch = 100

activation\_epoch = 200

epoch

validator is not activated

# Validator Status Epoch: example

activation\_eligibility\_epoch = 100

activation\_epoch = 200

epoch

validator is activated

# validator.slashed Boolean Flag

```
class Validator(Container):
    pubkey: BLSPubkey
    withdrawal_credentials: Hash # Commitment to pubkey for withdrawals and transfers
    effective_balance: Gwei # Balance at stake
    slashed: boolean
    # Status epochs
    activation_eligibility_epoch: Epoch # When criteria for activation were met
    activation_epoch: Epoch
    exit_epoch: Epoch
    withdrawable_epoch: Epoch # When validator can withdraw or transfer funds
```

A slashed validator will be forced exited.

# Weak Subjectivity

Only need to trust when

- a. You join the first time
- b. You were offline for a long time
  - How long? It depends on how long it takes for attacker to withdraw their stake.
  - “weak subjectivity period”

# Rate-limiting entry/exits queues

1. Ensure the validator set is stable enough between two points
2. Ensure that **finality guarantees** still remain between two chains as long as a validator logs on often enough

Reference: <https://notes.ethereum.org/@vbuterin/rkhCgQteN?type=view#Exiting>

# Churn rate

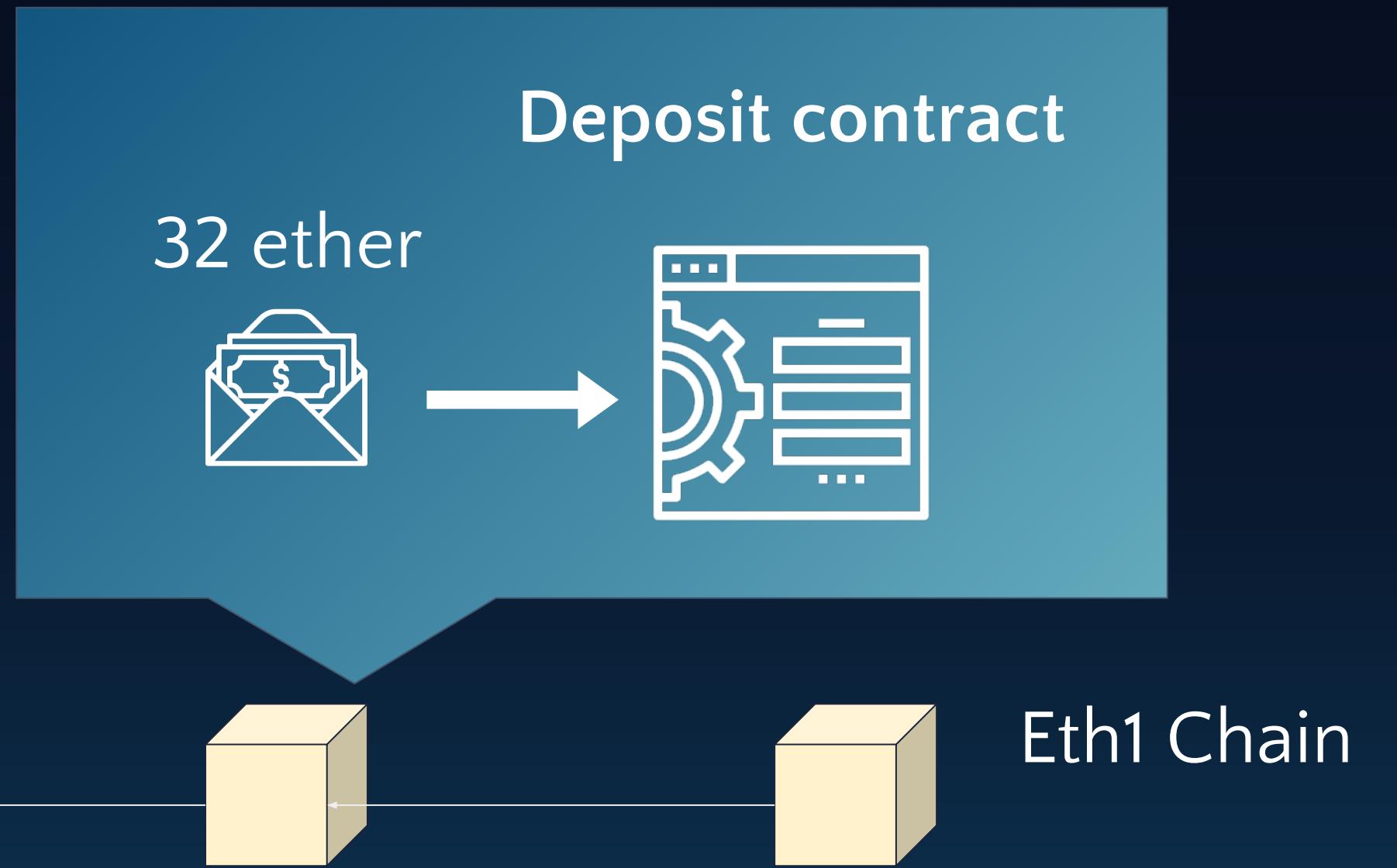
- The churn rate is based on current **active validators count**
- Maximum **max (4 , |V| / 65535)** validators can join per epoch

```
def get_validator_churn_limit(state: BeaconState) -> uint64:  
    """  
    Return the validator churn limit for the current epoch.  
    """  
  
    active_validator_indices = get_active_validator_indices(state, get_current_epoch(state))  
    return max(MIN_PER_EPOCH_CHURN_LIMIT, len(active_validator_indices) // CHURN_LIMIT_QUOTIENT)
```

# Lifecycle

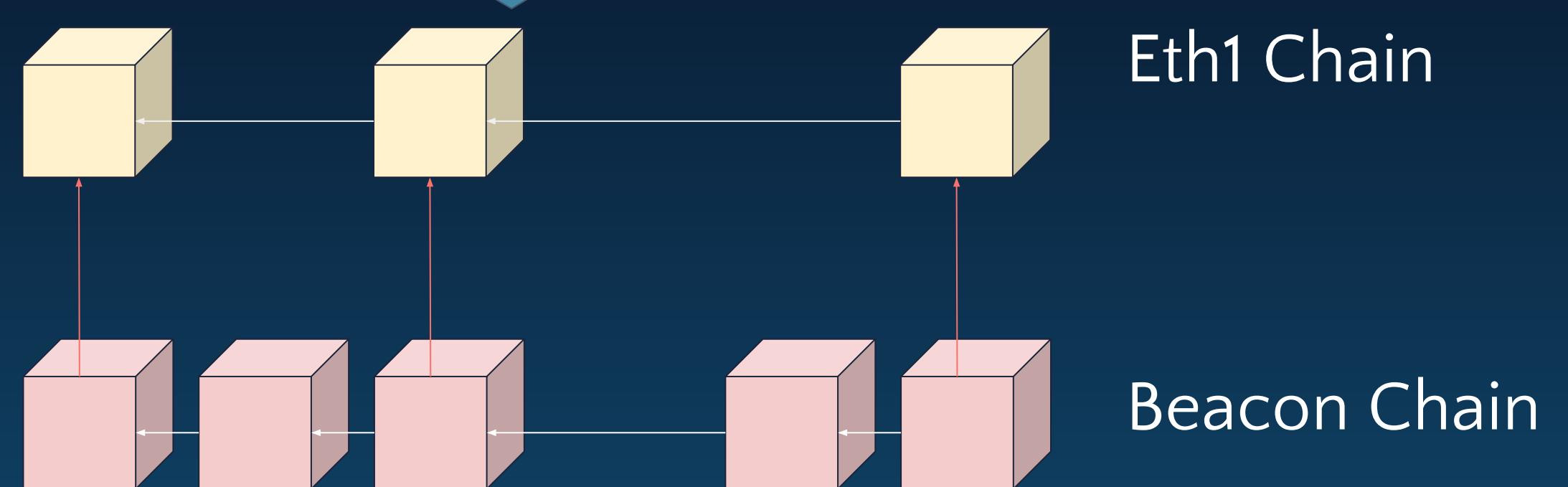
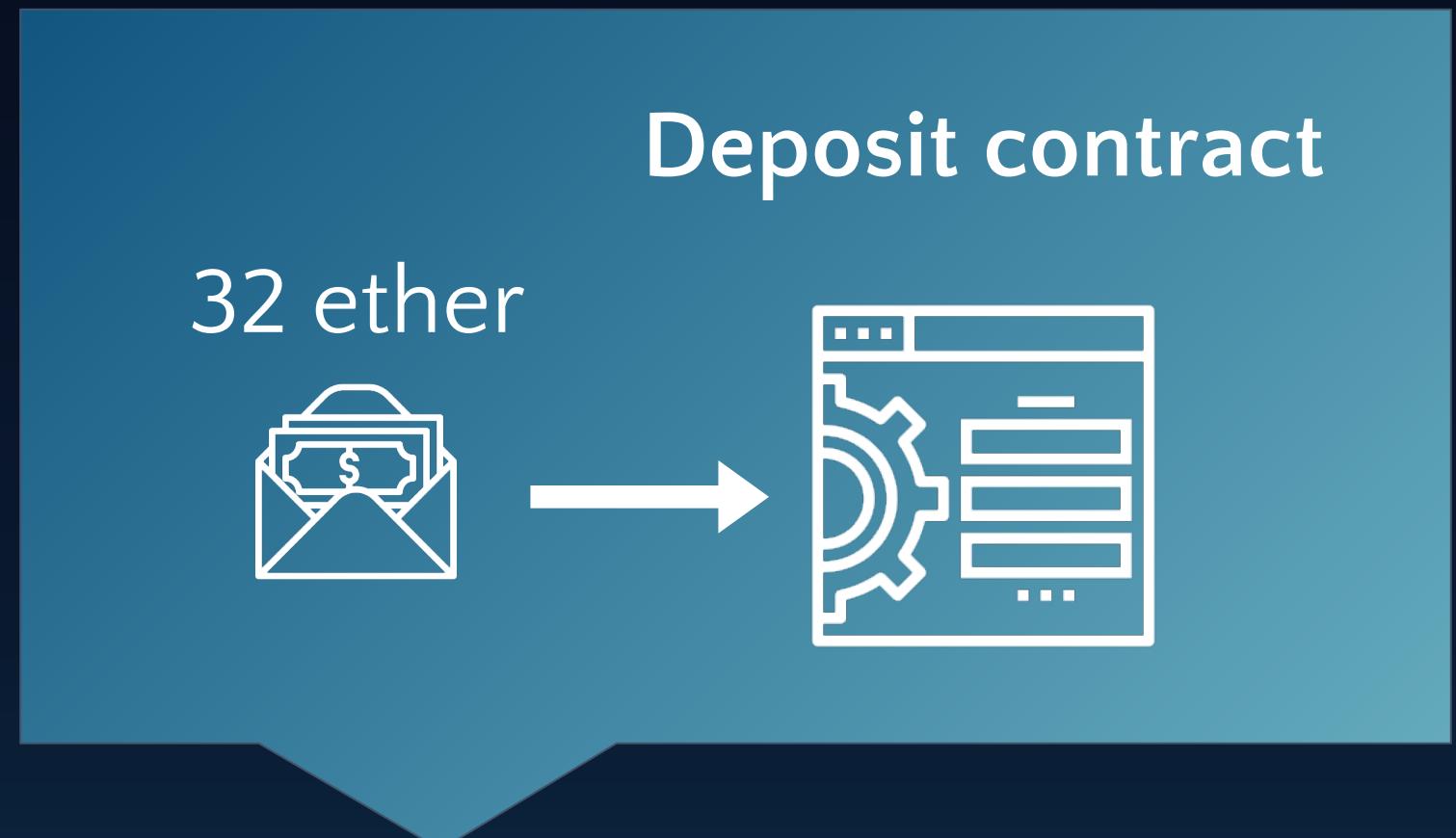
# Join the Staking

1. Deposit MAX\_DEPOSIT\_AMOUNT  
(32 ether) to a special  
**deposit contract**

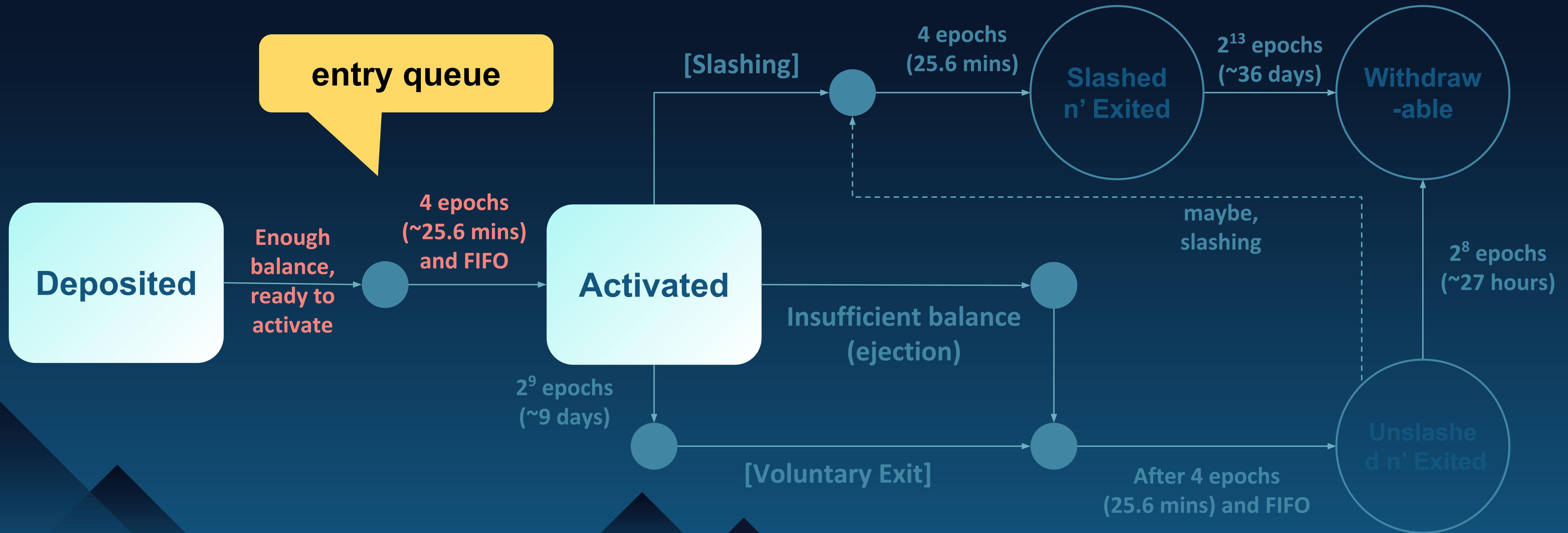


# Join the Staking

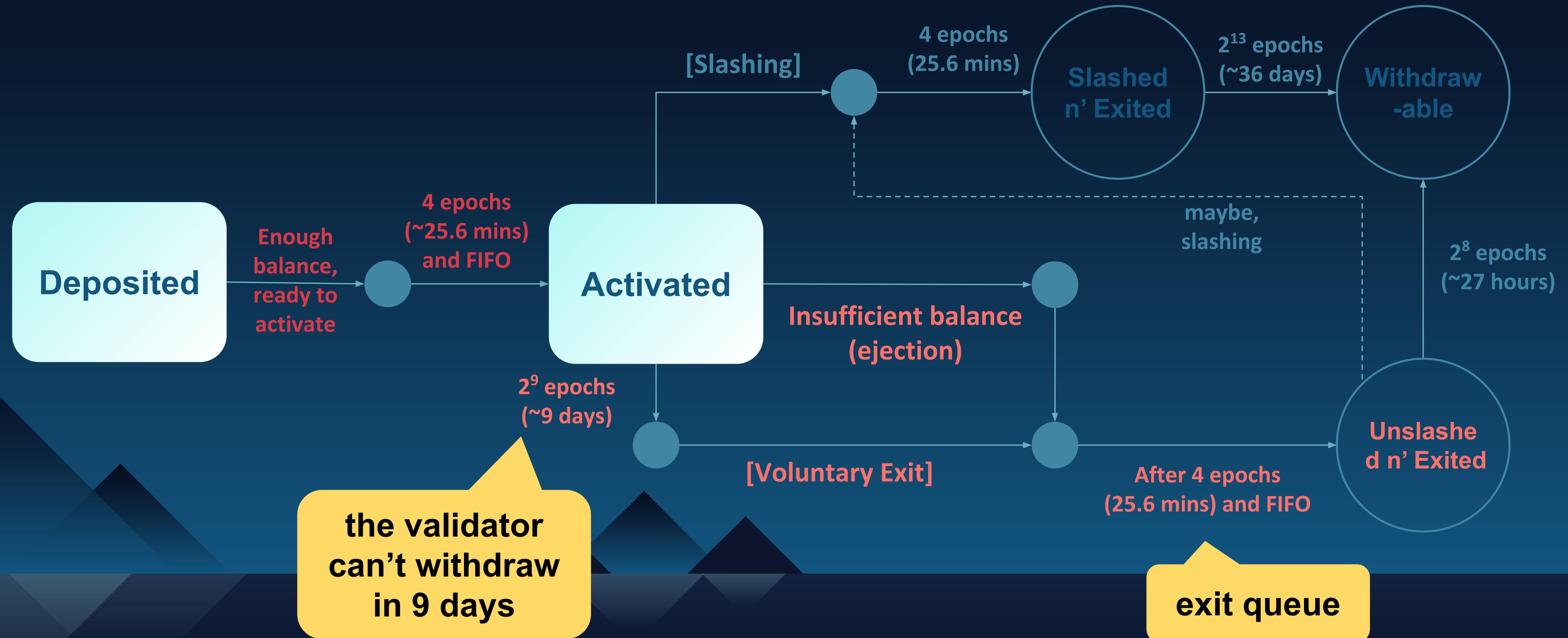
1. Deposit MAX\_DEPOSIT\_AMOUNT  
(32 ether) to a special  
**deposit contract**
2. Watch the deposit contract status



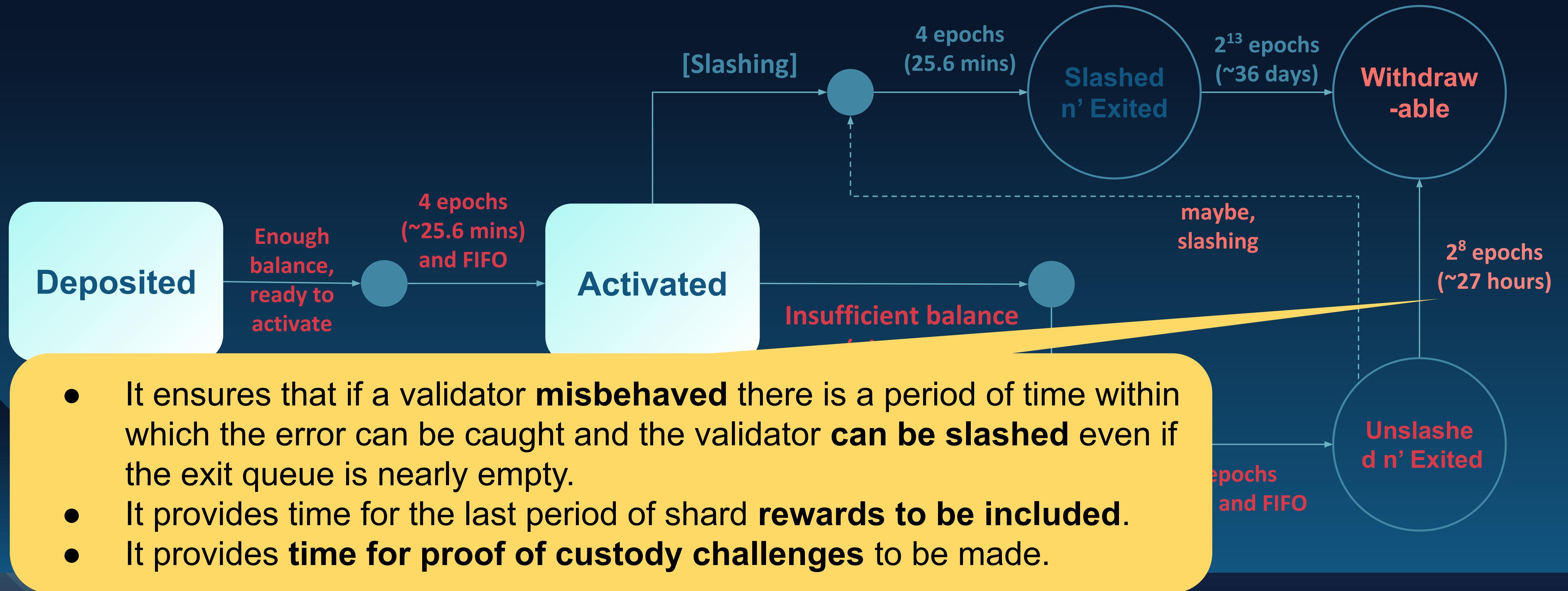
# Validator Status (v0.8.3)



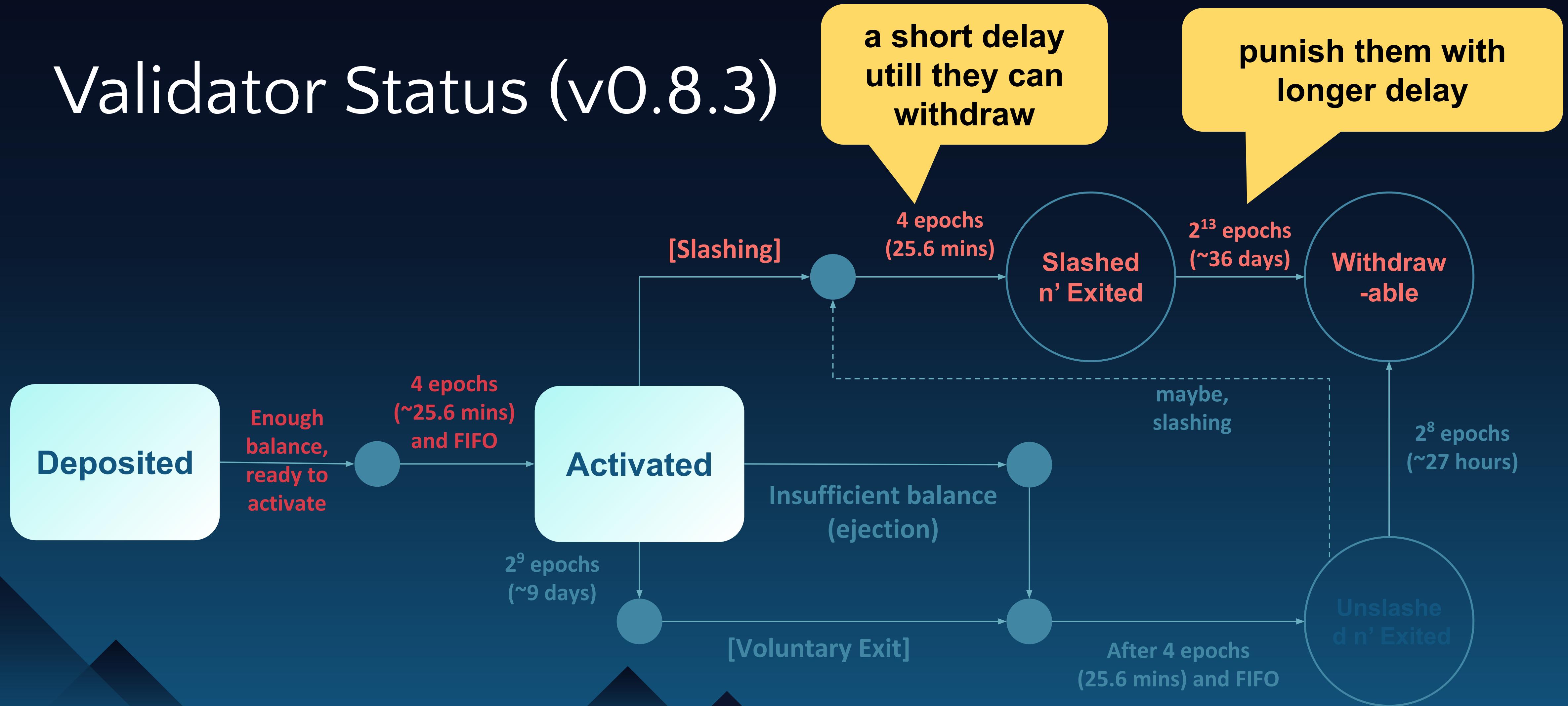
# Validator Status (v0.8.3)



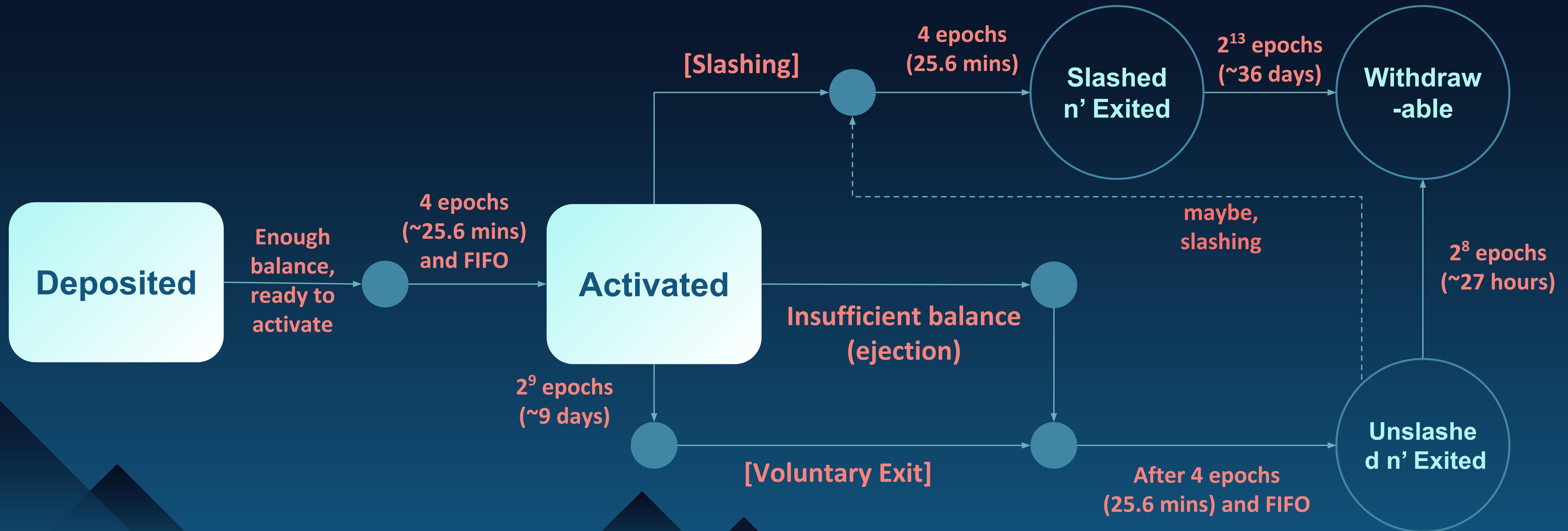
# Validator Status (v0.8.3)



# Validator Status (v0.8.3)



# Validator Status (v0.8.3)



# Resource credit

- ◊ Slide template: 24Slides.com
- ◊ Icons: designed by Freepik from [www.flaticon.com](http://www.flaticon.com)

# Thank you!

beacon chain

state transition function

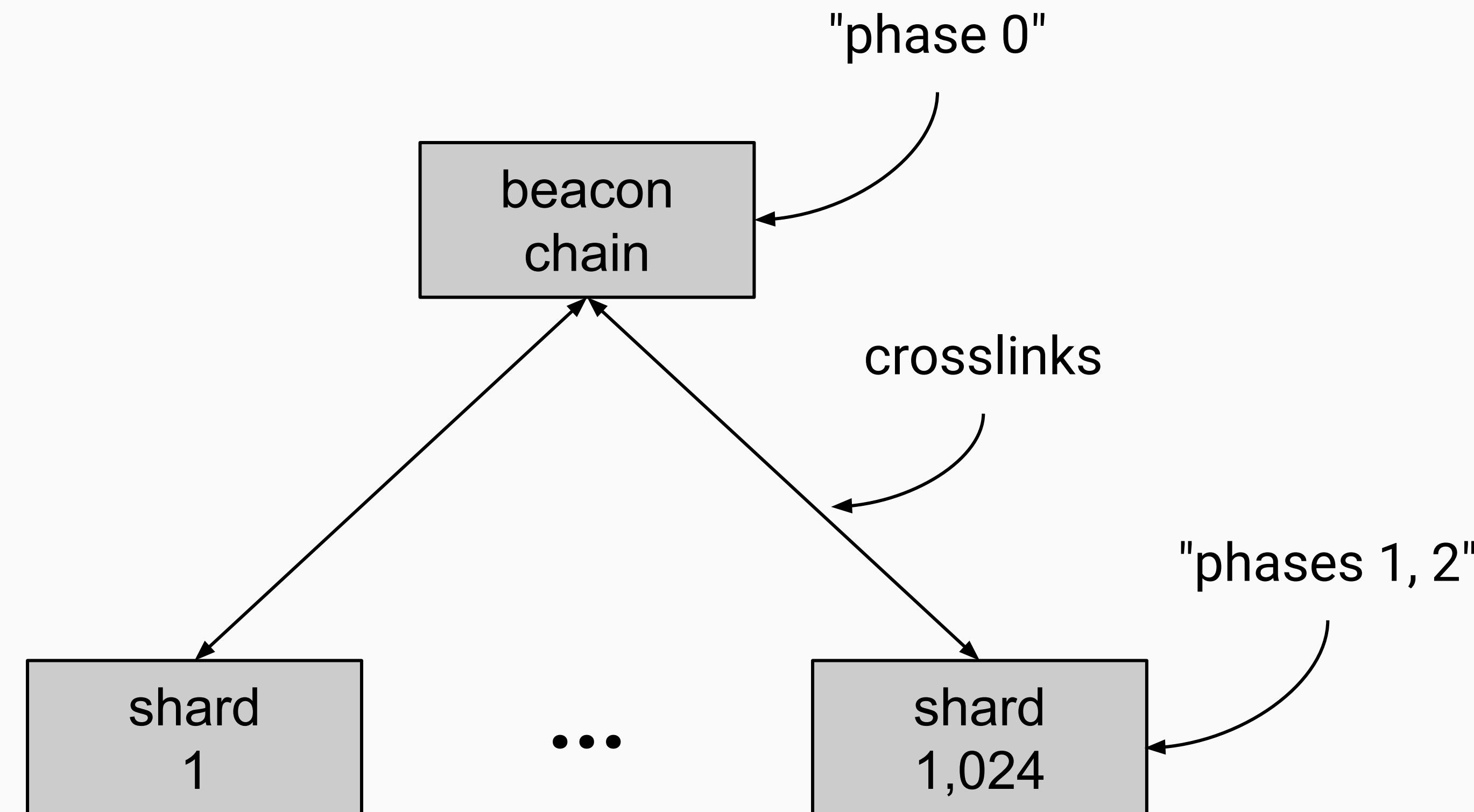
read the specs

[github.com/ethereum/eth2.0-specs/blob/dev/specs/core/0\\_beacon-chain.md](https://github.com/ethereum/eth2.0-specs/blob/dev/specs/core/0_beacon-chain.md)

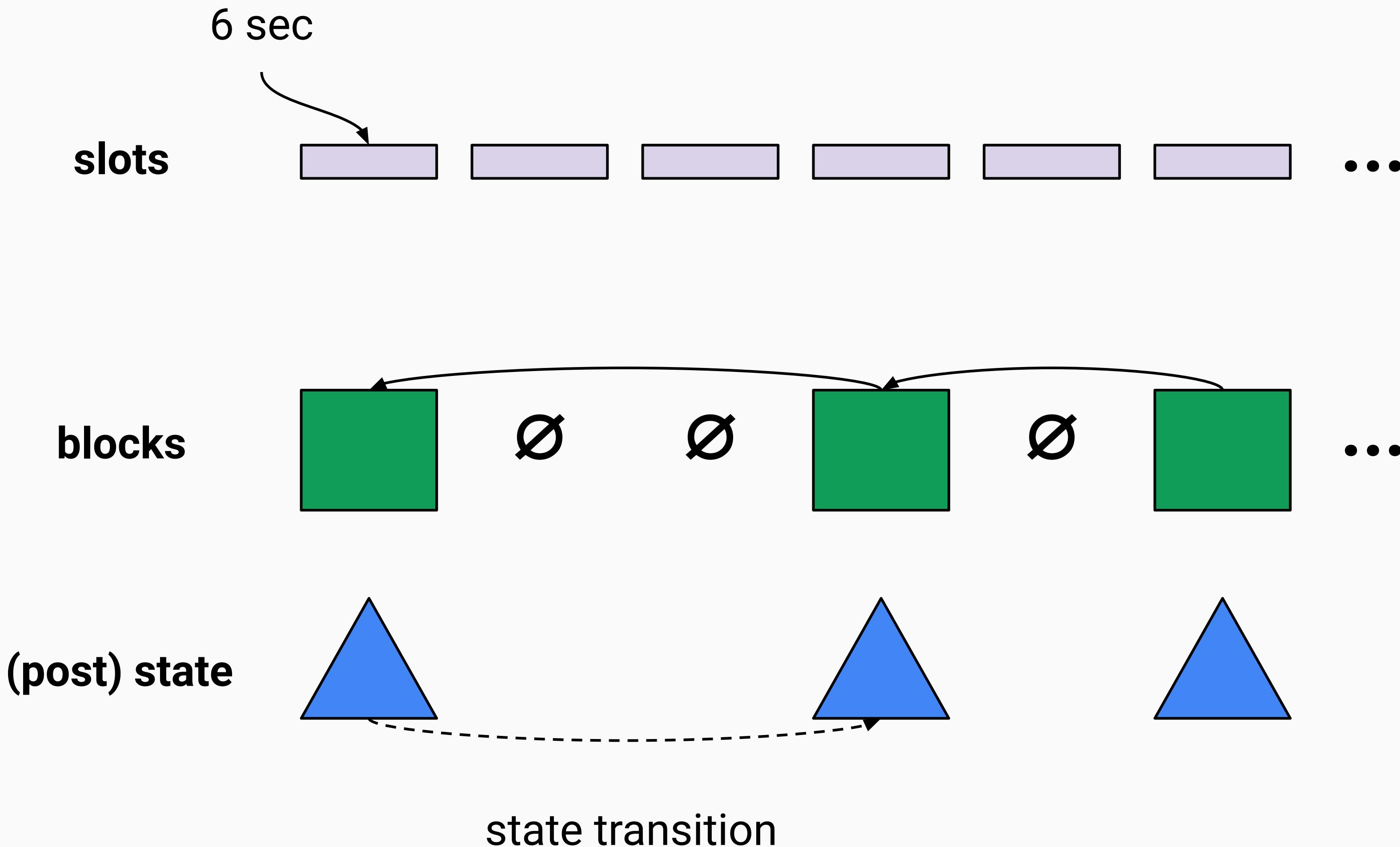


[tiny.cc/beaconchain](http://tiny.cc/beaconchain)

## hub-and-spoke

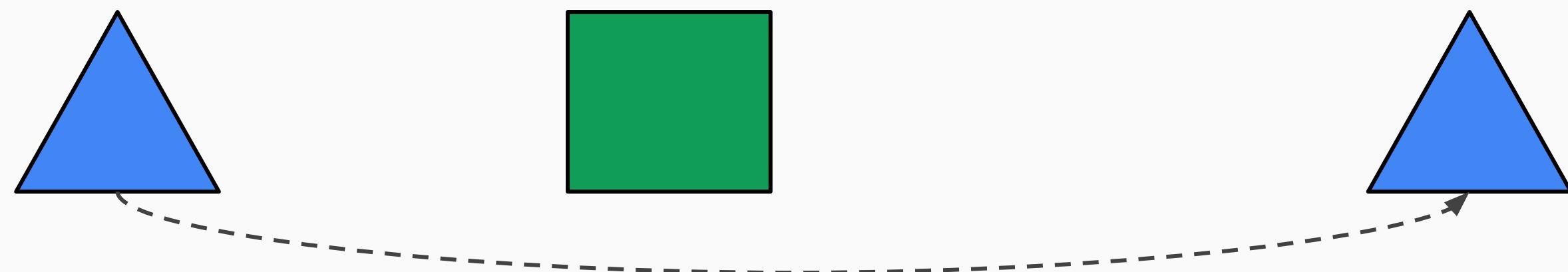


## slots, blocks, state

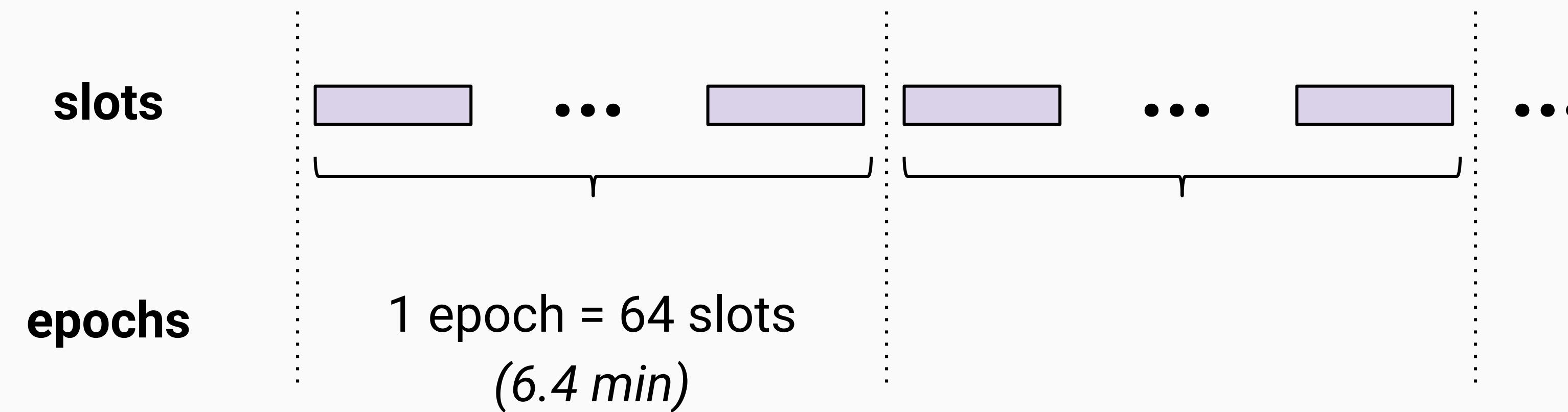


state transition function

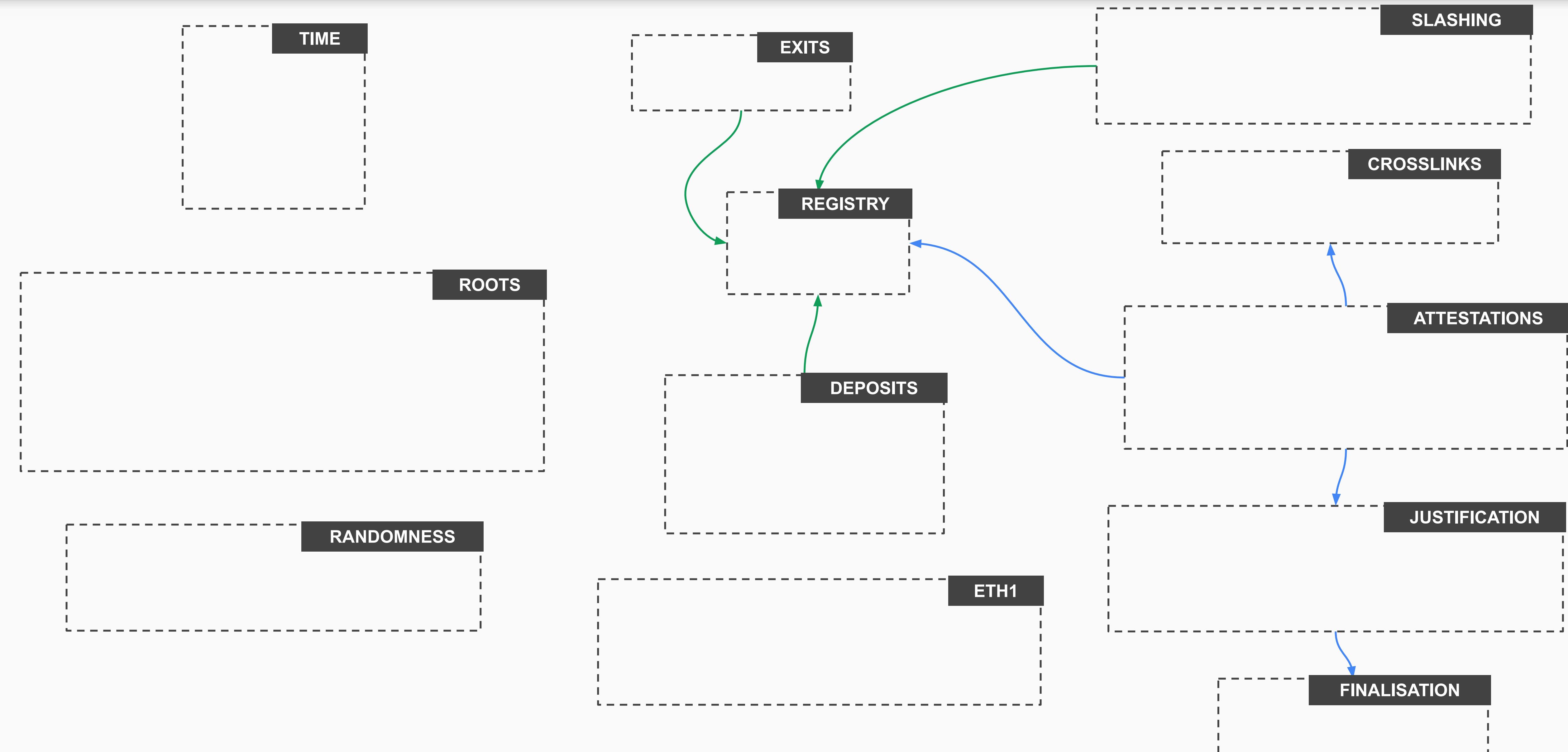
$(\text{pre\_state}, \text{block}) \rightarrow \text{post\_state} \text{ (or error)}$



epochs

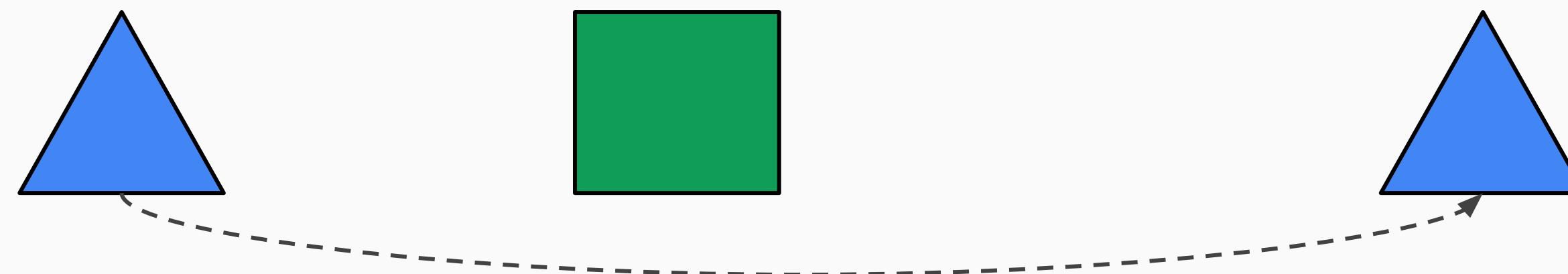


# modularity



state transition function

$(\text{pre\_state}, \text{block}) \rightarrow \text{post\_state} \text{ (or error)}$



## BeaconState

```
1  class BeaconState(Container):  
2      # Versioning  
3      genesis_time: uint64  
4      slot: Slot  
5      fork: Fork
```

## BeaconState

```
1 class BeaconState(Container):
2     # Versioning
3     genesis_time: uint64
4     slot: Slot
5     fork: Fork
6     # History
7     latest_block_header: BeaconBlockHeader
8     block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9     state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10    historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
```

## BeaconState

```
1 class BeaconState(Container):
2     # Versioning
3     genesis_time: uint64
4     slot: Slot
5     fork: Fork
6     # History
7     latest_block_header: BeaconBlockHeader
8     block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9     state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10    historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11    # Eth1
12    eth1_data: Eth1Data
13    eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14    eth1_deposit_index: uint64
```

## BeaconState

```
1  class BeaconState(Container):
2      # Versioning
3      genesis_time: uint64
4      slot: Slot
5      fork: Fork
6      # History
7      latest_block_header: BeaconBlockHeader
8      block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9      state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10     historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11     # Eth1
12     eth1_data: Eth1Data
13     eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14     eth1_deposit_index: uint64
15     # Registry
16     validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
17     balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
```

## BeaconState

```
1 class BeaconState(Container):
2     # Versioning
3     genesis_time: uint64
4     slot: Slot
5     fork: Fork
6     # History
7     latest_block_header: BeaconBlockHeader
8     block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9     state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10    historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11    # Eth1
12    eth1_data: Eth1Data
13    eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14    eth1_deposit_index: uint64
15    # Registry
16    validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
17    balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
18    # Shuffling
19    start_shard: Shard
20    randao_mixes: Vector[Hash, EPOCHS_PER_HISTORICAL_VECTOR]
```

## BeaconState

```
1 class BeaconState(Container):
2     # Versioning
3     genesis_time: uint64
4     slot: Slot
5     fork: Fork
6     # History
7     latest_block_header: BeaconBlockHeader
8     block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9     state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10    historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11    # Eth1
12    eth1_data: Eth1Data
13    eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14    eth1_deposit_index: uint64
15    # Registry
16    validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
17    balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
18    # Shuffling
19    start_shard: Shard
20    randao_mixes: Vector[Hash, EPOCHS_PER_HISTORICAL_VECTOR]
21    # Slashings
22    slashings: Vector[Gwei, EPOCHS_PER_SLASHINGS_VECTOR]
```

## BeaconState

```
1 class BeaconState(Container):
2     # Versioning
3     genesis_time: uint64
4     slot: Slot
5     fork: Fork
6     # History
7     latest_block_header: BeaconBlockHeader
8     block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9     state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10    historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11    # Eth1
12    eth1_data: Eth1Data
13    eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14    eth1_deposit_index: uint64
15    # Registry
16    validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
17    balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
18    # Shuffling
19    start_shard: Shard
20    randao_mixes: Vector[Hash, EPOCHS_PER_HISTORICAL_VECTOR]
21    # Slashings
22    slashings: Vector[Gwei, EPOCHS_PER_SLASHINGS_VECTOR]
23    # Attestations
24    previous_epoch_attestations: List[PendingAttestation, MAX_ATTESTATIONS * SLOTS_PER_EPOCH]
25    current_epoch_attestations: List[PendingAttestation, MAX_ATTESTATIONS * SLOTS_PER_EPOCH]
```

# BeaconState

```
1  class BeaconState(Container):
2      # Versioning
3      genesis_time: uint64
4      slot: Slot
5      fork: Fork
6      # History
7      latest_block_header: BeaconBlockHeader
8      block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9      state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10     historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11     # Eth1
12     eth1_data: Eth1Data
13     eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14     eth1_deposit_index: uint64
15     # Registry
16     validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
17     balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
18     # Shuffling
19     start_shard: Shard
20     randao_mixes: Vector[Hash, EPOCHS_PER_HISTORICAL_VECTOR]
21     # Slashings
22     slashings: Vector[Gwei, EPOCHS_PER_SLASHINGS_VECTOR]
23     # Attestations
24     previous_epoch_attestations: List[PendingAttestation, MAX_ATTESTATIONS * SLOTS_PER_EPOCH]
25     current_epoch_attestations: List[PendingAttestation, MAX_ATTESTATIONS * SLOTS_PER_EPOCH]
26     # Crosslinks
27     previous_crosslinks: Vector[Crosslink, SHARD_COUNT]
28     current_crosslinks: Vector[Crosslink, SHARD_COUNT]
```

# BeaconState

- SHA256
- tree hashing

- RANDAO
- swap-or-not

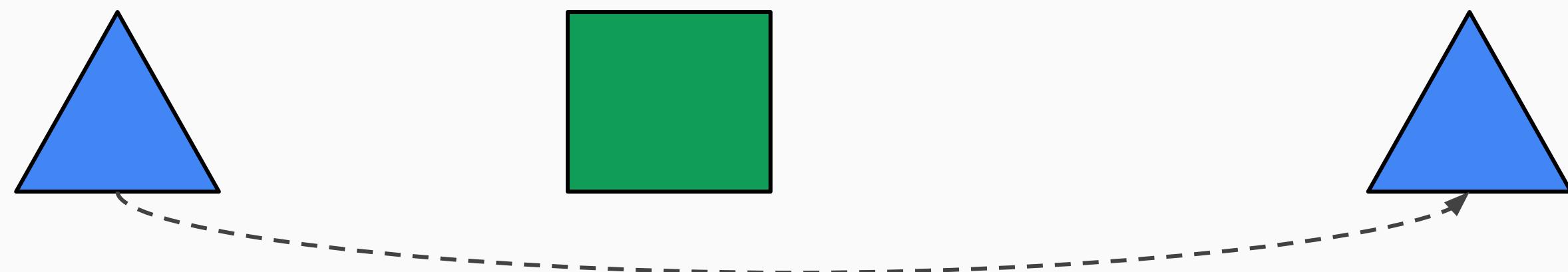
- BLS
- GHOST

- FFG

```
1  class BeaconState(Container):
2      # Versioning
3      genesis_time: uint64
4      slot: Slot
5      fork: Fork
6      # History
7      latest_block_header: BeaconBlockHeader
8      block_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
9      state_roots: Vector[Hash, SLOTS_PER_HISTORICAL_ROOT]
10     historical_roots: List[Hash, HISTORICAL_ROOTS_LIMIT]
11     # Eth1
12     eth1_data: Eth1Data
13     eth1_data_votes: List[Eth1Data, SLOTS_PER_ETH1_VOTING_PERIOD]
14     eth1_deposit_index: uint64
15     # Registry
16     validators: List[Validator, VALIDATOR_REGISTRY_LIMIT]
17     balances: List[Gwei, VALIDATOR_REGISTRY_LIMIT]
18     # Shuffling
19     start_shard: Shard
20     randao_mixes: Vector[Hash, EPOCHS_PER_HISTORICAL_VECTOR]
21     # Slashings
22     slashings: Vector[Gwei, EPOCHS_PER_SLASHINGS_VECTOR]
23     # Attestations
24     previous_epoch_attestations: List[PendingAttestation, MAX_ATTESTATIONS * SLOTS_PER_EPOCH]
25     current_epoch_attestations: List[PendingAttestation, MAX_ATTESTATIONS * SLOTS_PER_EPOCH]
26     # Crosslinks
27     previous_crosslinks: Vector[Crosslink, SHARD_COUNT]
28     current_crosslinks: Vector[Crosslink, SHARD_COUNT]
29     # Finality
30     justification_bits: Bitvector[JUSTIFICATION_BITS_LENGTH]
31     previous_justified_checkpoint: Checkpoint
32     current_justified_checkpoint: Checkpoint
33     finalized_checkpoint: Checkpoint
```

state transition function

$(\text{pre\_state}, \text{block}) \rightarrow \text{post\_state} \text{ (or error)}$



## BeaconBlock

```
1  class BeaconBlock(Container):  
2      slot: Slot  
3      parent_root: Hash  
4      state_root: Hash  
5      body: BeaconBlockBody  
6      signature: BLSSignature
```

## BeaconBlock

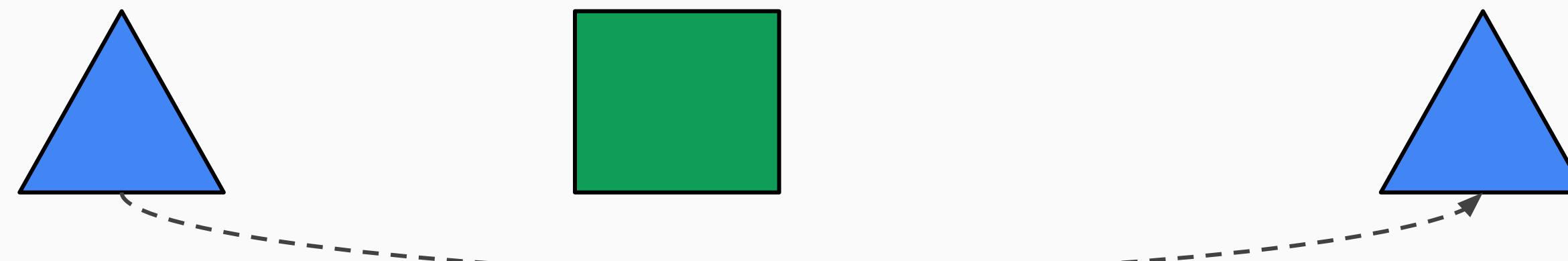
```
1  class BeaconBlock(Container):
2      slot: Slot
3      parent_root: Hash
4      state_root: Hash
5      body: BeaconBlockBody
6      signature: BLSSignature
7
8  class BeaconBlockBody(Container):
9      randao_reveal: BLSSignature
10     eth1_data: Eth1Data
11     graffiti: Bytes32
```

## BeaconBlock

```
1  class BeaconBlock(Container):
2      slot: Slot
3      parent_root: Hash
4      state_root: Hash
5      body: BeaconBlockBody
6      signature: BLSSignature
7
8  class BeaconBlockBody(Container):
9      randao_reveal: BLSSignature
10     eth1_data: Eth1Data
11     graffiti: Bytes32
12     # Operations
13     proposer_slashings: List[ProposerSlashing, MAX_PROPOSER_SLASHINGS]
14     attester_slashings: List[AttesterSlashing, MAX_ATTESTER_SLASHINGS]
15     attestations: List[Attestation, MAX_ATTESTATIONS]
16     deposits: List[Deposit, MAX_DEPOSITS]
17     voluntary_exits: List[VoluntaryExit, MAX_VOLUNTARY_EXITS]
18     transfers: List[Transfer, MAX_TRANSFERS]
```

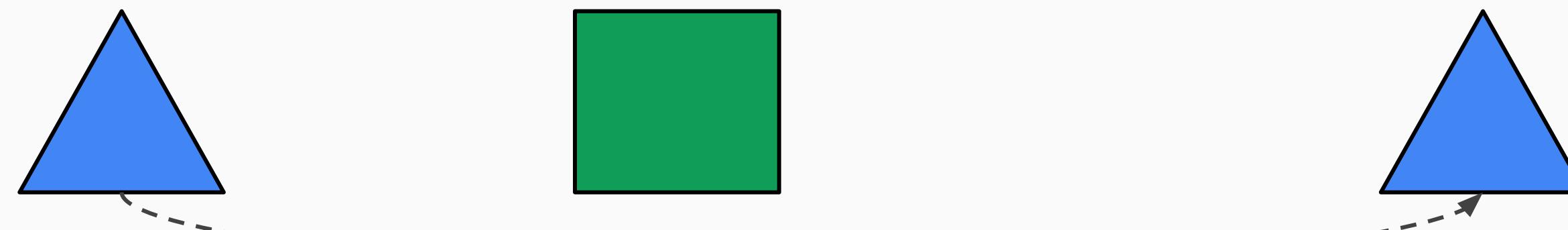
**honest state transition function**

$(\text{pre\_state}, \text{block}) \rightarrow \text{post\_state} \text{ (or } \cancel{\text{error}}\text{)}$



## honest state transition function

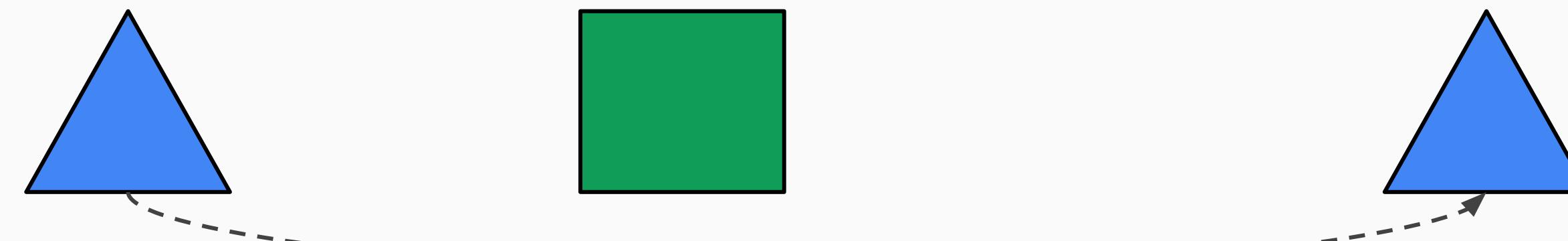
(pre\_state, block) -> post\_state (or error)



state.some\_field = some\_value

## honest state transition function

(pre\_state, block) -> post\_state (or error)

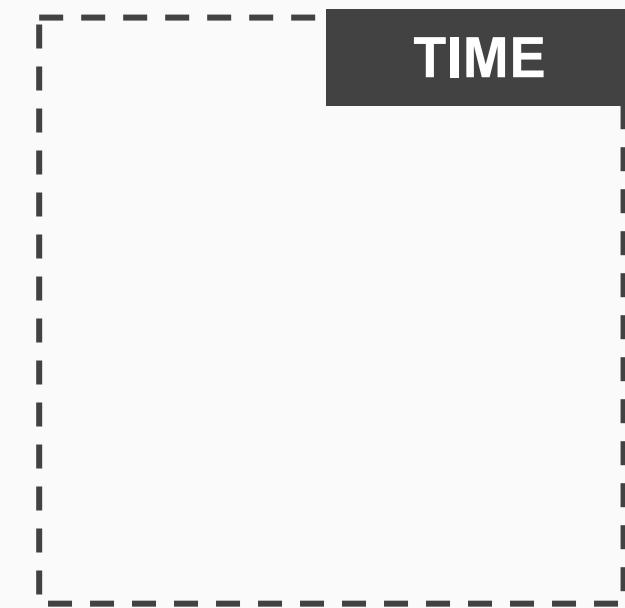


`state.some_field = some_value`



`assert someInvariant(block, state)`

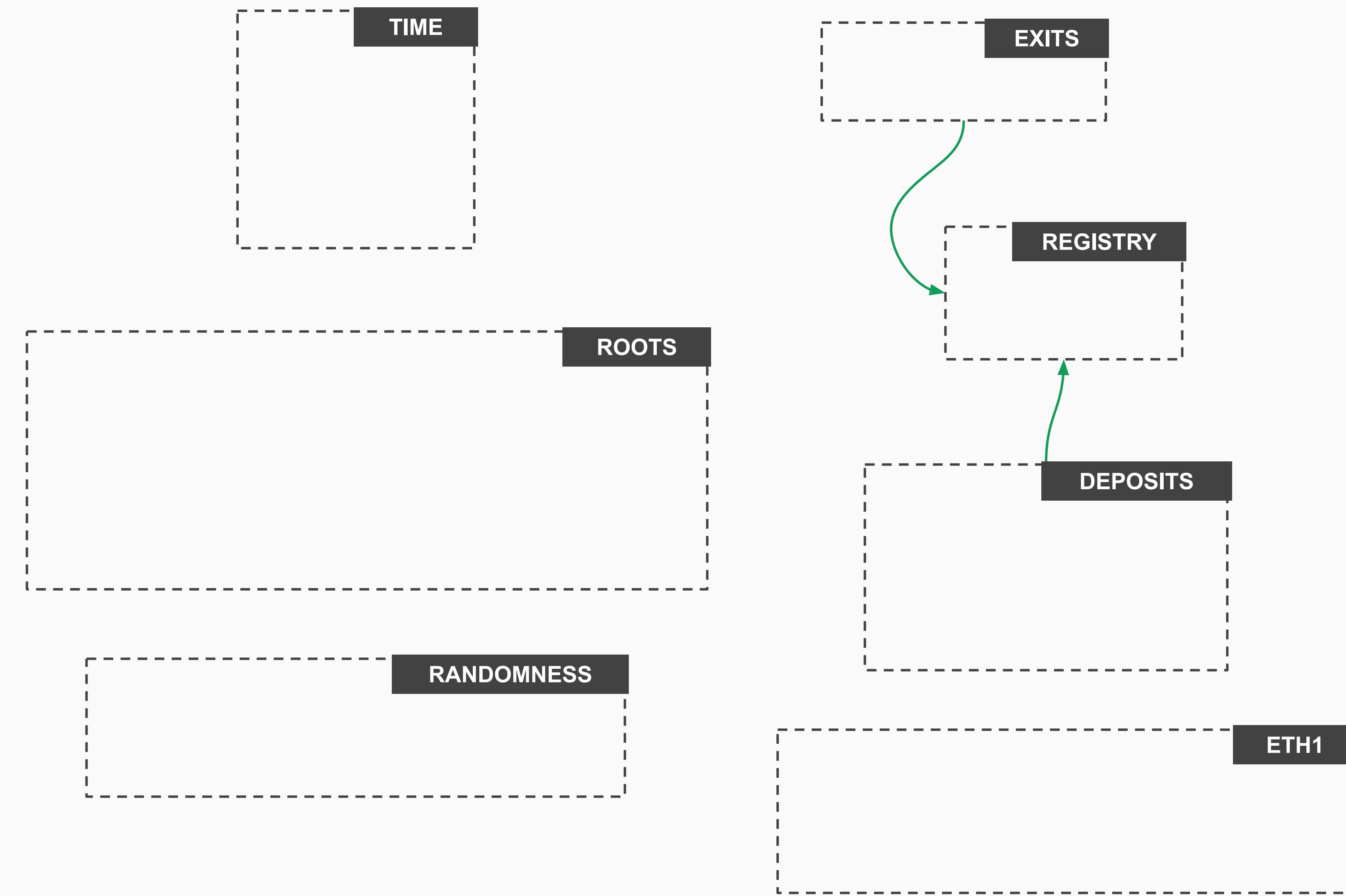
# state transition function



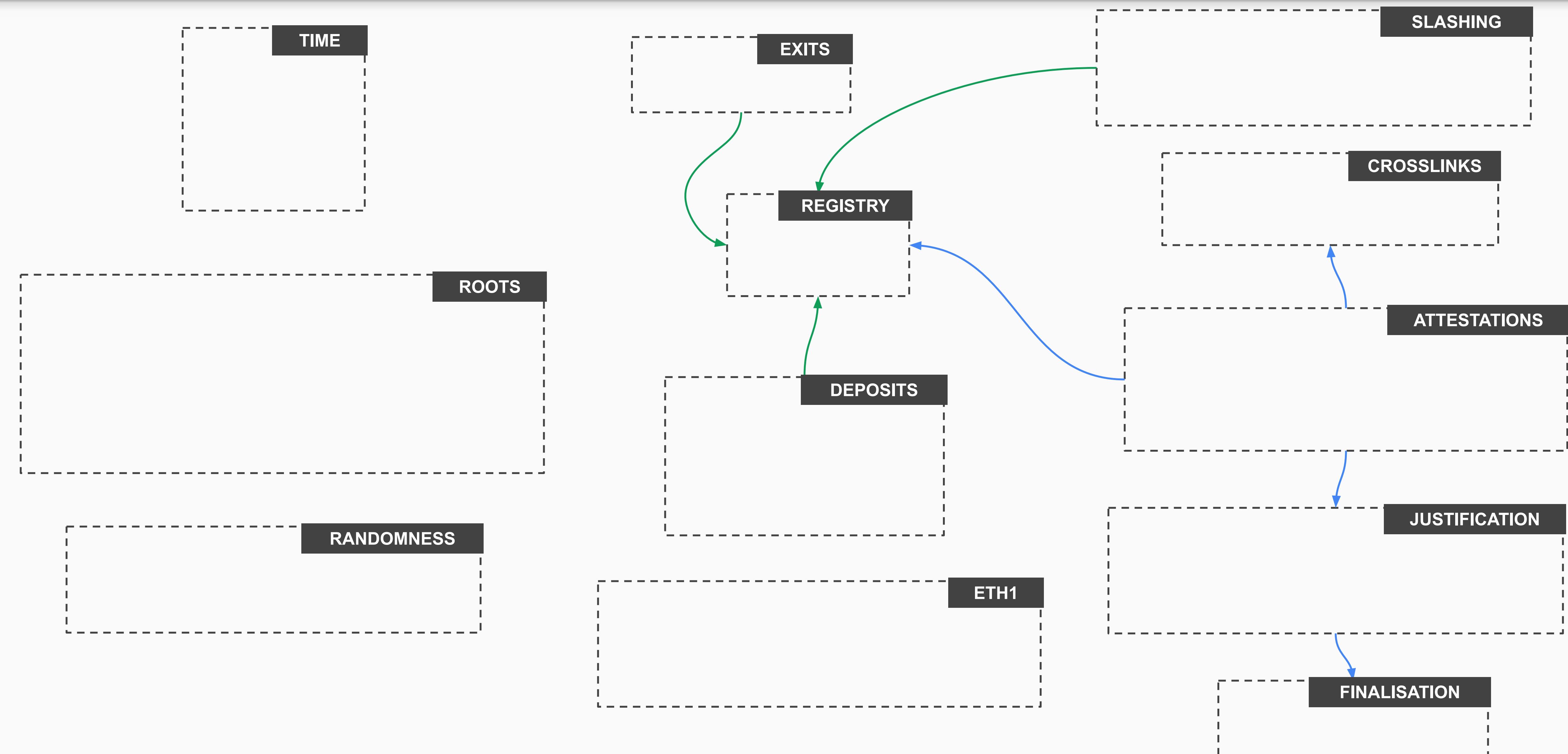
ROOTS

RANDOMNESS

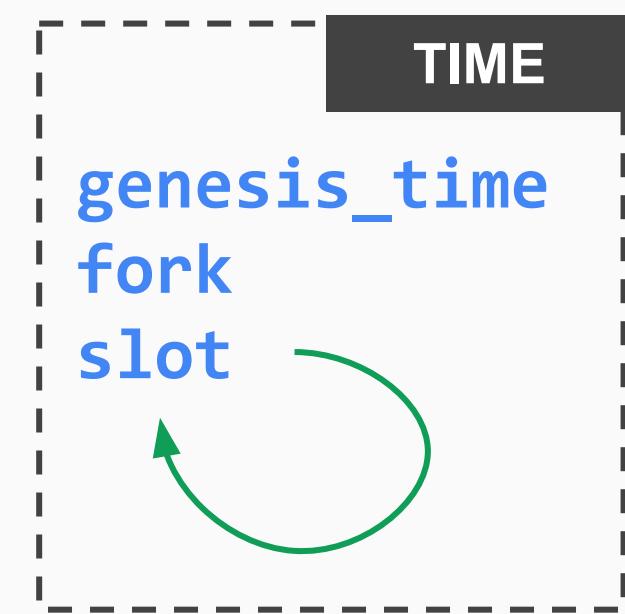
# state transition function



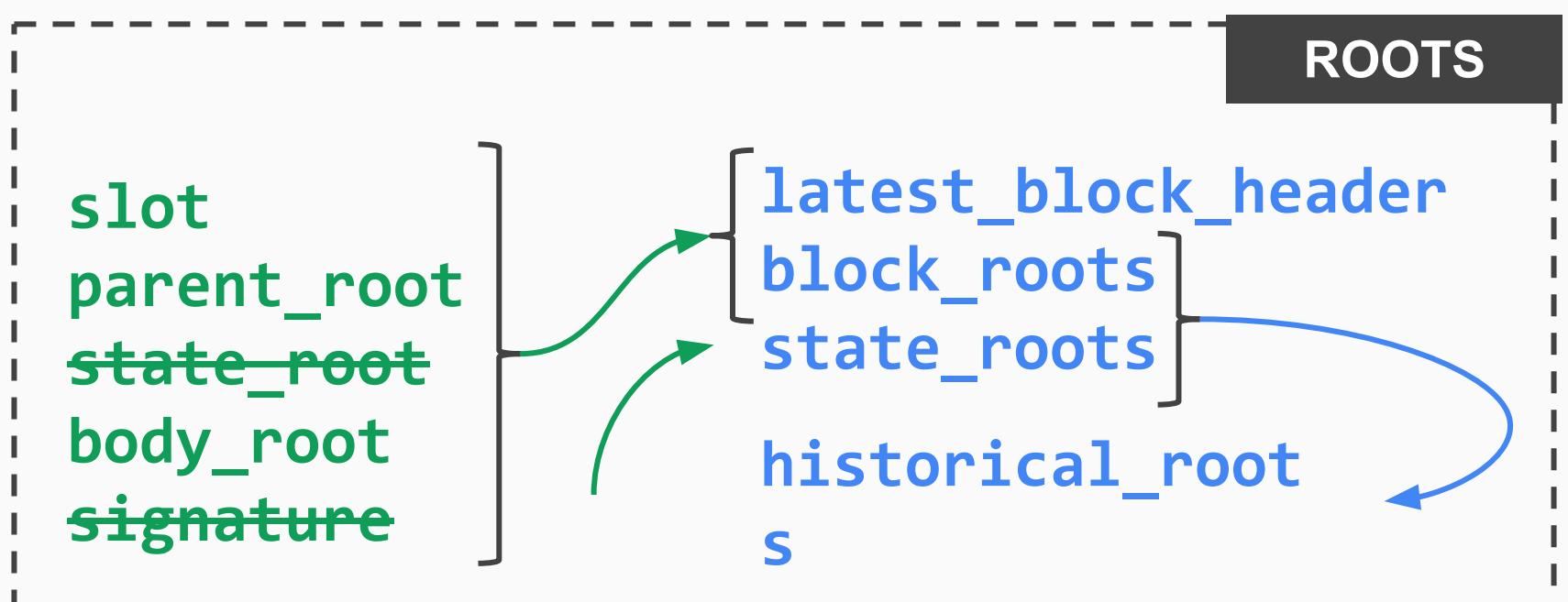
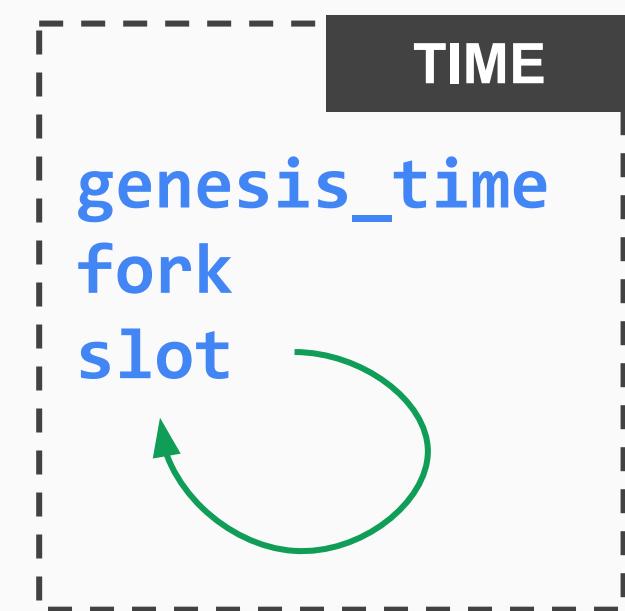
# state transition function



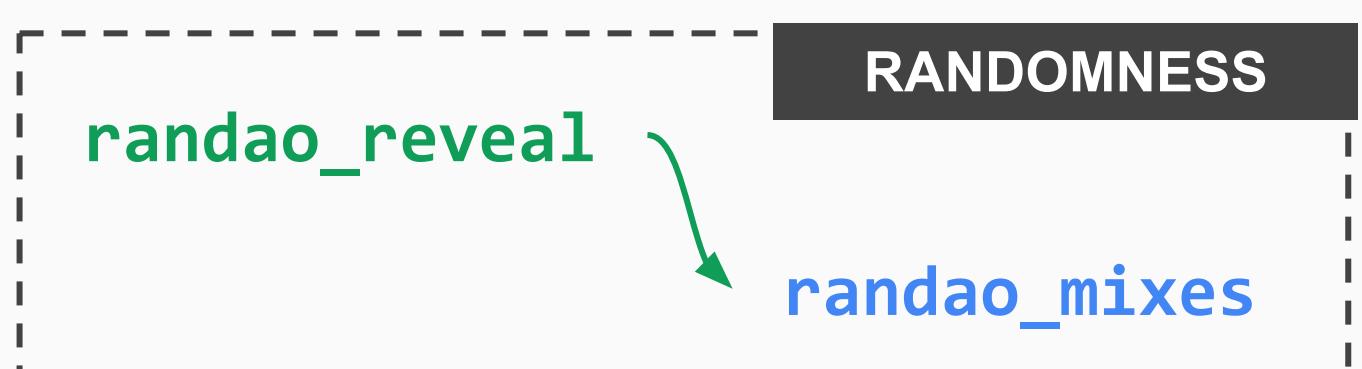
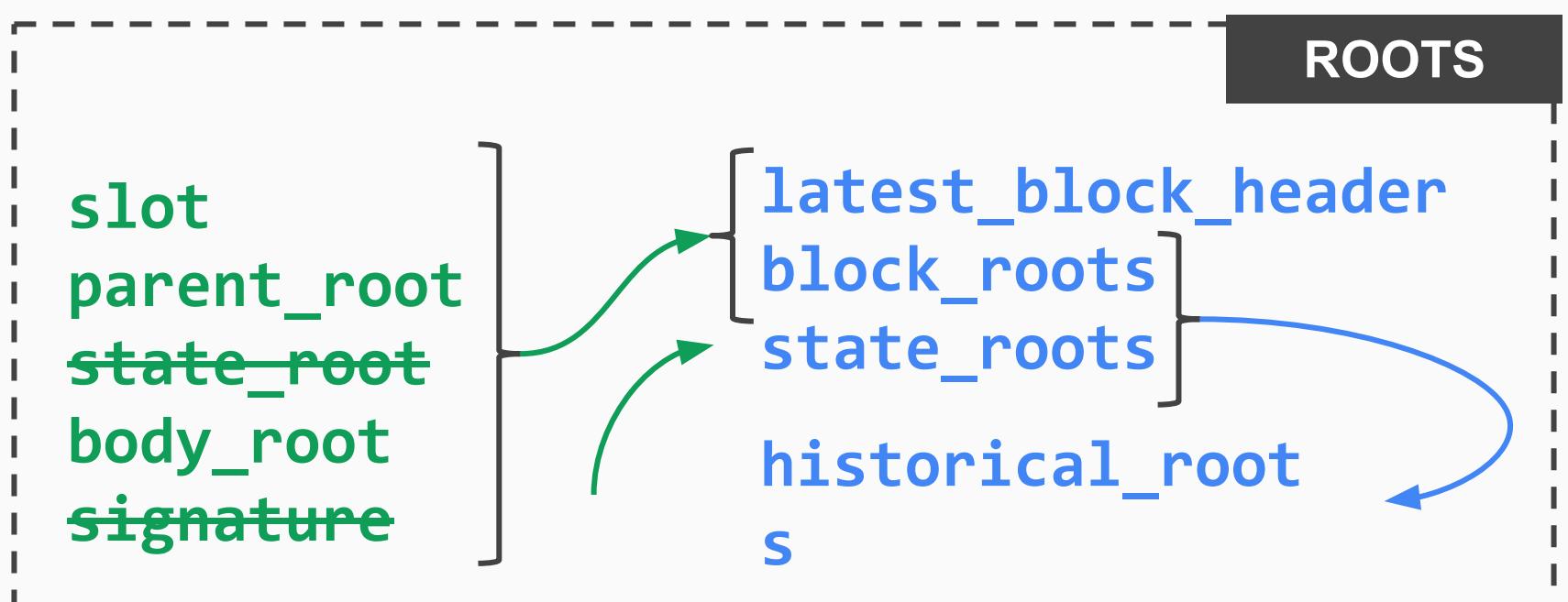
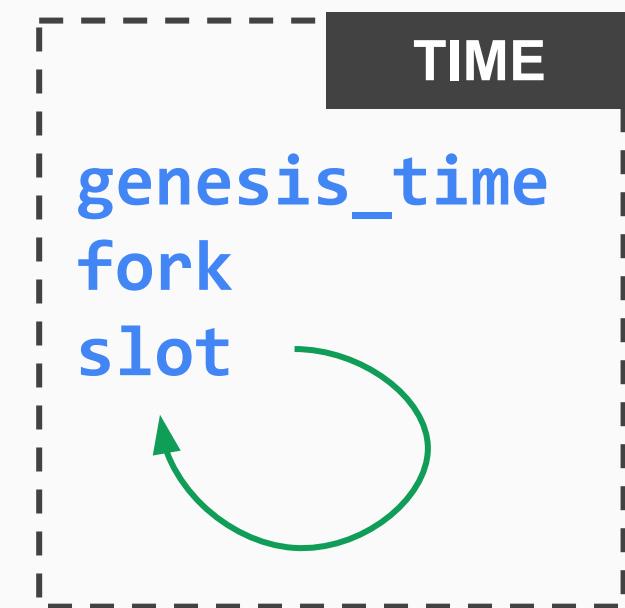
## state transition function



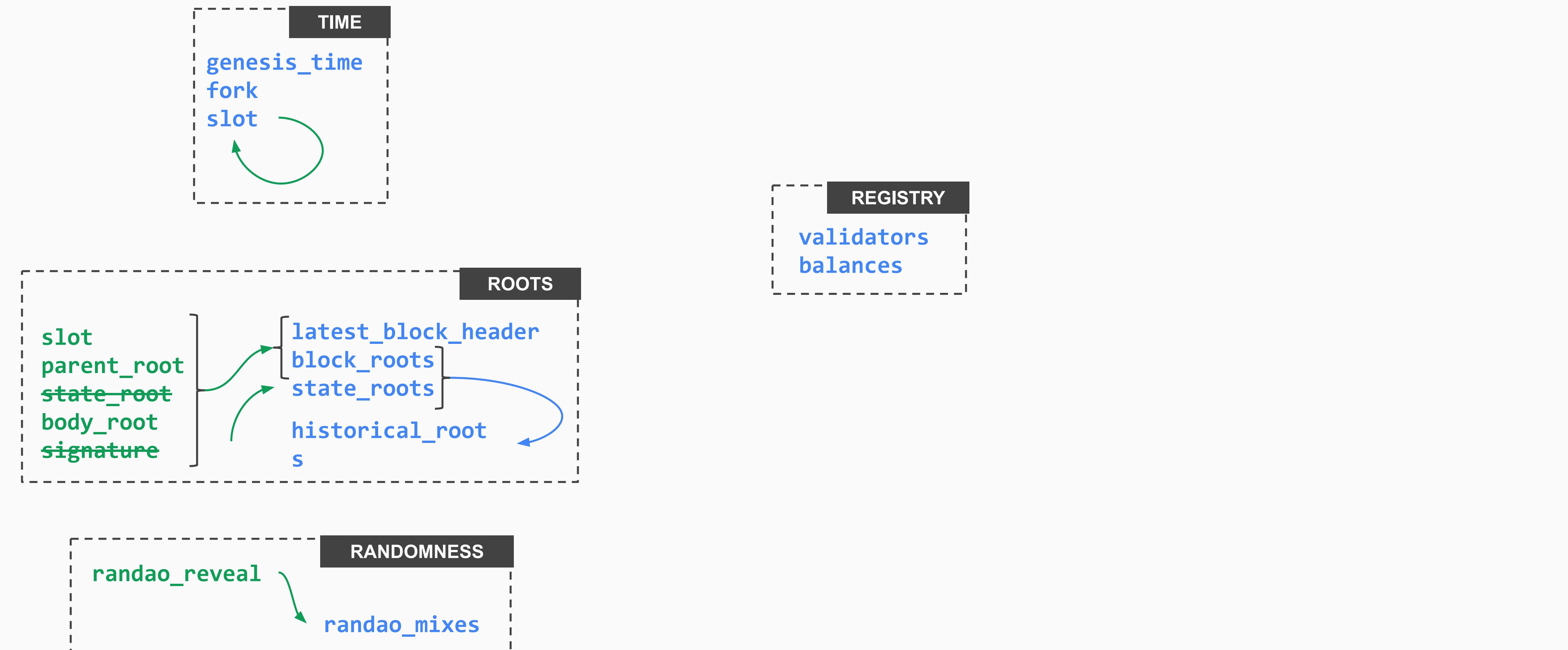
## state transition function



# state transition function



# state transition function



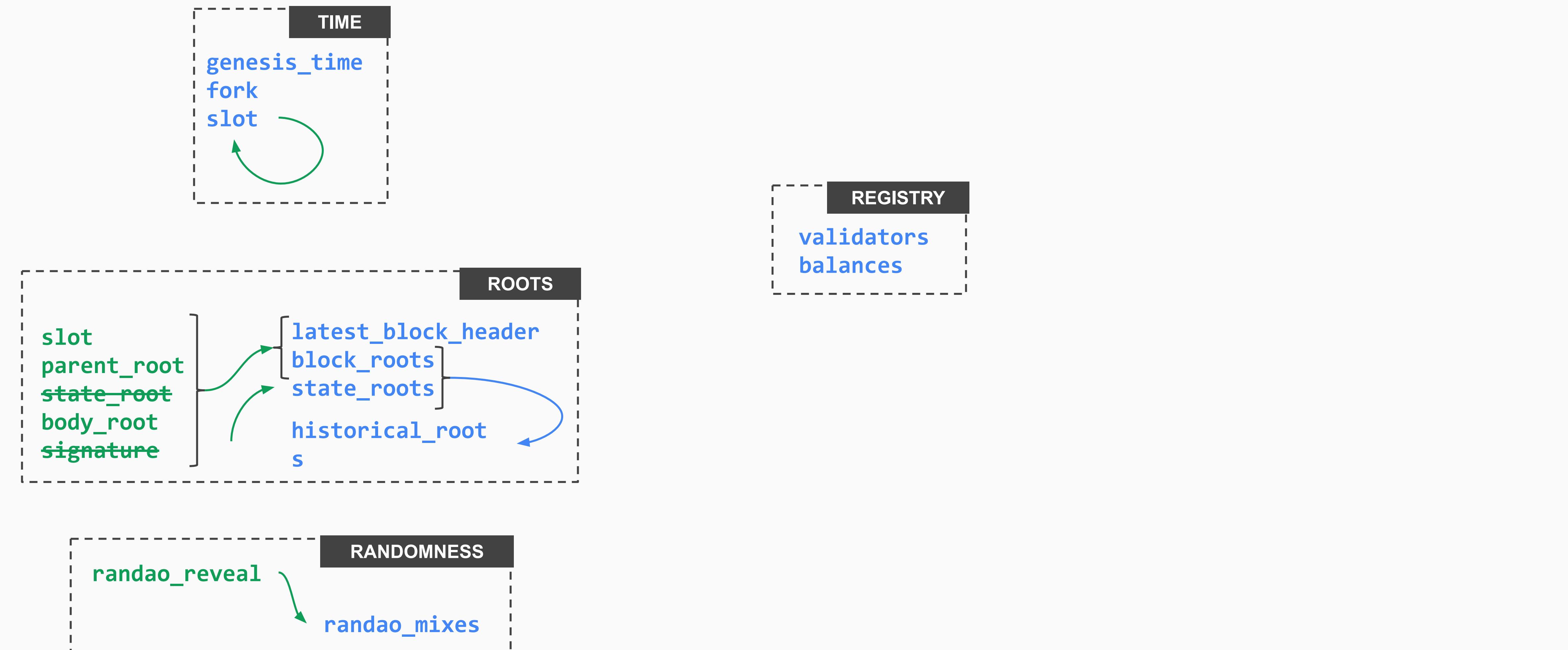
## Validator

```
1 class Validator(Container):  
2     pubkey: BLSPubkey  
3     withdrawal_credentials: Hash  
4     effective_balance: Gwei  
5     slashed: boolean
```

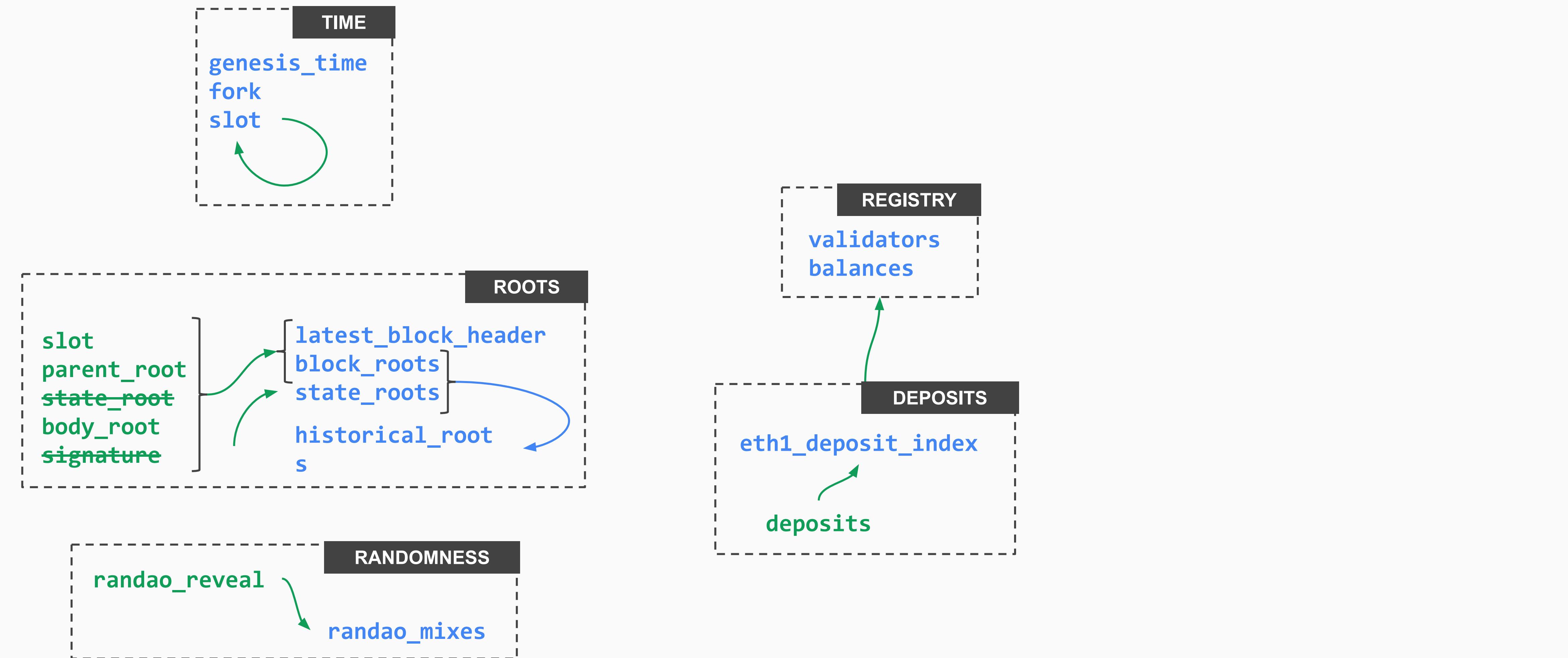
## Validator

```
1 class Validator(Container):
2     pubkey: BLSPubkey
3     withdrawal_credentials: Hash
4     effective_balance: Gwei
5     slashed: boolean
6     # Status epochs
7     activation_eligibility_epoch: Epoch
8     activation_epoch: Epoch
9     exit_epoch: Epoch
10    withdrawable_epoch: Epoch
```

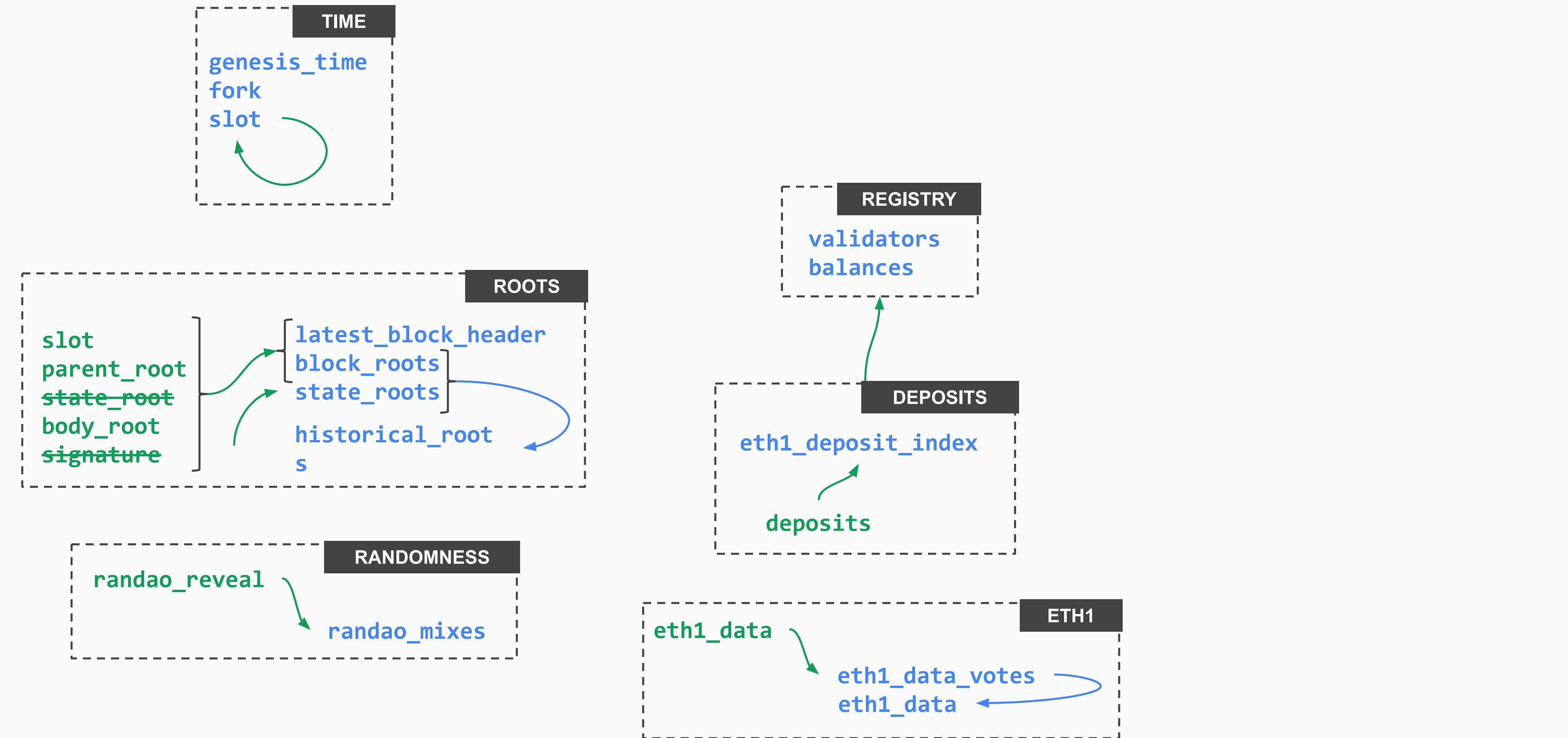
# state transition function



# state transition function

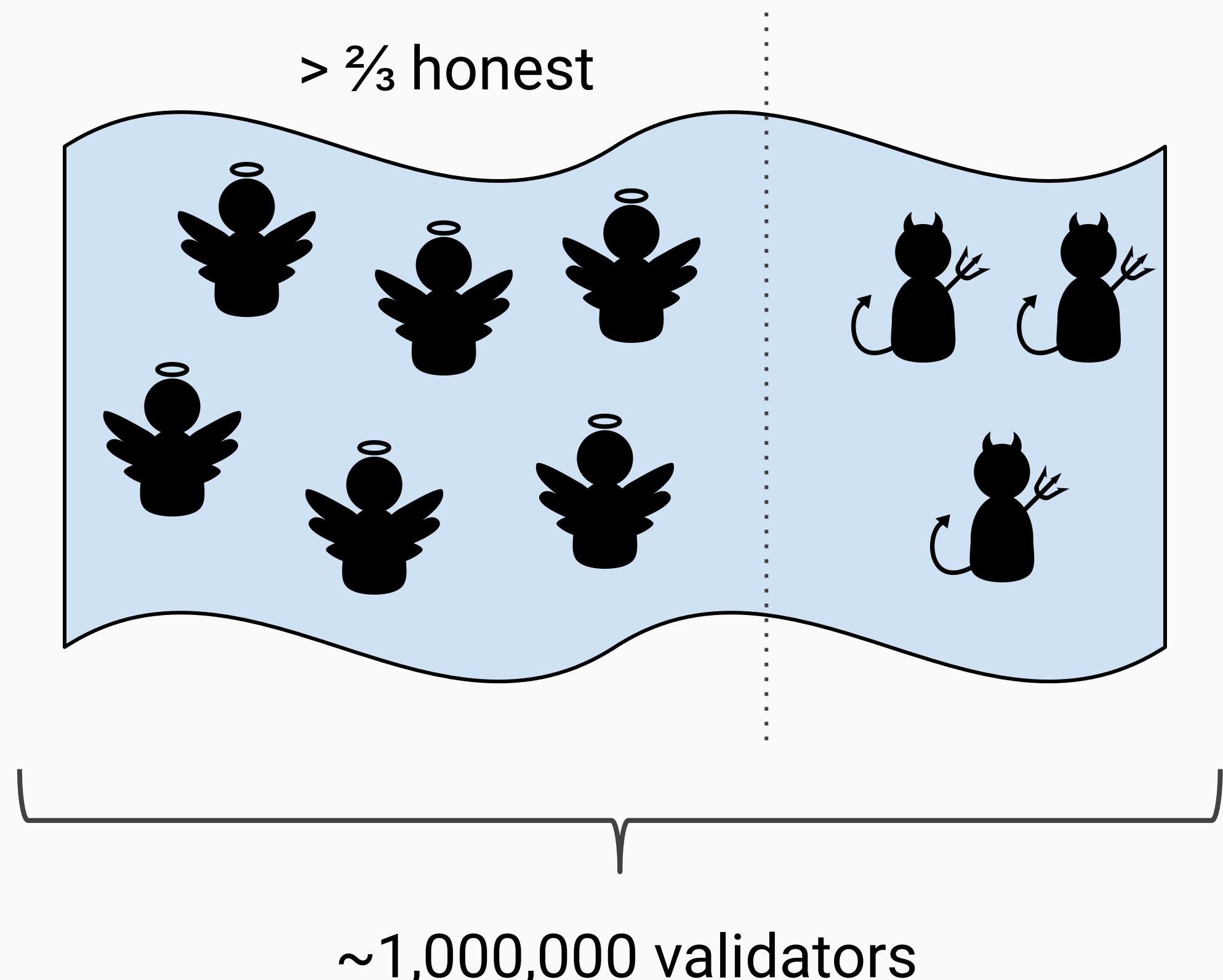


# state transition function

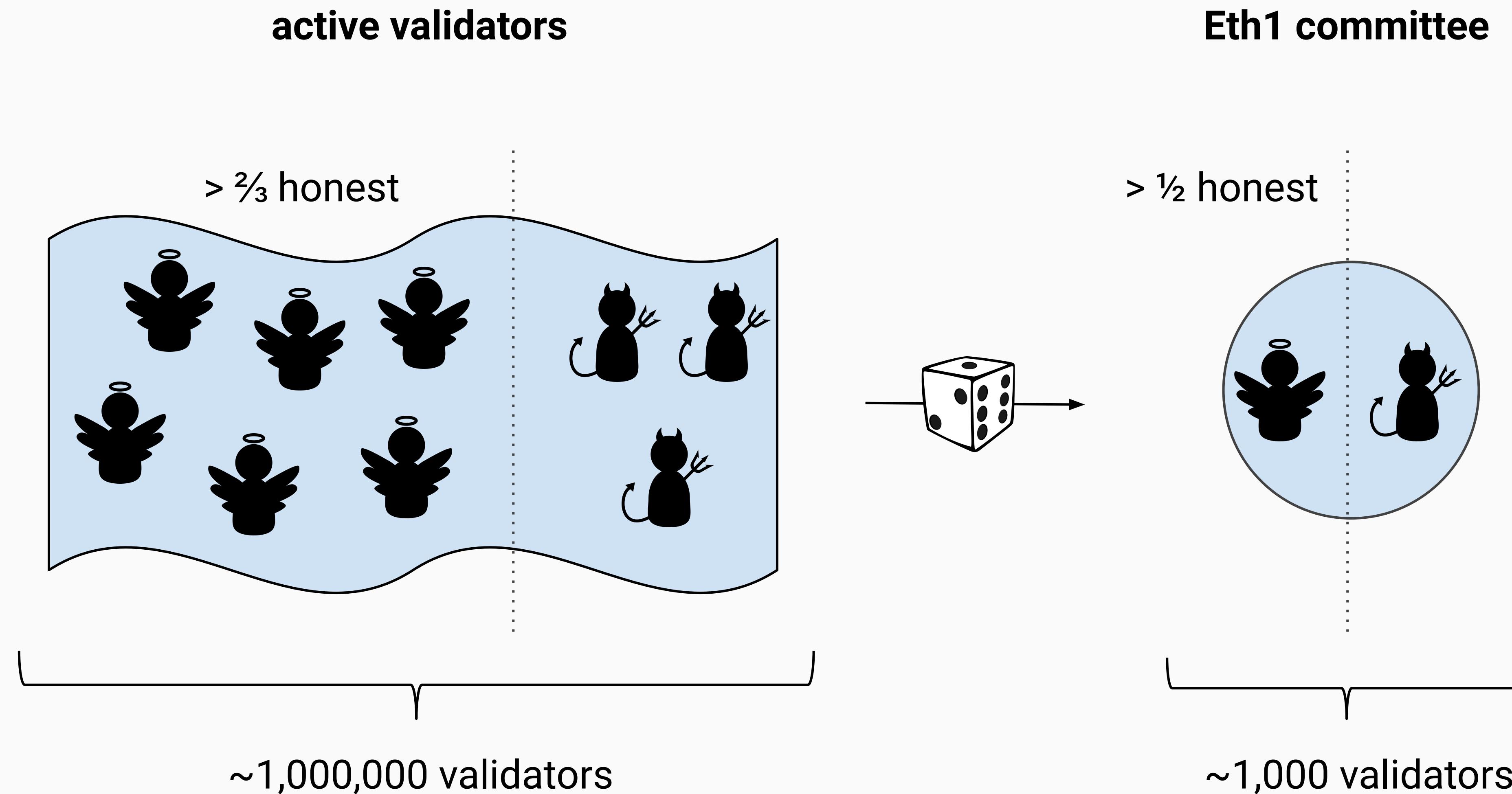


honest majority assumption

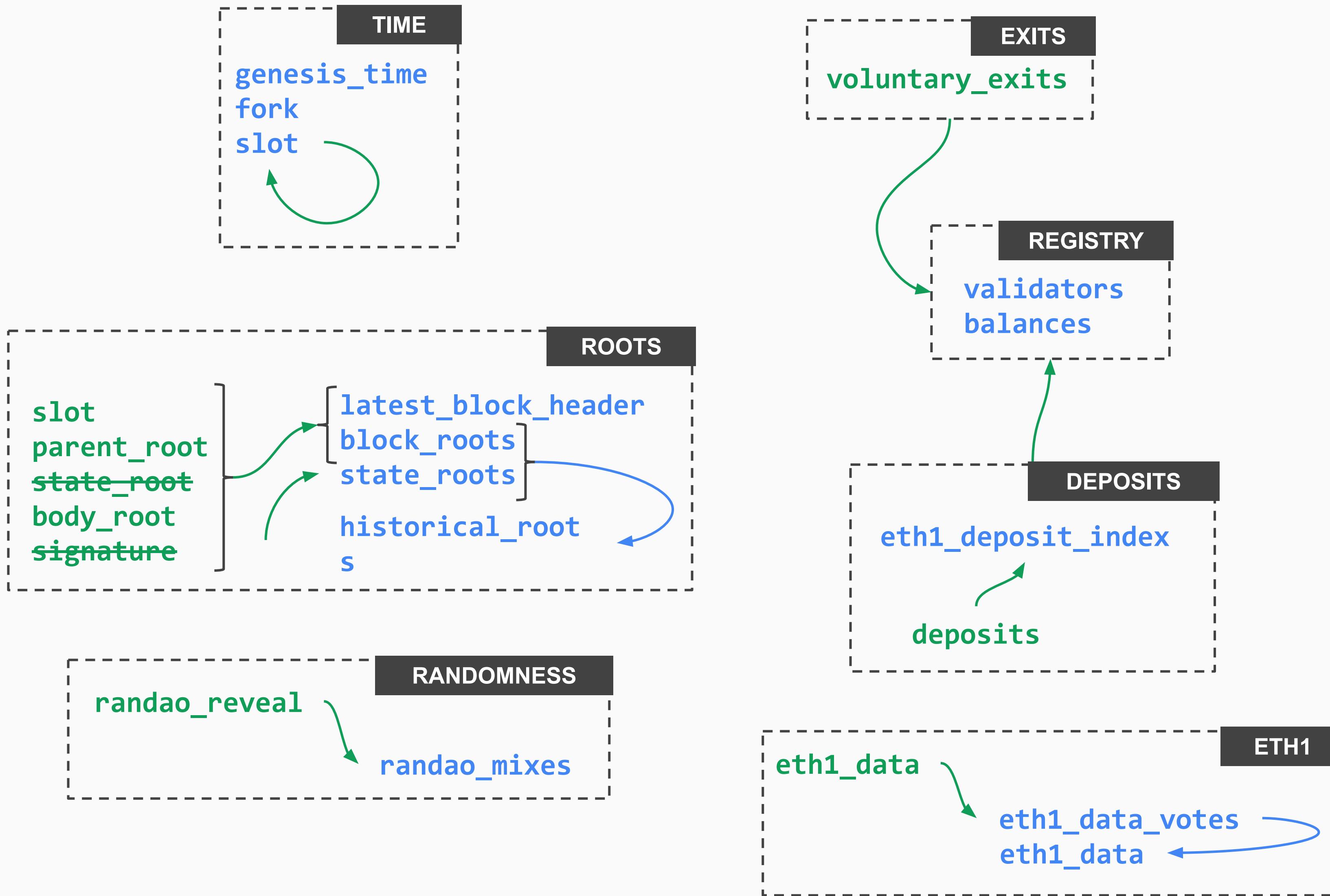
## active validators



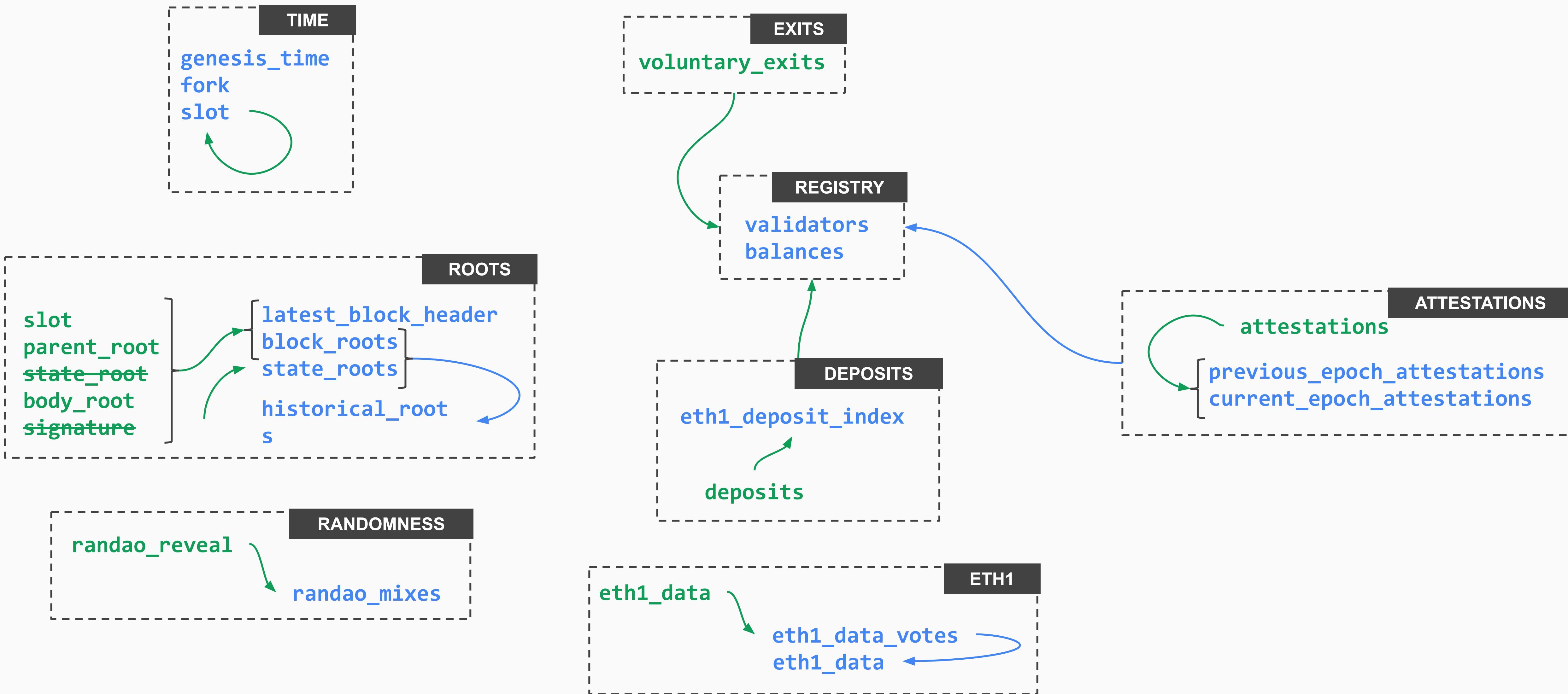
honest majority assumption



# state transition function



# state transition function



## Attestation

```
1 class Attestation(Container):
2     aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
3     data: AttestationData
4     custody_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
5     signature: BLSSignature
```

## Attestation

```
1  class Attestation(Container):
2      aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
3      data: AttestationData
4      custody_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
5      signature: BLSSignature
6
7  class AttestationData(Container):
8      # LMD GHOST vote
9      beacon_block_root: Hash
10     # FFG vote
11     source: Checkpoint
12     target: Checkpoint
13     # Crosslink vote
14     crosslink: Crosslink
```

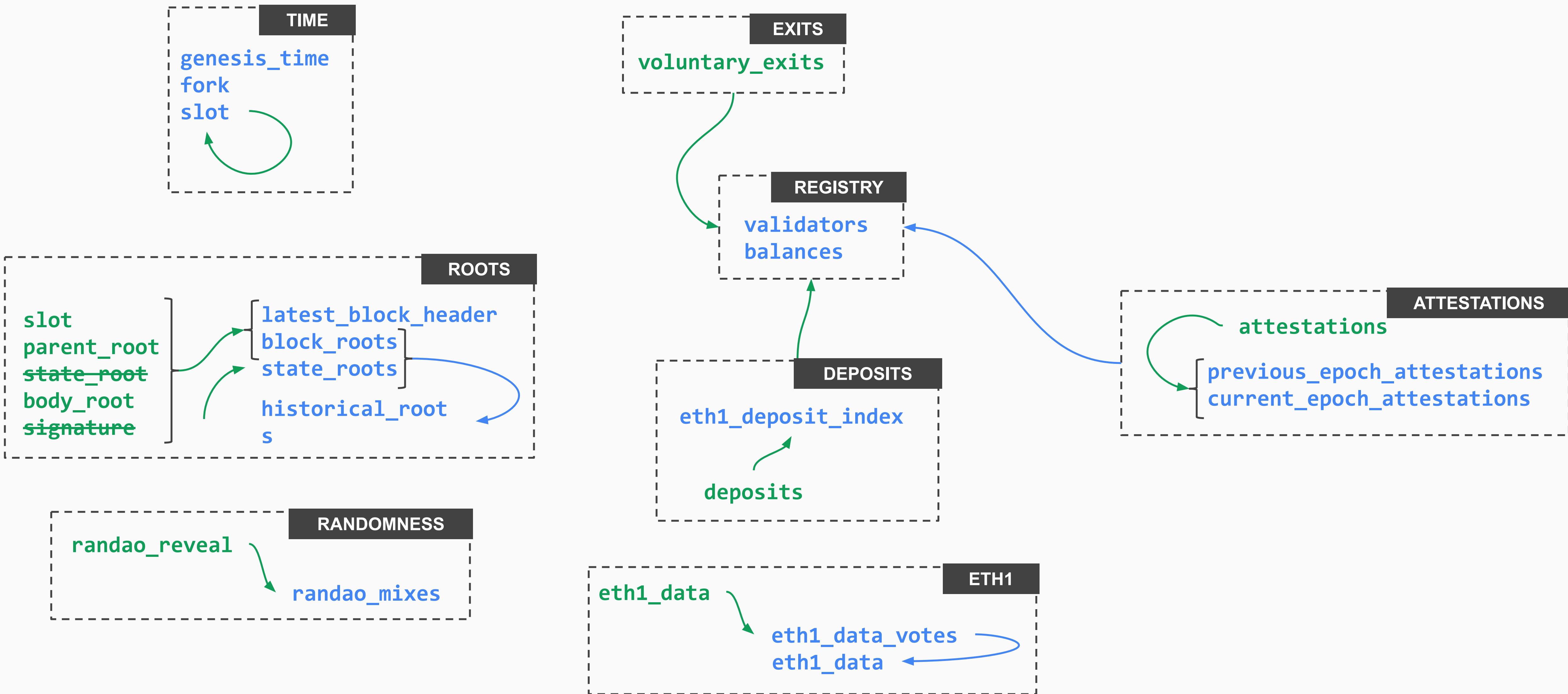
## Attestation

```
1  class Attestation(Container):
2      aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
3      data: AttestationData
4      custody_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
5      signature: BLSSignature
6
7  class AttestationData(Container):
8      # LMD GHOST vote
9      beacon_block_root: Hash
10     # FFG vote
11     source: Checkpoint
12     target: Checkpoint
13     # Crosslink vote
14     crosslink: Crosslink
15
16 class Checkpoint(Container):
17     epoch: Epoch
18     root: Hash
```

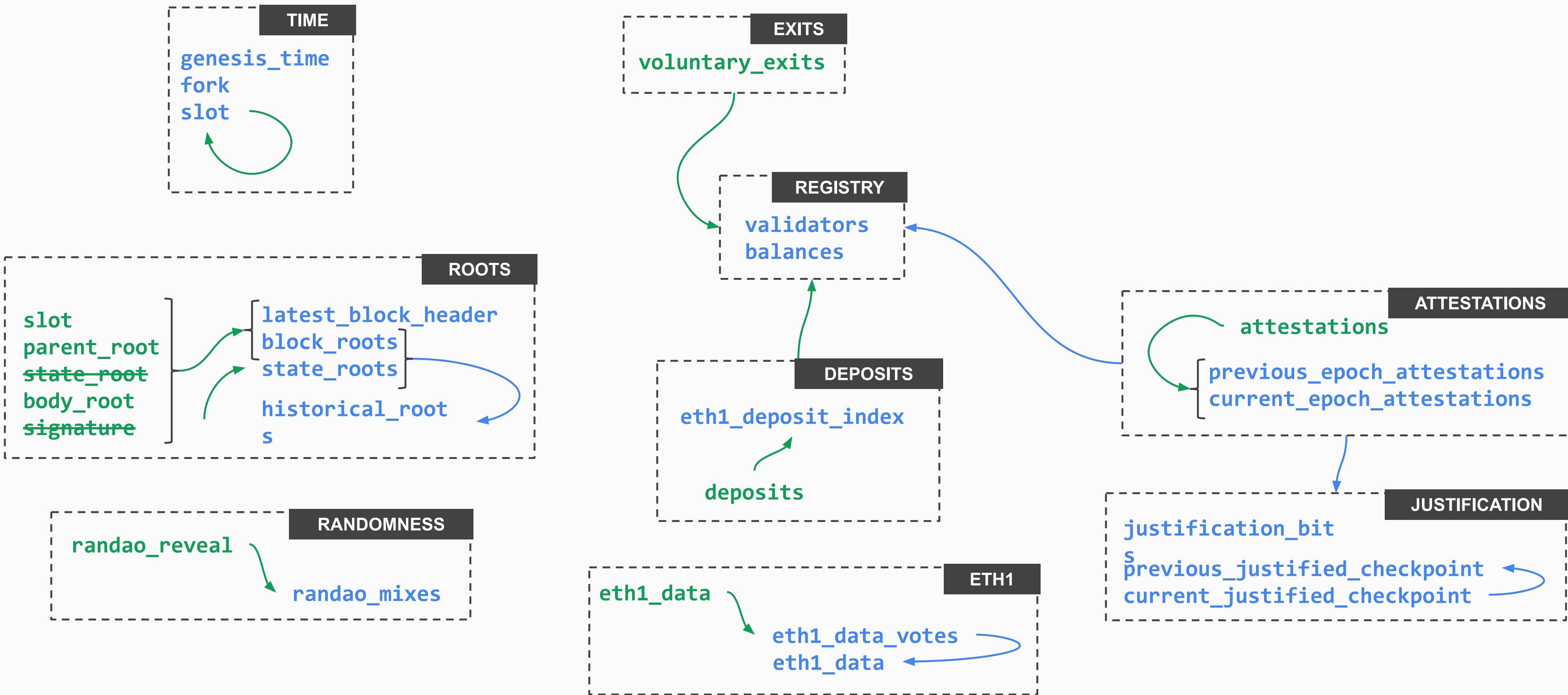
## Attestation

```
1  class Attestation(Container):
2      aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
3      data: AttestationData
4      custody_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
5      signature: BLSSignature
6
7  class AttestationData(Container):
8      # LMD GHOST vote
9      beacon_block_root: Hash
10     # FFG vote
11     source: Checkpoint
12     target: Checkpoint
13     # Crosslink vote
14     crosslink: Crosslink
15
16 class Checkpoint(Container):
17     epoch: Epoch
18     root: Hash
19
20 class Crosslink(Container):
21     shard: Shard
22     parent_root: Hash
23     # Crosslinking data
24     start_epoch: Epoch
25     end_epoch: Epoch
26     data_root: Hash
```

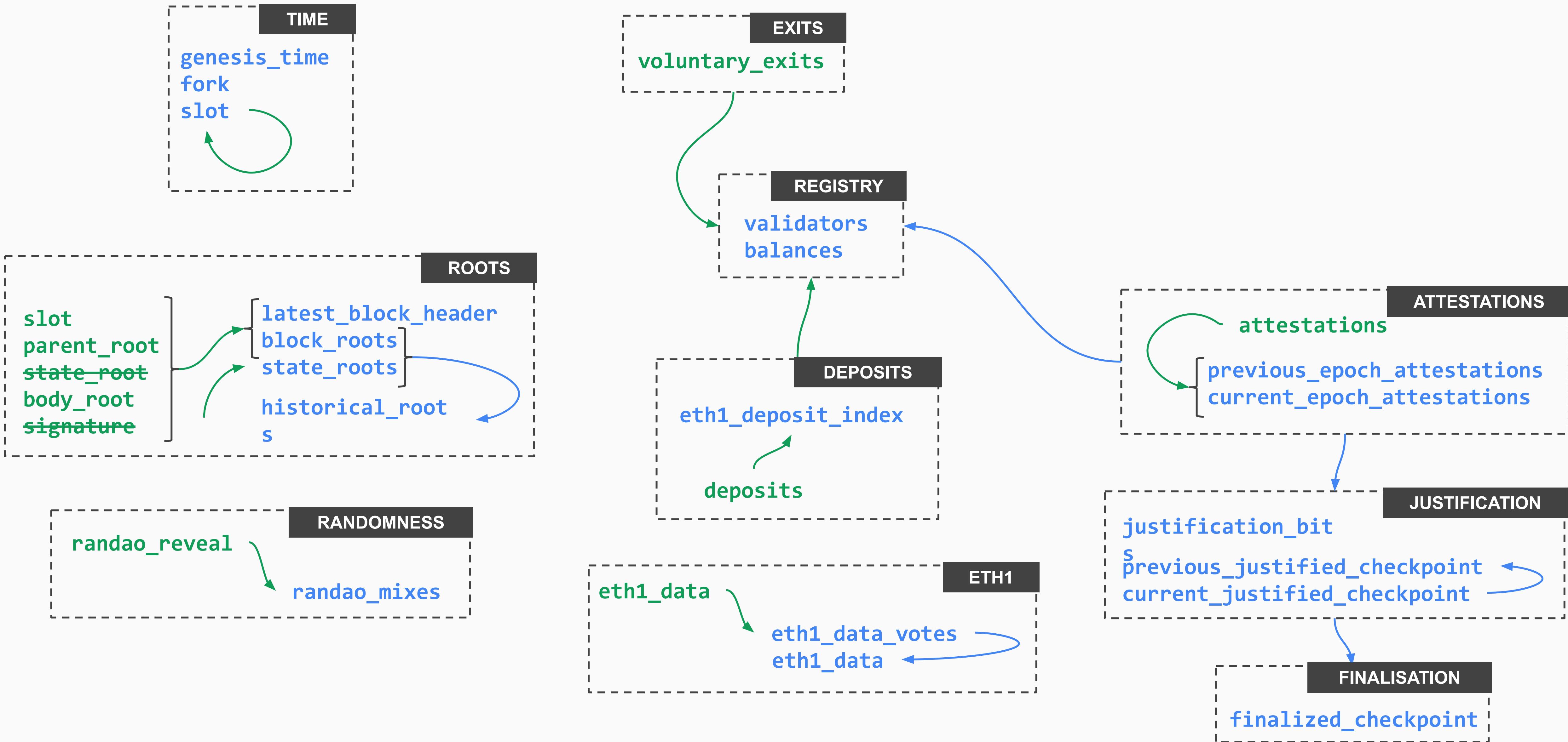
# state transition function



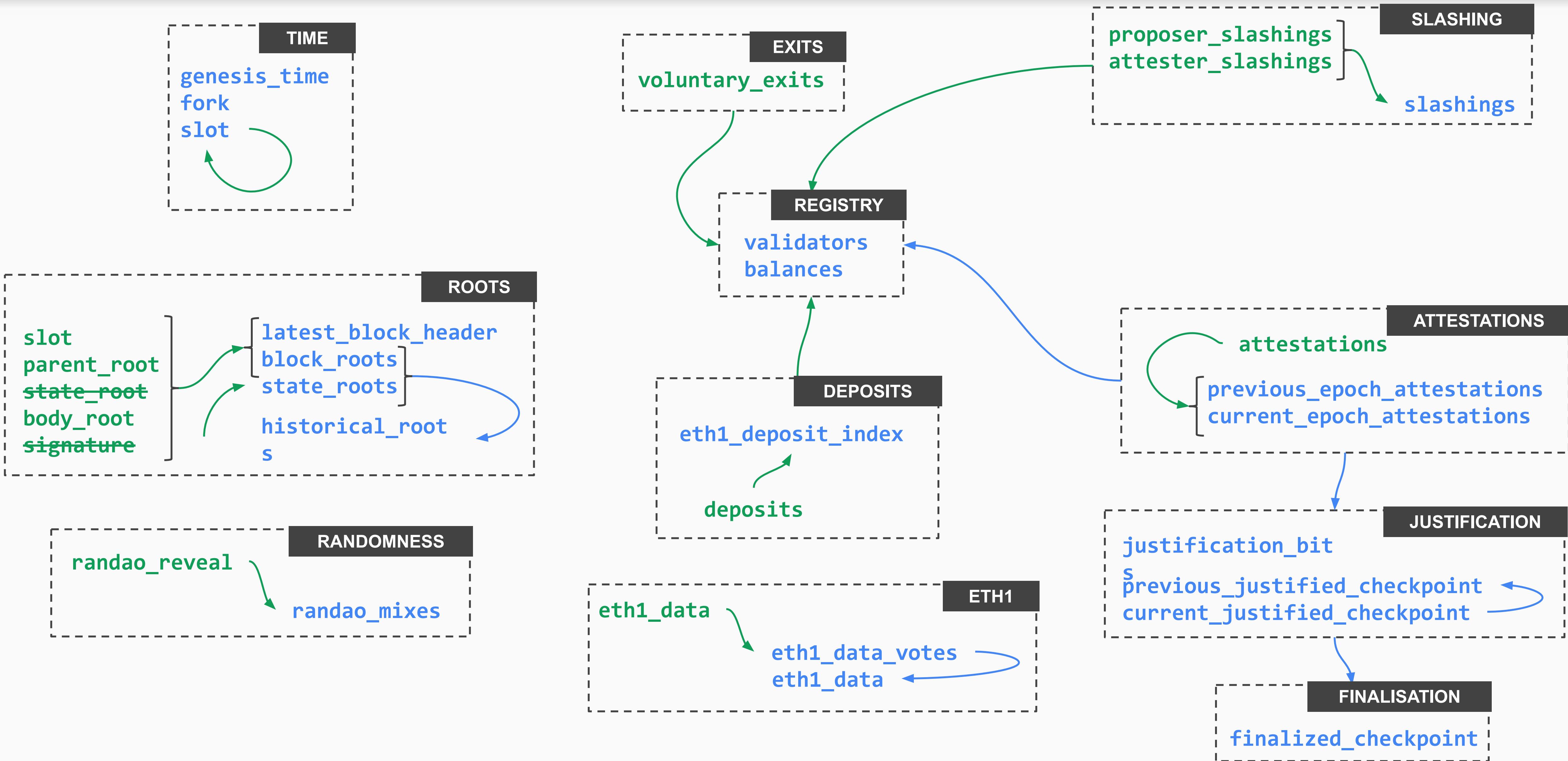
# state transition function



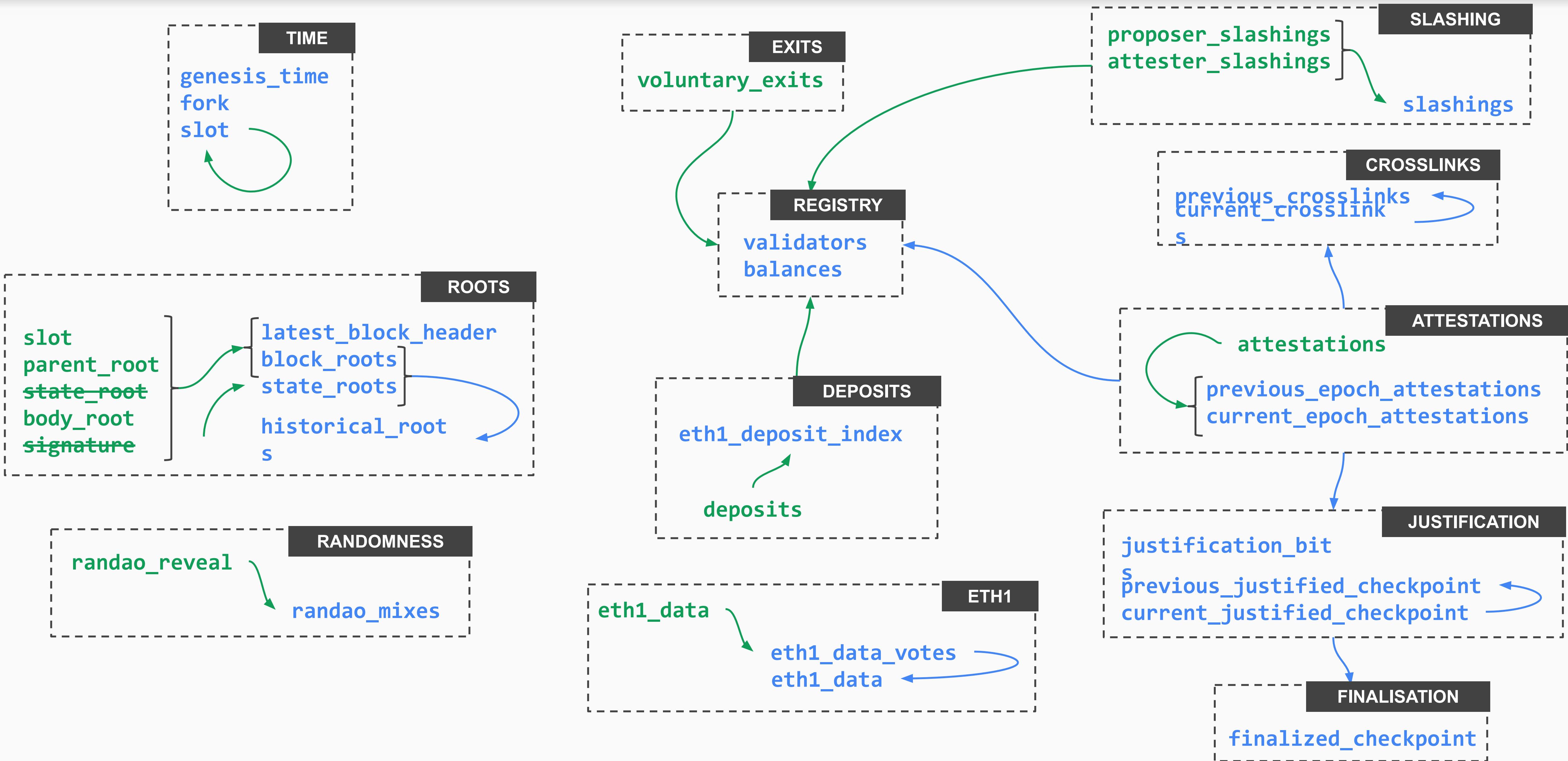
# state transition function



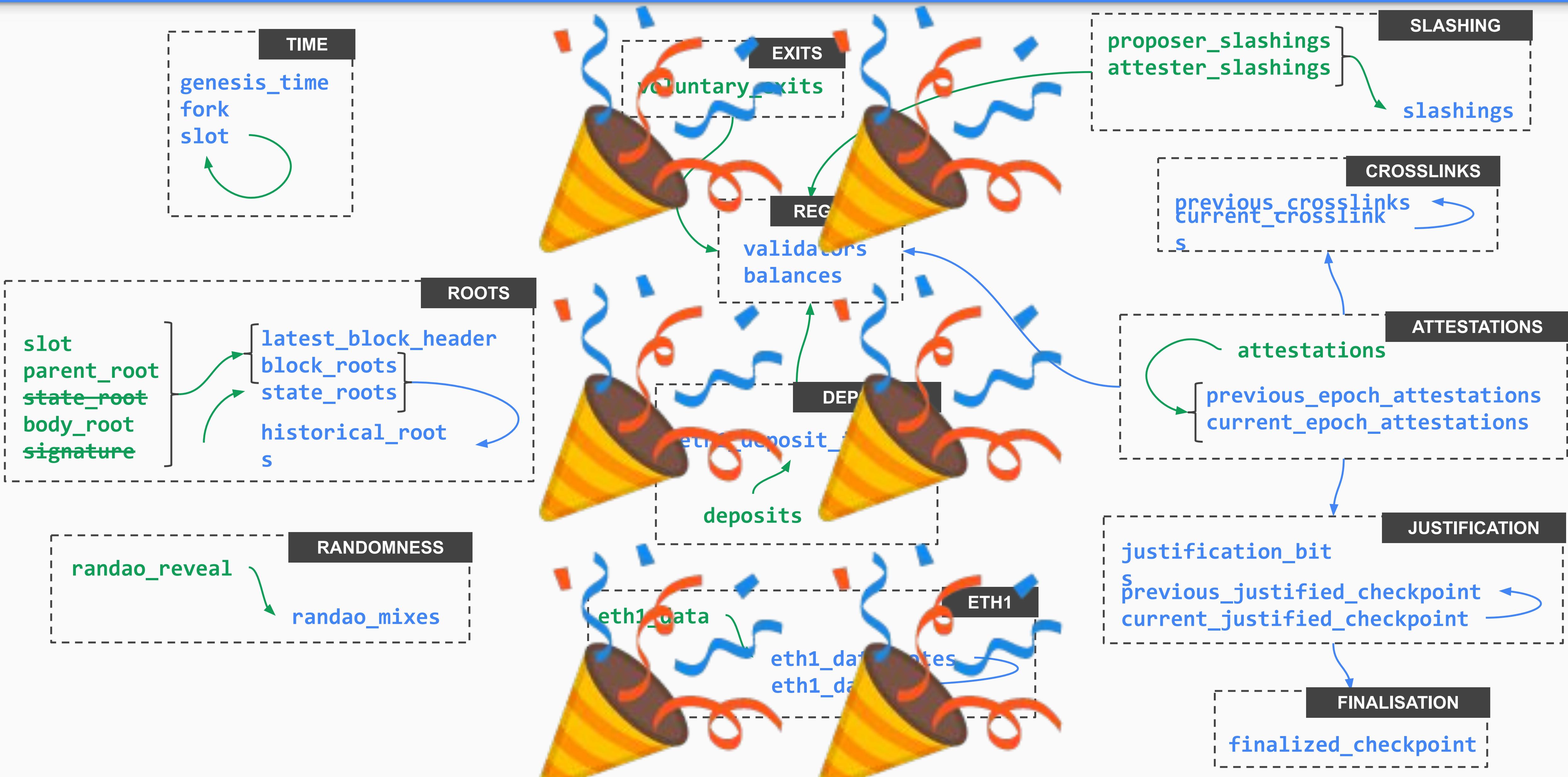
# state transition function



# state transition function



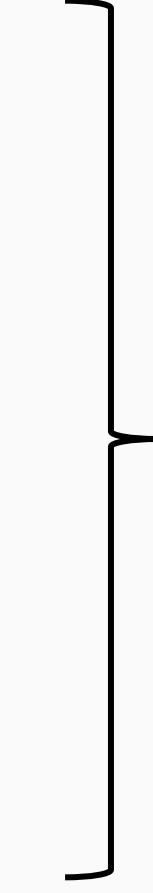
# state transition function



after phase 0

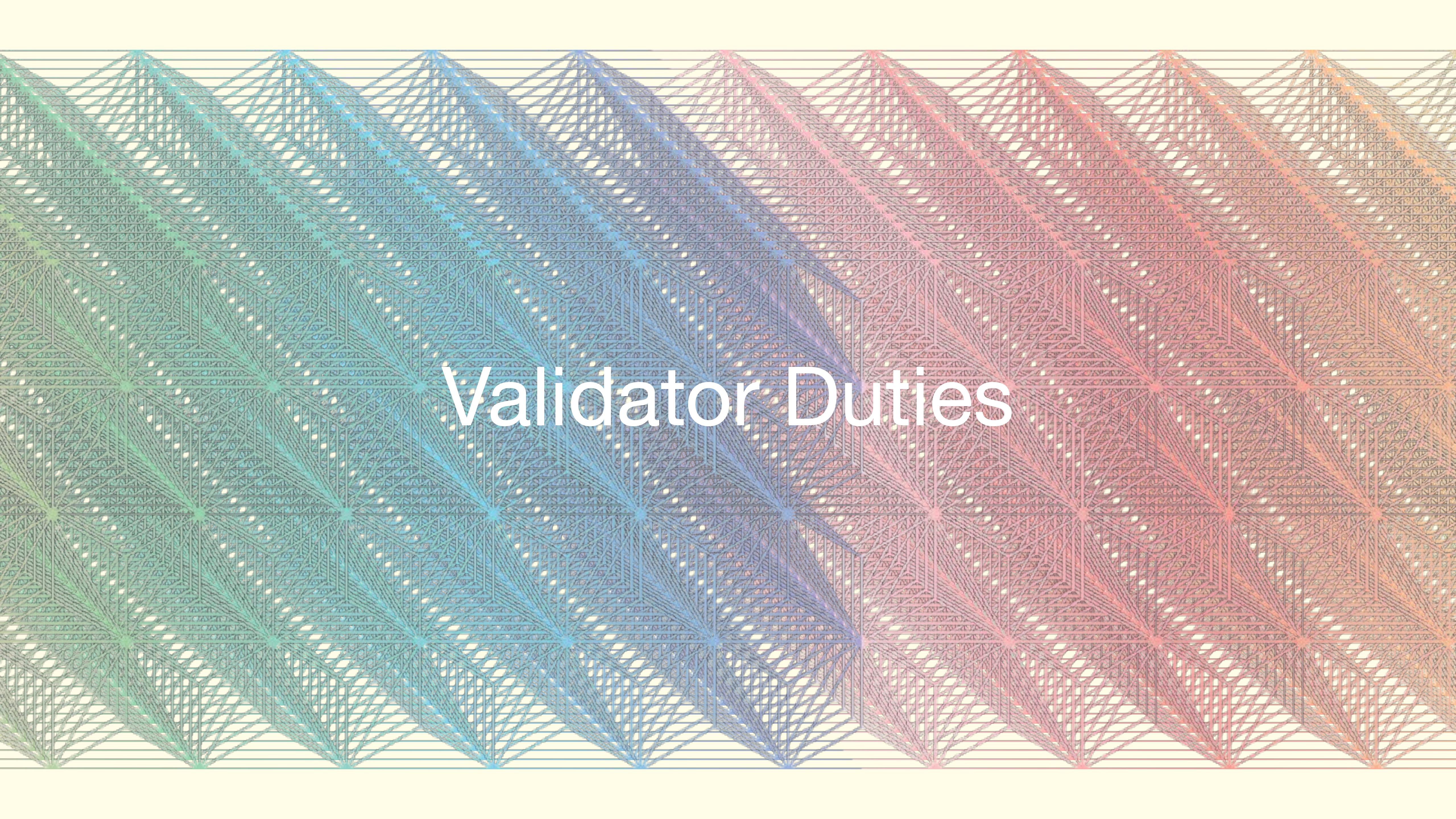
- transfers

## after phase 0

- transfers
  - custody proofs
  - secret proposers
  - VDF randomness
  - availability proofs
- 
- security upgrades**  
*(optional; fancy crypto)*

## after phase 0

- transfers
  - custody proofs
  - secret proposers
  - VDF randomness
  - availability proofs
  - multi hashing
  - quantum-security
- 
- security upgrades**  
(optional; fancy crypto)
- STARKs, Eth3**



# Validator Duties

# read the spec

## Ethereum 2.0 Phase 0 -- Honest Validator

[https://github.com/ethereum/eth2.0-specs/blob/dev/specs/validator/0\\_beacon-chain-validator.md](https://github.com/ethereum/eth2.0-specs/blob/dev/specs/validator/0_beacon-chain-validator.md)



[tiny.cc/phase0validator](http://tiny.cc/phase0validator)

# Proposer Assignment

```
def is_proposer(state: BeaconState,  
                validator_index: ValidatorIndex) -> bool:  
    return get_beacon_proposer_index(state) == validator_index
```

```
def compute_proposer_index(state: BeaconState, indices: Sequence[ValidatorIndex], seed: Hash) -> ValidatorIndex  
    """  
        Return from ``indices`` a random index sampled by effective balance.  
    """  
    assert len(indices) > 0  
    MAX_RANDOM_BYTE = 2**8 - 1  
    i = 0  
    while True:  
        candidate_index = indices[compute_shuffled_index(ValidatorIndex(i % len(indices)), len(indices),  
                                                random_byte = hash(seed + int_to_bytes(i // 32, length=8))[i % 32])]  
        effective_balance = state.validators[candidate_index].effective_balance  
        if effective_balance * MAX_RANDOM_BYTE >= MAX_EFFECTIVE_BALANCE * random_byte:  
            return ValidatorIndex(candidate_index)  
        i += 1
```

- Independent of committee assignment
- Knowable *within* the epoch of proposal
- Action performed at slot\_start\_time
- Publicly known and DOS concern

# Block Proposal

```
class BeaconBlock(Container):
    slot: Slot
    parent_root: Hash
    state_root: Hash
    body: BeaconBlockBody
    signature: BLSSignature
```

```
class BeaconBlockBody(Container):
    randao_reveal: BLSSignature
    eth1_data: Eth1Data # Eth1 data vote
    graffiti: Bytes32 # Arbitrary data
    # Operations
    proposer_slashings: List[ProposerSlashing, MAX_PROPOSER_SLASHINGS]
    attester_slashings: List[AttesterSlashing, MAX_ATTESTER_SLASHINGS]
    attestations: List[Attestation, MAX_ATTESTATIONS]
    deposits: List[Deposit, MAX_DEPOSITS]
    voluntary_exits: List[VoluntaryExit, MAX_VOLUNTARY_EXITS]
```

# Eth1 Data

```
def get_eth1_vote(state: BeaconState, previous_eth1_distance: uint64) -> Eth1Data:
    new_eth1_data = [get_eth1_data(distance) for distance in range(ETH1_FOLLOW_DISTANCE, 2 * ETH1_FOLLOW_DISTANCE)]
    all_eth1_data = [get_eth1_data(distance) for distance in range(ETH1_FOLLOW_DISTANCE, previous_eth1_distance + 1)]

    valid_votes = []
    for slot, vote in enumerate(state.eth1_data_votes):
        period_tail = slot % SLOTS_PER_ETH1_VOTING_PERIOD >= integer_sqreroot(SLOTS_PER_ETH1_VOTING_PERIOD)
        if vote in new_eth1_data or (period_tail and vote in all_eth1_data):
            valid_votes.append(vote)

    return max(
        valid_votes,
        key=lambda v: (valid_votes.count(v), -all_eth1_data.index(v)), # Tiebreak by smallest distance
        default=get_eth1_data(ETH1_FOLLOW_DISTANCE),
    )
```

- Mechanism to come to consensus on recent eth1 data
- Mechanism to avoid stale data winning

# Slashability of Block Proposals

```
def process_proposer_slashing(state: BeaconState, proposer_slashing: ProposerSlashing) -> None:
    proposer = state.validators[proposer_slashing.proposer_index]
    # Verify that the epoch is the same
    assert (compute_epoch_of_slot(proposer_slashing.header_1.slot)
            == compute_epoch_of_slot(proposer_slashing.header_2.slot))
    # But the headers are different
    assert proposer_slashing.header_1 != proposer_slashing.header_2
```

# Committee Assignment

```
def get_committee_assignment(state: BeaconState,
                             epoch: Epoch,
                             validator_index: ValidatorIndex) -> Optional[Tuple[Sequence[ValidatorIndex]]]:
    """
    Return the committee assignment in the ``epoch`` for ``validator_index``.
    ``assignment`` returned is a tuple of the following form:
        * ``assignment[0]`` is the list of validators in the committee
        * ``assignment[1]`` is the shard to which the committee is assigned
        * ``assignment[2]`` is the slot at which the committee is assigned
    Return None if no assignment.
    """
    next_epoch = get_current_epoch(state) + 1
    assert epoch <= next_epoch

    committees_per_slot = get_committee_count(state, epoch) // SLOTS_PER_EPOCH
    start_slot = compute_start_slot_of_epoch(epoch)
    for slot in range(start_slot, start_slot + SLOTS_PER_EPOCH):
        offset = committees_per_slot * (slot % SLOTS_PER_EPOCH)
        slot_start_shard = (get_start_shard(state, epoch) + offset) % SHARD_COUNT
        for i in range(committees_per_slot):
            shard = Shard((slot_start_shard + i) % SHARD_COUNT)
            committee = get_crosslink_committee(state, epoch, shard)
            if validator_index in committee:
                return committee, shard, Slot(slot)
    return None
```

- Assigned one per epoch
- At least one epoch of lookahead
- Tunable via `MIN_SEED_LOOKAHEAD`
- Action performed at `slot_start + 0.5*SECONDS_PER_SLOT`

# Attestation Data

```
class AttestationData(Container):
    # LMD GHOST vote
    beacon_block_root: Hash
    # FFG vote
    source: Checkpoint
    target: Checkpoint
    # Crosslink vote
    crosslink: Crosslink
```

# Crosslink within AttestationData

Construct `attestation_data.crosslink` via the following.

- Set `attestation_data.crosslink.shard = shard` where `shard` is the shard associated with the validator's committee.
- Let `parent_crosslink = head_state.current_crosslinks[shard]` .
- Set `attestation_data.crosslink.start_epoch = parent_crosslink.end_epoch` .
- Set `attestation_data.crosslink.end_epoch = min(attestation_data.target.epoch, parent_crosslink.end_epoch + MAX_EPOCHS_PER_CROSSLINK)` .
- Set `attestation_data.crosslink.parent_root = hash_tree_root(head_state.current_crosslinks[shard])` .
- Set `attestation_data.crosslink.data_root = ZERO_HASH` . Note: This is a stub for Phase 0.

# Custody Bit (Phase 0)

```
class AttestationDataAndCustodyBit(Container):
    data: AttestationData
    custody_bit: bit # Challengeable bit (SSZ-bool, 1 byte) for the custody of crosslink data
```

- The actual object signed
- Stubbed `custody_bit` as 0 for Phase 0

# Outer Attestation Structure

```
class Attestation(Container):
    aggregation_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
    data: AttestationData
    custody_bits: Bitlist[MAX_VALIDATORS_PER_COMMITTEE]
    signature: BLSSignature
```

# Crosslink Committee Incentives

- Correct Head
- Correct Target
- Correct Source
- Correct Crosslink
- Fast Inclusion

See process\_rewards\_and\_penalties

# Slashability of Attestations

## ↳ `is_slashable_attestation_data`

```
def is_slashable_attestation_data(data_1: AttestationData, data_2: AttestationData) -> bool:  
    """  
        Check if ``data_1`` and ``data_2`` are slashable according to Casper FFG rules.  
    """  
  
    return (  
        # Double vote  
        (data_1 != data_2 and data_1.target.epoch == data_2.target.epoch) or  
        # Surround vote  
        (data_1.source.epoch < data_2.source.epoch and data_2.target.epoch < data_1.target.epoch)  
    )
```